

Predictive Learning applied to Muon Chamber Monitoring

Data Quality Monitoring with Neural Networks

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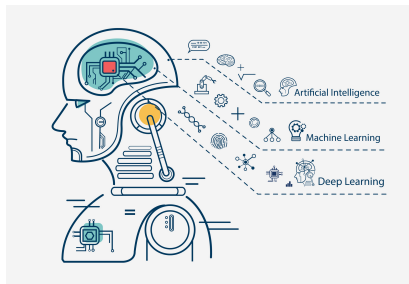
Introduction



Deep learning algorithms for data quality monitoring

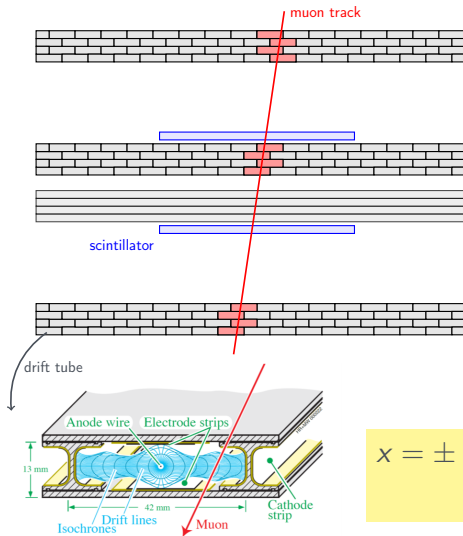
Employement of **deep learning** allows for

- Flexibility
- Accuracy
- Automation



The Detector

Experimental setup



- 4 muon chambers (*superlayers*)
- 4 staggered layers of 16 *drift tubes* each
- *trigger-less* data acquisition system
- 2 *scintillator* tiles

$$x = \pm v_{\text{drift}} \underbrace{(t - t_0)}_{\text{drift time}}$$

The Drift Time Distribution

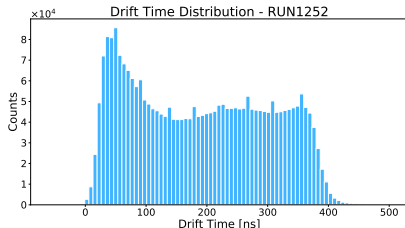


Main features of the time box

Collection of the times that the electrons take to reach the anodic wire in the center of the cell

The external trigger

- allows to discriminate *muon hits* from background noise
- provides a *timing reference* t_0 for computing the drift time



Time box shape:

- approximately *uniform*
- ~ 400 ns width

The Deep Learning Algorithm

A brief overview

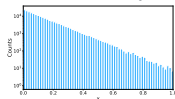


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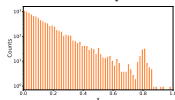
INPUT

OUTPUT

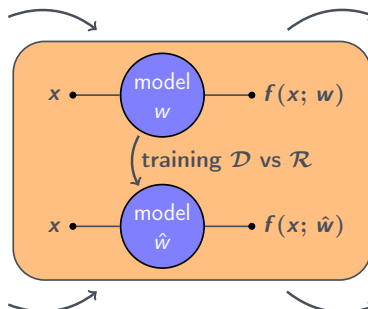
reference sample \mathcal{R}



data sample \mathcal{D}

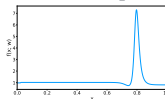


NEURAL NETWORK



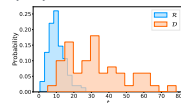
log-ratio distribution

$$f(x; \hat{w}) \approx \log \left[\frac{n(x | \mathcal{T})}{n(x | \mathcal{R})} \right]$$



t distribution

$$t(\mathcal{D}) = -2 \min_w L[f]$$



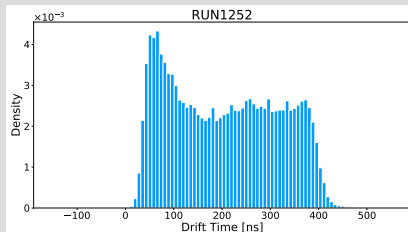
Tuning the Neural Network

Training the network on the reference dataset



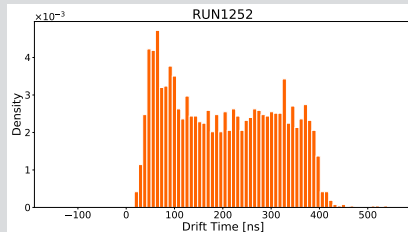
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Reference sample \mathcal{R}



$$N_{\mathcal{R}} = 200000$$

Data sample \mathcal{D}



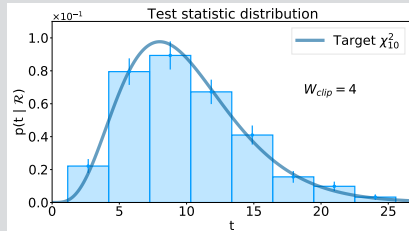
$$N_{\mathcal{D}} = 3000 \text{ sampled from } \mathcal{R}$$

Tuning the Neural Network

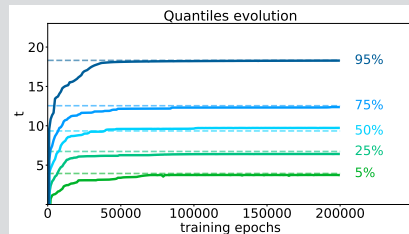
Optimal weight clipping



Test statistic distribution



Quantiles evolution

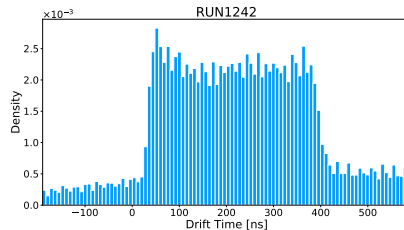
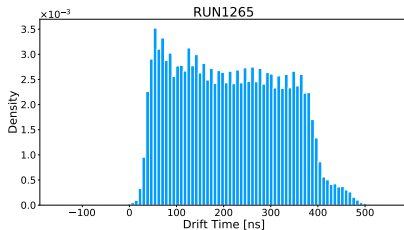
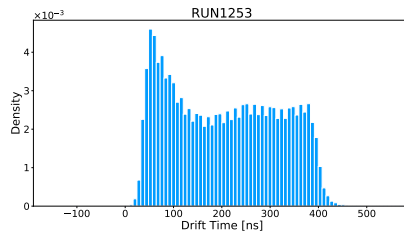
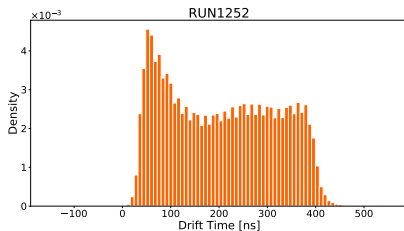


400 samples of $\mathcal{N}_{\mathcal{D}} = 3000$ each

Testing the algorithm performance



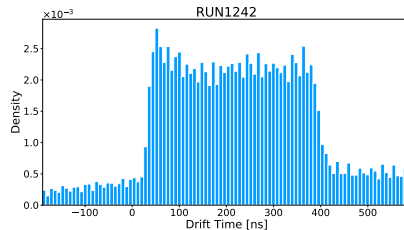
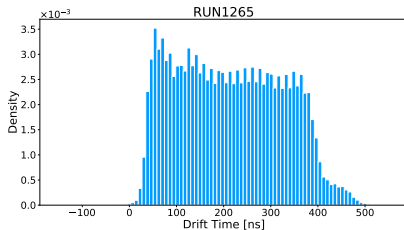
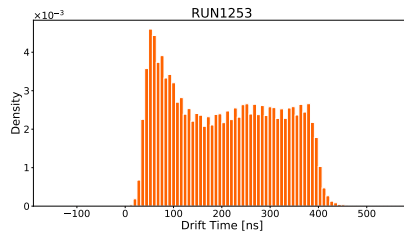
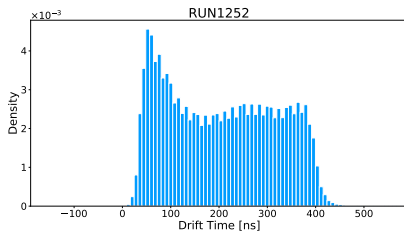
Drift time distributions



Testing the algorithm performance



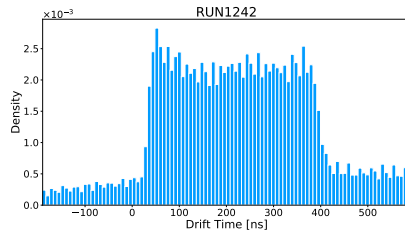
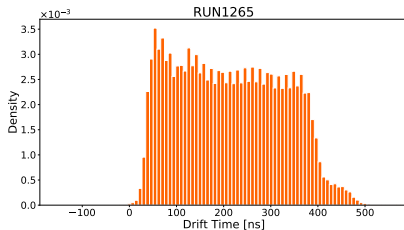
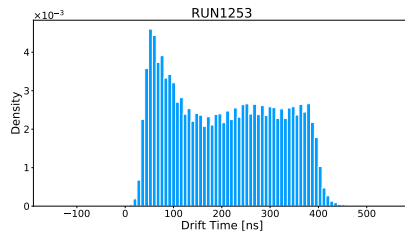
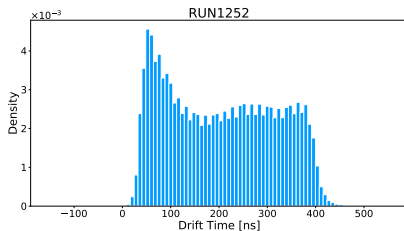
Drift time distributions



Testing the algorithm performance



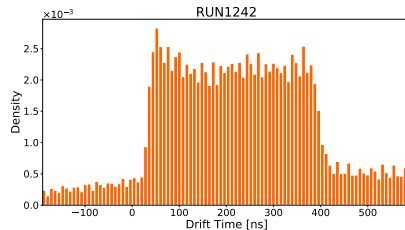
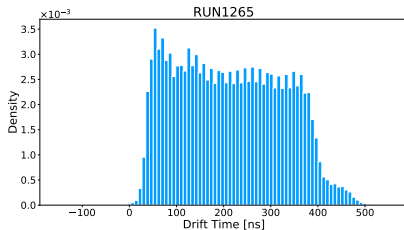
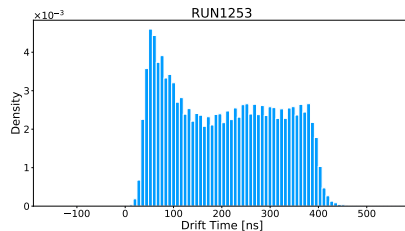
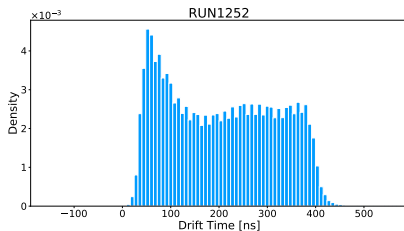
Drift time distributions



Testing the algorithm performance

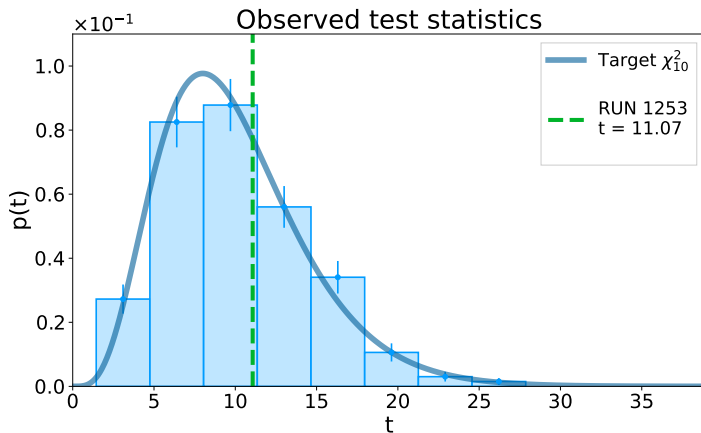


Drift time distributions



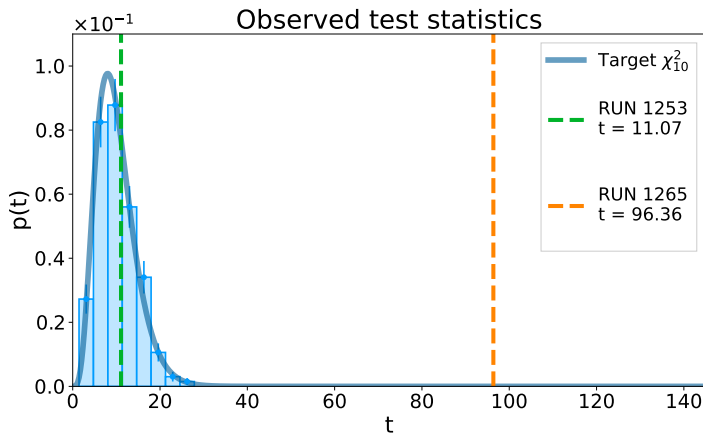
Testing the algorithm performance

Discrepancy assessment



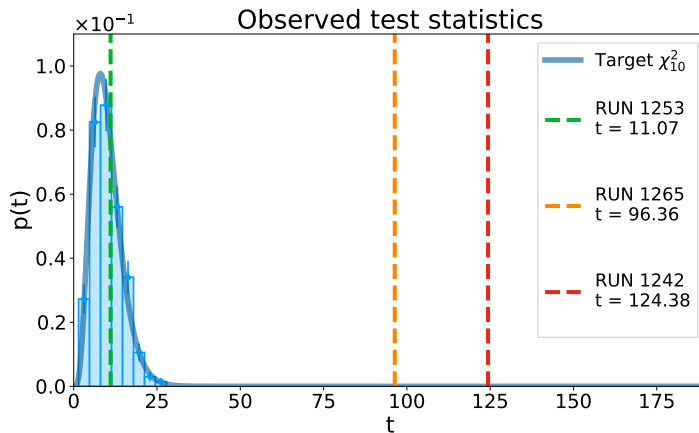
Testing the algorithm performance

Discrepancy assessment



Testing the algorithm performance

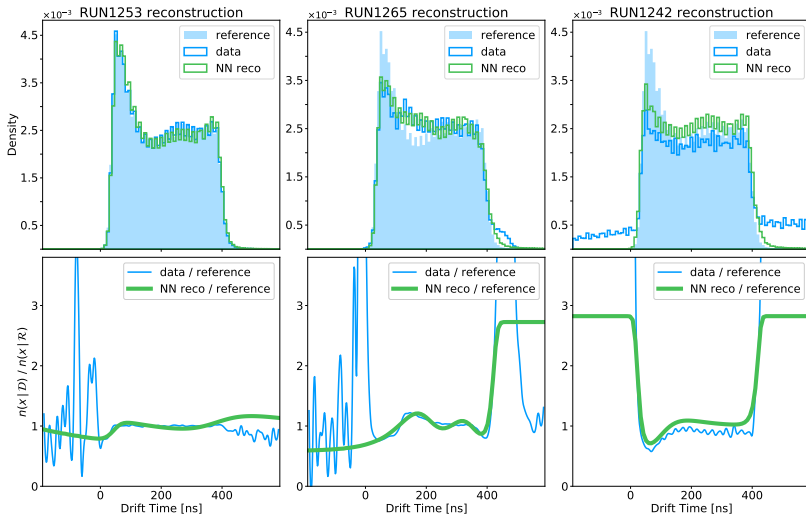
Discrepancy assessment



Testing the algorithm performance



Neural network's data reconstruction



Summary of the Results

Improving the procedure automation



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The current implementation of the algorithm

- correctly detects discrepancies between \mathcal{R} and \mathcal{D}
- returns larger t_{obs} when the anomalies are more evident

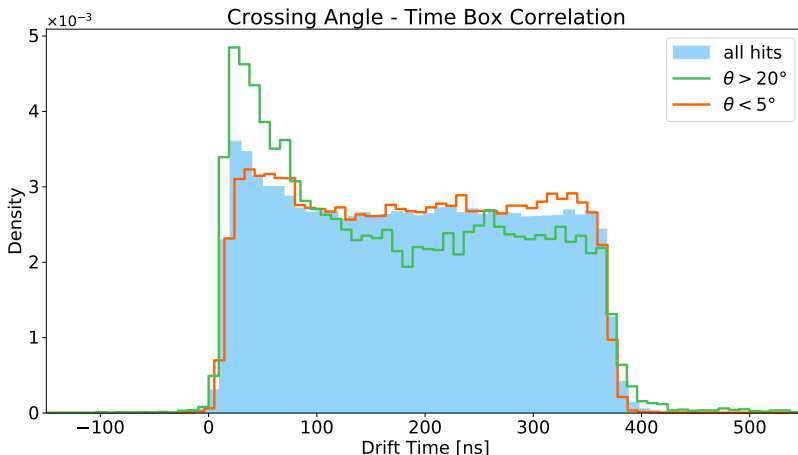
However

- the most critical anomalies are not always the most obvious
- the time box shape may vary for other reasons
(e.g. due to correlations with other observables)

Example of Correlated Observables



Correlation between time box shape and muon crossing angle



- 1 Gathering correlated observables to improve flexibility
 - multi-dimensional input datasets
- 2 Mapping different data anomalies to the corresponding detector failures
 - systematic study of discrepant data collected with well-known detector setups
- 3 Building an *online* DQM framework for full automation
 - the current implementation of the algorithm is too slow
 - FalkonML¹ can be exploited to emulate our algorithm
 - training time lowers from ~ 47 min to ~ 2 sec

¹ GitHub repository: <https://github.com/FalkonML/falkon>

Thank you for
your attention!



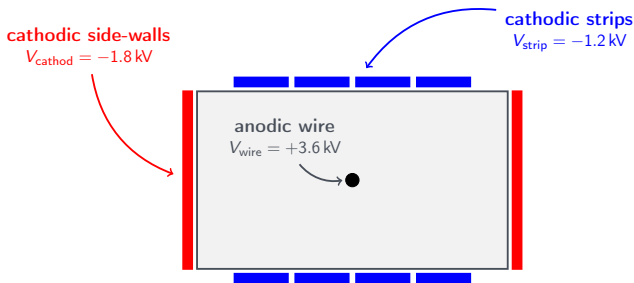
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Drift Tubes



Specifics of the detector elementary cells

- DTs' transverse cross section is $L \times h = 42 \times 13 \text{ mm}^2$
- Filled with an Ar-CO_2 (85/15 %) gas mixture at $\sim 1 \text{ atm}$
- Precise electrode configuration ensures $\vec{E} \simeq \text{uniform}$ inside DTs
- Almost constant drift velocity $v_{\text{drift}} \approx 54 \mu\text{m/ns}$



- Null hypothesis H_0 :
 $n(x | \mathcal{R}) \rightarrow$ data following the reference model \mathcal{R}
- Alternative hypothesis H_1 :
 $n(x | \mathbf{w}) = n(x | \mathcal{R}) e^{f(x; \mathbf{w})} \rightarrow$ parametrized by the NN

The most powerful statistical test is the **likelihood-ratio test**
(Neyman-Pearson lemma)

The algorithm compares $n(x | \mathcal{R})$ with $n(x | \hat{\mathbf{w}})$ where $\hat{\mathbf{w}}$ is the parameters configuration that maximizes the likelihood

The Wilks' Theorem



Asymptotic distribution of the log-likelihood ratio statistic

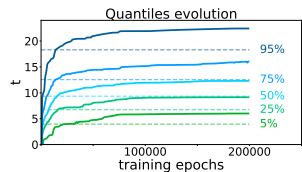
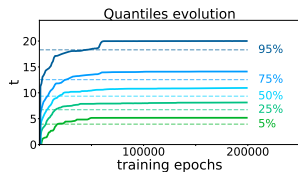
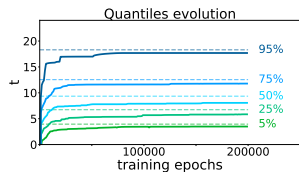
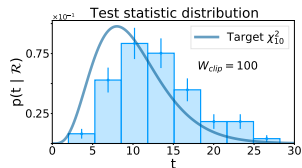
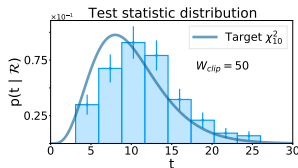
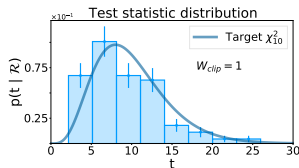
The test statistic is given by

$$\begin{aligned} t(\mathcal{D}) &= 2 \log \left[\frac{e^{-\mathcal{N}(\hat{\mathbf{w}})}}{e^{-\mathcal{N}(\mathcal{R})}} \prod_{x \in \mathcal{D}} \frac{n(x | \hat{\mathbf{w}})}{n(x | \mathcal{R})} \right] \\ &= -2 \min_{\mathbf{w}} \left[\frac{\mathcal{N}(\mathcal{R})}{\mathcal{N}_{\mathcal{R}}} \sum_{x \in \mathcal{R}} \left(e^{f(x; \mathbf{w})} - 1 \right) - \sum_{x \in \mathcal{D}} f(x; \mathbf{w}) \right] \end{aligned}$$

Wilks' theorem states that the $t(\mathcal{D})$ distribution asymptotically approaches a χ^2 **distribution** under the null hypothesis H_0

Tuning the Neural Network

Testing different weight clipping values



Kernel methods:

- $\hat{f}(x) = \sum_i \alpha_i k(x, x_i)$ where $k(x, x') = \exp(\frac{\|x-x'\|^2}{2\sigma^2})$

FalkonML:

- implements the **Nyström approximation**

$$\hat{f}(x) = \sum_i \alpha_i k(x, \tilde{x}_i) \text{ where } \{\tilde{x}_i\}_{i=1}^m \subset \{x_i\}_{i=1}^n$$

- uses the **logistic loss function**

$$L[f] = \frac{N(\mathcal{R})}{N_{\mathcal{R}}} (1-y) \log(1 + e^{f(x; \mathbf{w})}) + y \log(1 + e^{-f(x; \mathbf{w})})$$

- the test statistic $t(\mathcal{D})$ is computed using $f(x; \hat{\mathbf{w}})$