

$$1. \cos q = \frac{1-t^2}{1+t^2} = 2 \cos^2 \frac{1}{2} q - 1$$

$$\cos^2 \frac{1}{2} q = \frac{1}{1+t^2} \rightarrow \cos \frac{q}{2} = \frac{1}{\sqrt{1+t^2}} \quad (B)$$

$$2. \cos x = \frac{\sqrt{5}}{5} = \frac{1}{\sqrt{5}}$$

$\cos x$ positif berada di kuadran I dan IV

$$\operatorname{Ctg} \left(\frac{\phi}{2} - x \right) = \operatorname{tg} x = \pm \frac{2}{1} = \pm 2 \quad (B)$$

$$3. \text{Sudut } C = 90^\circ$$

$$\cos (A+C) = k$$

$$\cos (A+C) = \cos (90^\circ + A)$$

$$= -\sin A$$

$$= k$$

Maka:

$$\sin A = -k$$

$$A+B = 90^\circ$$

$$\cos B = \cos (90^\circ - A)$$

$$= \sin A$$

$$\sin A + \cos B = \sin A + \sin A$$

$$= 2 \sin A$$

$$= -2k \quad (D)$$

$$4. \cos (a-b) = \frac{1}{2} \sqrt{3}$$

$$\cos a \cdot \cos b = \frac{1}{2}$$

$$2 \cos a \cos b = 1$$

$$\cos (a+b) + \cos (a-b) = 1$$

$$\cos (a+b) = 1 - \cos (a-b)$$

$$\frac{\cos (a+b)}{\cos (a-b)} = \frac{1 - \cos (a-b)}{\cos (a-b)}$$

$$= \frac{2}{3} \sqrt{3} - 1 \quad (A)$$

$$5. 2 \cos [x+\phi/4] = 2 \cos x \cos \phi/4 - 2 \sin x \sin \phi/4$$

$$= \frac{1}{2} \sqrt{2} (\cos x + \sin x) \dots \dots (i)$$

$$\cos [x+\phi/4] = \cos x \cdot \cos \phi/4 - \sin x \cdot \sin \phi/4$$

$$= \frac{1}{2} \sqrt{2} (\cos x + \sin x) \dots \dots (ii)$$

Dari persamaan (i) = (ii) didapat :

$$\sqrt{2} (\cos x - \sin x) = \frac{1}{2} \sqrt{2} (\cos x + \sin x)$$

Sehingga :

$$\operatorname{Tg} 2x = 2 \operatorname{tg} x / 1 - \operatorname{tg}^2 x = 3/4 \quad (C)$$

$$6. \cos 4x - 3 \sin 2x + 4 = 0$$

$$\cos (2x + 2x) - 3 \sin 2x + 4 = 0$$

$$1 - 2 \sin^2 2x - 3 \sin 2x + 4 = 0$$

$$2 \sin^2 2x + 3 \sin 2x - 5 = 0$$

$$(2 \sin 2x + 5)(\sin 2x - 1) = 0$$

$$2 \sin 2x + 5 = 0 \rightarrow \sin 2x = -5/2$$

(tak mungkin $-1 \leq \sin a \leq 1$)

$$\sin 2x - 1 = 0$$

$$\sin 2x = 1$$

$$2x = \phi/2$$

$$x = \frac{1}{4} \phi \quad (A)$$

$$7. \text{Misal:}$$

$$\sqrt{3} \cos x - \sin x = k \cos (x-a)$$

Untuk $0 \leq x \leq \phi/2$

Dimana $k = \sqrt{a^2 + b^2}$

$$= \sqrt{(\sqrt{3})^2 + (-1)^2}$$

$$= 2$$

Maka:

$\tan \alpha = b/a = -1/\sqrt{3}$ (dikuadran IV)

$\alpha = -\pi/6$ sehingga :

$$\sqrt{3} \cos x - \sin x = 2 \cos (x + \pi/6) \quad (A)$$

$$8. \sin (2x + 110)^\circ + \sin (2x - 10)^\circ = \frac{1}{2}$$

$$2 \sin (2x + 5)^\circ \cos 60^\circ = \frac{1}{2}$$

$$2 \sin (2x + 5) = \frac{1}{2}$$

$$(1) \quad 2x + 50 = 30 + k \cdot 360$$

$$2x = -20 + k \cdot 360$$

$$x = -10 + k \cdot 180$$

$$x = 170, 350$$

$$(2) \quad 2x + 50 = 150 + k \cdot 360$$

$$2x = 100 + k \cdot 360$$

$$x = 50, 230$$

$$HP = \{50, 170, 230, 350\}$$

$$9. \cos 40^\circ + \cos 80^\circ + \cos 160^\circ$$

$$= 2 \cos 60^\circ \cos 20^\circ + \cos 160^\circ$$

$$= \cos 20^\circ + \cos 160^\circ$$

$$= 2 \cos 90^\circ \cdot \cos 70^\circ$$

$$= 2 \cdot 0 \cdot \cos 70^\circ$$

$$= 0 \quad (C)$$

$$10. \cos \alpha = \frac{36 + 64 - 16}{2 \cdot 8 \cdot 6}$$

$$= \frac{21}{24} \quad (B)$$

$$11. 2 \sin^2 x + 5 \sin x - 3 = 0$$

$$(2 \sin x - 1)(\sin x + 3) = 0$$

$$\sin x = \frac{1}{2}, \cos x = \frac{1}{2} \sqrt{3} \quad (C)$$

$$12. 2 \cos x - 2\sqrt{3} \sin x = k \cos (x - \alpha)$$

$$k = \sqrt{4+12} = 4$$

$$\alpha = \arctan \frac{-2\sqrt{3}}{2},$$

$$\alpha = 300^\circ$$

$$2 \cos x - 2\sqrt{3} \sin x = 4 \cos (x - 300^\circ) \quad (C)$$

$$13. \text{Missal : sudut BAD} = \alpha$$

$$\text{Sudut BCD} = \beta$$

$$\text{Maka } \alpha + \beta = 180^\circ$$

$$= 108^\circ - \alpha$$

Aturan cosinus pada segitiga BAD

$$BD^2 = AB^2 + AD^2 - 2AB \cdot AD \cos \alpha$$

$$= 1 + 16 - 2 \cdot 1 \cdot 4 \cos \alpha$$

$$= 17 - 8 \cos \alpha \quad (1)$$

Aturan cosinus pada segitiga BCD

$$BD^2 = BC^2 + CD^2 - 2BC \cdot CD \cos \beta$$

$$= 4 + 9 - 2 \cdot 2 \cdot 3 \cos (180 - \alpha)$$

$$= 13 + 12 \cos \alpha \quad (2)$$

$$(1) \& (2) : 17 - 8 \cos \alpha = 13 + 12 \cos \alpha$$

$$4 = 2 \cos \alpha$$

$$\cos \alpha = \frac{1}{5} \quad (C)$$

14. $\sin 105^\circ \cos 15^\circ + 2 \cos 75^\circ \sin 45^\circ$
 $= \frac{1}{2} \sin 120^\circ + \frac{1}{2} \sin 90^\circ + \sin 120^\circ - \sin 30^\circ$
 $= \frac{1}{2} \cdot \frac{1}{2} \sqrt{3} + \frac{1}{2} \cdot 1 + \frac{1}{2} \cdot \sqrt{3} - \frac{1}{2} = \frac{3}{4} \sqrt{3}$ (D)
15. $\sin (3x - 20)^\circ + \cos (x + 10)^\circ = \sin (3x - 20)^\circ + \sin (80 - x)^\circ$
 $= 2 \sin \frac{1}{2} (3x - 20 + 80 - x)^\circ \cos \frac{1}{2} (3x - 20 - 80 + x)^\circ$
 $= 2 \sin (x + 30)^\circ \cdot \cos (2x - 50)^\circ$ (C)
16. Grafik tersebut adalah grafik dari $y = 2 \sin x$ digeser ke kiri sejauh $\phi/2$, sehingga persamaan menjadi : $y = 2 \sin (x + \phi/2)$ (C)
17. $2 \sin x \cos x - \sqrt{3} \cos 2x - 1 = \sin 2x - \sqrt{3} \cos 2x - 1 = 0$
 $2 \cos (2x - 150)^\circ = 1$
 $\cos (2x - 150)^\circ = \frac{1}{2}$
 $\cos (2x - 150)^\circ = \cos 60^\circ$
 (i) $2x - 150^\circ = 60^\circ + n \cdot 360^\circ$
 $X = 105^\circ + n - 180^\circ$
 $X = 105^\circ, 295^\circ$
 (ii) $2x - 150 = -60^\circ + n \cdot 360^\circ$
 $X = 45^\circ + N \cdot 180^\circ$
 $X = 45^\circ, 225^\circ$ (D)
18. $\cos 465^\circ - \cos 165^\circ = -2 \sin 315^\circ \cdot \sin 150^\circ$
 $= -2 - \frac{1}{2} \sqrt{2} \cdot \frac{1}{2}$
 $= \frac{1}{2} \sqrt{2}$ (A)
19. Dengan aturan cosinus
 $BC^2 = 10^2 + 6^2 - 2 \cdot 10 \cdot 6 \cos 60$
 $= 136 - 60$
 $= 2 \sqrt{19}$ (A)
20. Segitga 1
 $\cos A = \frac{3}{5}$
 $\sin A = \frac{4}{5}$
 Segitiga 2
 $\sin B = \frac{12}{13}$
 $\cos B = -\frac{5}{13}$ (negative Karena tumpul)
 $\cos (A - B) = \cos A \cos B + \sin A \cdot \sin B$
 $= \frac{3}{5} \cdot -\frac{5}{13} + \frac{4}{5} \cdot \frac{12}{13} = \frac{33}{65}$ (C)
21. Bentuk umum grafik pada soal
 $y = a \sin n(x + \alpha)^\circ$, $-\alpha$: pergeseran 60° ke kanan, $a = 2$, periode $2\phi/n = 180$
 $y = 2 \sin 2 (x + 60)^\circ \rightarrow n = 2$
 $y = 2 \sin (2x - 120)^\circ$ (C)
22. $\cos \alpha + \cos \beta = 2 \cos (\alpha + \beta / 2) \cos (\alpha - \beta) / 2$
 $\cos (2x + 30)^\circ + \cos (2x - 30)^\circ < \frac{1}{2} \sqrt{3}$
 $2 \cos 2x \cos 30^\circ < \frac{1}{2} \sqrt{3}$
 $2 \cos 2x \cdot \frac{1}{2} \sqrt{3} < \frac{1}{2} \sqrt{3}$
 $\cos 2x < \frac{1}{2}$
 $60^\circ < 2x < 300^\circ$ atau $420^\circ < 2x < 660^\circ$
 $30^\circ < x < 150^\circ$ atau $210^\circ < x < 330^\circ$ (B)
23. $\sqrt{3} \cos x + \sin x = \sqrt{2}$, $0 \leq x < 2\phi$
 Rumus : $a \cos x + b \sin x = c$
 $k \cos (x - \alpha) = c$; $k = \sqrt{a^2 + b^2}$
 $\alpha = \arctan b/a$

$$K = \sqrt{3+1} \quad \alpha = \arctan \frac{1}{\sqrt{3}}$$

$$= 2 \quad = 30$$

$$2 \cos (x-30^\circ) = \sqrt{2}$$

$$\cos (x-30^\circ) = \frac{1}{2} \sqrt{2}$$

$$x-30^\circ = 45^\circ \text{ atau } x-30^\circ = 315^\circ$$

$$x = 75^\circ \quad x = 345^\circ$$

$$= \frac{5}{12} \pi \quad x = \frac{23}{12} \pi \quad (D)$$

$$24. \sin 105^\circ - \sin 15^\circ / \cos 75^\circ - \cos 15^\circ = 2 \cos 60^\circ \sin 45^\circ / -2 \sin 45^\circ \sin 30^\circ$$

$$= -1 \quad (B)$$

$$25. \cos 75^\circ = \cos (45^\circ + 30^\circ)$$

$$= \cos 45^\circ \cos 30^\circ - \sin 45^\circ \sin 30^\circ$$

$$= \frac{1}{2} \sqrt{2} \cdot \frac{1}{2} \sqrt{3} - \frac{1}{2} \sqrt{2} \cdot \frac{1}{2}$$

$$= \frac{1}{4} \sqrt{6} - \frac{1}{4} \sqrt{2}$$

$$= \frac{1}{4} (\sqrt{6} - \sqrt{2}) \quad (B)$$

$$26. \sin \alpha = \frac{12}{13} \rightarrow \cos \alpha = \frac{5}{13}$$

$$\cos \beta = -\frac{3}{5} \rightarrow \sin \beta = \frac{4}{5}$$

$$\sin \theta = \sin (180^\circ - (\alpha + \beta))$$

$$= \sin (\alpha + \beta)$$

$$= \sin \alpha \cos \beta + \sin \beta \cos \alpha$$

$$= \frac{12}{13} \cdot -\frac{3}{5} + \frac{4}{5} \cdot \frac{5}{13} \rightarrow -\frac{36}{65} + \frac{20}{65}$$

$$= -\frac{16}{65} \quad (B)$$

$$27. \cos \alpha \cos \beta = \frac{48}{65}$$

$$\tan \alpha - \tan \beta = \frac{1}{3}$$

$$\sin \alpha / \cos \alpha \cdot \sin \beta / \cos \beta = \frac{1}{3}$$

$$\sin (\alpha - \beta) / \cos \alpha \cdot \cos \beta = \frac{1}{3}$$

$$\sin (\alpha - \beta) = \frac{1}{3} \cos \alpha \cos \beta$$

$$= \frac{1}{3} \cdot \frac{48}{65}$$

$$= \frac{16}{65} \quad (C)$$

$$28. CT = x/\sqrt{2} \rightarrow AC = \sqrt{AT^2 + CT^2}$$

$$= \sqrt{\left(\frac{9}{2}\right)^2 + \left(\frac{1}{2}x\right)^2}$$

$$= x\sqrt{5}$$

$$\cos A = TA/AC = \frac{3/2 \cdot \sqrt{2}}{x\sqrt{5}} \rightarrow \cos A = \frac{3}{10\sqrt{10}} \quad (A)$$

$$29. \sin 2x + 2 \cos x = 0 ; 0 < x < 2\pi$$

$$2 \sin x \cos x + 2 \cos x = 0$$

$$\cos x = 0 \text{ atau } \sin x = -1$$

$$x = 90^\circ, 270^\circ \quad x = \frac{3\pi}{2}$$

$$\text{Himpunan penyelesaian } (\frac{\pi}{2}, \frac{3\pi}{2}) \quad (D)$$

$$30. BC = CD = a$$

$$AD = a \tan x$$

$$AB = \sqrt{(2a)^2 + (a^2 \tan^2 x)}$$

$$= a \sqrt{4 + \tan^2 x}$$

$$\sin B = \frac{a \tan x}{a \sqrt{4 + \tan^2 x}}$$

$$= \frac{\tan x}{\sqrt{4 + \tan^2 x}} \quad (B)$$