

1. diketahui  $\cos \alpha = 4/5$  ; dimana  $\cos \alpha = x/r$

$$x = 4 \quad r = 5 \quad r = \sqrt{x^2 + y^2}$$

$$r^2 = x^2 + y^2$$

$$y^2 = r^2 - x^2$$

$$= 25 - 16$$

$$= 9$$

$Y = \sqrt{9} = \pm 3$  karena sudut lancip berada di kuadran 1 maka nilai yang diambil adalah +3

Sehingga  $\sin a = y/r = 3/5$

\*diketahui  $\cos b = 24/25$  ; dimana  $\cos b = x/r$

$$Y^2 = r^2 - x^2$$

$$= 625 - 576$$

$$= 49$$

$Y = \sqrt{49} = 7$  (sudut lancip); sehingga  $\sin b = y/r = 7/25$

$\cos(a-b)$  dari rumus dijabarkan menjadi  $\cos(a-b) = \cos a \cos b + \sin a \sin b$

Masukan nilai - nilai diatas:

$$= 4/5 \cdot 24/25 + 3/5 \cdot 7/25$$

$$= 96/125 + 21/125 = 117/125$$

2. gunakan aturan cosinus

$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$2ab \cos C = a^2 + b^2 - c^2$$

$$\cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

$$= \frac{4^2 + 5^2 - 3^2}{2 \cdot 4 \cdot 5} = \frac{38}{40} = \frac{19}{20}$$

3. berada di kuadran kedua berarti x nya negative

kuadran I  $x = +$  ;  $y = +$

kuadran II  $x = -$  ;  $y = +$

kuadran III  $x = -$  ;  $y = -$

kuadran IV  $x = +$  ;  $y = -$

$\cos A = 4/5$  karena di kuadran kedua maka nilai  $\cos A = -4/5$

$$\cos A = -4/5 = x/r$$

$$r^2 = x^2 + y^2$$

$$y^2 = r^2 - x^2$$

$$= 25 - 16$$

$$= 9$$

$Y = 3$  sehingga  $\sin A = y/r = 3/5$

$$\sin 2A = 2 \sin A \cos A$$

$$= 2 \cdot 3/5 \cdot -4/5 = -24/25$$

4.  $1 - \cos 4x / 2 = \frac{1}{2} - \cos 4x / 2$

$$= \frac{1}{2} - \cos(2x+2x) / 2$$

$$= \frac{1}{2} - \cos 2x \cos 2x - \sin 2x \sin 2x / 2$$

$$= \frac{1}{2} - \cos^2 2x - \sin^2 2x / 2$$

$$= \frac{1}{2} - (1 - 2\sin^2 2x) / 2$$

$$= \frac{1}{2} - \frac{1}{2} + \sin^2 2x$$

$$= \sin^2 2x$$

$$5. (1 - \cos a / \sin a)^2 = (\sqrt{3}/3)^2$$

$$1 - 2\cos a + \cos^2 a / \sin^2 a = 1/3$$

$$1 - 2\cos a + \cos^2 a / 1 - \cos^2 a = 1/3$$

$$1 - 2\cos a + \cos^2 a = 1/3 (1 - \cos^2 a)$$

$$1 - 2\cos a + \cos^2 a = 1/3 - 1/3 \cos^2 a$$

$$2/3 - 2\cos a + 4/3 \cos^2 a = 0$$

$$4/3 \cos^2 a - 2\cos a + 2/3 = 0 \quad \times 3$$

$$4 \cos^2 a - 6\cos a + 2 = 0$$

Pakai rumus ABC :

$$6 \pm \sqrt{36 - 32} / 8$$

Masukan kedalam persamaan:

$$a = 0^\circ \quad a = 60^\circ$$

$$1 - \cos a / \sin a = \sqrt{3} / 3 = \text{memenuhi}$$

Sehingga nilai  $a = 60^\circ$

$$6. \sin 6x + \sin 4x / \cos 6x + \cos 4x = 2 \sin \frac{1}{2} (6x+4x) / 2 \cos \frac{1}{2} (6x+4x) \cos \frac{1}{2} (6x-4x) \\ = \tan \frac{1}{2} 10x = \tan 5x$$

$$7. \sin x + \cos x = (\sin x + \cos x)^2 = 0^2$$

$$= 1 + \sin 2x = 0$$

$$= \sin 2x = -1$$

$$\text{Sehingga HP} = \{135^\circ, 315^\circ\}$$

$$8. -1 < 3-2a / a-4 \leq 1 \quad \text{-----} \rightarrow 3-2a / a-4 \geq -1 \text{ n } 3-2a / a-4 \leq 1$$

$$\text{-----} \rightarrow -a-1 / a-4 \geq 0 \text{ n } 7-3a / a-4 \geq 0$$

Jadi banyak anggota himpunan penyelesaian yang merupakan bilangan bulat ada 4 buah

$$9. \cos 105 = \cos 60 \cdot \cos 45 - \sin 60 \cdot \sin 45$$

$$\cos 105 = \frac{1}{4} \sqrt{2}(1 - \sqrt{3})$$

$$10. \cos 75 = \cos(30+45)$$

$$\cos 75 = \cos 30 \cdot \cos 45 - \sin 30 \cdot \sin 45$$

$$\cos 75 = \frac{1}{4} \sqrt{6} - \frac{1}{4} \sqrt{2}$$

$$11. \text{Jadi } \cos(a+b) = \cos a \cdot \cos b - \sin a \cdot \sin b$$

$$= 3/15 \times 5/13 - 4/5 \times 12/13 = -33/65$$

$$12. \cos(63+87) = \cos 150$$

$$= \cos(90+60) = -\sin 60$$

$$13. \sin 105 = \sin(60+45)$$

$$= \frac{1}{2} \sqrt{3} \cdot \frac{1}{2} \sqrt{2} + \frac{1}{2} \cdot \frac{1}{2} \sqrt{2}$$

$$= \frac{1}{4} \sqrt{2} (1 + \sqrt{3})$$

$$14. \sin 75 = \sin(30+45)$$

$$= \frac{1}{2} \cdot \frac{1}{2} \sqrt{2} + \frac{1}{2} \sqrt{3} \cdot \frac{1}{2} \sqrt{2}$$

$$= \frac{1}{4} \sqrt{6} + \frac{1}{4} \sqrt{2}$$

$$15. \sin(a+b) = \sin a \cdot \cos b + \cos a \cdot \sin b = 4/15 \times 5/13 + 3/5 \times 12/13 = 20/65 + 36/65$$

$$= 56/65$$

$$16. \sin 63 \cdot \cos 87 + \cos 63 \cdot \sin 87 = \sin(63+87) = \sin(150) = \frac{1}{2}$$

$$17. \cos 15 = \cos(60-45)$$

$$= \frac{1}{2} \cdot \frac{1}{2} \sqrt{2} + \frac{1}{2} \sqrt{3} \cdot \frac{1}{2} \sqrt{2}$$

$$= \frac{1}{4} \sqrt{2} (1 + \sqrt{3})$$

$$\begin{aligned}
 18. \cos(-15) &= \cos 30 \cdot \cos 45 + \sin 30 \cdot \sin 45 \\
 &= \frac{1}{2} \sqrt{3} \cdot \frac{1}{2} \sqrt{2} + \frac{1}{2} \cdot \frac{1}{2} \sqrt{2} \\
 &= \frac{1}{4} \sqrt{6} + \frac{1}{4} \sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 19. \cos(a-b) &= \cos a \cdot \cos b + \sin a \cdot \sin b = \frac{3}{15} \cdot \frac{5}{13} + \frac{4}{5} \cdot \frac{12}{13} \\
 &= \frac{63}{65}
 \end{aligned}$$

$$20. \cos 70 \cdot \cos 25 + \sin 70 \cdot \sin 25 = \cos (70 - 25) = \cos 45 = \frac{1}{2} \sqrt{2}$$