

ARC-Check

October 17, 2022

```
[9]: import matplotlib.pyplot as plt # Import library for direct plotting functions
# if using a Jupyter notebook, include:
%matplotlib inline
import matplotlib as mpl
import numpy as np # Import Numerical Python
#from IPython.core.display import display, HTML #Import HTML for formatting
→output

# NOTE: Uncomment following lines ONLY if you are not using installation via pip
# import sys, os
# rootDir = '/path/to/arc/directory' # e.g. '/Users/Username/Desktop/'
→ARC-Alkali-Rydberg-Calculator'
# sys.path.insert(0,rootDir)
# import sys, os
# sys.path.insert(0,"..")

import arc
from arc import * #Import ARC (Alkali Rydberg Calculator)

calc = PairStateInteractions(
    Rubidium(),
    61, 0, 0.5,
    61, 0, 0.5,
    0.5, 0.5,
    s=0.5,
    atom2=Rubidium(),
    s2=0.5
)
theta=0; #Polar Angle [0-pi]
phi=0; #Azimuthal Angle [0-2pi]
dn = 1; #Range of n to consider (n0-dn:n0+dn)
dl = 1; #Range of l values
deltaMax = 25e9 #Max pair-state energy difference [Hz]

RLeRoy = calc.getLeRoyRadius()
print("LeRoy radius = %.1f mum" % RLeRoy)
```

```

RvdW=calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=False,minStateContribution=0)
print("vdW radius = %.1f mum" % RvdW)
calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=1)

c6 = calc.getC6perturbatively(theta,phi, dn, deltaMax)
print("C_6 = %.5f GHz (mu m)^6" % (c6))

#-----

#Generate pair-state interaction Hamiltonian
calc.defineBasis(theta,phi, dn,dl, deltaMax,progressOutput=True,
    →debugOutput=False)
#Diagonalise
r=np.linspace(RLeRoy,10,100)
nEig=150 #Number of eigenstates to extract
calc.diagonalise(r,nEig,progressOutput=True)
#Plot
calc.plotLevelDiagram()
#Zoom-on on pair state
calc.ax.set_xlim(0,10)
calc.ax.set_ylim(-2,2)
calc.showPlot() # by default program will plot interactive plots
# however plots are interactive only if open oin standard window
# and not in the %inline mode of the notebooks
rvdw = calc.getVdwFromLevelDiagram(1.000000,8.000000,minStateContribution=0.
    →6,showPlot=True)
calc.getC3fromLevelDiagram(RLeRoy, 5+rvdw*0.
    →99,showPlot=True,minStateContribution=0)
calc.getC6fromLevelDiagram(RLeRoy, 10.,showPlot=True,minStateContribution=0)

#calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=0)

```

LeRoy radius = 1.1 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

vdW radius = 0.0 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

C_6 = -169.20012 GHz (mu m)⁶

Calculating Hamiltonian matrix...

matrix (dimension 19)

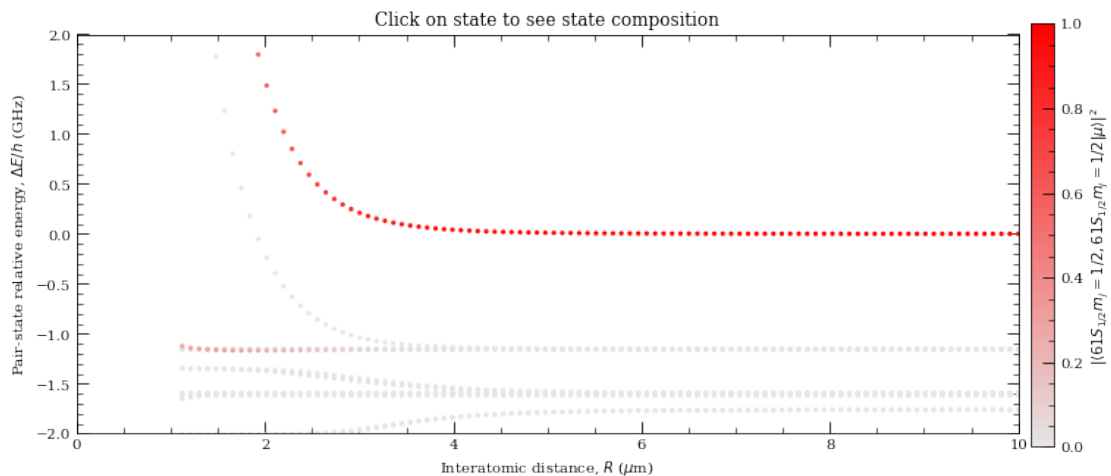
Matrix R3 100.0 % (state 11 of 11)

Warning: Requested number of eigenvectors >=dimension-1

ARPACK can only find up to dimension-1 eigenvectors, where dimension is matrix dimension.

Diagonalizing interaction matrix...

99% Now we are plotting...

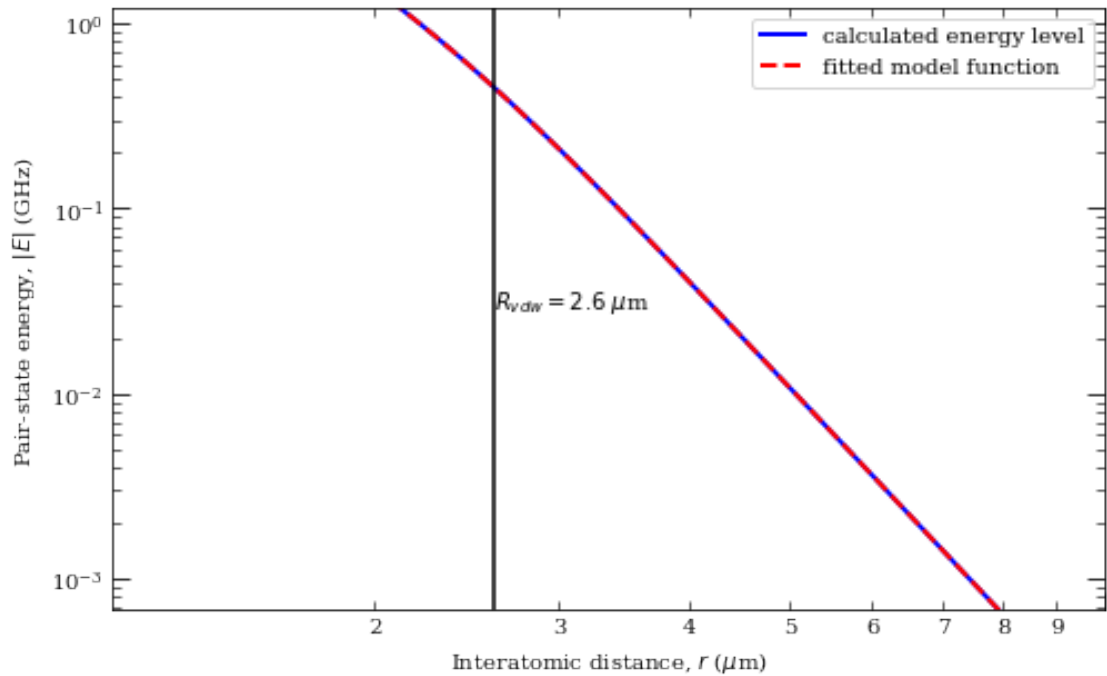


Data points to fit = 66

Rvdw = 2.6043704564694843 μm

offset = 3.552643445906704e-07

scale = -18.108836030539134



```

/Users/ahmedm.farouk/opt/anaconda3/lib/python3.7/site-
packages/arc/calculations_atom_pairstate.py:2240: RuntimeWarning: invalid value
encountered in log

```

```

    return np.log(c3 / r**3 + offset)

```

```

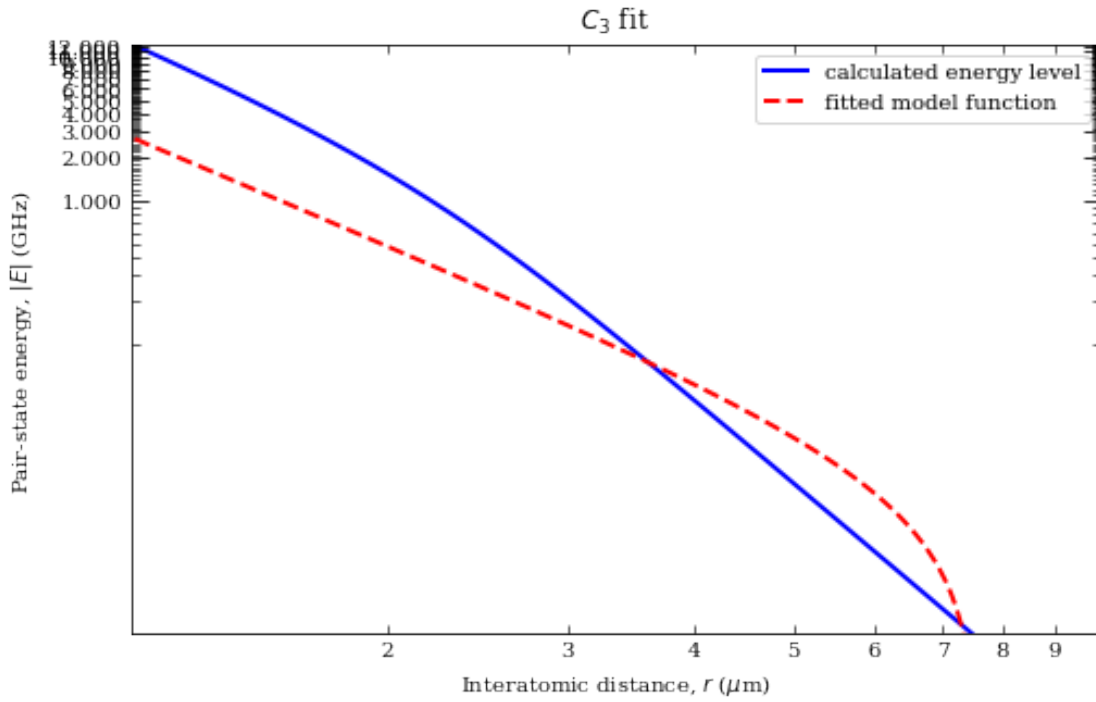
c3 = 3.9187382988074417 GHz /R^3 (mu m)^3

```

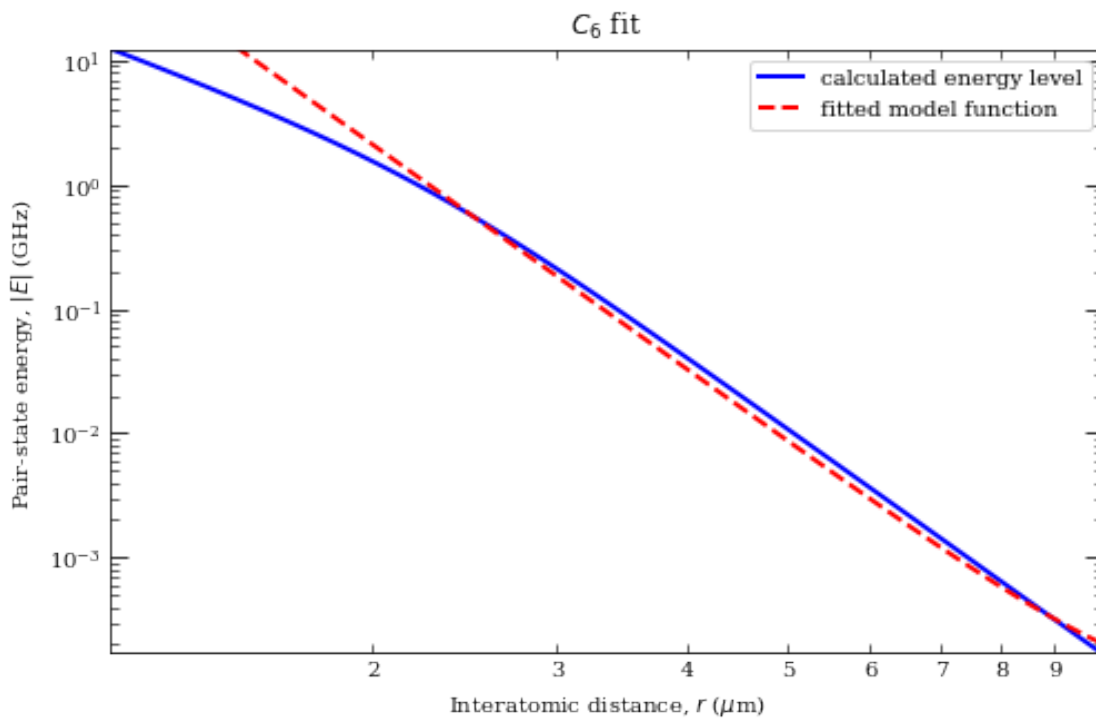
```

offset = -0.00896395381635674

```



$c_6 = 134.55160767062722 \text{ GHz} / R^6 (\mu\text{m})^6$
 $\text{offset} = 6.888234984185386\text{e-}05$



[9]: 134.55160767062722

```
[10]: import matplotlib.pyplot as plt # Import library for direct plotting functions
# if using a Jupyter notebook, include:
%matplotlib inline
import matplotlib as mpl
import numpy as np # Import Numerical Python
from IPython.core.display import display, HTML #Import HTML for formatting
→output

# NOTE: Uncomment following lines ONLY if you are not using installation via pip
# import sys, os
# rootDir = '/path/to/arc/directory' # e.g. '/Users/Username/Desktop/
→ARC-Alkali-Rydberg-Calculator'
# sys.path.insert(0,rootDir)
# import sys, os
# sys.path.insert(0,"..")

import arc
from arc import * #Import ARC (Alkali Rydberg Calculator)

calc = PairStateInteractions(
    Caesium(),
    65, 0, 0.5,
    65, 0, 0.5,
    0.5, 0.5,
    s=0.5,
    atom2=Caesium(),
    s2=0.5
)
theta=0; #Polar Angle [0-pi]
phi=0; #Azimuthal Angle [0-2pi]
dn = 1; #Range of n to consider (n0-dn:n0+dn)
dl = 1; #Range of l values
deltaMax = 25e9 #Max pair-state energy difference [Hz]

RLeRoy = calc.getLeRoyRadius()
print("LeRoy radius = %.1f mum" % RLeRoy)

RvdW=calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=False,minStateContribution=0)
print("vdW radius = %.1f mum" % RvdW)
calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=1)
```

```

c6 = calc.getC6perturbatively(theta,phi, dn, deltaMax)
print("C_6 = %.5f GHz (mu m)^6" % (c6))

#-----

#Generate pair-state interaction Hamiltonian
calc.defineBasis(theta,phi, dn,dl, deltaMax,progressOutput=True,
↳debugOutput=False)
#Diagonalise
r=np.linspace(RLeRoy,10,100)
nEig=150 #Number of eigenstates to extract
calc.diagonalise(r,nEig,progressOutput=True)
#Plot
calc.plotLevelDiagram()
#Zoom-on on pair state
calc.ax.set_xlim(0,10)
calc.ax.set_ylim(-2,2)
calc.showPlot() # by default program will plot interactive plots
# however plots are interactive only if open oin standard window
# and not in the %inline mode of the notebooks
rvdw = calc.getVdwFromLevelDiagram(1.000000,8.000000,minStateContribution=0.
↳6,showPlot=True)
calc.getC3fromLevelDiagram(RLeRoy, 5+rvdw*0.
↳99,showPlot=True,minStateContribution=0)
calc.getC6fromLevelDiagram(RLeRoy, 10.,showPlot=True,minStateContribution=0)

#calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=0)

```

LeRoy radius = 1.2 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

vdW radius = 0.0 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

C_6 = -269.00000 GHz (mu m)^6

Calculating Hamiltonian matrix...

matrix (dimension 21)

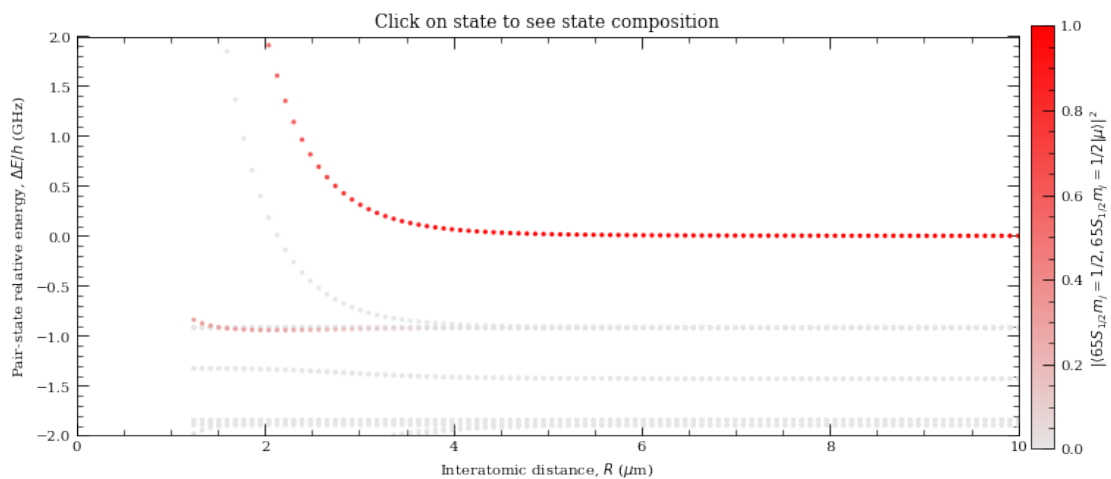
Matrix R3 100.0 % (state 13 of 13)

Warning: Requested number of eigenvectors \geq dimension-1

ARPACK can only find up to dimension-1 eigenvectors, where dimension is matrix dimension.

Diagonalizing interaction matrix...

99% Now we are plotting...

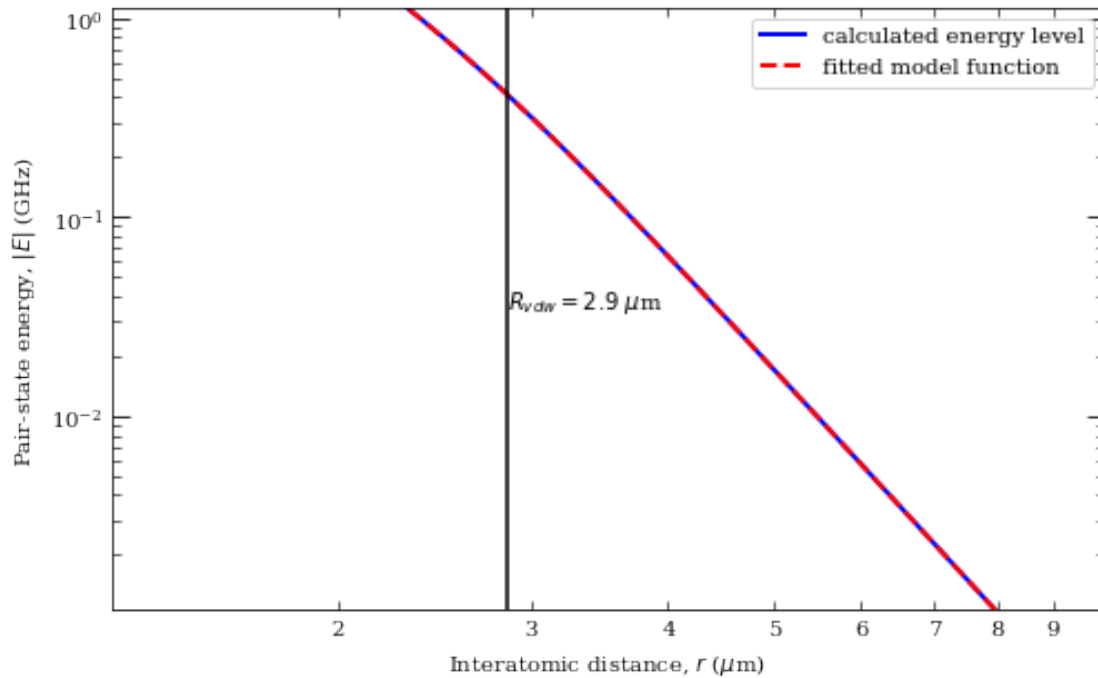


Data points to fit = 65

Rvdw = 2.856455173893658 μm

offset = $-3.610096921172615 \times 10^{-7}$

scale = -22.10967392295105

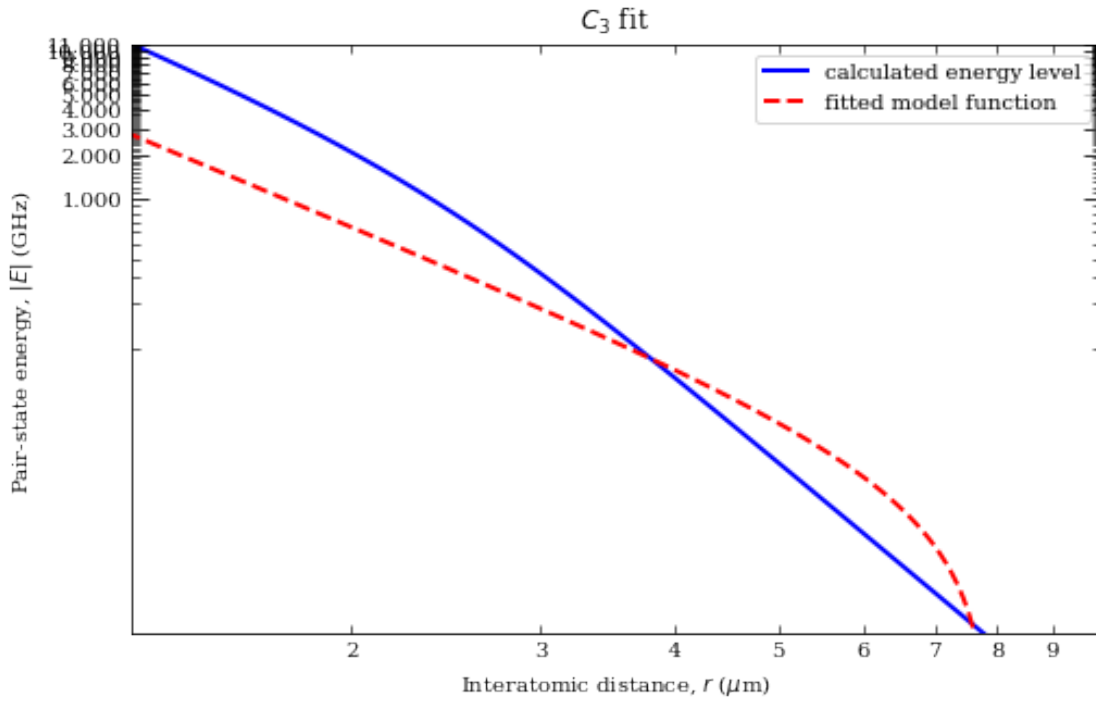


```
/Users/ahmedm.farouk/opt/anaconda3/lib/python3.7/site-
packages/arc/calculations_atom_pairstate.py:2240: RuntimeWarning: invalid value
encountered in log
```

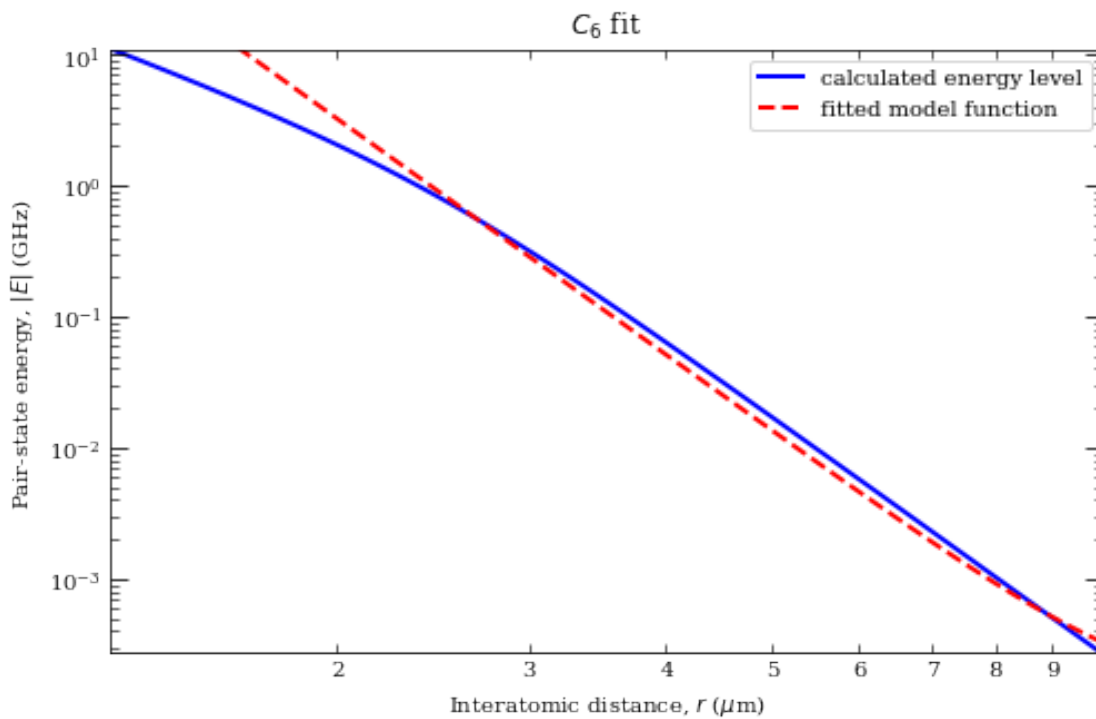
```
    return np.log(c3 / r**3 + offset)
```

```
c3 = 5.266593366950124 GHz /R^3 (mu m)^3
```

```
offset = -0.010681022505011132
```



$c_6 = 209.5677244576279 \text{ GHz} / R^6 (\mu\text{m})^6$
 offset = 0.00011906896382412626



[10]: 209.5677244576279

```
[8]: import matplotlib.pyplot as plt # Import library for direct plotting functions
# if using a Jupyter notebook, include:
%matplotlib inline
import matplotlib as mpl
import numpy as np # Import Numerical Python
from IPython.core.display import display, HTML #Import HTML for formatting
→output

# NOTE: Uncomment following lines ONLY if you are not using installation via pip
# import sys, os
# rootDir = '/path/to/arc/directory' # e.g. '/Users/Username/Desktop/
→ARC-Alkali-Rydberg-Calculator'
# sys.path.insert(0,rootDir)
# import sys, os
# sys.path.insert(0,"..")

import arc
from arc import * #Import ARC (Alkali Rydberg Calculator)

calc = PairStateInteractions(
    Rubidium(),
    67, 0, 0.5,
    69, 0, 0.5,
    0.5, 0.5,
    s=0.5,
    atom2=Rubidium(),
    s2=0.5
)
theta=0; #Polar Angle [0-pi]
phi=0; #Azimuthal Angle [0-2pi]
dn = 1; #Range of n to consider (n0-dn:n0+dn)
dl = 1; #Range of l values
deltaMax = 25e9 #Max pair-state energy difference [Hz]

RLeRoy = calc.getLeRoyRadius()
print("LeRoy radius = %.1f mum" % RLeRoy)

RvdW=calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=False,minStateContribution=0)
print("vdW radius = %.1f mum" % RvdW)
calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=1)
```

```

c6 = calc.getC6perturbatively(theta,phi, dn, deltaMax)
print("C_6 = %.5f GHz (mu m)^6" % (c6))

#-----

#Generate pair-state interaction Hamiltonian
calc.defineBasis(theta,phi, dn,dl, deltaMax,progressOutput=True,
    →debugOutput=False)
#Diagonalise
r=np.linspace(RLeRoy,10,100)
nEig=150 #Number of eigenstates to extract
calc.diagonalise(r,nEig,progressOutput=True)
#Plot
calc.plotLevelDiagram()
#Zoom-on on pair state
calc.ax.set_xlim(0,10)
calc.ax.set_ylim(-2,2)
calc.showPlot() # by default program will plot interactive plots
# however plots are interactive only if open oin standard window
# and not in the %inline mode of the notebooks
rvdw = calc.getVdwFromLevelDiagram(1.000000,8.000000,minStateContribution=0.
    →6,showPlot=True)
calc.getC3fromLevelDiagram(RLeRoy, 5+rvdw*0.
    →99,showPlot=True,minStateContribution=0)
calc.getC6fromLevelDiagram(RLeRoy, 10.,showPlot=True,minStateContribution=0)

#calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=0)

```

LeRoy radius = 1.4 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

vdW radius = 0.0 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

C_6 = 32553.11707 GHz (mu m)^6

Calculating Hamiltonian matrix...

matrix (dimension 49)

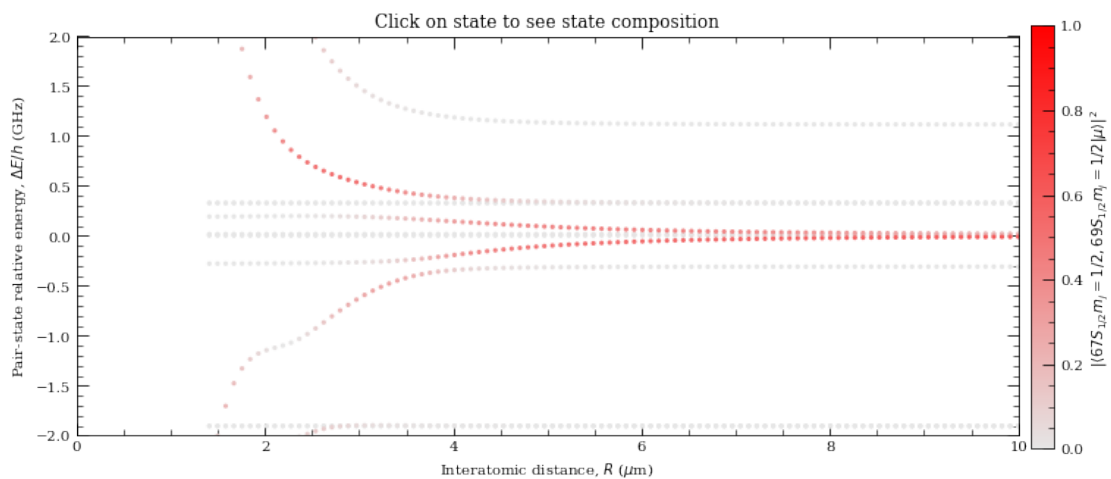
Matrix R3 100.0 % (state 27 of 27)

Warning: Requested number of eigenvectors >=dimension-1

ARPACK can only find up to dimension-1 eigenvectors, where dimension is matrix dimension.

Diagonalizing interaction matrix...

99% Now we are plotting...



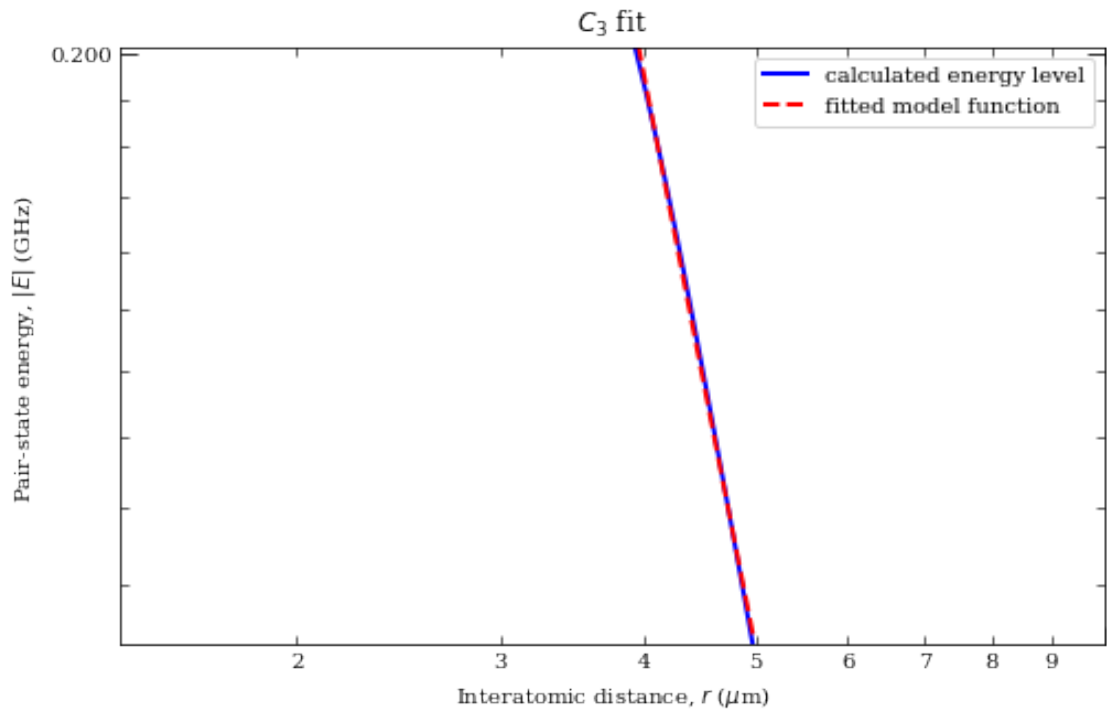
Data points to fit = 0

index 0 is out of bounds for axis 0 with size 0

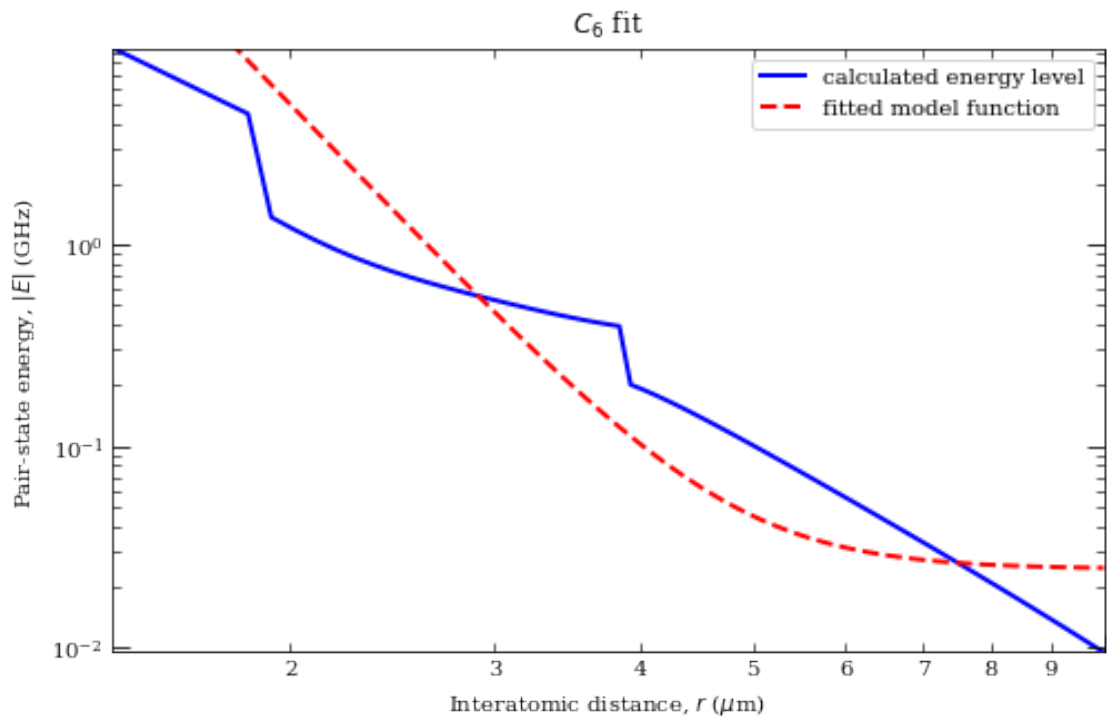
ERROR: unable to find a fit for van der Waals distance.

$c3 = 12.180880082658248 \text{ GHz} / R^3 (\mu\text{m})^3$

offset = 0.004645560531022837



$c_6 = 319.0668493251698 \text{ GHz} / R^6 (\mu\text{m})^6$
 offset = 0.02448343261711797



[8]: 319.0668493251698

[]:

```
[11]: import matplotlib.pyplot as plt # Import library for direct plotting functions
# if using a Jupyter notebook, include:
%matplotlib inline
import matplotlib as mpl
import numpy as np # Import Numerical Python
#from IPython.core.display import display, HTML #Import HTML for formatting
→output

# NOTE: Uncomment following lines ONLY if you are not using installation via pip
# import sys, os
# rootDir = '/path/to/arc/directory' # e.g. '/Users/Username/Desktop/'
→ARC-Alkali-Rydberg-Calculator'
# sys.path.insert(0,rootDir)
# import sys, os
# sys.path.insert(0,"..")

import arc
from arc import * #Import ARC (Alkali Rydberg Calculator)

calc = PairStateInteractions(
    Rubidium(),
    61, 0, 0.5,
    65, 0, 0.5,
    0.5, 0.5,
    s=0.5,
    atom2=Caesium(),
    s2=0.5
)
theta=0; #Polar Angle [0-pi]
phi=0; #Azimuthal Angle [0-2pi]
dn = 1; #Range of n to consider (n0-dn:n0+dn)
dl = 1; #Range of l values
deltaMax = 25e9 #Max pair-state energy difference [Hz]

RLeRoy = calc.getLeRoyRadius()
print("LeRoy radius = %.1f mum" % RLeRoy)

RvdW=calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=False,minStateContribution=0)
print("vdW radius = %.1f mum" % RvdW)
```

```

calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=1)

c6 = calc.getC6perturbatively(theta,phi, dn, deltaMax)
print("C_6 = %.5f GHz (mu m)^6" % (c6))

#-----

#Generate pair-state interaction Hamiltonian
calc.defineBasis(theta,phi, dn,dl, deltaMax,progressOutput=True,
↳debugOutput=False)
#Diagonalise
r=np.linspace(RLeRoy,10,100)
nEig=150 #Number of eigenstates to extract
calc.diagonalise(r,nEig,progressOutput=True)
#Plot
calc.plotLevelDiagram()
#Zoom-on on pair state
calc.ax.set_xlim(0,10)
calc.ax.set_ylim(-2,2)
calc.showPlot() # by default program will plot interactive plots
# however plots are interactive only if open oin standard window
# and not in the %inline mode of the notebooks
rvdw = calc.getVdwFromLevelDiagram(1.000000,8.000000,minStateContribution=0.
↳6,showPlot=True)
calc.getC3fromLevelDiagram(RLeRoy, 5+rvdw*0.
↳99,showPlot=True,minStateContribution=0)
calc.getC6fromLevelDiagram(RLeRoy, 10.,showPlot=True,minStateContribution=0)

#calc.getVdwFromLevelDiagram(RLeRoy,10,showPlot=True,minStateContribution=0)

```

LeRoy radius = 1.2 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

vdW radius = 0.0 mum

ERROR: could not find data for energy levels for interatomic distances between 1 and 10.00 mu m.

C_6 = 4022.69858 GHz (mu m)^6

Calculating Hamiltonian matrix...

matrix (dimension 27)

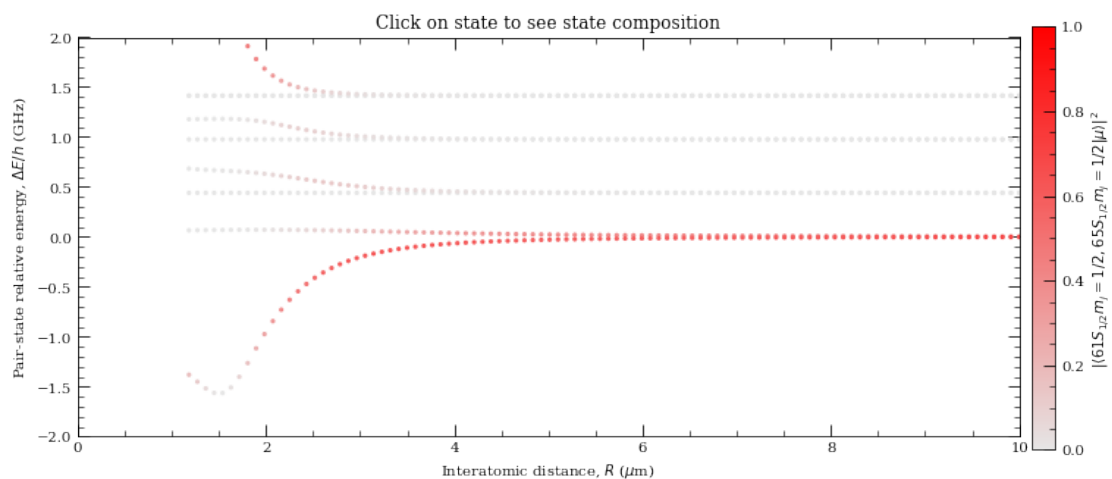
Matrix R3 100.0 % (state 15 of 15)

Warning: Requested number of eigenvectors >=dimension-1

ARPACK can only find up to dimension-1 eigenvectors, where dimension is matrix dimension.

Diagonalizing interaction matrix...

99% Now we are plotting...



Data points to fit = 8

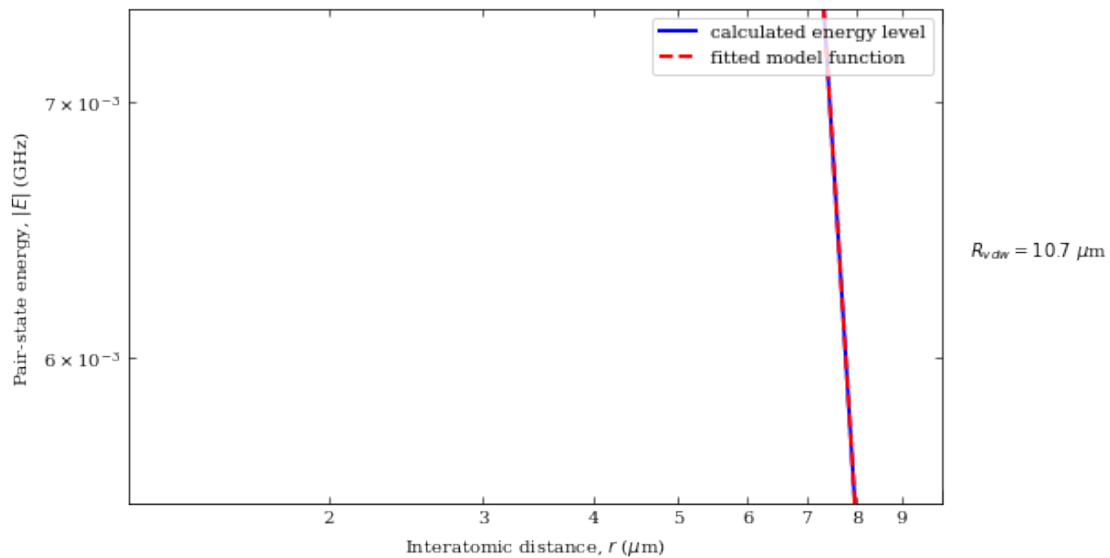
WARNING: vdw radius seems to be outside the fitting range!

It's estimated to be around 10.75 μm from the current fit.

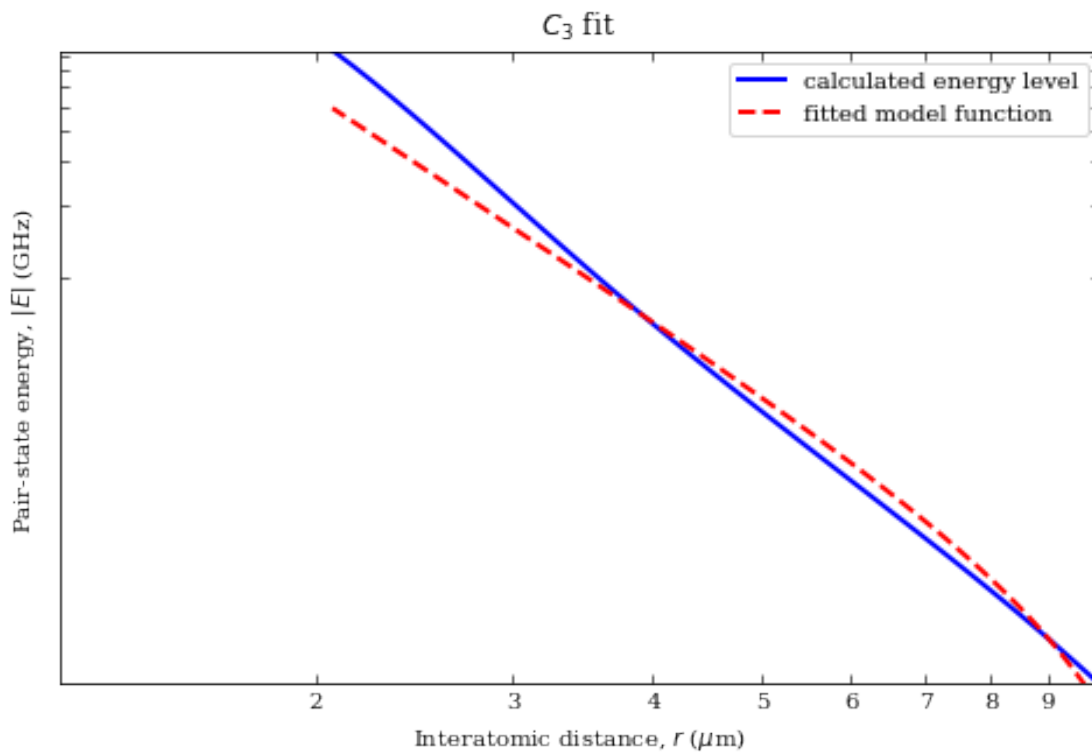
Rvdw = 10.74846057407525 μm

offset = -0.000553743466147596

scale = -3.6803683102701825

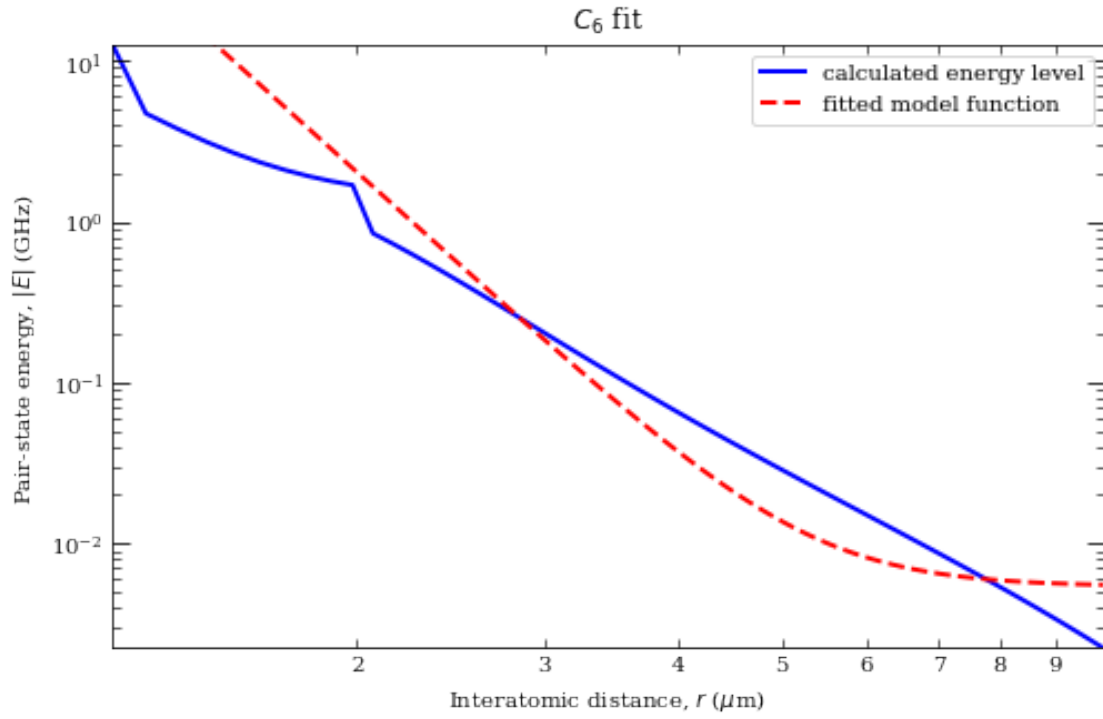


$c_3 = 4.4013765753340115 \text{ GHz} / R^3 (\mu\text{m})^3$
 offset = -0.0026067120665210874



$c_6 = 130.15517041731948 \text{ GHz} / R^6 (\mu\text{m})^6$

offset = 0.005411988677206995



[11]: 130.15517041731948

[]: