

ECE-150 Digital Logic Design, Fall 2025

Homework 1: due September 18th before class

Total: 30pts

Complete the following problems. Show your work through equations, diagrams, and a demo of any circuit built during class.

Use the TTL ICs for the multiplier *xor* CMOS ICs (not both together)!

Problem 1 (Number Systems (*3 pts total, each answer worth 0.5pts*)).

(a) Convert 101_{10} to:

- (a) Base 2
- (b) Base 6
- (c) Base 16

(b) Convert the following values to base 10:

- (a) $1100\ 1101\ 1111_2$
- (b) 923_8
- (c) $C38_{16}$

Problem 2 (Arithmetic (*3 pts total, each answer worth 0.5pts*)).

- (a) Convert 732_{16} to binary and octal without converting to base 10.
- (b) Perform the addition $101_{10} + 22_{10}$ in binary.
- (c) Perform the subtraction $5_{10} - 22_{10}$ in binary (using two's complement).
- (d) Give the largest number (in decimal) representable by:
 - (a) 4 Octal symbols.
 - (b) N symbols from Base B.

Problem 3 (Boolean Algebra (*3pts total, each answer worth 1pts*)).

Use boolean algebra to simplify these expressions:

- (a) $X = \bar{A}\bar{B}C + \bar{B}C + A\bar{B}C$
- (b) $Y = \overline{AB\bar{B} + \bar{C}} + \bar{A}C$
- (c) $Z = \overline{ABC} + \overline{\bar{A} + B + C}$

Problem 4 (Logic Diagram (5pts total)).

Consider the diagram in Figure 1:

- (a) Write a boolean expression for Z (1pt).
- (b) Fill out a truth table for the diagram (1pt).
- (c) Simplify the expression using a Karnaugh map (2pt).
- (d) Use the simplified expression to draw a sum of products implementation of the circuit (1pt).

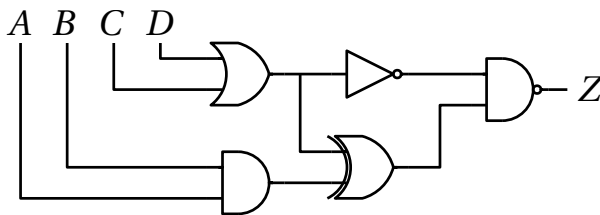


Figure 1: logic diagram

Problem 5 (2 Bit Multiplier). (8pts total)]

Consider the multiplication of two two-bit (unsigned) binary numbers, $A_1A_0 \times B_1B_0$, where A_1 and B_1 are the most significant bits of A and B .

- (a) How many bits are required to represent all possible outputs of $A \times B$? (1pt)
- (b) Fill out a truth table for the two-bit multiplication. (1pts)
- (c) Simplify expressions for each output variable using Karnaugh maps. (4pts)
- (d) Draw an implementation of the circuit based on your expressions. (2pts)

Problem 6 (2 Bit Multiplier Circuit). (8pts)]

Using a single breadboard, and any of the following IC chips in the lab,

- NOT, AND, OR, NAND, NOR, XOR, XNOR

implement a 2 Bit multiplier circuit from the previous problem.

You must:

- Use red wire for 5V and black for ground
- Provide inputs $A_1A_0B_1B_0$ via a 4-input DIP switch with *pull-down* resistors.
- Display your outputs on *light-on zero*¹ LEDs with current limiting resistors in series.

You may want to rearrange your previous boolean expressions to use as few IC chips as possible. If so, draw a logic diagram of your final implemented circuit.

You will demo your circuit at the start of class on the due date.

(2pt for performing demo, 4pt for correctness, 2pt for neat wiring)

¹Light on zero means electrically. I expect your LEDs to turn on corresponding to logical 1's in the truth table.