Modeling Frequency and Severity of Claims with the Generalized Cluster-Weighted Model

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September 26, 2018

Overview

Introduction to Risk

Sub-grouping of insurance policies based on risk classification is a standard practice in insurance. The heterogenous nature of insurance data allows for explorations of many different techniques for sub-grouping risk. As a result, there is a growing number of papers in the area of mixture modeling of univariate and multivariate insurance data to account for heterogeneity of risk.

Examples in Insurance

Automotive

Drivers of various levels of competency are mixed in with large groups rates and are often difficult to track within a cohort.

Health/Life

The variance among people's lifestyles tend to dictate their life expectancy as well as healthcare coverage. Again how do you define a "lifestyle" in a quantitative sense?

Maritime

Maritime Surveillance Radar data is often used to price maritime insurance which have had success being modelled as a mixture of distributions.

Cluster Weighted Models

Let $(\boldsymbol{X}', Y)'$ be the pair of a vector of covariates $\boldsymbol{X}$ and a response variable Y. Assume this set is defined on some sample space Ω that takes values in an appropriate Euclidian subspace. Furthermore, assume that there exists G partitions of Ω, denoted as $\Omega_1, \ldots, \Omega_G$.

Gershenfeld (1997) characterized the cluster-weighted models as a finite mixture of GLMs hence, the joint distribution $f(\boldsymbol{x}, y)$ of $(\boldsymbol{X}', Y)'$ is expressed as follows

$$f(\boldsymbol{x}, y) = \sum_{j=1}^{G} \tau_j q(y|\boldsymbol{x}; \Omega_j) p(\boldsymbol{x}; \Omega_j). \tag{1}$$

Extending CWM

(Ingrassia, Punzo et. al. 2015) proposed a flexible family of mixture models for fitting the joint distribution of a random vector $(\boldsymbol{X}', Y)'$ by splitting the covariates into continues and discrete as $\boldsymbol{X} = (\boldsymbol{V}', \boldsymbol{W}')'$.

$$f(\boldsymbol{x}, y; \boldsymbol{\Phi}) = \sum_{j=1}^{G} \tau_j q(y|\boldsymbol{x}; \boldsymbol{\vartheta}_j) p(\boldsymbol{x}; \boldsymbol{\theta}_j)$$

$$= \sum_{j=1}^{G} \tau_j q(y|\boldsymbol{x}; \boldsymbol{\vartheta}_j) p(\boldsymbol{v}; \boldsymbol{\theta}_j^{\star}) p(\boldsymbol{w}; \boldsymbol{\theta}_j^{\star\star})$$

Bullet Points

- Lorem ipsum dolor sit amet, consectetur adipiscing elit
- Aliquam blandit faucibus nisi, sit amet dapibus enim tempus eu
- Nulla commodo, erat quis gravida posuere, elit lacus lobortis est, quis porttitor odio mauris at libero
- Nam cursus est eget velit posuere pellentesque
- Vestibulum faucibus velit a augue condimentum quis convallis nulla gravida

Blocks of Highlighted Text

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Block 2

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Multiple Columns

Heading

1. Statement
2. Explanation
3. Example

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Table

Treatments	Response 1	Response 2
Treatment 1	0.0003262	0.562
Treatment 2	0.0015681	0.910
Treatment 3	0.0009271	0.296

Table: Table caption

Theorem

Theorem (Mass–energy equivalence)

$E = mc^2$

Verbatim

Example (Theorem Slide Code)

```
\begin{frame}
\frametitle{Theorem}
\begin{theorem}[Mass--energy equivalence]
$E = mc^2$
\end{theorem}
\end{frame}
```

Figure

Uncomment the code on this slide to include your own image from the same directory as the template .TeX file.

Citation

An example of the `\cite` command to cite within the presentation:

This statement requires citation [Smith, 2012].

References

John Smith (2012)
Title of the publication
Journal Name 12(3), 45 – 678.

The End