SALECx.wxmx 1 / 24

1 Author

Symbolic Analysis of Linear Electric Circuits with Maxima SALECx version 1.0 (2019-08-26) for Maxima 5.38+, wxMaxima 16+

Dr. Dejan Tošić, Full Professor, tosic@etf.rs University of Belgrade -- School of Electrical Engineering 11000 Belgrade, Serbia

Creative Commons

3 Acknowledgement

I thank Prof. Dr. Predrag Pejović for permanent encouragement and valuable discussions related to this project.

4 Presented and Published

Application of Free Software and Open Hardware,
PSSOH 2019, International Conference,
University of Belgrade -- School of Electrical Engineering,
Belgrade, Serbia, October 26, 2019. http://pssoh.etf.bg.ac.rs/

^¹ 5 SALECx in a Nutshell

SALECx is a Maxima program for solving linear time-invariant finite electric circuits in the complex domain of the Unilateral Laplace Transform or Phasor Transform.

[□] 5.1 Algorithm

SALECx uses Modified Nodal Analysis (MNA) to formulate equations and solve circuits.

One node, referred to as the reference node is labeled by zero, 0. Other nodes are labeled by consecutive integers starting from one, 1.

For all nodes except the reference node, Node 0, SALECx formulates the Kirchhoff's current law (KCL) equations. The reference direction for current is OUT OF the node (leaving the node).

The currents are expressed in terms of node voltages.

The node voltage of the reference node is set to zero, 0.

SALECx.wxmx 2 / 24

If a current cannot be expressed in terms of node voltages then the current becomes a MNA variable and the corresponding element equation is added to the system of the MNA equations.

MNA variables are node voltages, V[1], V[2], V[3], ... and currents of the ports which are not voltage controlled, i.e. the currents which cannot be expressed in terms of node voltages. These currents are labeled by I["id"] or I["id",pin] where "id" uniquely specifies a circuit element and pin stands for an integer assigned to a circuit node, 1, 2, 3, ...

5.2 Reserved symbols

```
s -- complex frequency, the Laplace variable [radian/second]
```

```
I -- MNA current variables
I[label] or I[label,node]
```

```
V -- MNA voltage variables, node voltages
V[1], V[2], V[3] ...
V[0] is set to 0
```

5.3 Units **5.3** Units

```
All quantities are assumed to be in SI units,
the International System of Units (SI), adopted by
the General Conference on Weights and Measures in 1960.
```

5.4 Electric Circuit Specification

```
The circuit to be analyzed is specified as a list [circuitElement_1, circuitElement_2 ..., circuitElement_N].
```

```
A circuit element is specified as a list of the form [type, label, a, b, p]
[type, label, a, b, p, IC]
[type, label, [a1,a2], b]
[type, label, [a1,a2], [b1,b2], p]
[type, label, [a1,a2], [b1,b2], p, IC]
```

```
type -- string that specifies the element type:
"R", "L", "C", "I", "V", "Z", "Y", "OpAmp",
"VCVs", "VCCs", "CCCs", "CCVs", "IT", "K", "T".
```

```
label -- string that uniquely identifies circuit element, e.g.
"Vgen", "Isource", "Rin", "Cfb", "Lprimary", "Zload", etc.
```

SALECx.wxmx 3 / 24

```
one-port element
  a -- positive terminal
 b -- negative terminal
two-port element
 al -- positive terminal of the 1st port
  a2 -- negative terminal of the 1st port
 b1 -- positive terminal of the 2nd port
 b2 -- negative terminal of the 2nd port
p -- parameter or parameters if p is list
IC -- initial conditions at 0-minus
 Vo for capacitors
  Io for inductors
  [Io1,Io2] for linear inductive transformers
5.5 Element Catalog
5.6 One-port elements
Resistor
 ["R", "id", plusTerminal, minusTerminal, resistance]
Inductor
 ["L", "id", plusTerminal, minusTerminal, inductance]
 ["L", "id", plusTerminal, minusTerminal, inductance, Io]
 Io -- initial condition, initial current at 0-minus
 from plusTerminal, across the element, to minusTerminal
Capacitor
 ["C", "id", plusTerminal, minusTerminal, capacitance]
 ["C", "id", plusTerminal, minusTerminal, capacitance, Vo]
Vo -- initial condition, initial voltage at 0-minus
Vo = V[plusTerminal] - V[minusTerminal]
Current source (ideal independent current generator)
 ["I", "id", plusTerminal, minusTerminal, excitation]
 excitation is the source (generator) current
from plusTerminal, across the element, to minusTerminal
Voltage source (ideal independent voltage generator)
 ["V", "id", plusTerminal, minusTerminal, excitation]
 excitation is the source (generator) voltage
voltage = V[plusTerminal] - V[minusTerminal]
 Impedance
 ["Z", "id", plusTerminal, minusTerminal, impedance]
```

SALECx.wxmx 4 / 24

```
Admitance
  ["Y", "id", plusTerminal, minusTerminal, admittance]
  5.7 Operational Amplifier
  Operational Amplifier (Ideal OpAmp)
  ["OpAmp", "id", [nonInvertingTerminal, invertingTerminal], outputTerminal]
  I["id"] is current into outputTerminal, MNA current variable
  5.8 Controlled Sources
  ["VCVS", "id", [plusControllingTerminal, minusControllingTerminal],
   [plusControlledTerminal, minusControlledTerminal], voltageGain]
  I["id"] is current into plusControlledTerminal, MNA current variable
  ["VCCS", "id", [plusControllingTerminal, minusControllingTerminal],
   [plusControlledTerminal, minusControlledTerminal], transconductance]
  ["CCCS", "id", [plusControllingTerminal, minusControllingTerminal],
   [plusControlledTerminal, minusControlledTerminal], currentGain]
  I["id"] is current into plusControllingTerminal, MNA current variable
  ["CCVS", "id", [plusControllingTerminal, minusControllingTerminal],
   [plusControlledTerminal, minusControlledTerminal], transresistance]
  I["id"] is current into plusControlledTerminal, MNA current variable
□ 5.9 Transformers
  Ideal Transformer
  ["IT", "id", [plusPrimaryTerminal, minusPrimaryTerminal],
   [plusSecondaryTerminal, minusSecondaryTerminal], turnsRatio]
  I["id"] is current into plusPrimaryTerminal, MNA current variable
  Linear Inductive Transformer
  ["K", "id", [plusPrimaryTerminal, minusPrimaryTerminal],
   [plusSecondaryTerminal, minusSecondaryTerminal], [L1,L2,L12]]
  ["K", "id", [plusPrimaryTerminal, minusPrimaryTerminal],
   [plusSecondaryTerminal, minusSecondaryTerminal], [L1,L2,L12], [Io1,Io2]]
  I["id",plusPrimaryTerminal] is
   current into plusPrimaryTerminal, MNA current variable
  I["id",plusSecondaryTerminal] is
   current into plusSecondaryTerminal, MNA current variable
  5.10 ABCD two-port
  ["ABCD", "id", [plusPrimaryTerminal, minusPrimaryTerminal],
   [plusSecondaryTerminal, minusSecondaryTerminal], [[A,B],[C,D]]]
  I["id",plusPrimaryTerminal] current into plusPrimaryTerminal
```

I["id",plusSecondaryTerminal] current OUT OF plusSecondaryTerminal

SALECx.wxmx 5 / 24

5.11 Transmission lines

```
Transmission Line, Phasor Transform
["T", "id", [plusSendingTerminal, minusSendingTerminal],
 [plusReceivingTerminal, minusReceivingTerminal], [Zc,theta]]
theta [radian] -- electrical length
I["id",plusSendingTerminal] current into plusSendingTerminal
I["id",plusReceivingTerminal] current OUT OF plusReceivingTerminal
Transmission Line, Laplace Transform
["T", "id", [plusSendingTerminal, minusSendingTerminal],
 [plusReceivingTerminal, minusReceivingTerminal], [Zc,tau]]
tau [second] -- delay (one-way time delay)
I["id",plusSendingTerminal] current into plusSendingTerminal
I["id",plusReceivingTerminal] current into plusReceivingTerminal
5.12 Calling SALECx
Laplace Transform s-domain
 SALECx[circuitSpecification]
Phasor Transform j*omega-domain, sinusoidal steady state
 SALECx[circuitSpecification, omegaPhasorTransform]
omegaPhasorTransform [radian] -- angular frequency
5.13 Options
Return only the response
 SALECxPrint: false
Return some analysis details and the response
 SALECxPrint: true
5.14 Declaration and Initialization
Declare complex domain
 domain: complex$
Remove values of symbols, e.g.
 remvalue(Ig, s, Vg, Z, Yeq)$
Declare complex variables, e.g.
 declare([Ig, s, Vg, Z, Yeq], complex)$
Declare real variables, e.g.
 declare([Cload, L12, R, Vgeff, omega1], real)$
```

SALECx.wxmx 6 / 24

```
Declare integer variables, e.g.
 declare(nHarmonic, integer)$
Make assumptions, e.g.
 assume(C > 0, L2 > 0, Vgeff > 0, notequal(m, 0), n > -1)$
Introduce aliases, e.g.
 alias(j, %i)$
5.15 Circuit Graph Assumption
The electric circuit graph is assumed to be connected.
If the graph is not connected then
(1) identify the disconnected components,
(2) choose one node in each component, and
(3) connect the chosen nodes to make the graph connected.
The refence node (ground) is numbered by zero, 0.
The other nodes are numbered by consecutive integers starting from one, 1.
6 References
6.1 Classic
Charles A. Desoer, Ernest S. Kuh,
Basic Circuit Theory, New York, NY, McGraw-Hill, 1969.
Leon O. Chua, Charles A. Desoer, and Ernest S. Kuh,
Linear and nonlinear circuits, New York, NY, McGraw-Hill, 1987.
6.2 General
Charles K. Alexander, Matthew N. O. Sadiku,
Fundamentals of Electric Circuits, 6/e, New York, NY, McGraw-Hill, 2017.
James W. Nilsson, Susan A. Riedel,
Electric Circuits, 10/e, Upper Saddle River, NJ, Prentice Hall, 2015.
J. David Irwin, R. Mark Nelms,
Basic Engineering Circuit Analysis, 11/e, Hoboken, NJ, Wiley, 2015.
James A. Svoboda, Richard C. Dorf,
Introduction to Electric Circuits, 9/e, Hoboken, NJ, Wiley, 2014.
William H. Hayt, Jr., Jack E. Kemmerly, Steven M. Durbin,
Engineering circuit analysis, 8/e, New York, NY, McGraw-Hill, 2012.
```

SALECx.wxmx 7 / 24

Farid N. Najm, Circuit Simulation, Hoboken, New Jersey, John Wiley & Sons, 2010. Omar Wing, Classical Circuit Theory, Springer Science+Business Media, LLC, New York, NY, 2008. Wai-Kai Chen (Editor), Circuit Analysis and Feedback Amplifier Theory, CRC Press, Taylor & Francis Group, Boca Raton, FL, 2006. **6.3 Power Engineering** Arieh L. Shenkman, Transient Analysis of Electric Power Circuits Handbook, Springer, Dordrecht, The Netherlands, 2005. Arieh L. Shenkman, Circuit Analysis for Power Engineering Handbook, Springer, Dordrecht, The Netherlands, 1998. **6.4 Transmission Lines** Paul R. Clayton, Analysis of Multiconductor Transmission Lines, 2/e, Hoboken, NJ, Wiley IEEE Press, 2008. 7 ElementStamp (subprogram) 8 SALECx (main program)

SALECx.wxmx 8 / 24

```
(%i2)
         SALECx(circuit_, [w_]) := block([i_, n_],
          if w_=[] then PhasorTransform_: false
                   else PhasorTransform_: true,
          if w #[] then
           print("Phasor Transform at angular frequency ", first(w_)),
          if w_=[] then remvalue(s)
                   else s: %i*first(w_),
          n_: lmax(flatten(
          map(lambda([x], part(x,[3,4])), circuit_)
          )),
          elementValues_: map(lambda([x],
           if length(x)>4 then part(x,5) else false), circuit_
          ),
          initialConditions : map(lambda([x],
           if length(x)=6 then part(x,6) else false), circuit_
          remvalue(I, J, JJ, V, VV),
          for i_: 0 thru n_ do J[i_]: 0,
          JJ: [],
          V[0]: 0,
          potentials_: makelist(V[i_], i_, n_),
          VV: [],
          m_: map(ElementStamp, circuit_),
          equationsVn_: makelist(J[i]=0, i, n_),
          equationsMNA_: append(equationsVn_, JJ),
          variablesMNA_: append(potentials_, VV),
          responseMNA_: linsolve(equationsMNA_, variablesMNA_),
          if SALECxPrint then (
          print("Symbolic Analysis of Linear Electric Circuits with Maxima"),
          print("SALECx version 1.0, Prof. Dr. Dejan Tošić, tosic@etf.rs"),
          print("Number of nodes excluding 0 node: ", n_),
          print("Electric circuit specification:", circuit_),
          print("Supported element: ", m_),
          print("Element values: ", elementValues_),
          print("Initial conditions: ", initialConditions_),
          print("MNA equations: ", equationsMNA_),
          print("MNA variables: ", variablesMNA_)
          ),
         responseMNA_) $
```

8.1 SALECxPrint (reserved symbol, verbose option)

```
(%i3) SALECxPrint: false $
```

SALECx.wxmx 9 / 24

9 domain, declare, assume

```
(%i4)
          domain: complex$
(%i5)
          remvalue(I, J, JJ, s, t, V, VV, omega)$
/(%i6)
          remvalue(C, C1, C2, Ea, Eb, Ec, g,
           I1, I2, Ig, Io, Io1, Io2,
           L, L1, L2, L12, m,
           R, R1, R2, R3, R4, R5,
           V1, V2, Vg, Vgeff, Vo, Vstep,
           Y1, Y2, Z, Z0, Z1, Z2, Zc,
           theta, thetag, tau)$
(%i7)
          declare([Ea, Eb, Ec,
           I, I1, I2, Ig, s,
           V, V1, V2, Vg,
           Y1, Y2, Z, Z0, Z1, Z2],
          complex)$
(%i8)
          declare([C, C1, C2, g,
           Io, Io1, Io2,
           L, L1, L2, L12, m,
           R, R1, R2, R3, R4, R5,
           t, Vgeff, Vo, Vstep, Zc,
           omega, theta, thetag, tau],
          real)$
/(%i9)
          declare(n, integer)$
(%i10)
          assume(C > 0, C1 > 0, C2 > 0,
           L > 0, L1 > 0, L2 > 0, L12 > 0,
           notequal(m, 0), n > -1,
           R > 0, R1 > 0, R2 > 0, R3 > 0, R4 > 0, R5 > 0,
           Vgeff > 0, Vstep > 0, Zc > 0, omega > 0, tau > 0)$
(%i11) alias(j, %i)$
  10 The Simplest Circuit
        Vg_Shema: [ ["V", "Vgen", 1, 0, Vg] ]$
(%i13) Vg_Response: SALECx(Vg_Shema);
_{	ext{(Vg\_Response)}} [ {V}_1 {=} {V} g , {I}_{	ext{Vgen}} {=} 0 ]
  11 Ig Simple Circuit
          IgR_Shema: [ ["I", "Igen", 0, 1, Ig],
                        ["R", "R", 1, 0, R] ]$
```

SALECx.wxmx 10 / 24

```
(*i15) IgR_Response: SALECx(IgR_Shema); [V_1 = Ig R]
```

12 Vg Simple Circuit

13 Capacitor Simple Circuit

```
(%i18) VgRCVo_Shema: [
             ["V", "Vgen", 1, 0, Vg], ["R", "R", 1, 2, R],
            ["C", "C", 2, 0, C, Vo]];
 (vgRCVo\_Shema) [ [V, Vgen, 1, 0, Vg], [R, R, 1, 2, R], [C, C, 2, 0, C, Vo]]
(%i19) VgRCVo_Response_PT: SALECx(VgRCVo_Shema, omega);
 Phasor Transform at angular frequency \omega
 (V_{2RCVO\_Response\_PT}) [V_{1}=Vg,V_{2}=\frac{Vg}{\text{%i} CR\omega+1},I_{Vgen}=-\frac{\text{%i} CVg}{\text{%i} CR\omega+1}]
/(%i21) VgRCVo_Response: SALECx(VgRCVo_Shema),
             SALECxPrint: true;
 Symbolic Analysis of Linear Electric Circuits with Maxima
 SALECx version 1.0, Prof. Dr. Dejan Tošić, tosic@etf.rs
 Number of nodes excluding 0 node: 2
 Electric circuit specification: [[V, Vgen, 1, 0, Vg], [R, R, 1, 2, R], [C,
 C, 2, 0, C, Vo]]
 Supported element: [true, true, true]
 Element values: [Vg,R,C]
 Initial conditions: [false,false,Vo]
 MNA equations:  [\frac{V_1-V_2}{P} + I_{Vgen} = 0, V_2 C s - C Vo + \frac{V_2-V_1}{P} = 0, V_1 = Vg] 
 \textit{MNA variables:} \quad [\, \textit{V}_{\,1}\,, \textit{V}_{\,2}\,, \textit{I}_{\,\textit{Vgen}} \,]
 (VgRCVo_Response) [V_1 = Vg, V_2 = \frac{CRVo + Vg}{CRS + 1}, I_{Vgen} = -\frac{CVgS - CVo}{CRS + 1}]
```

SALECx.wxmx 11 / 24

14 Ideal Transmission Line with Zc and tau, Laplace Transform, s-domain

```
(%i25) TLineZc_Shema: [
             ["V", "Vgen", 3, 0, Vg],
["R", "R1", 3, 1, Zc],
              ["T", "TL", [1,0], [2,0], [Zc,tau]],
              ["R", "R2", 2, 0, Zc]
(%i26) TLineZc_Response: SALECx(TLineZc_Shema);
 (\text{TLineZc\_Response}) \; [\; V_1 = \frac{Vg}{2} \; , V_2 = \frac{Vg \; \text{\%e}^{-s \; \tau}}{2} \; , V_3 = Vg \; , I_{TL \; , \; 2} = -\frac{Vg \; \text{\%e}^{-s \; \tau}}{2 \; Zc} \; , I_{TL \; , \; 1} = \frac{Vg}{2 \; Zc} \; , 
 I_{Vgen} = -\frac{Vg}{2 Zc}]
   I["TL",1] is current into transmission line pin 1 and
   I["TL",2] is current into transmission line pin 2.
(%i27) V1s: V[1], TLineZc_Response;
(V1s) \frac{Vg}{2}
(%i28) V2s: V[2], TLineZc_Response;
[(%i29) V[1]/I["TL",1], TLineZc_Response;
(%i30) V[2]/I["TL",2], TLineZc_Response;
```

SALECx.wxmx 12 / 24

```
Zc [Ohm] is characteristic impedanse of transmission line.
tau [second] is transmission line one-way time delay.
tau = D/v = D*sqrt(Lprim*Cprim) = D/(KVF*c0),
D [meter] is length, KVF is velocity factor.
c0 = 299792458 [meter/second]
```

Maxima does not have rules and patterns, yet, to compute the Inverse Laplace Transform of V2s:

```
(%i31) ilt(V2s,s,t);

(%o31) ilt \left(\frac{Vg e^{-s\tau}}{2}, s, t\right)
```

^¹ 15 Ideal Transmission Line with Zc and theta, at omega, Phasor Transfor, j*omega domain

(%i33) TLineZc_PT_Response: SALECx(TLineZc_PT_Shema, omega); Phasor Transform at angular frequency ω [$V_1 = \frac{Vg}{2}$, $V_2 = \frac{Vg}{2 \sin(\theta) + 2\cos(\theta)}$, $V_3 = Vg$, $I_{TL,2} = \frac{Vg}{Zc\left(2 \sin(\theta) + 2\cos(\theta)\right)}$, $I_{TL,1} = \frac{Vg}{2 Zc}$, $I_{Vgen} = -\frac{Vg}{2 Zc}$]

```
 \begin{array}{lll} & \text{TLineZc\_PT\_Response, exponentialize;} \\ & \text{(%o34)} & \text{[$V_1$=}\frac{Vg}{2}\text{,$V_2$=}\frac{Vg\ \text{\%e}^{-\text{\%i}\ \theta}}{2}\text{,$V_3$=}Vg\text{,$I_{TL}$,$2$=}\frac{Vg\ \text{\%e}^{-\text{\%i}\ \theta}}{2\ Zc}\text{,$I_{TL}$,$1$=}\frac{Vg}{2\ Zc}\text{,} \\ & I_{Vgen}=-\frac{Vg}{2\ Zc}\text{]} \end{array}
```

I["TL",1] is current into transmission line pin 1, I(z=0), and I["TL",2] is current *OUT OF* transmission line pin 2, I(z=D).

```
(%i35) V1w: V[1], TLineZc_PT_Response;
(V1w) \frac{Vg}{2}
(%i36) V2w: V[2] TLineZc_PT_Response exponential
```

SALECx.wxmx 13 / 24

```
theta [radian] is electrical length.
          theta = beta*D = 2*pi*D/lambda, D [meter] is line length.
                              V[1]/I["TL",1], TLineZc_PT_Response;
[(%i38) V[2]/I["TL",2], TLineZc_PT_Response;
        16 OTA-C Filter
         Second-order bandpass and lowpass filters:
         the single-ended transconductor-C realization.
         Rolf Schaumann, Mac E. Van Valkenburg,
         Design of Analog Filters,
          Oxford University Press, 2001. Figure 16.22, p. 631
   (%i39)
                               OTA_C_Shema: [
                                          ["V", "Vgen", 4, 0, Vg],
                                          ["R", "R", 4, 1, R],
                                         ["VCCS", "OTA1", [1,0], [2,0], g],
                                         ["VCCS", "OTA2", [2,0], [2,0], g],
                                         ["VCCS", "OTA3", [2,0], [3,0], g],
                                         ["VCCS", "OTA4", [3,0], [0,2], g],
                                          ["C", "C1", 2, 0, C],
                                          ["C", "C2", 3, 0, C]
                                    OTA_C_Response: SALECx(OTA_C_Shema),
                                         SALECxPrint: true;
    Symbolic Analysis of Linear Electric Circuits with Maxima
    SALECx version 1.0, Prof. Dr. Dejan Tošić, tosic@etf.rs
    Number of nodes excluding 0 node:
    Electric circuit specification: [[V,Vgen,4,0,Vg],[R,R,4,1,R],[
    VCCS, OTA1, [1,0], [2,0], g], [VCCS, OTA2, [2,0], [2,0], g], [VCCS, OTA3
     ,[2,0],[3,0],g],[VCCS,OTA4,[3,0],[0,2],g],[C,C1,2,0,C],[C,C2
     ,3,0,C]]
    Supported element: [true, true, true, true, true, true, true, true]
    Element values:
                                                                    [Vg,R,g,g,g,g,C,C]
    Initial conditions: [false, false, fals
    false]
    MNA equations:  [ \ \frac{V_1 - V_4}{_{P}} = 0 \ , V_2 \ C \ s - V_3 \ g + V_2 \ g + V_1 \ g = 0 \ , V_3 \ C \ s + V_2 \ g = 0 \ , V_3 \ C \ s + V_2 \ g = 0 \ , V_3 \ C \ s + V_2 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_2 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_2 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ g = 0 \ , V_3 \ C \ s + V_3 \ G \ s +
      \frac{V_4-V_1}{R}+I_{Vgen}=0, V_4=Vg]
    \textit{MNA variables:} \quad [\, \textit{V}_{\,1}\,, \textit{V}_{\,2}\,, \textit{V}_{\,3}\,, \textit{V}_{\,4}\,, \textit{I}_{\textit{Vgen}} \,]
     \text{\tiny (OTA\_C\_Response)} \quad \text{\tiny [V_1=Vg,V_2=-\frac{C\,Vg\,g\,s}{C^2\,s^2+C\,g\,s+g^2}} \text{ , } V_3=\frac{Vg\,g^2}{C^2\,s^2+C\,g\,s+g^2} \text{ , } V_4=Vg\text{ , } I_{Vgen}=0
```

SALECx.wxmx 14 / 24

```
\frac{C g s}{C^2 s^2 + C q s + q^2}
(%i42) Hs3lowpass: V[3]/Vg, OTA_C_Response;
└ (%i43) numHs: num(Hs2bandpass);
\lceil (numHs) - Cgs
[(%i44) zeros: solve(numHs=0,s);
(zeros) [s=0]
(%i45) denHs: denom(Hs2bandpass);
(denHs) C^2 s^2 + C g s + g^2
(%i46) poles: solve(denHs=0,s);
(poles) [s = -\frac{(\sqrt{3} i+1)g}{2C}, s = \frac{(\sqrt{3} i-1)g}{2C}]
  17 Three-phase Circuit
(%i47)
          ThreePhase Shema: [
           ["Z", "ZO", 7, 0, ZO],
           ["V", "Ea", 4, 7, Ea],
           ["V", "Eb", 5, 7, Eb],
           ["V", "Ec", 6, 7, Ec],
           ["Z", "Zv1", 1, 4, Z],
           ["Z", "Zv2", 2, 5, Z],
["Z", "Zv3", 3, 6, Z],
["L", "L", 1, 2, L],
           ["R", "R", 2, 3, R],
           ["C", "C", 3, 1, C]
/(%i48) ThreePhase_Response: SALECx(ThreePhase_Shema, omega)$
Phasor Transform at angular frequency \omega
```

(%i49) ThreePhase_Response_CL: ThreePhase_Response,

C = 1/(sqrt(3)*R*omega),
L = sqrt(3)*R/omega\$

SALECx.wxmx 15 / 24

SALECx.wxmx 16 / 24

```
[%i57] IsymmetricalComponents: invert(A).I123, ratsimp, factor; \begin{bmatrix} -\frac{2 * i E a}{\sqrt{3} (z + R)} \\ -\frac{* i (\sqrt{3} * i - 1) E a}{2 \sqrt{3} (z + R)} \\ 0 \end{bmatrix}
[%i58] Iabc: [-I["Ea"], -I["Eb"], -I["Ec"]], ThreePhase_Response_E;
[Iabc) [\frac{Ea}{z + R}, -\frac{(\sqrt{3} * i + 1) E a}{2 z + 2 R}, \frac{(\sqrt{3} * i - 1) E a}{2 z + 2 R}]
[%i59] IabcSymmetricalComponents: invert(A).Iabc, ratsimp; \begin{bmatrix} 0 \\ \frac{Ea}{z + R} \\ 0 \end{bmatrix}
[%i60] substitute([j*sqrt(3)+1 = polarform(j*sqrt(3)+1), j*sqrt(3)-1 = polarform(j*sqrt(3)-1)], Iabc); [\frac{Ea}{z + R}, -\frac{2 * e^{\frac{i \pi}{3}} E a}{2 z + 2 R}, \frac{2 * e^{\frac{i \pi}{3}} E a}{2 z + 2 R}]
```

[⊔] 18 Lumped Wilkinson Power Divider

```
lumpedWilkinson_Shema: [
              ["V", "Vgen", 4, 0, Vg],
["R", "R1", 1, 4, R],
["R", "R2", 2, 0, R],
              ["R", "R3", 3, 0, R],
              ["R", "R4", 2, 3, 2*R],
              ["L", "L2", 1, 2, sqrt(2)*R/omega],
              ["L", "L1", 1, 3, sqrt(2)*R/omega],
              ["C", "C1", 1, 0, 1/(sqrt(2)*R*omega)],
              ["C", "C2", 3, 0, 1/(sqrt(2)*R*omega)],
["C", "C3", 1, 0, 1/(sqrt(2)*R*omega)],
              ["C", "C4", 2, 0, 1/(sqrt(2)*R*omega)]
             ]$
(%i62)
            lumpedWilkinson Response:
              SALECx(lumpedWilkinson_Shema, omega),
            ratsimp;
 Phasor Transform at angular frequency
            [V_1 = \frac{Vg}{2}, V_2 = -\frac{\text{%i} Vg}{2^{3/2}}, V_3 = -\frac{\text{%i} Vg}{2^{3/2}}, V_4 = Vg, I_{Vgen} = -\frac{Vg}{2 R}]
```

SALECx.wxmx 17 / 24

```
⟨%i63⟩
       V[2]-V[3], lumpedWilkinson_Response;
[(%i64) P2: abs(V[2])^2/R, lumpedWilkinson_Response;
(%i65) P3: abs(V[3])^2/R, lumpedWilkinson_Response;
(%i67) P1: abs(Vg-V[1])^2/R, lumpedWilkinson_Response;
(%i68) P1 + P2 + P3 + Pg = 0, ratsimp;

\frac{|vg|^2 - vg}{2R} = 0
(\%i69) P1 + P2 + P3 + Pg = 0,
        Vg = Vgeff*exp(%i*thetag), ratsimp;
(\$069) \quad 0=0
  19 Wilkinson Power Divider
 (%i70) Wilkinson_Shema: [
         ["V", "Vgen", 4, 0, Vg],
          ["R", "R1", 1, 4, R],
          ["R", "R2", 2, 0, R],
          ["R", "R3", 3, 0, R]
          ["R", "R4", 2, 3, 2*R],
          ["T", "T1", [1,0], [2,0], [sqrt(2)*R,%pi/2]],
          ["T", "T2", [1,0], [3,0], [sqrt(2)*R,%pi/2]]
```

$$\begin{array}{lll} & \text{Wilkinson_Response: SALECx(Wilkinson_Shema, omega),} \\ & \text{ratsimp:} \\ \hline & Phasor Transform at angular frequency } & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & &$$

18 / 24 SALECx.wxmx

19.1 IR1, 2, 3

```
V[2] - V[3], Wilkinson_Response;
(%072)
(%i73)
          IR1: I["T1",1] + I["T2",1], Wilkinson_Response;
 (IR1)
         IR2: V[2]/R, Wilkinson_Response;
          -\frac{\$i Vg}{2^{3/2}R}
 (IR2)
(%i75)
         IR3: V[3]/R, Wilkinson_Response;
          -\frac{\text{%i }Vg}{2^{3/2}R}
  19.2 PR1, 2, 3
/(%i76)
          PR1: R*abs(IR1)^2;
 (PR1)
            4 R
(%i77)
          PR2: R*abs(IR2)^2;
 (PR2)
(%i78)
          PR3: R*abs(IR3)^2;
 (PR3)
            8 R
```

19.3 I["Vgen"]

SALECx.wxmx 19 / 24

```
(8082) \frac{Vg}{2R} + I_{Vgen} = 0
(3183) I["Vgen"] + IR1 = 0, Wilkinson_Response;
            0 = 0
   19.4 props
(%i84)
          props;
          [nset, {,}, trylevel, maxmin, nummod, conjugate, erf_generalized,
 \beta, desolve, eliminate, adjoint, invert_by_adjoint, wxmaxima, Ea, Eb, Ec, I,
 I1 , I2 , Ig , s , V , V1 , V2 , Vg , Y1 , Y2 , Z , Z0 , Z1 , Z2 , C , C1 , C2 , g , Io , Io1 , Io2 , L
 ,L1,L2,L12,m,R,R1,R2,R3,R4,R5,t,Vgeff,Vo,Vstep,Zc,\omega,\theta,thetag,	au,
(%i85) properties(I);
(%o85) [database info,kind(I,complex)]
(%i86) properties(J);
(%o86) [hashed array]
(%i87) properties(V);
(%o87) [hashed array, database info, kind(V, complex)]
  20 Noninverting OpAmp Amplifier
 (%i88) nonInvOpAmp_Shema: [
             ["V", "Vgen", 1, 0, Vg], ["R", "R1", 2, 0, R1],
             ["R", "R2", 2, 3, R2],
             ["OpAmp", "OpAmp", [1,2], 3]
            ]$
(%i89) nonInvOpAmp_Response: SALECx(nonInvOpAmp_Shema);
[NonInvOpAmp_Response] [V_1 = Vg, V_2 = Vg, V_3 = \frac{R2\ Vg + R1\ Vg}{R1}, I_{OpAmp} = -\frac{Vg}{R1}, I_{Vgen} = 0]
 (%i90) voltageGain: V[3]/Vg, nonInvOpAmp_Response, expand;
\begin{bmatrix} (\text{voltageGain}) & \frac{R2}{R1} + 1 \end{bmatrix}
```

□ 21 Voltage Follower

SALECx.wxmx 20 / 24

22 Riordan Gyrator Synthetic Inductor

```
(%i94) Riordan_Shema: [
                  ["V", "Vgen", 1, 0, Vg],
                  ["OpAmp", "OpAmp1", [1,4], 5],
                 ["R", "R1", 4, 0, R1],
                          "C2", 4, 5, C2],
                  ["R", "R3", <mark>5</mark>, 2, R3],
                 ["OpAmp", "OpAmp2", [1,2], 3], ["R", "R4", 2, 3, R4],
                 ["R", "R5", 1, 3, R5]
               Riordan Response: SALECx(Riordan Shema),
                 SALECxPrint: true;
 Symbolic Analysis of Linear Electric Circuits with Maxima
 SALECx version 1.0, Prof. Dr. Dejan Tošić, tosic@etf.rs
 Number of nodes excluding 0 node:
 Electric circuit specification: [[V, Vgen, 1, 0, Vg], [OpAmp, OpAmp1, [1
  ,4],5],[R,R1,4,0,R1],[C,C2,4,5,C2],[R,R3,5,2,R3],[OpAmp,
 OpAmp2, [1,2],3], [R,R4,2,3,R4], [R,R5,1,3,R5]]
 Supported element: [true, true, true, true, true, true, true, true]
 Element values: [Vg, false, R1, C2, R3, false, R4, R5]
 Initial conditions: [false, false, false, false, false, false,
 false]
 MNA equations: \left[ \frac{V_1 - V_3}{P_5} + I_{Vgen} = 0, \frac{V_2 - V_3}{P_4} + \frac{V_2 - V_5}{P_3} = 0, \frac{V_3 - V_1}{P_5} + \frac{V_3 - V_2}{P_4} + \frac{V_3 - V_2}{P_5} \right]
 I_{OpAmp2} = 0, (V_4 - V_5)C2s + \frac{V_4}{R_1} = 0, (V_5 - V_4)C2s + \frac{V_5 - V_2}{R_3} + I_{OpAmp1} = 0, V_1 - V_2 = 0,
 V_1 - V_4 = 0, V_1 = Vg]
 \textit{MNA variables:} \quad [\, \textit{V}_{1}\,, \textit{V}_{2}\,, \textit{V}_{3}\,, \textit{V}_{4}\,, \textit{V}_{5}\,, \textit{I}_{\textit{OpAmp2}}\,, \textit{I}_{\textit{OpAmp1}}\,, \textit{I}_{\textit{Vgen}} \,]
 \begin{array}{l} \text{\tiny (Riordan\_Response)} \;\; [\; V_1 = Vg \;, V_2 = Vg \;, V_3 = - \; \frac{R4\; Vg - C2\; R1\; R3\; Vg\; s}{C2\; R1\; R3\; s} \;\;, V_4 = Vg \;, V_5 = \frac{C2\; R1\; Vg\; s + Vg}{C2\; R1\; s} \\ \text{\tiny (I_{OpAmp2} = } \; \frac{R5\; Vg + R4\; Vg}{C2\; R1\; R3\; R5\; s} \;\;, I_{OpAmp1} = - \; \frac{C2\; R3\; Vg\; s + Vg}{C2\; R1\; R3\; s} \;\;, I_{Vgen} = - \; \frac{R4\; Vg}{C2\; R1\; R3\; R5\; s} \;\;]
```

22.1 Input Impedance

SALECx.wxmx 21 / 24

23 Wien Bridge Oscillator

$^{\sqcup}$ 24 ABCD Circuit

 $\frac{Ig2 Y1 (a11 a22-a12 a21)+Ig1 (-Y2 a22-a21)}{Y2 a22+a21+Y1 (Y2 a12+a11)}]$

 $\frac{\textit{Ig2 a22} + \textit{Ig2 Y1 a12} + \textit{Ig1}}{\textit{Y2 a22} + \textit{a21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)} \;, \; \textit{I}_{ABCD} \;, \; 2 = \frac{\textit{Ig2 a21} + \textit{Ig2 Y1 a11} - \textit{Ig1 Y2}}{\textit{Y2 a22} + \textit{a21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)} \;, \; \textit{I}_{ABCD} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)} \;, \; \textit{I}_{ABCD} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)} \;, \; \text{I}_{ABCD} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{a11}\right)} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)}{\textit{Y2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)} \;, \; 1 = \frac{\textit{Ig2 a22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)}{\textit{Y2 a22} + \textit{A22} + \textit{A21} + \textit{Y1}\left(\textit{Y2 a12} + \textit{A21}\right)} \;, \; 1 = \frac{\textit{A21} + \textit{A22} + \textit{A21} + \textit{A21}}{\textit{Y2 a22} + \textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;, \; 1 = \frac{\textit{A22} + \textit{A22}}{\textit{A22} + \textit{A22}} \;$

SALECx.wxmx 22 / 24

```
(%i104) ABCD_Response_noIg: eliminate(ABCD_Response, [Ig1,Ig2]);
 (ABCD_Response_noig) [-(Y2\ a12+a11)(Y2\ a22+a21+Y1\ Y2\ a12+Y1\ a11)^2
  \left( \left( V_{2} \text{ all} - V_{1} \right) \text{ a22} - V_{2} \text{ al2} \text{ a21} + I_{ABCD, 1} \text{ a12} \right), -\left( Y_{2} \text{ a12} + \text{a11} \right) 
 \left( Y_{2} \text{ a22} + \text{a21} + Y_{1} \text{ Y2} \text{ a12} + Y_{1} \text{ a11} \right)^{2} 
   \left[I_{ABCD,2} all a22+\left(V_1-I_{ABCD,2} al2
ight) a21-I_{ABCD,1} al1\left(V_1
(%i105) ABCD_Response_VI: solve(ABCD_Response_noIg, [V[1],I["ABCD",1]]);
(ABCD_Response_VI) [[V_1 = I_{ABCD}, 2 a12+V_2 a11, I_{ABCD}, 1=I_{ABCD}, 2 a22+V_2 a21]]
   I["ABCD",1] is current into pin 1, and
   I["ABCD",2] is current *OUT OF* pin 2.
  25 Time and Date
(%i106) timedate();
(%o106) 2019-08-26 17:00:24+02:00
   25.1 aliases, arrays
(<mark>%i10</mark>7) aliases;
(%o107) [%i]
^{\prime\prime}(%i108) arrays;
(%o108) [J,V]
(\%i109) arrayinfo(J);
(%o109) [hashed, 1, [0], [1], [2], [3], [4], [5], [6], [7]]
(%i110) arrayinfo(V);
(%o110) [hashed,1,[0]]
```

□ 25.2 facts, functions

SALECx.wxmx 23 / 24

```
(%i111)
 (\$ol11) [kind(Ea, complex), kind(Eb, complex), kind(Ec, complex),
 kind(I, complex), kind(I1, complex), kind(I2, complex), kind(Ig, complex),
 kind(s, complex), kind(V, complex), kind(V1, complex), kind(V2, complex),
 kind(Vg, complex), kind(Y1, complex), kind(Y2, complex), kind(Z, complex),
 kind(Z0, complex), kind(Z1, complex), kind(Z2, complex), kind(C, real),
 kind(C1, real), kind(C2, real), kind(g, real), kind(Io, real),
 kind(Io1, real), kind(Io2, real), kind(L, real), kind(L1, real),
 kind(L2, real), kind(L12, real), kind(m, real), kind(R, real), kind(R1, real)
 , kind(R2, real), kind(R3, real), kind(R4, real), kind(R5, real),
 kind(t, real), kind(Vgeff, real), kind(Vo, real), kind(Vstep, real),
 kind(Zc, real), kind(\omega, real), kind(\theta, real), kind(thetag, real),
 kind(\tau, real), kind(n, integer), C>0, C1>0, C2>0, L>0, L1>0, L2>0, L12>0,
 notequal(m, 0), n>-1, R>0, R1>0, R2>0, R3>0, R4>0, R5>0, Vgeff>0, Vstep>0
 0,Zc > 0,\omega > 0,\tau > 0]
(%i112) functions;
          [ElementStamp(e), SALECx(circuit_, [w])]
  25.3 infolists, props
(%i113) infolists;
 (%ol13) [labels, values, functions, macros, arrays, myoptions, props,
 aliases, rules, gradefs, dependencies, let_rule_packages, structures]
(%i114)
          props;
 (%o114) [nset, {,}, trylevel, maxmin, nummod, conjugate, erf_generalized,
 eta , desolve , eliminate , adjoint , invert\_by\_adjoint , wxmaxima , Ea , Eb , Ec , I ,
 I1, I2, Ig, S, V, V1, V2, Vg, Y1, Y2, Z, Z0, Z1, Z2, C, C1, C2, g, I0, I01, I02, L
 ,L1,L2,L12,m,R,R1,R2,R3,R4,R5,t,Vgeff,Vo,Vstep,Zc,\omega,	heta,thetag,	au,
 n
(%i115) propvars(complex);
         [Ea,Eb,Ec,I,I1,I2,Ig,s,V,V1,V2,Vg,Y1,Y2,Z,Z0,Z1,Z2]
 (%0115)
(%i116)
          propvars(real);
 (%o116) [C,C1,C2,g,Io,Io1,Io2,L,L1,L2,L12,m,R,R1,R2,R3,R4,R5,t
 ,Vgeff ,Vo ,Vstep ,Zc ,\omega ,	heta ,thetag ,	au ]
```

¹ 25.4 values

SALECx.wxmx 24 / 24

```
(%i117)
        values;
(%0117)
        [SALECxPrint, Vg_Shema, PhasorTransform_, elementValues_,
initialConditions_, potentials_, m, equationsVn_, equationsMNA_,
variablesMNA_, responseMNA_, Vg_Response, IgR_Shema, IgR_Response,
VgR_Shema, VgR_Response, VgRCVo_Shema, VgRCVo_Response_PT, V2PT,
VgRCVo_Response, V2s, v2ilt, v2t, TLineZc_Shema, tau_, a1_, a2_, b1_, b2_,
TLineZc_Response, V1s, TLineZc_PT_Shema, TLineZc_PT_Response, V1w, V2w,
OTA_C_Shema,OTA_C_Response,Hs2bandpass,Hs3lowpass,numHs,zeros,denHs
, poles , ThreePhase_Shema , ThreePhase_Response , ThreePhase_Response_CL ,
ThreePhase\_Response_E, I12, I23, I31, I123, A, IsymmetricalComponents, Iabc
, IabcSymmetricalComponents, lumpedWilkinson_Shema,
lumpedWilkinson_Response , P2 , P3 , Pg , P1 , Wilkinson_Shema ,
Wilkinson_Response, IR1, IR2, IR3, PR1, PR2, PR3, nonInvOpAmp_Shema,
nonInvOpAmp_Response, voltageGain, VoltageFollower_Shema,
VoltageFollower_Response, Riordan_Shema, Riordan_Response, Zin,
Lsynthetic, V54, Wien_Shema, Wien_Reponse, ABCD_Shema, JJ, VV, a11_, a12_,
a21_,a22_,ABCD_Response,ABCD_Response_noIg,ABCD_Response_VI]
```

26 End-of-File

```
(%i118) timedate();
(%o118) 2019-08-26 17:00:25+02:00
END-OF-FILE
```