

# Doing Gravitational Wave Astronomy with binaries of compact objects

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Pau Amaro Seoane

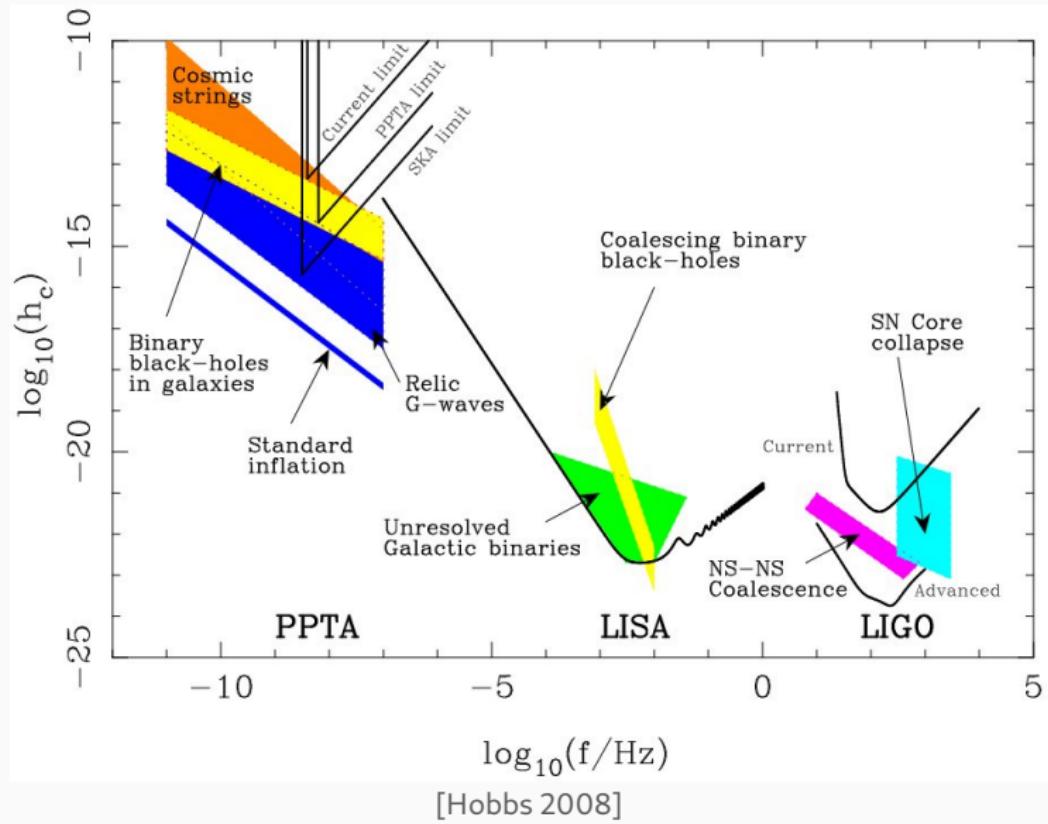
Thessaloniki, October 2018

<http://astro-gr.org>

pau@ice.cat

# Frequencies

# The different windows in GW Astronomy



A universe of black holes

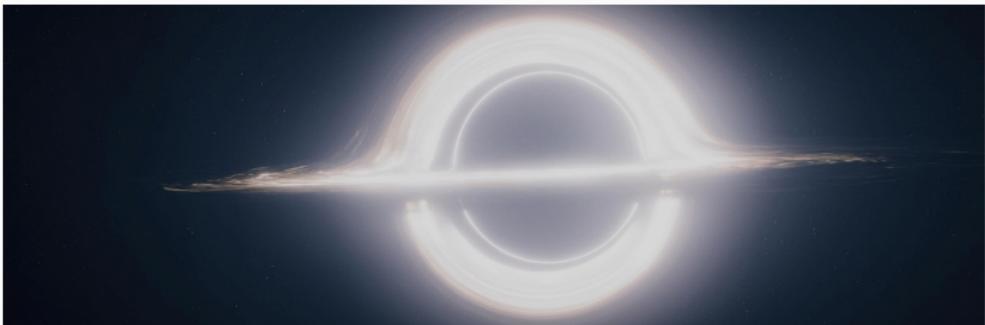
## Black holes come in different flavors



[Warner Bros, Entertainment Inc. and Paramount Pictures Corporation. Author:  
double negative, <http://www.dneg.com>]

- Stellar-mass black holes:

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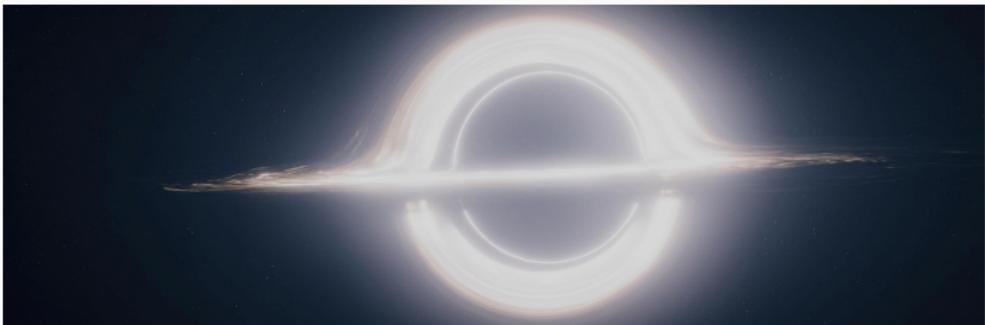


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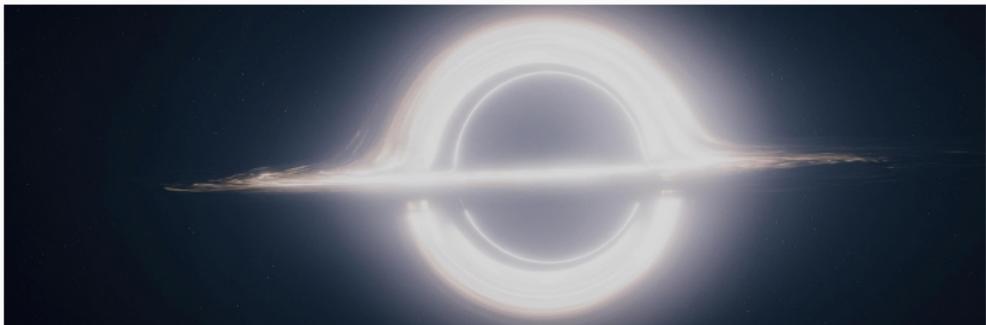
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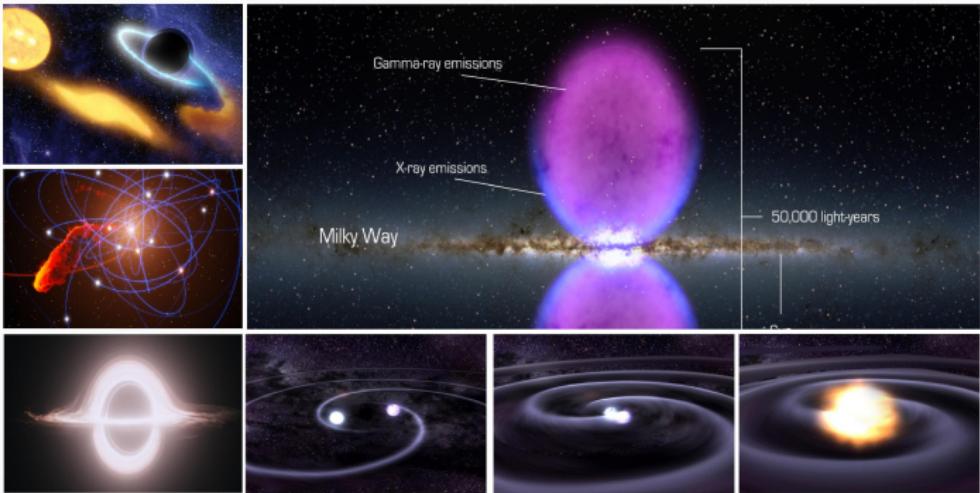
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Formation unclear,  $100 \lesssim M_{IMBH}/M_\odot < 10^5$ , probably in clusters

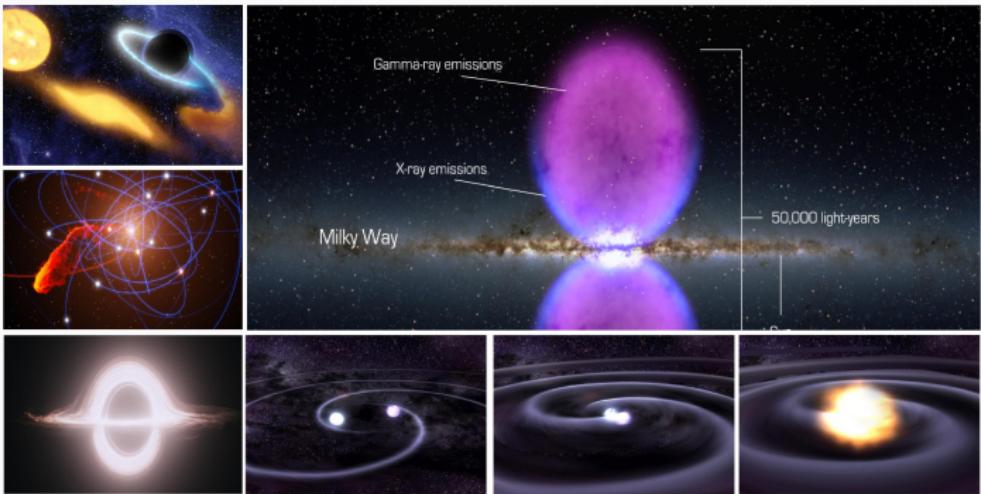
Black holes: Do they exist?

# Do black holes exist?



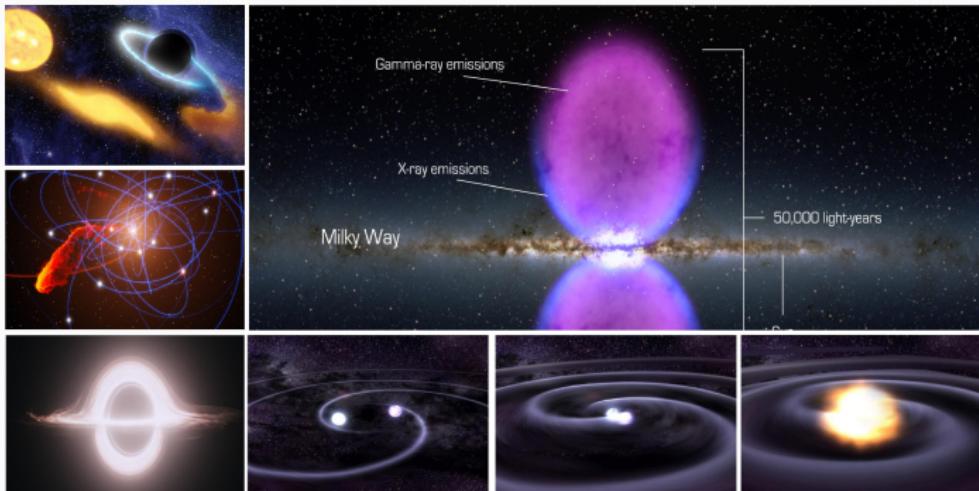
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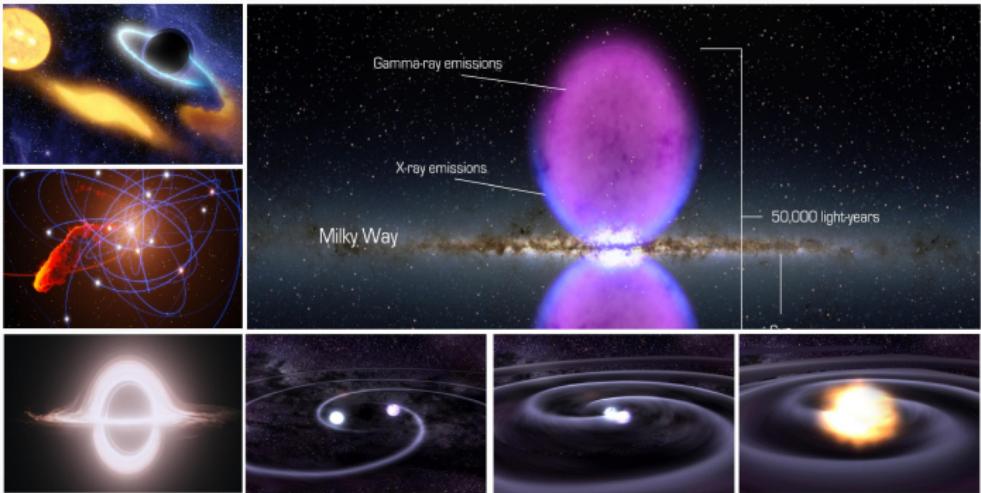
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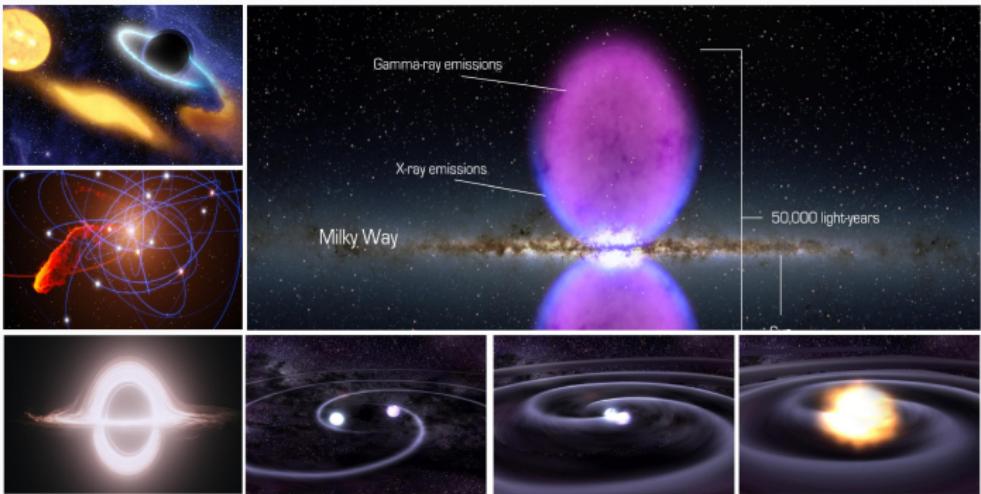
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**Gravitational waves**

## An excellent probe: Gravitational Waves



[Henze, NASA]

- ▷ Predicted in 1918 by Albert Einstein
- ▷ Electromagnetic waves produced by accelerated charged particles
- ▷ Gravitational Waves produced by accelerated masses

# What are they good for?



[ESO/L. Calçada]

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# What are they good for?



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- ▷ Slow decay: Propagate to very long distances
- ▷ Difficult to detect: Almost do not interact with matter
- ▷ Pristine probe: They contain very detailed information about space and time



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Stellar-mass black holes

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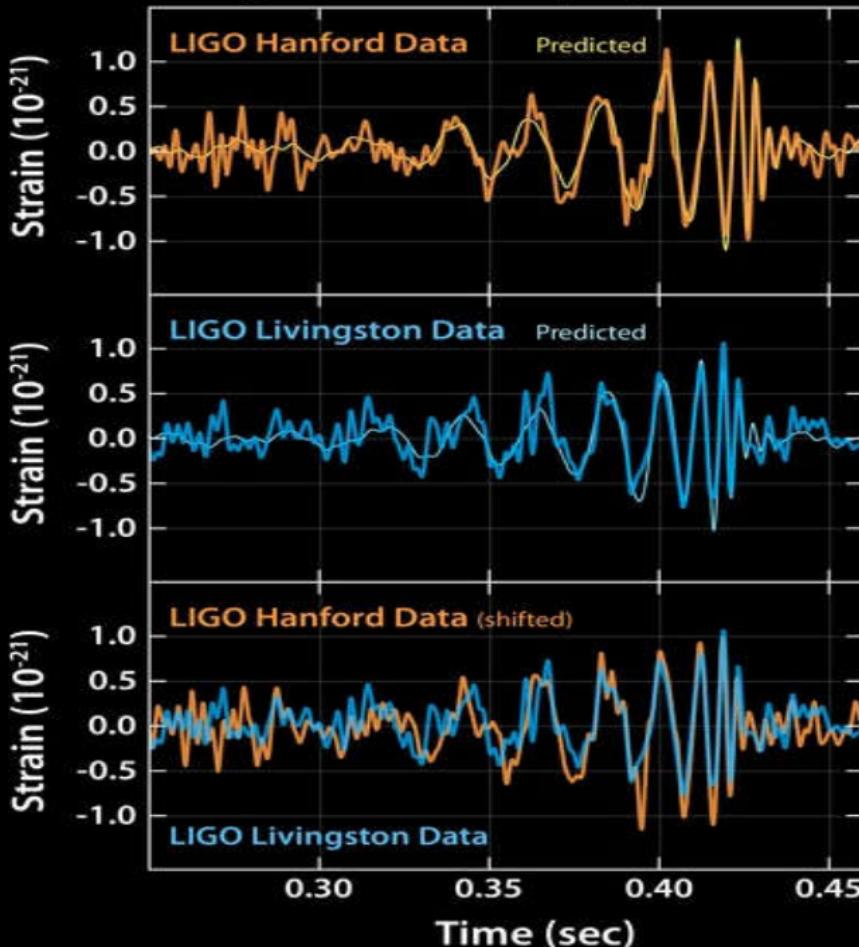
# Wait... We do have direct proofs now!

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Image Credit: Caltech/MIT/LIGO Lab



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3. They merge

Do supermassive black holes exist?

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- They can emit up to a thousand of times the energy of our Galaxy
- How do you create a luminosity of  $10^{40}$  W??

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[NASA/JPL-Caltech]

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- ▷ The largest one known devours 600 Earths per minute

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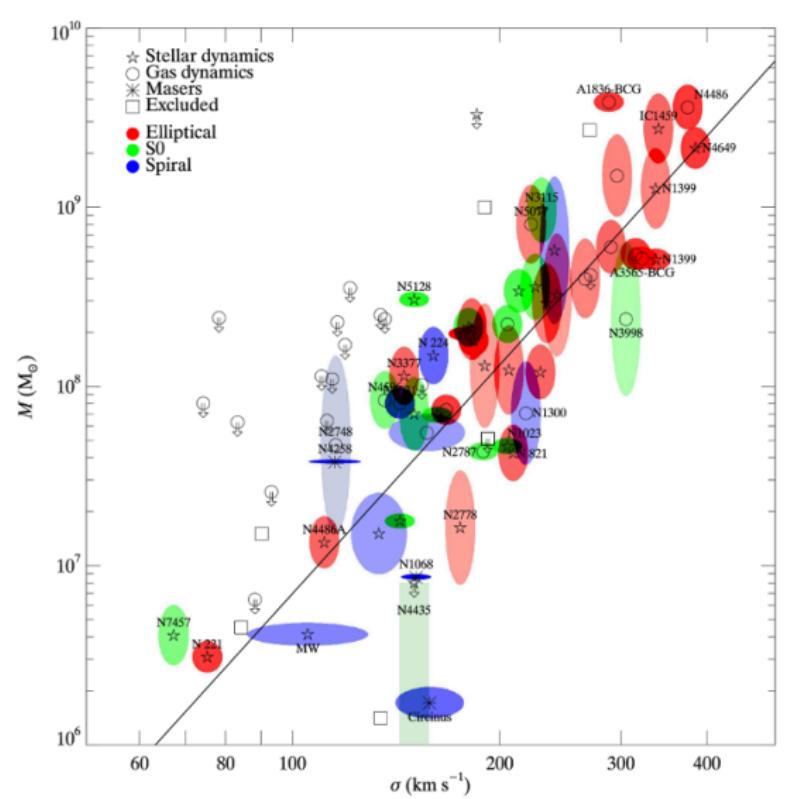
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- ▷ Observations of the Galactic Center reveal a strange fact
- ▷ Stars move... around a point (a radio source called SgrA\*)
- ▷ Four millions of solar masses, four millions of Suns
- ▷ Within a radius of 22 millions of km, enclosed in  $\sim 1/3$  times the distance to the Sun



[Vídeo: S-Stars]

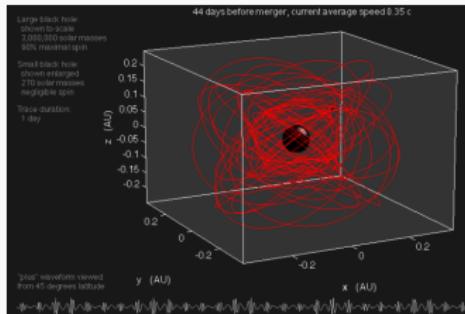
# Correlations



[Guelketin et al 2009]

Capture of compact objects: A unique probe

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[Vídeo: Extreme-mass ratio inspiral, by S. Drasco]

- ✗ Stellar mass object spiraling into  $10^4 - 10^6 M_\odot$ .
- ✗ This range of masses corresponds to relaxed nuclei (!)
- ✗ Only compact objects – extended stars disrupted early
- ✗ With LISA  $z \sim 1$

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[Amaro-Seoane et al 2012a b]

## Four important points

- ① Extreme-mass ratio inspirals: There has not been any other mission conceived, planned or even thought of ever that can do the science that we can do with them

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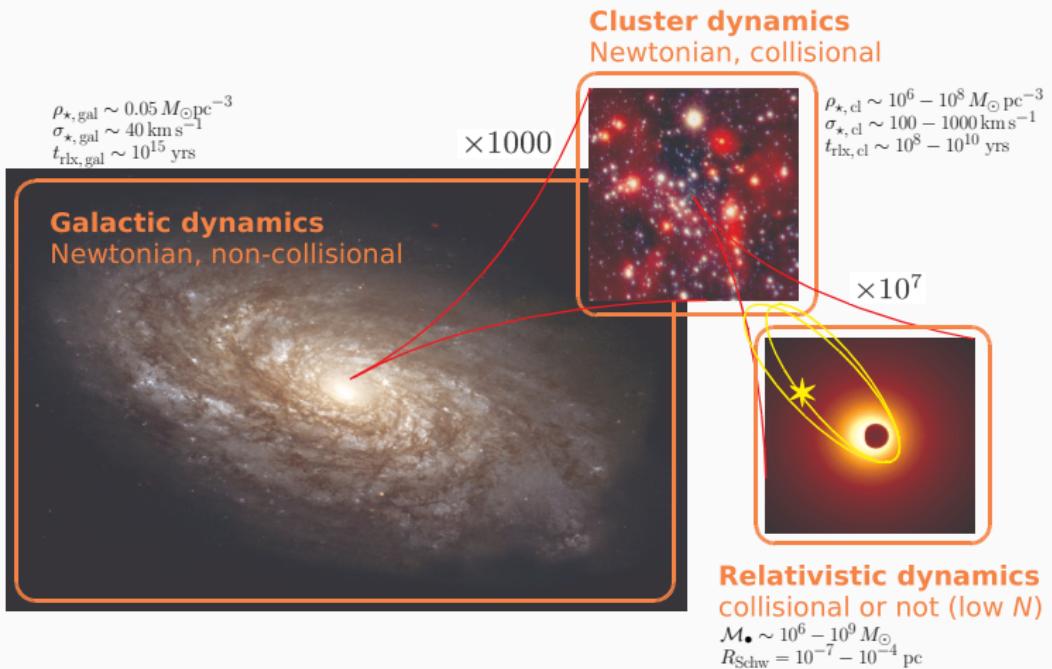
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- ③ Tests of alternative theories of gravity: "Geo"desic mapping of space-time
- ④ Measures mass and spin with unprecedent precision

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# A problem of 10 orders of magnitude



Note:  $1 \text{ pc} \sim 3 \text{ light years}$

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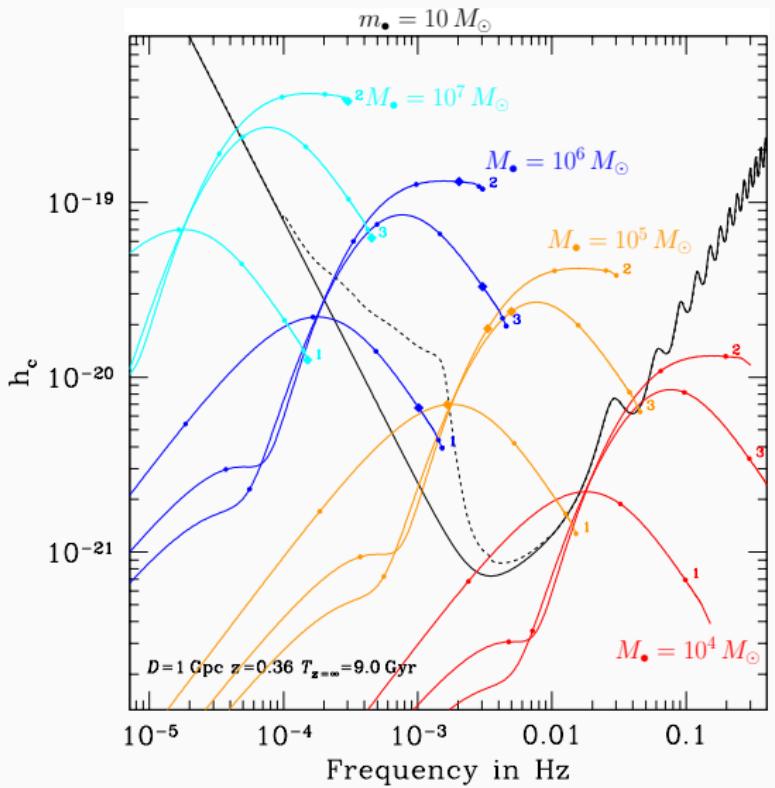
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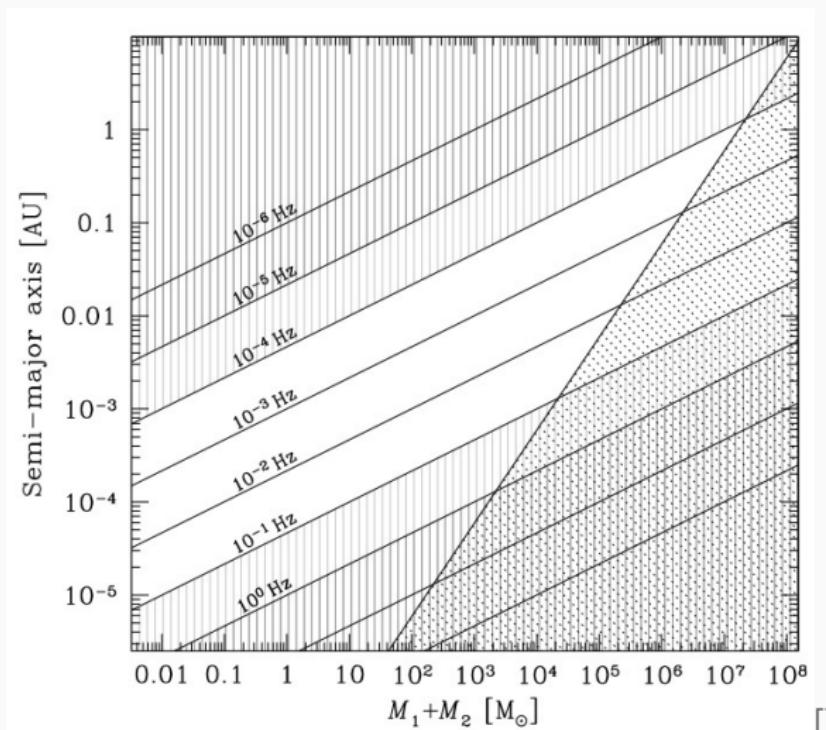
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- We are already making completely new discoveries many years before LISA

# Range of masses

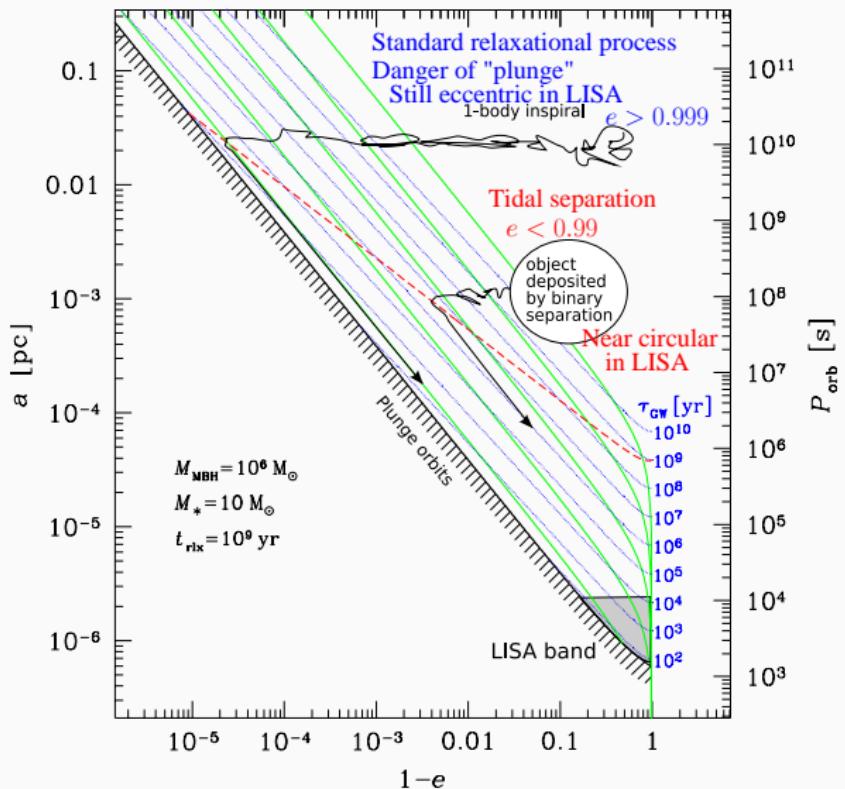


## Another way of looking at it



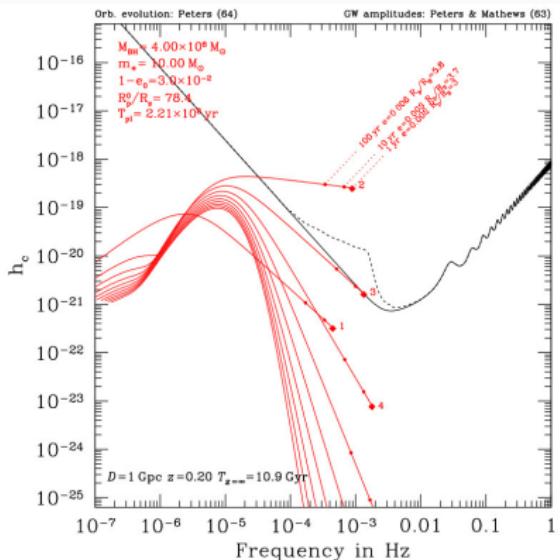
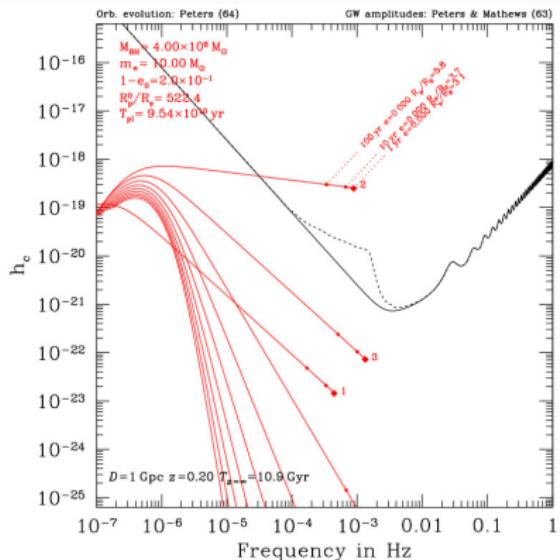
□

# Dichotomizing an EMRI

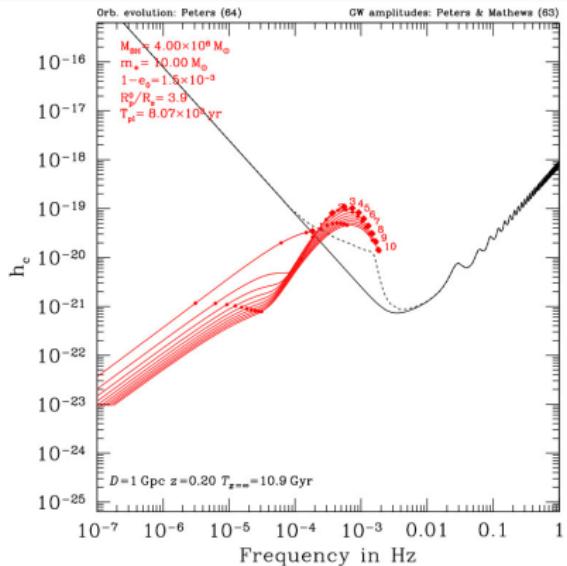
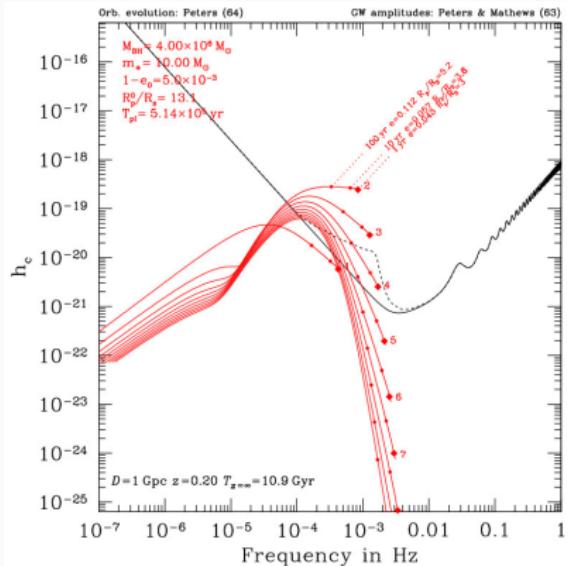


[Amaro-Seoane 2012]

# Low eccentricity, 0.8, 0.97

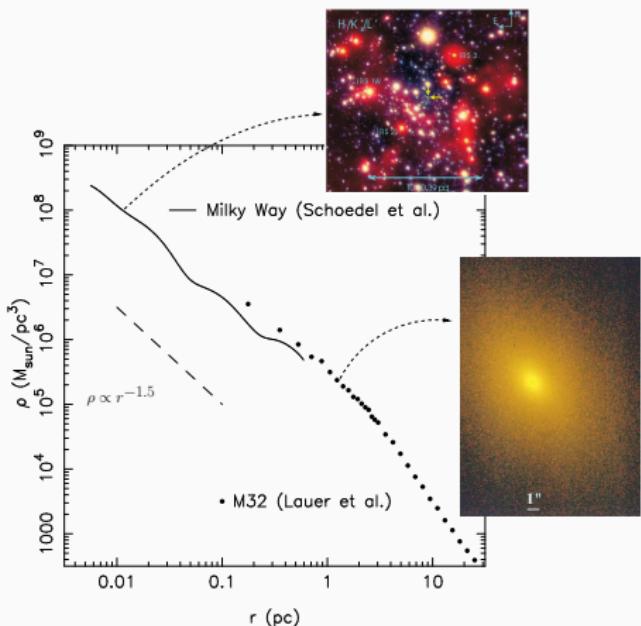


# High eccentricity, 0.995, 0.9985



Do we expect these things to exist?

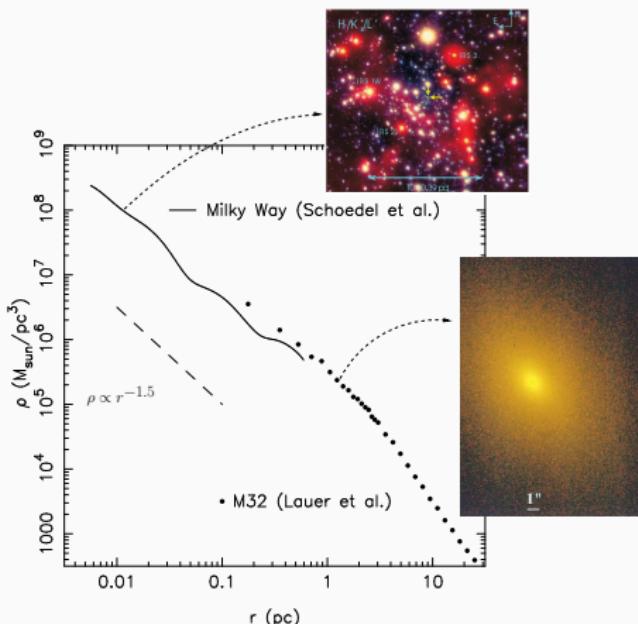
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[Adapted from Merritt 2006]

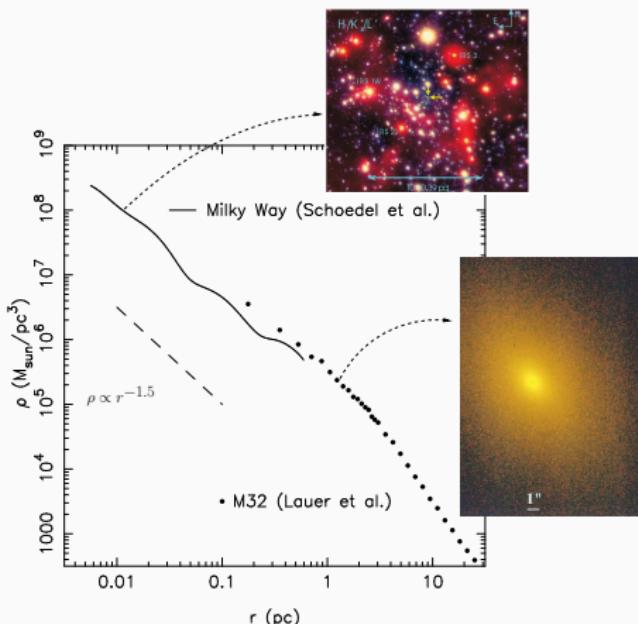
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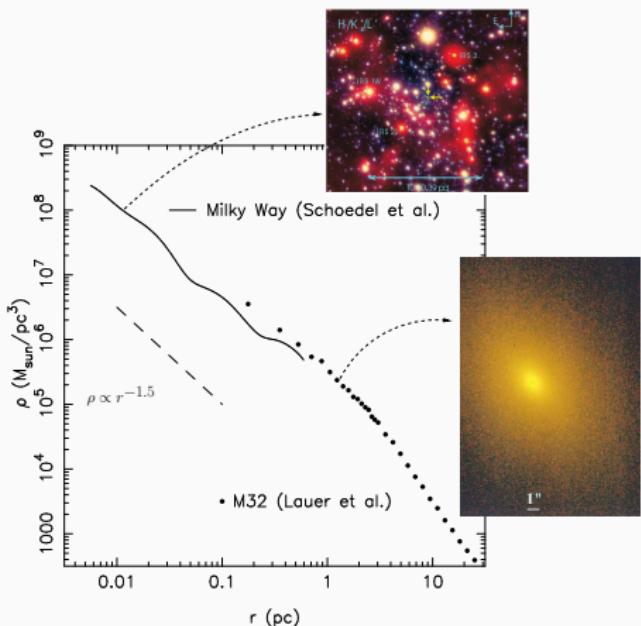
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- ▷ Very few observations: **Relevant region difficult to resolve**
- ▷ Because of obscuration: **Many assumptions made to study inner region**
- ▷ Considerable amount of modelling: **Are these profiles a coincidence?**

[Adapted from Merritt 2006]

## Mass segregation

- ▷ Classical problem in stellar dynamics: Statistical thermal equilibrium  $f(E) \propto e^{-E/\sigma^2}$  must be violated close to the MBH ( $R_t, R_{\text{Schw}}, R_{\text{coll}}$ )

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- ▷ If single-mass: quasi-steady solution takes power-law form (isotropic DF)  $f(E) \sim E^p, \rho(r) \sim r^{-\gamma}$ , with  $\gamma = 3/2 + p$
- ▷ Confirmed later with a detailed kinematic treatment for single-mass [Bahcall & Wolf 1976]:  $\gamma = 7/4$  and  $p = \gamma - 3/2 = 1/4$

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- ▷ Two branches for the solution: A “weak” (unrealistic) branch and a “strong” branch

[Hopman & Alexander 2009, Preto & Amaro-Seoane 2010, Amaro-Seoane & Preto 2011]

## Impact on rates

$$\Gamma_{\text{EMRI}} = f_{\bullet} \int_{E_{\text{GW}}}^{+\infty} dE \frac{n(E)}{\ln(J_c(E)/J_{lc}) T_{rlx}(E)}$$

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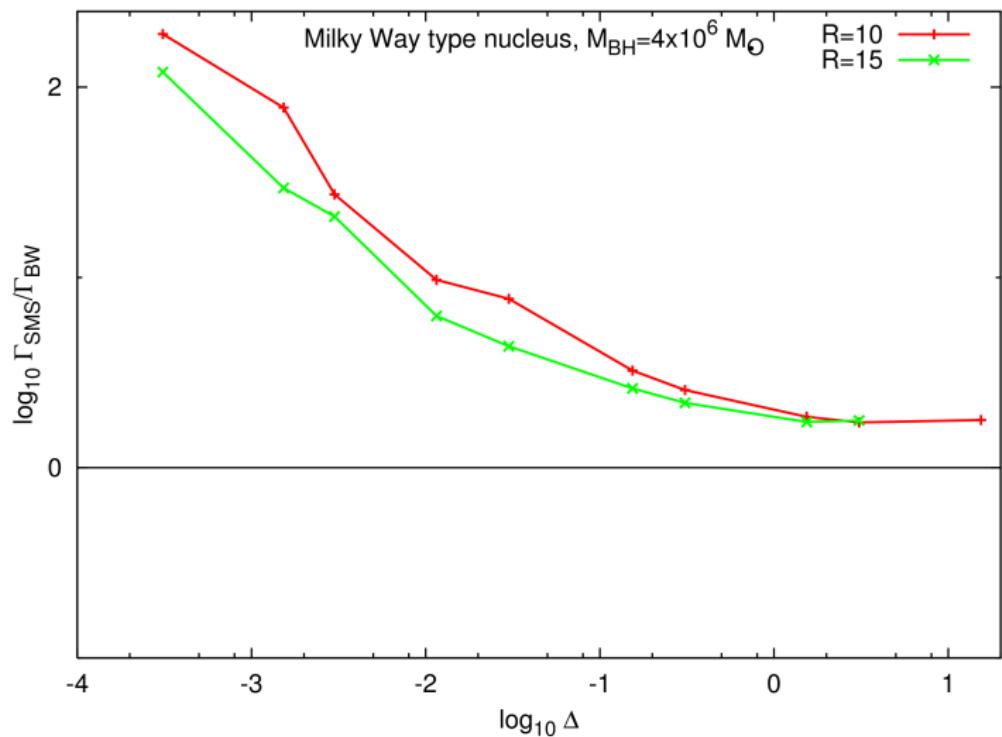
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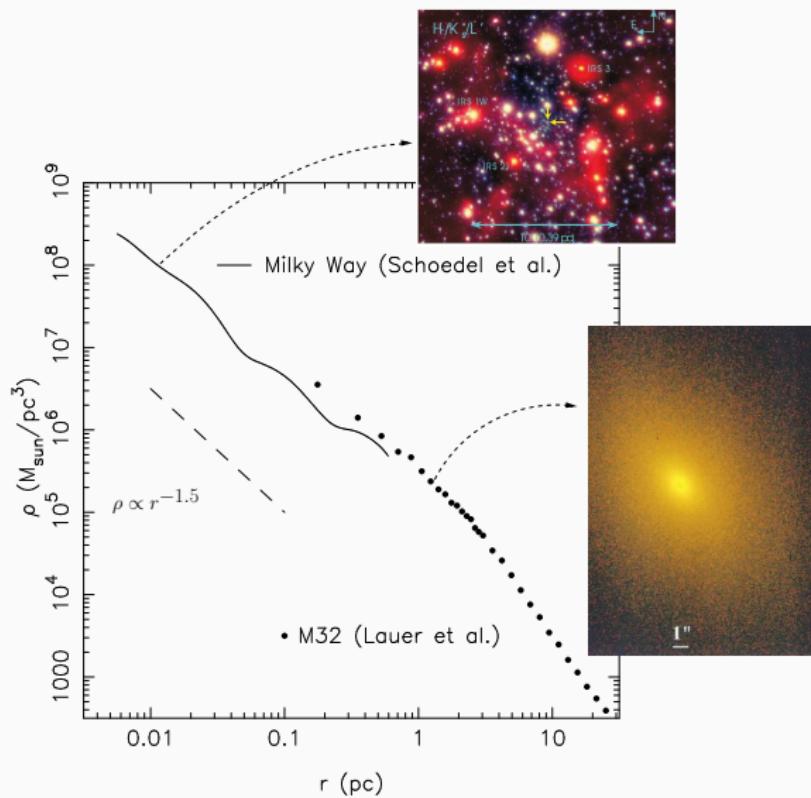
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- $a_{\text{GW}}$ , or energy  $E_{\text{GW}}$ , for EMRIs is:  $a_{\text{GW}} = 0.01r_h$

## Boost on rates



Cusps - Observers: You got it right

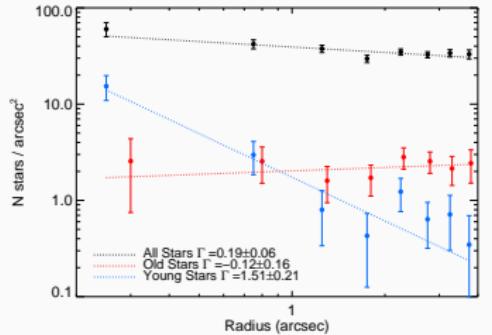
# Old times



[Adapted from Merritt 2006]

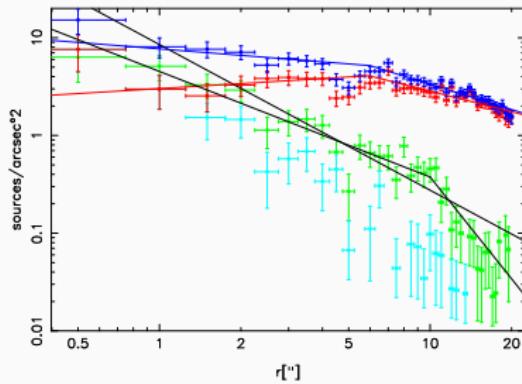
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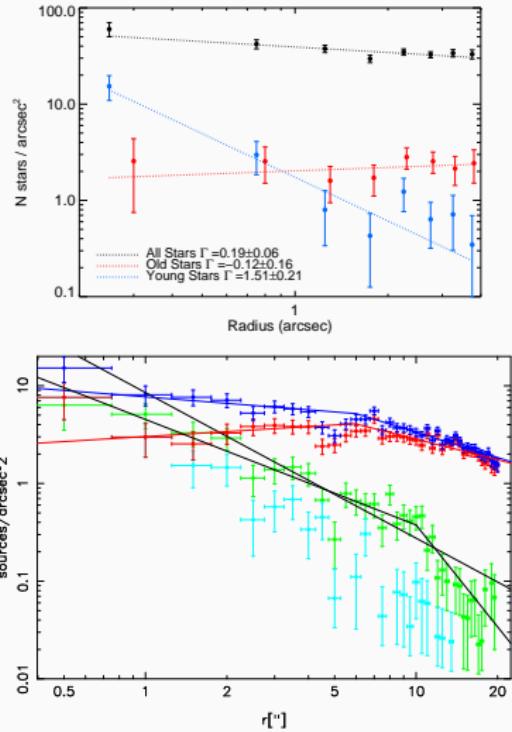


► We can distinguish the young and old population and see a **deficit of old stars**

[Do et al. 2009, Buchholz et al 2009]

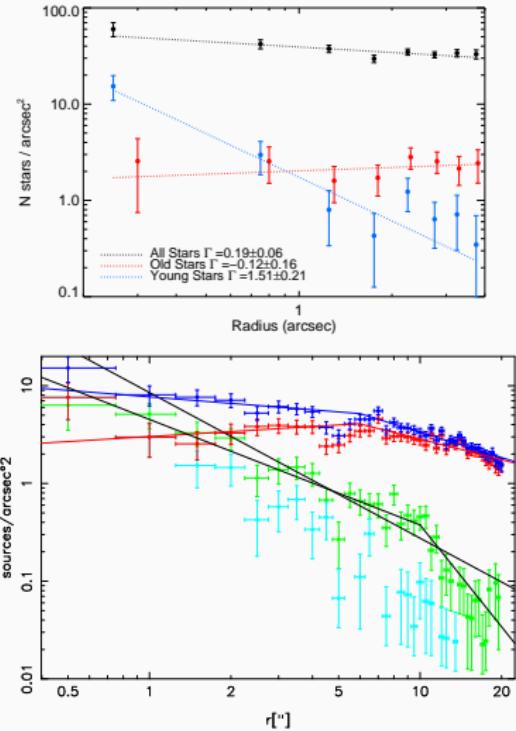


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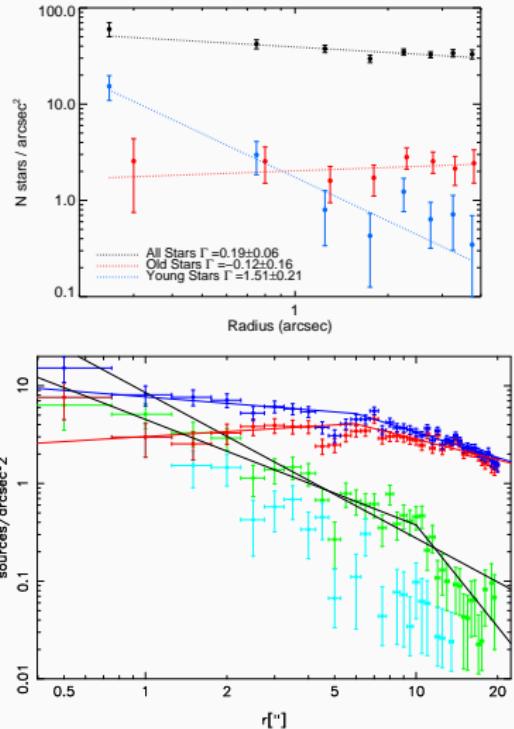
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- ▷ This is old news We know that the problem is not that acute

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# How do you carve a hole at the Galactic Center?

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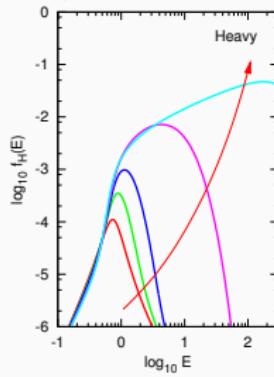
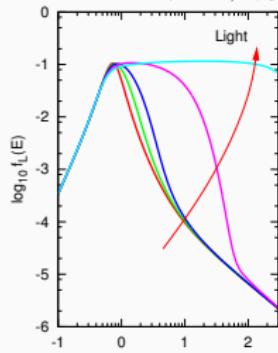
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---

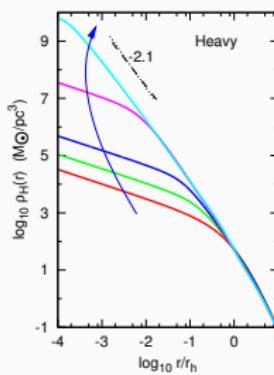
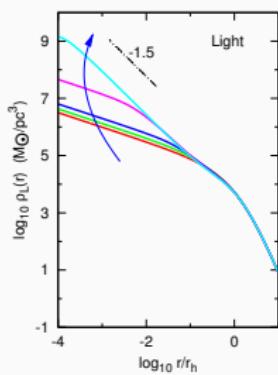
[Preto & Amaro-Seoane 2010, Amaro-Seoane & Preto 2010]

# Isocore ... regrowth

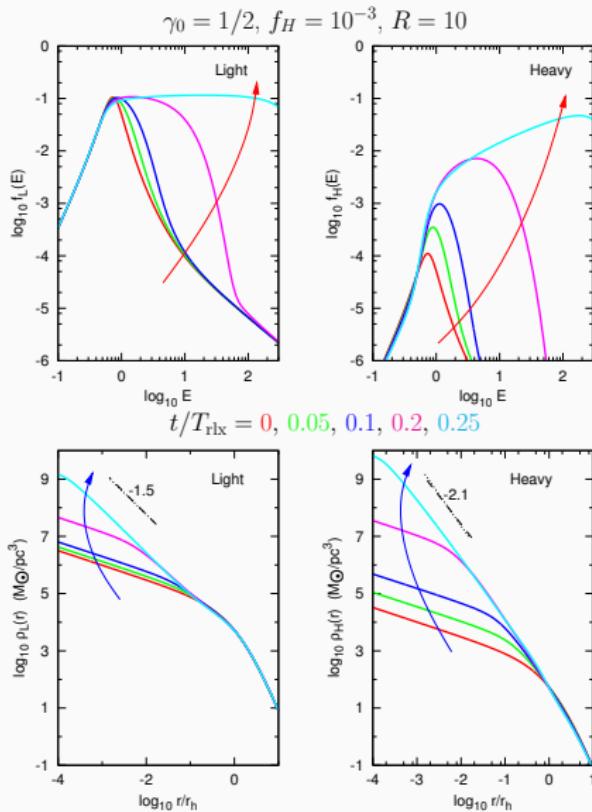
$$\gamma_0 = 1/2, f_H = 10^{-3}, R = 10$$



▷ By  $t \sim 0.25 T_{\text{rlx}}(r_h)$ , cusps fully developed ( $\sim 0.02$  pc if scaled to MW)

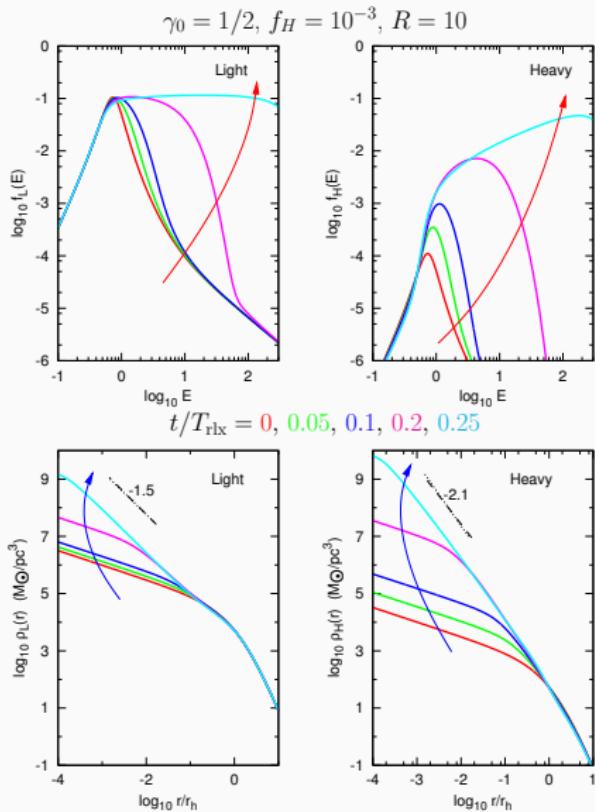


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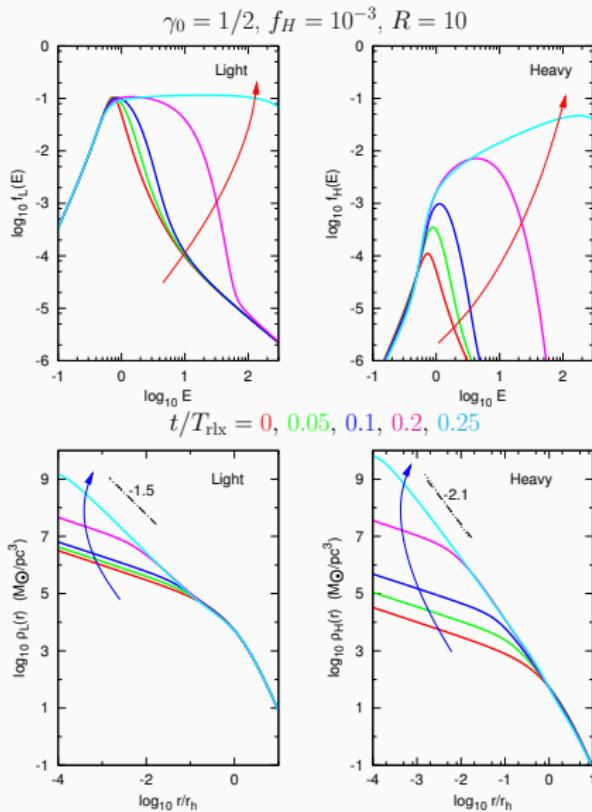
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- ▷ Our results confirmed later [Gualandris & Merritt 2011]

## What does this mean for EMRIs?

- Stellar cusps may re-grow in less than a  $T_H$  but the existence of cored nuclei still remains a possibility

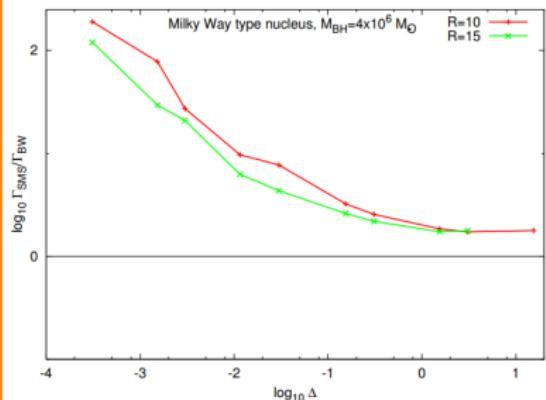
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- The Milky Way nucleus is not necessarily the prototype of the nucleus from which LISA detections will be more frequent
- We still expect that a substantial fraction of EMRI events will originate from segregated stellar cusps, in particular with our new solution of mass segregation

## So: Stellar-mass black holes pile up in galactic nuclei

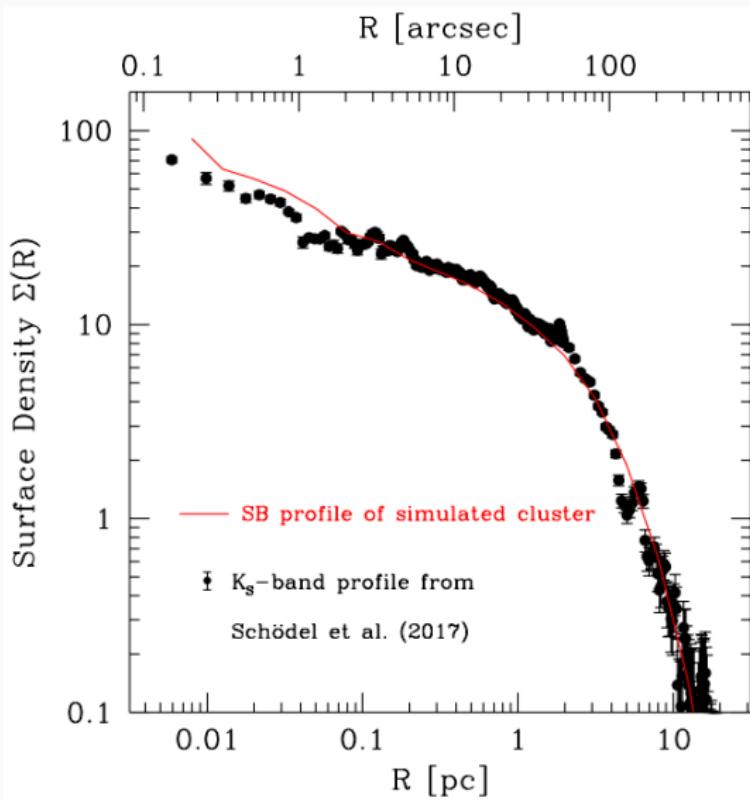


Stars and stellar-mass black holes distribute in the galactic nucleus trying to reach an equipartition of energy in such a way that compact objects (stellar-mass black holes) will dominate in mass density close to the density center of the nucleus.

[PAS et al 2004, Khalisi, PAS & Spurzem 2006, PAS & Preto 2010, Preto & PAS 2010]

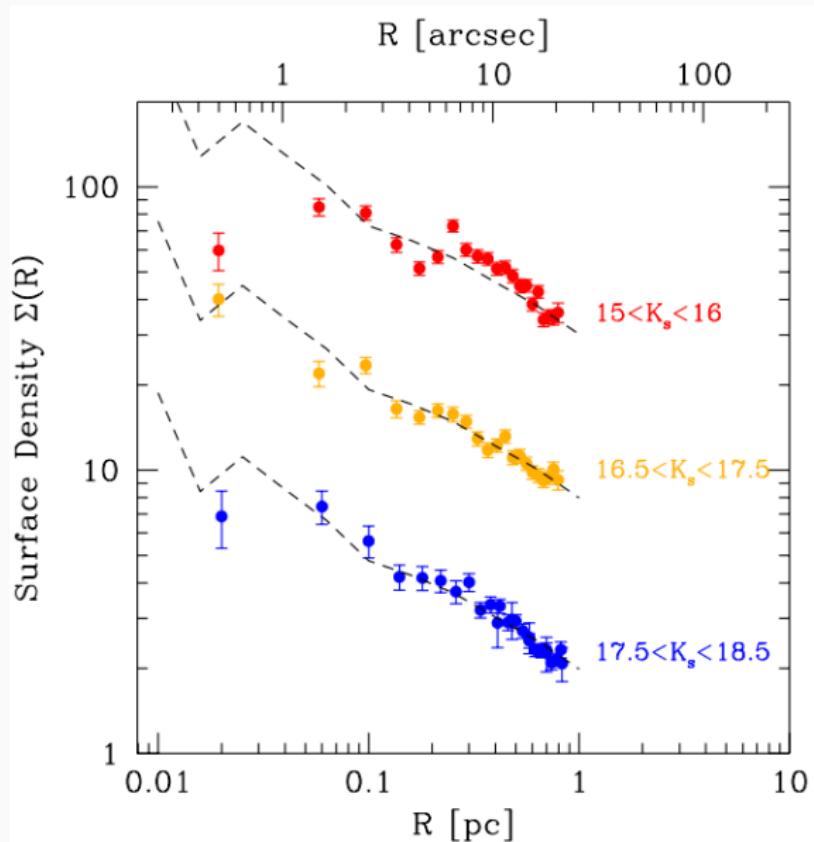
Cusps - Observers and theoreticians:  
We got it right

# Things are just fine



[Baumgardt, Amaro-Seoane & Schödel 2018, and data from Schödel et al + Gallego et al, including PAS 2018]

# Observations confirmed with simulations confirm our model



Binaries of supermassive black holes

## Merging galaxies



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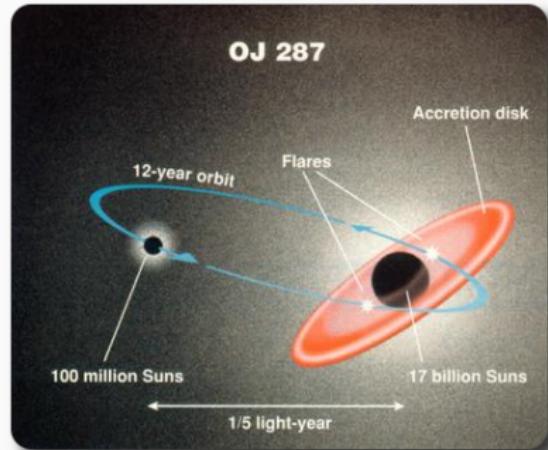
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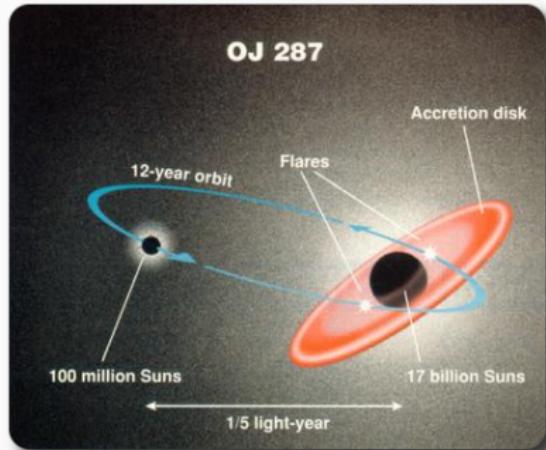
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How many have we seen?

# Observed binaries of MBHs



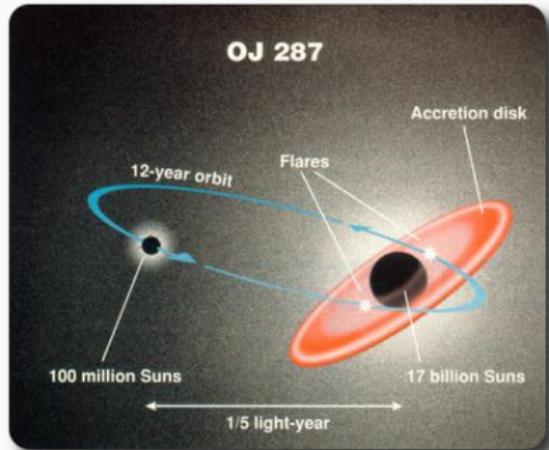
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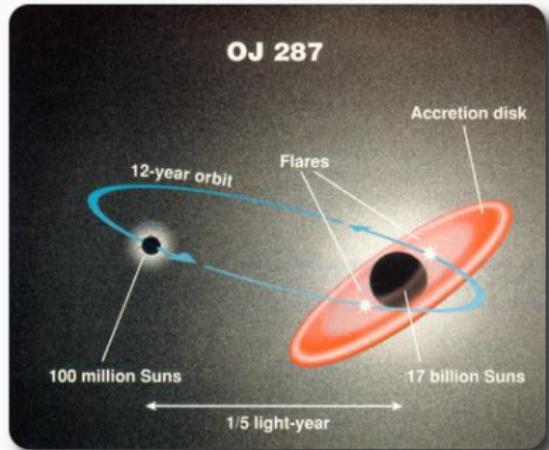
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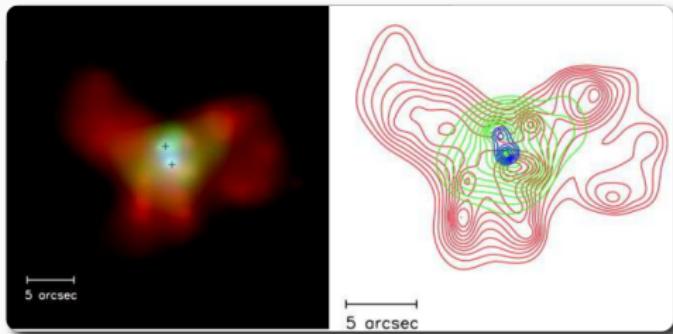
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# Observed binaries of MBHs



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OJ287 – or not? It's a blazar! BL Lac

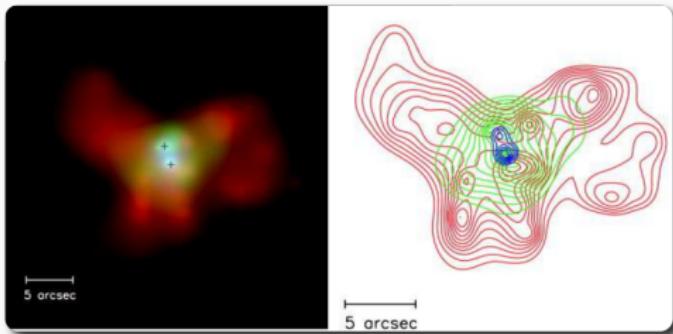
## Alternatives



[Komossa et al. 2003]

- ✓ Observations can be explained with other alternatives

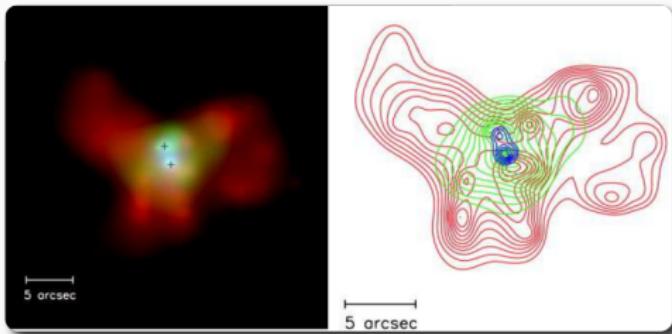
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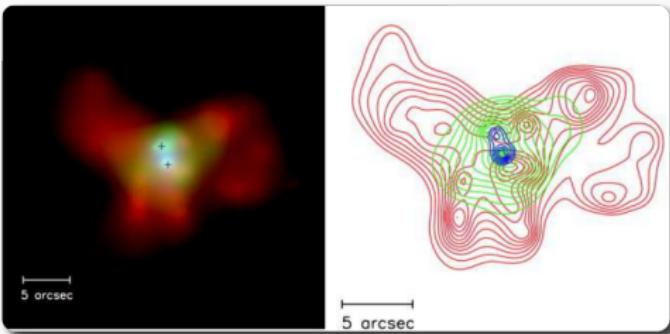
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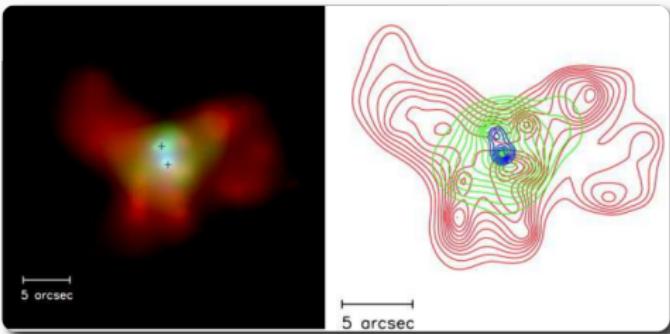
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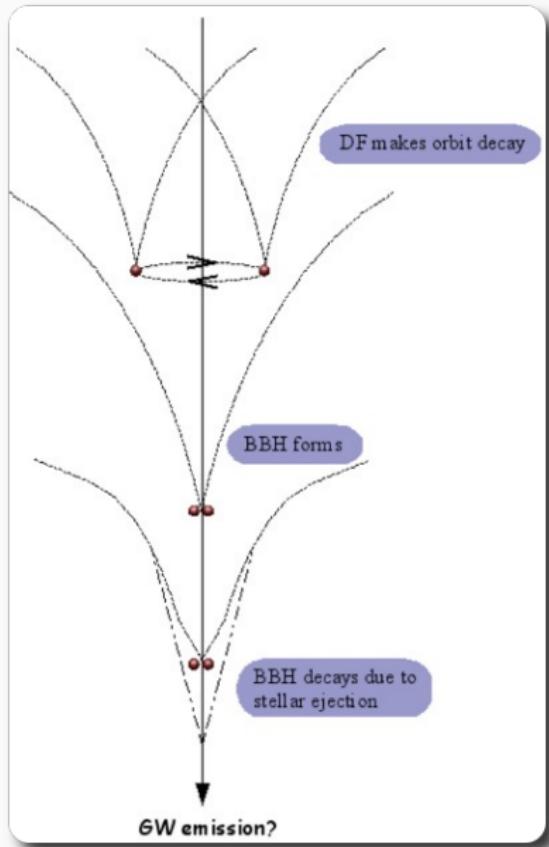
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- ✓ Another example: NGC6240 - Note: 1 arcsec = 700 pc

## No observed systems

Reference	Object	Feature	$M_1, M_2$ ( $10^9 M_\odot$ )	Separation (pc)
Sillanpaa et al. 1988	OJ 287	Optical light curve	5, 0.02	0.1
Kaastra & Roos 1992	3C 273	Wiggly jet	>1, ?	0.01
Roos et al. 1993	1928+738	Wiggly jet	0.1, 0.01	0.01
Conway & Wrobel 1995	Mrk 501	Jet mis-alignment	0.1, 0.01	0.01
Gaskell 1990	3C390.3	$H\beta$ radial velocity changes	4, 2	0.3

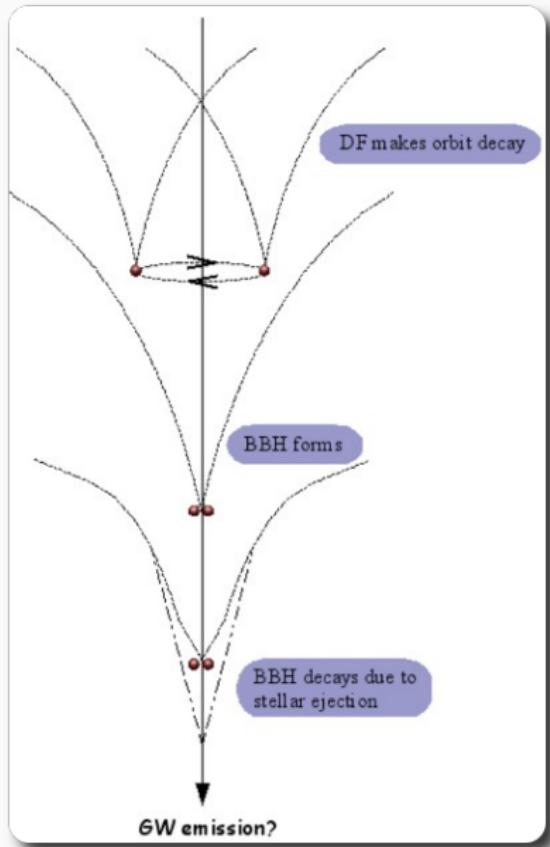
## Forming binaries of SMBHs

# Formation of binaries of MBHs

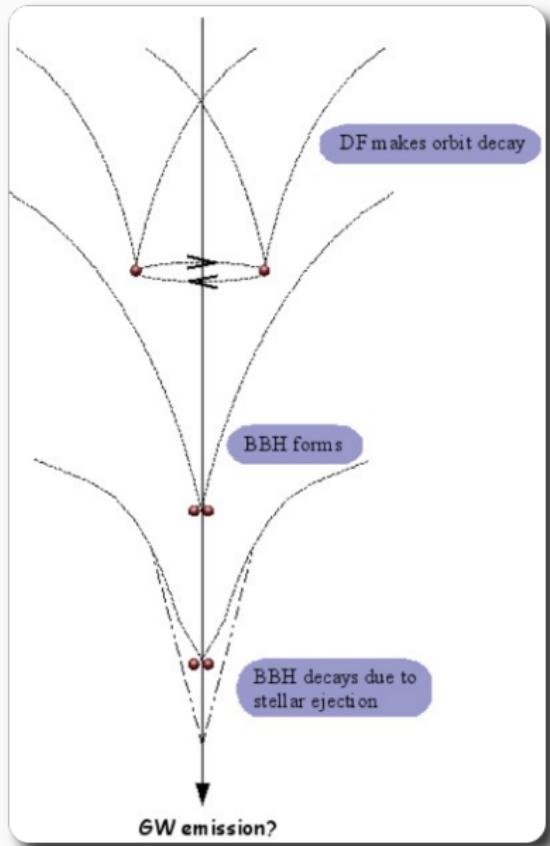


▷ Galaxies collide

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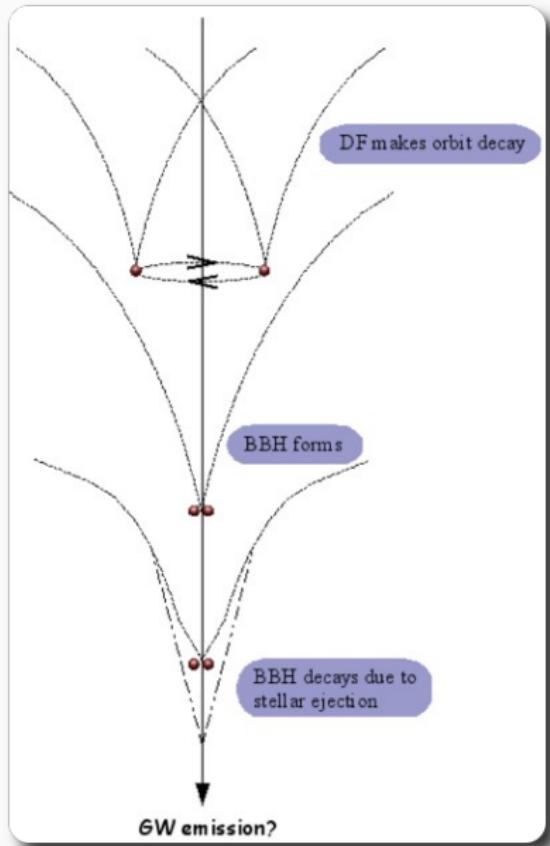


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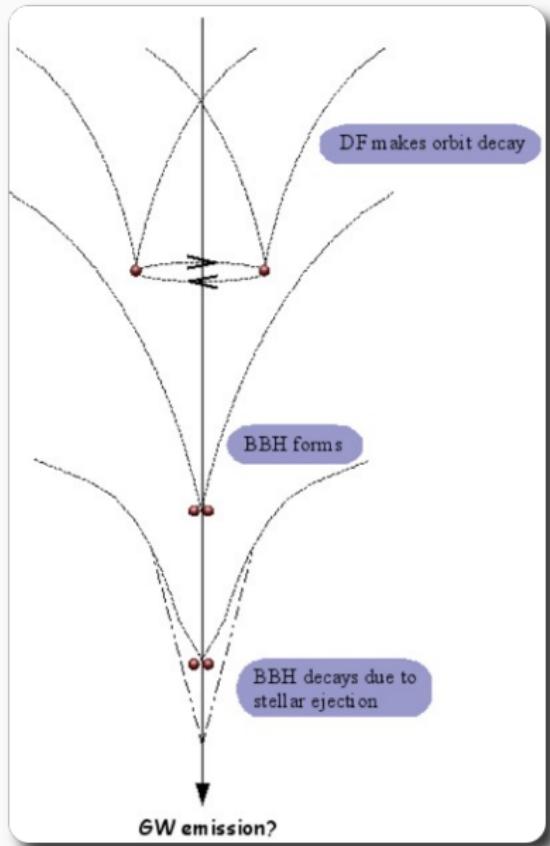
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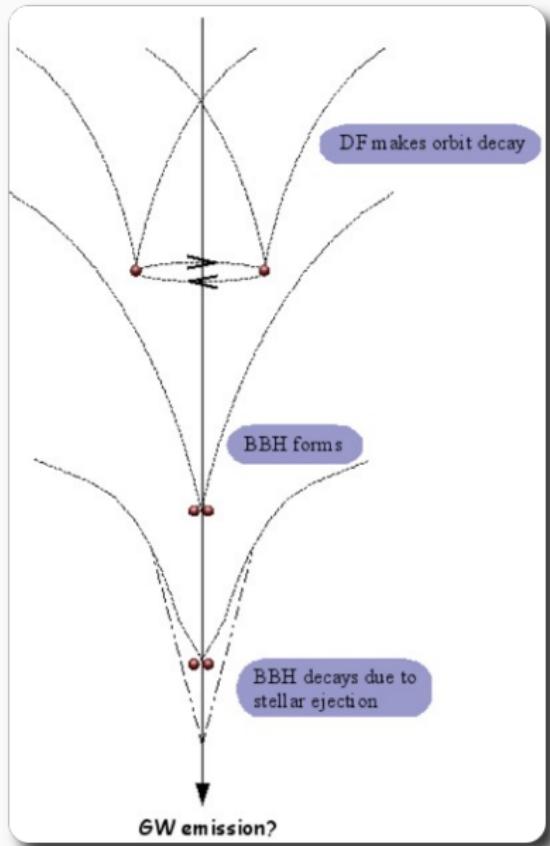
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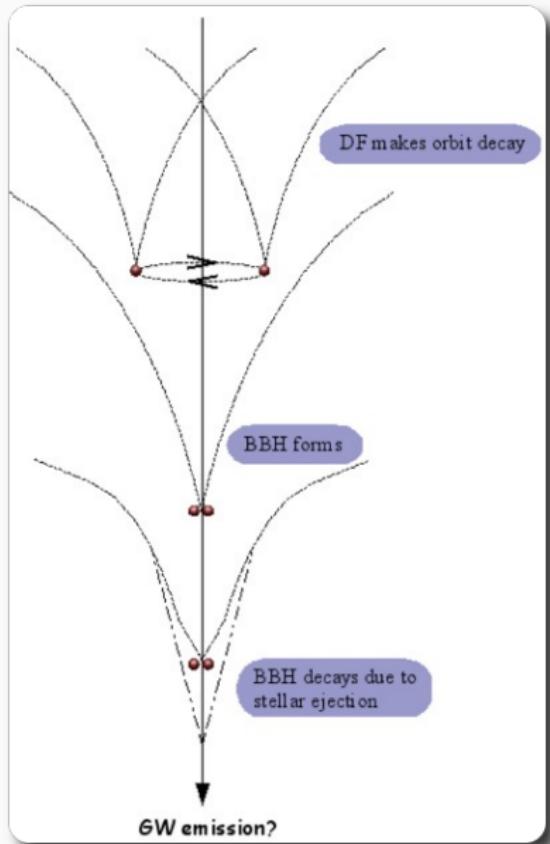
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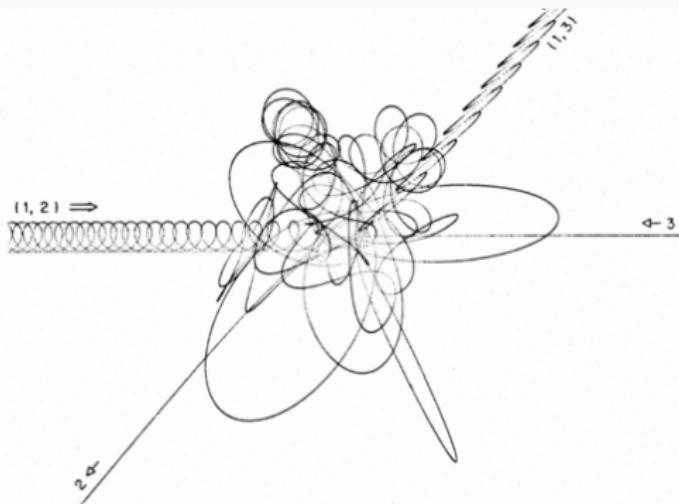
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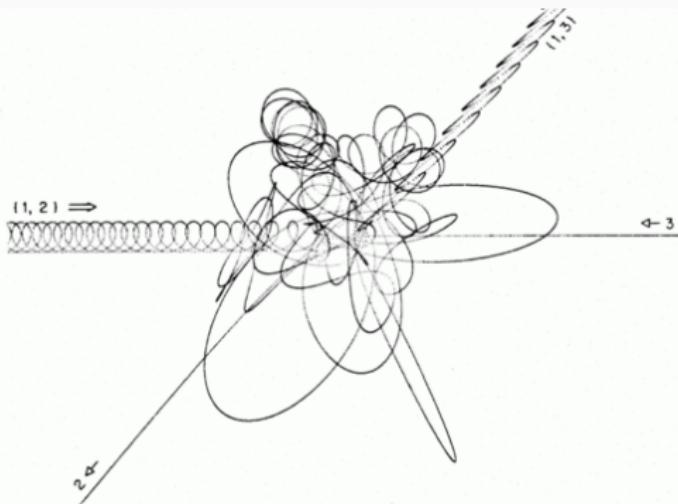
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- ▷ How will the binary evolve?

## Further shrinking the binary with chaos



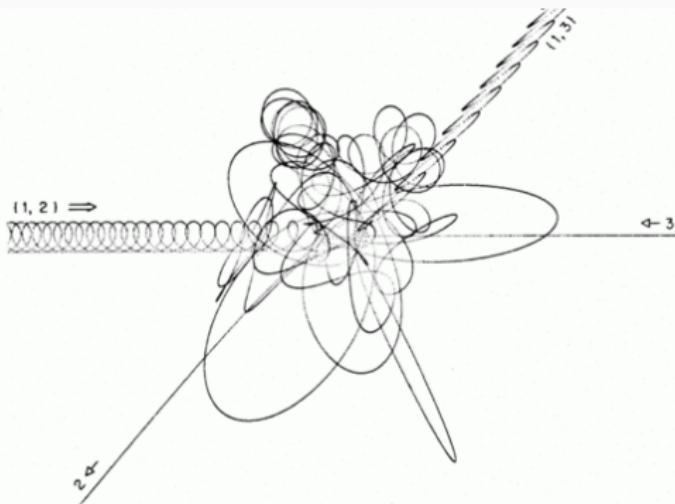
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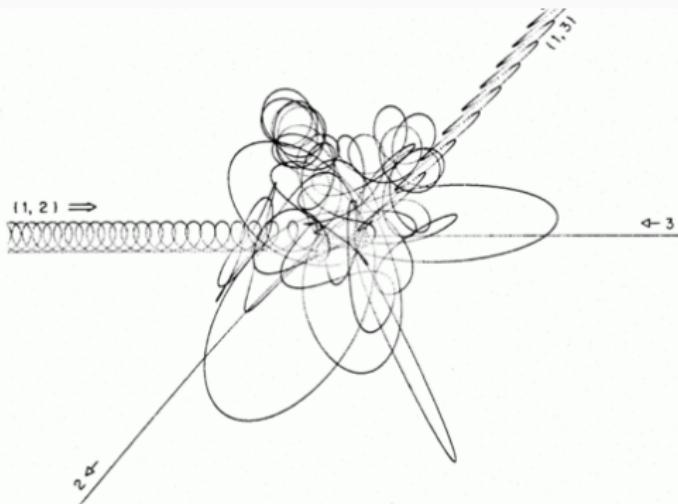
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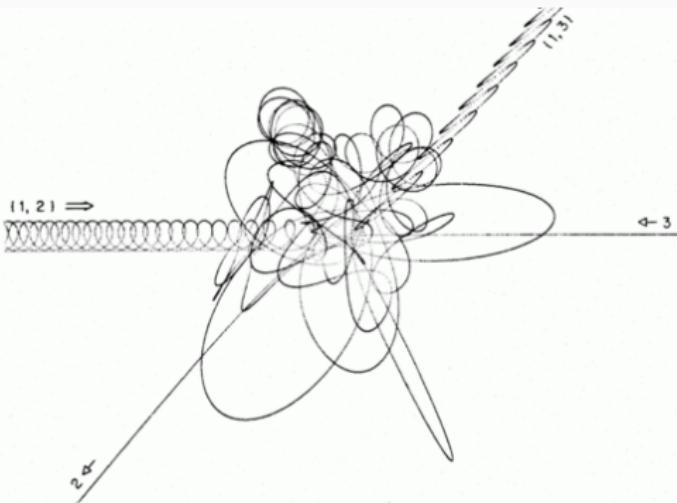
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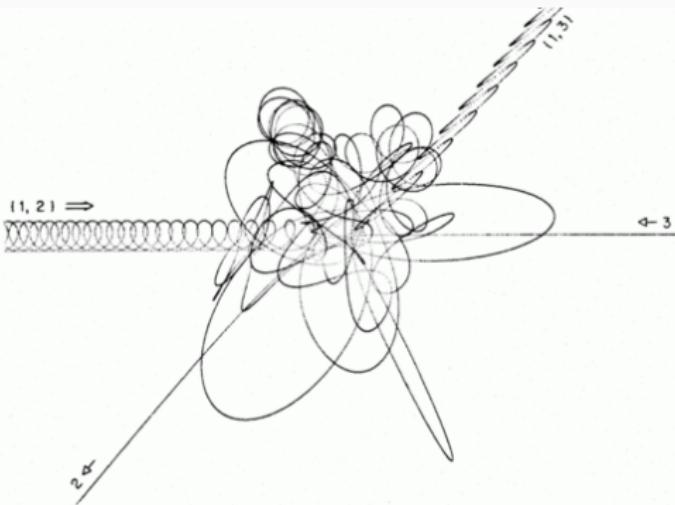
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For spherical nuclei models  $\mathcal{M}_{\text{LC}}/(\mathcal{M}_{1\bullet} + \mathcal{M}_{2\bullet}) \approx 0.01 - 1$  [Yu 2002]

- Only loss-cone stars interact with the BBH  
But in a few  $t_{\text{orb}}$ , it is depleted
- $\mathcal{M}_{\text{LC}}$  not sufficient  
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- It seems we are preparing an instrument that will see nothing

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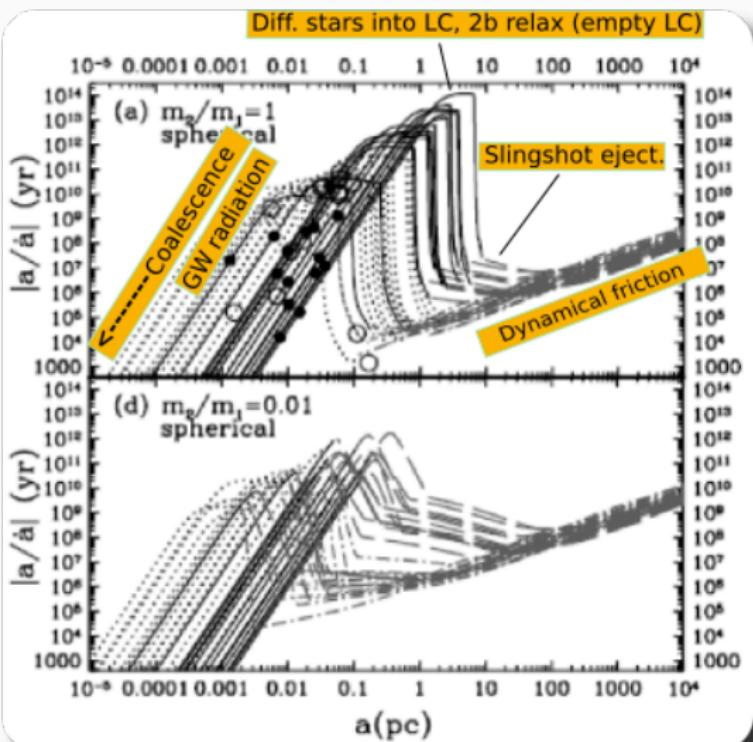
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Inducing a binary of SMBHs to decay from  $a \approx a_h \approx 1 \text{ pc}$  to a separation  $t_{gr} \lesssim 10^{10}$  yrs

# The last parsec problem



## Some possible ways to overcome the last pc problem

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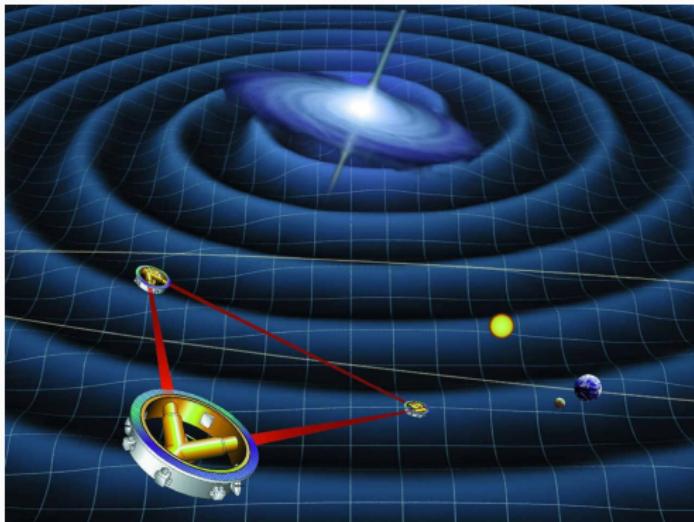
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- **IMBHs would play a similar role**, and we expect within the innermost central 10 pc some 50 IMBHs [Portegies Zwart et al. 2006]

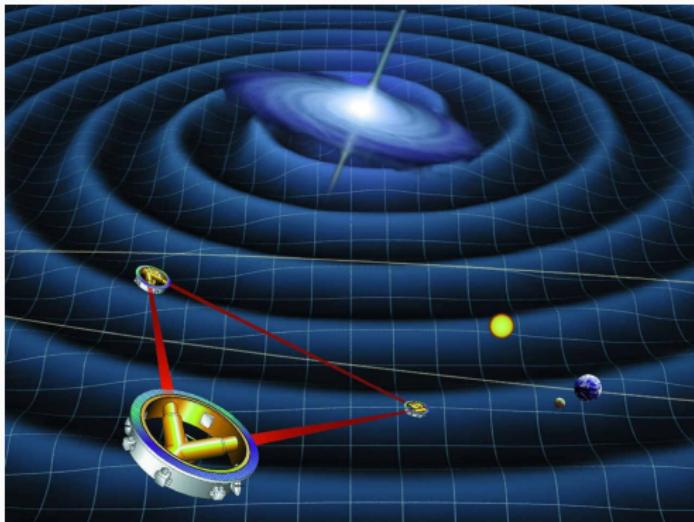
Can we detect them?

# The Laser Interferometer Space Antenna



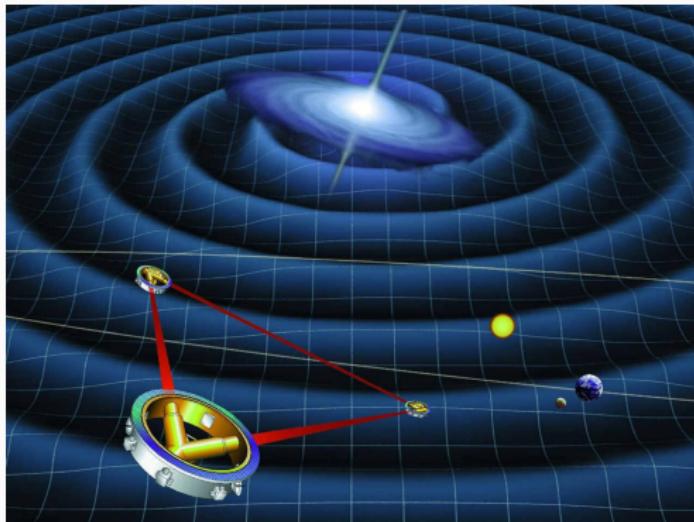
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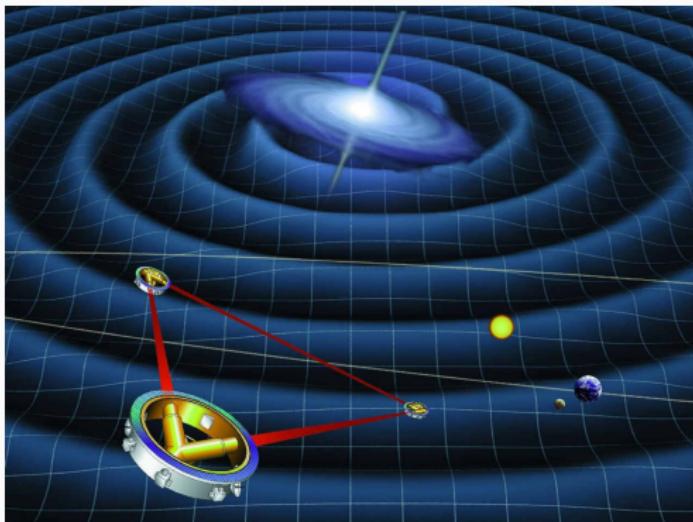
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- ★ LISA flies along an Earth-like heliocentric orbit

# The Laser Interferometer Space Antenna



- ★ On June 20, 2017 the suggested mission received its clearance goal from ESA, and was approved as one of the main research missions

[Amaro-Seoane et al 2017, arXiv170200786A]



[Vídeo: LISA, win+L]

Is this sci-fi?

No, it is not



**lisa pathfinder**

[“LISA Pathfinder mission logo” by the European Space Agency, URL

[http://sci.esa.int/science-e-media/img/6e/LISA\\_Pathfinder\\_mission\\_logo.jpg](http://sci.esa.int/science-e-media/img/6e/LISA_Pathfinder_mission_logo.jpg)]

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- ★ We approached LISA design requirements, we did 10-100 times better than ESA required

# Intermediate-mass black holes

# IMBHs



[IMBH in NGC 3783, Credit: ESO/M. Kornmesser]

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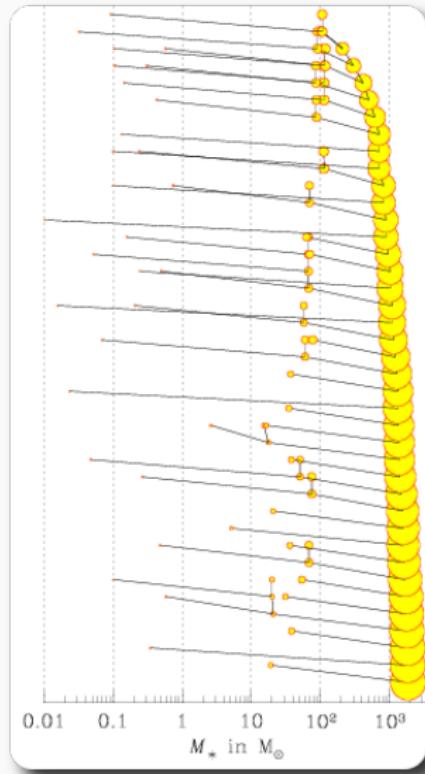
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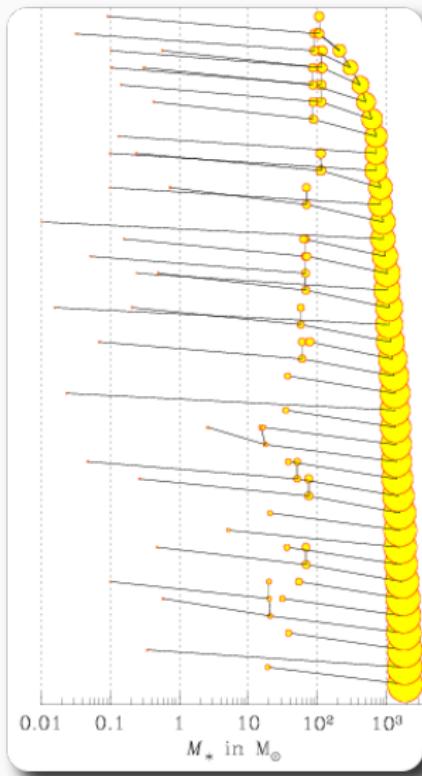
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“Intermediate-mass black holes”

# Formation of IMBHs



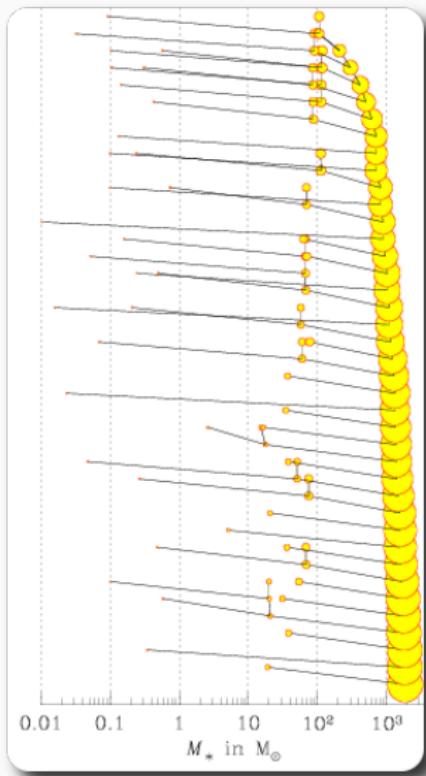
▷ Follow the growth of a runaway star

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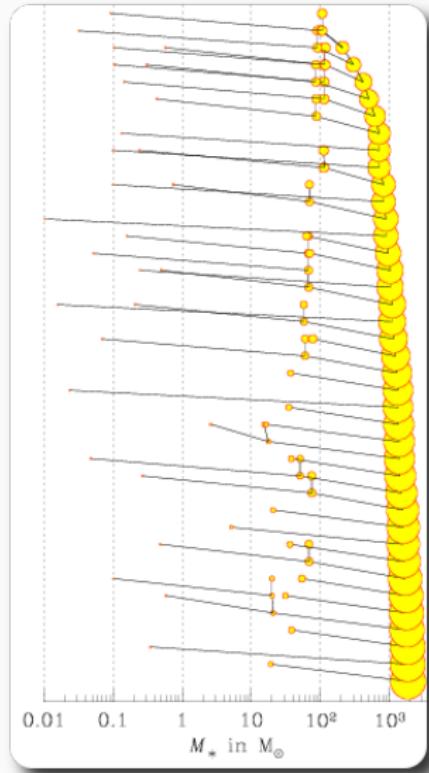
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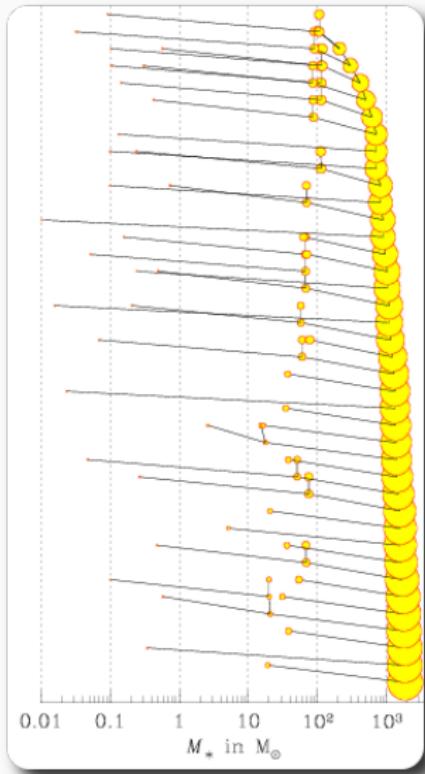
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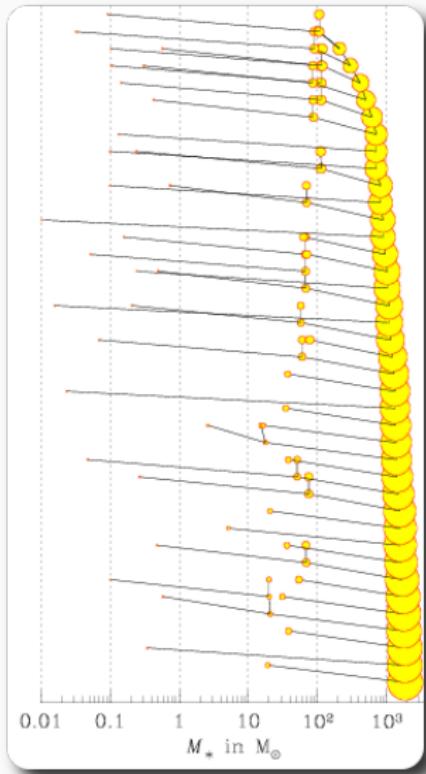
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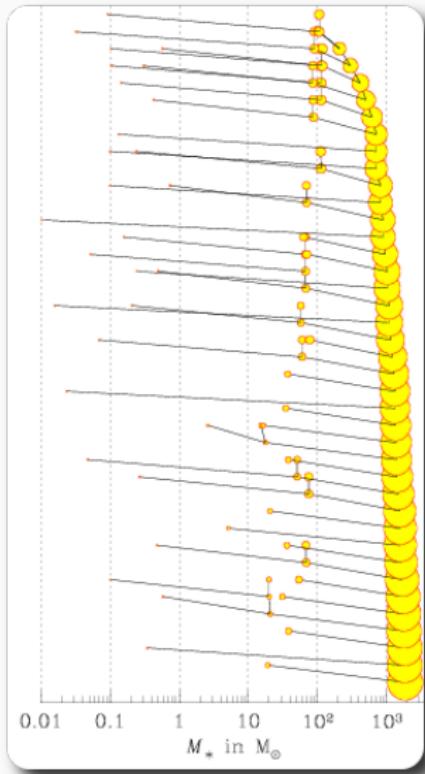
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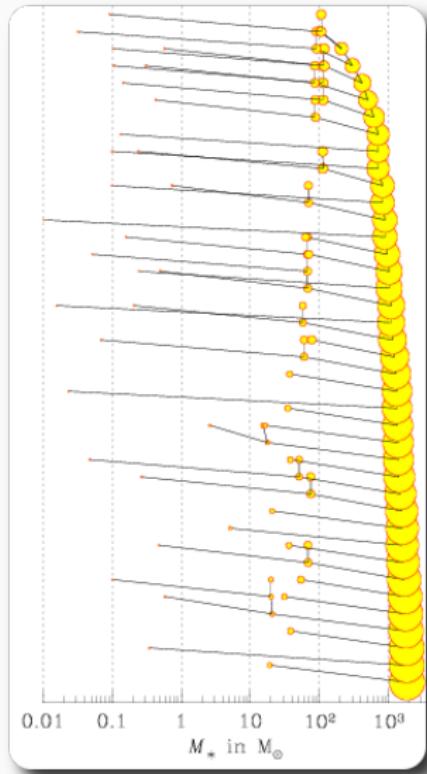
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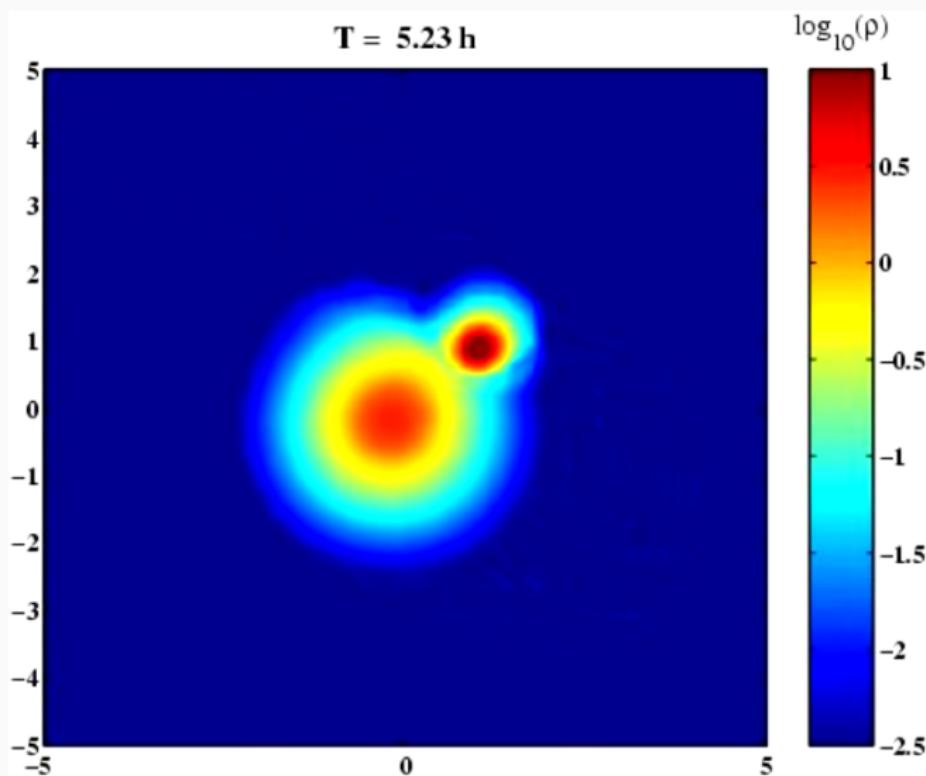
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(Stellar winds, sticky spheres)

$T = 5.23 \text{ h}$



[Vídeo: Stellar collisions]

## Binaries of intermediate-mass black holes



[Author ALMA (ESO/NAOJ/NRAO). Visible light image: the NASA/ESA Hubble Space Telescope.]

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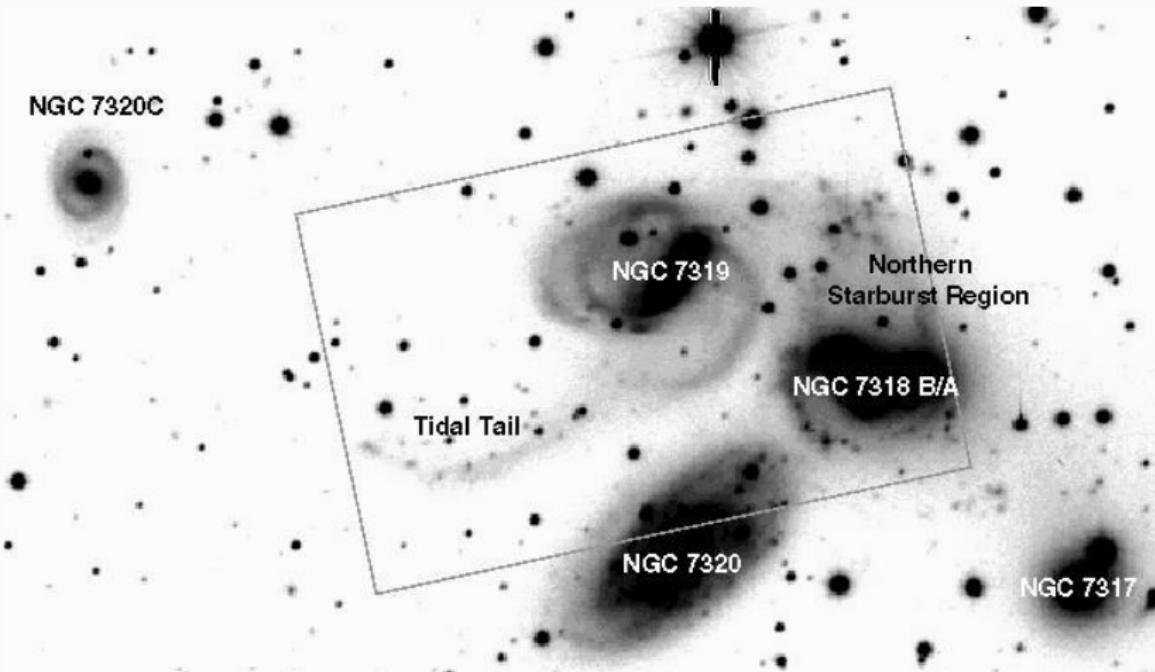
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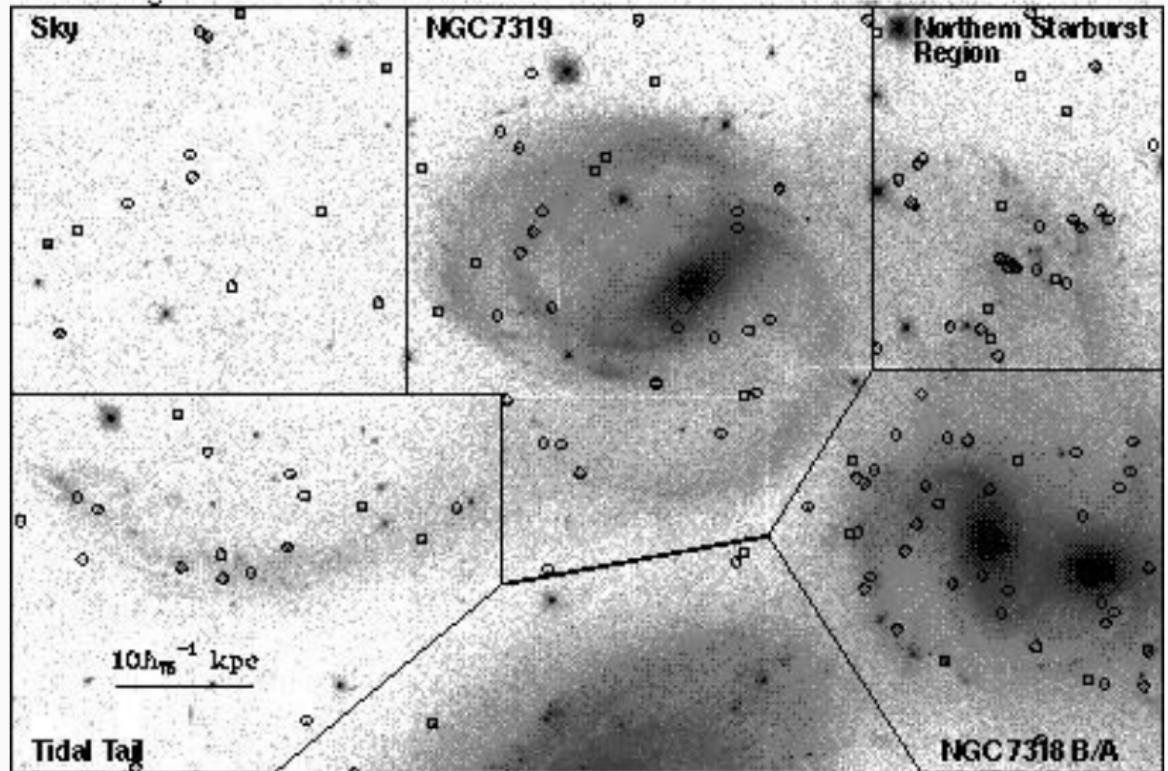


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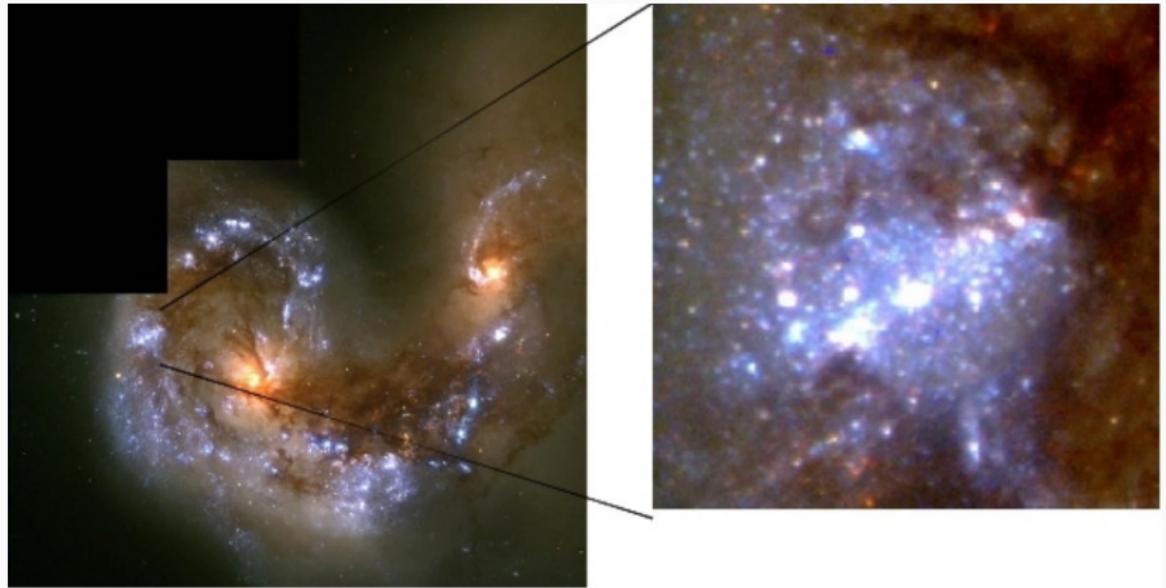
- ▶ Modern cosmology predicts hierarchical formation in the Universe
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- ▶ Star formation: **clusters of clusters, many of which bound**



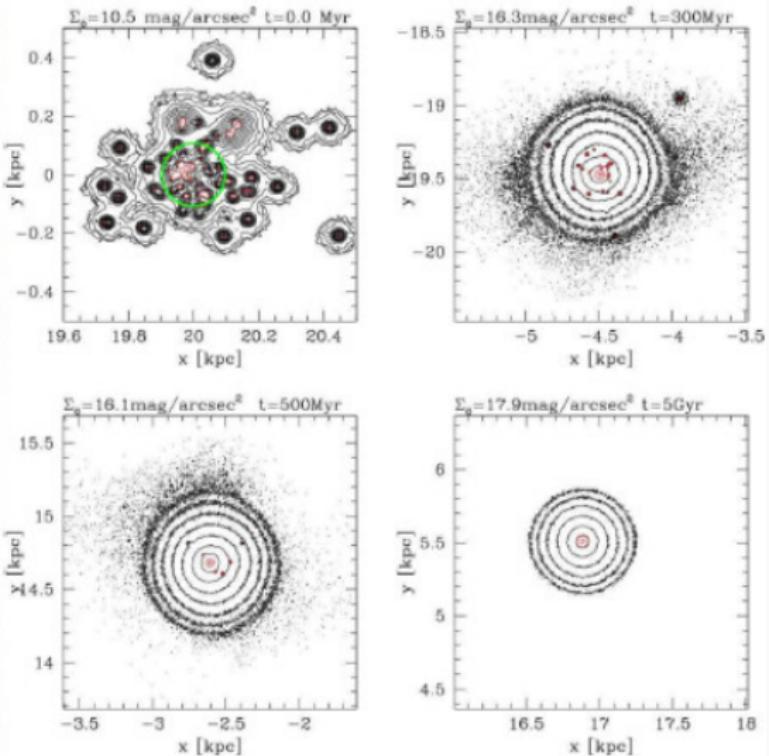
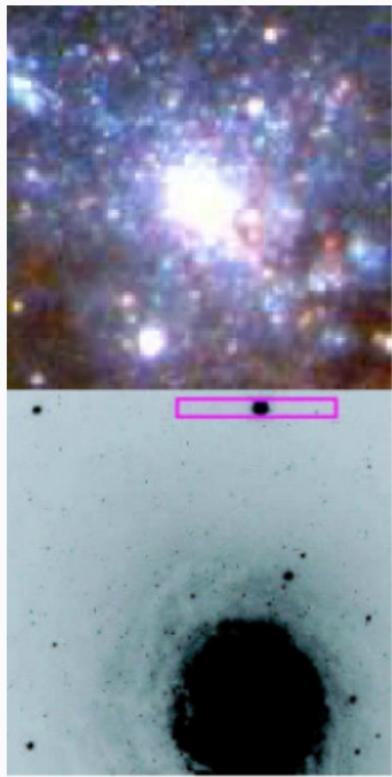
Stephan's Quintet, [Gallagher et al. 2005]



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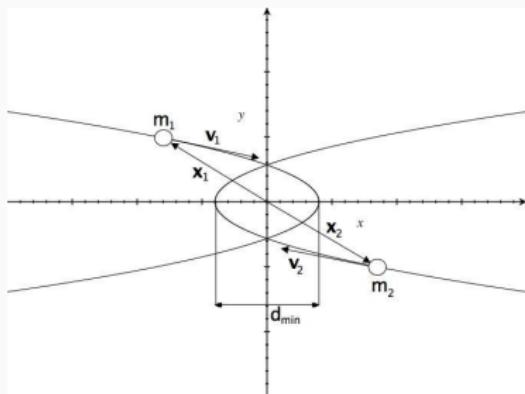


[Vídeo: Clusters of clusters]



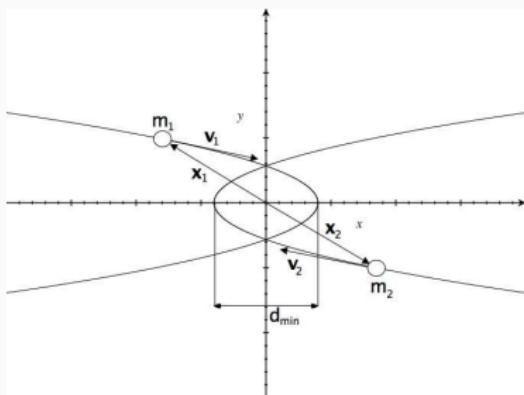
Possible formation of W3 in NGC7252 [Fellhauer & Kroupa 2002]

# Numerical experiments



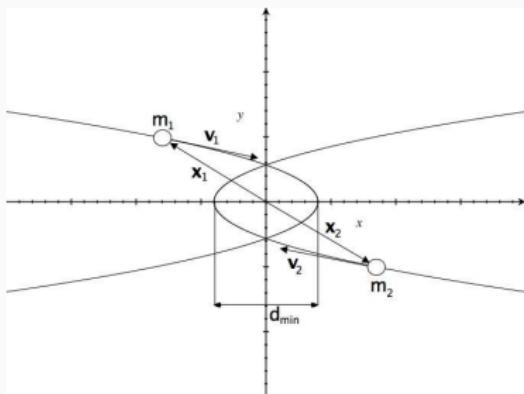
- ▷ The most accurate thing we can do **Direct summation of all forces, N-body**

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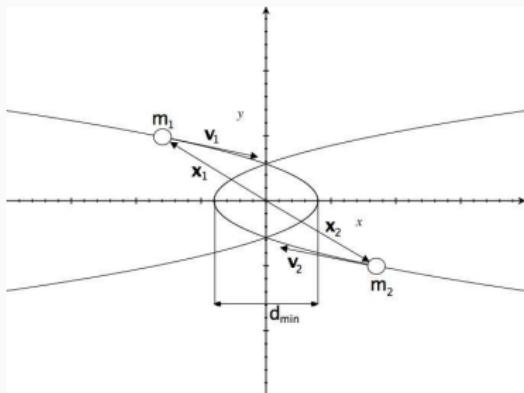
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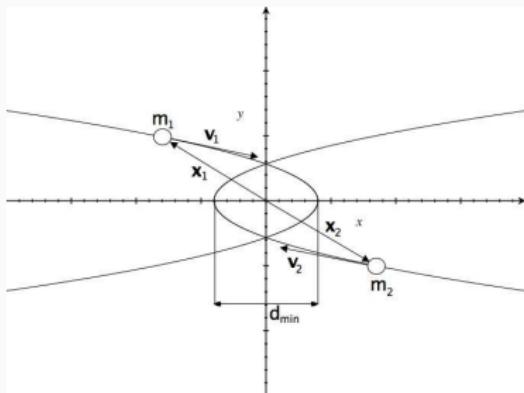
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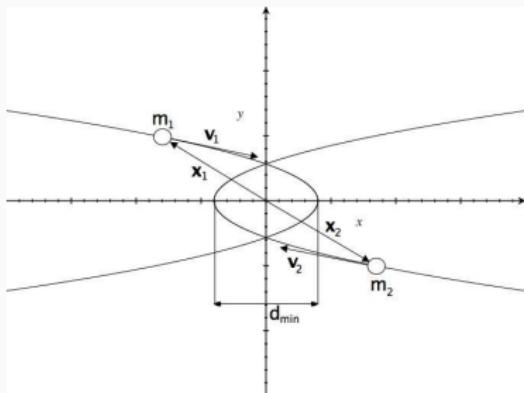
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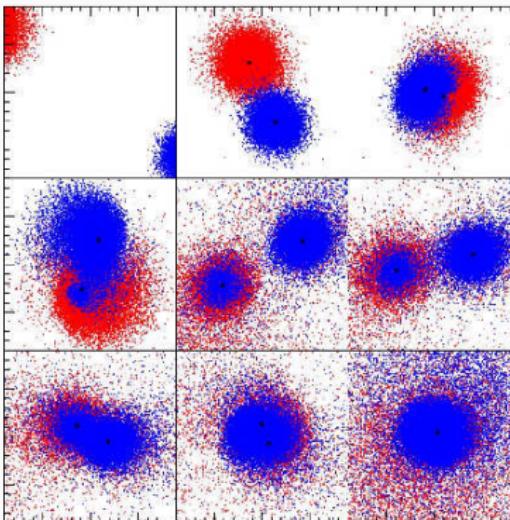
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- ▷ Only early evolution, **impossible to simulate down to GW regime**

# Merging clusters

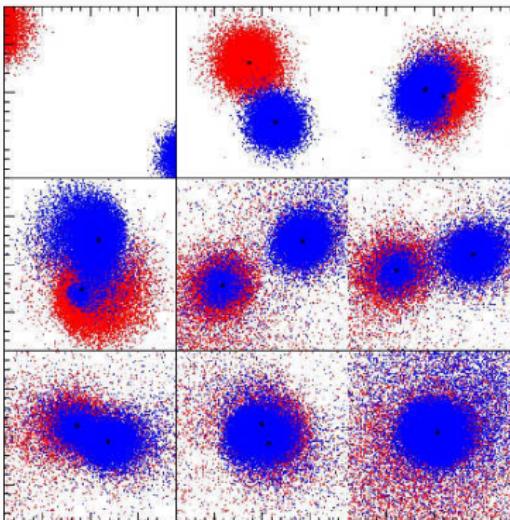


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[Vídeo: Crash of two clusters]

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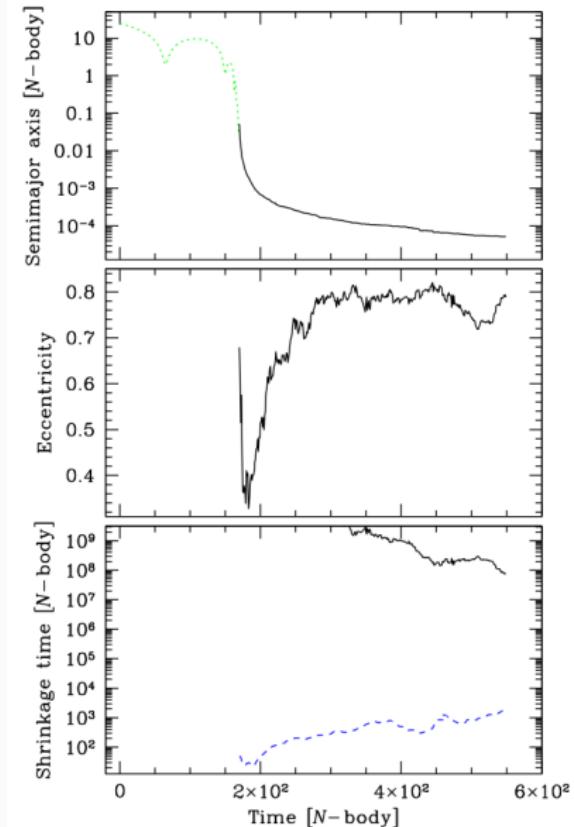


- ▷ As with massive black holes, IMBHs can form binaries
- ▷ This constitutes a **powerful source of GW** for LIGO and LISA



[Vídeo: Crash of two clusters]

# Evolution of the binary



## Down to the relativistic regime

- ▷ How will it enter the detection band?

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Two different cases, using 128,000 stars

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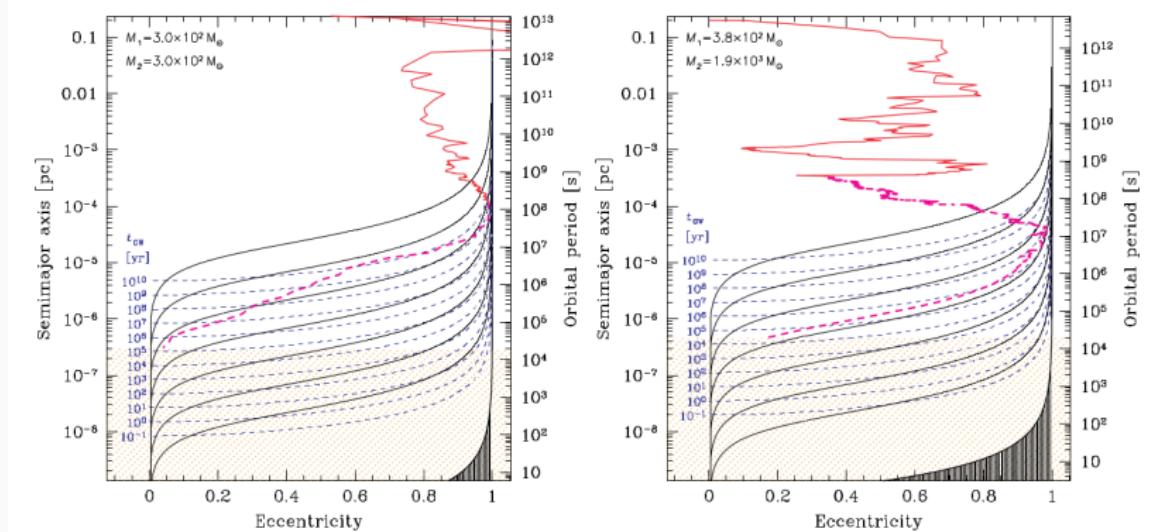
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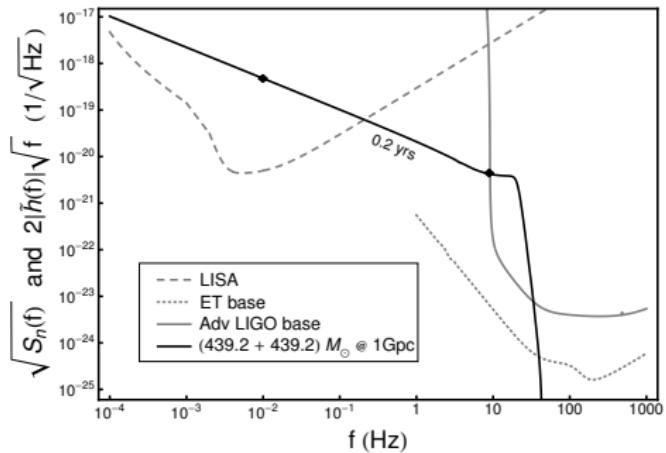
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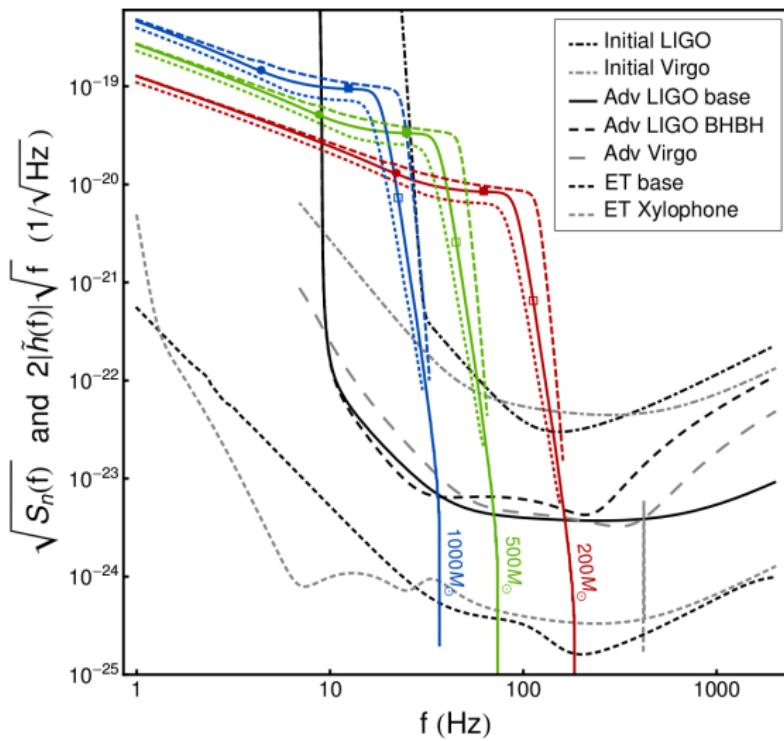


[Amaro-Seoane & Freitag 2006]



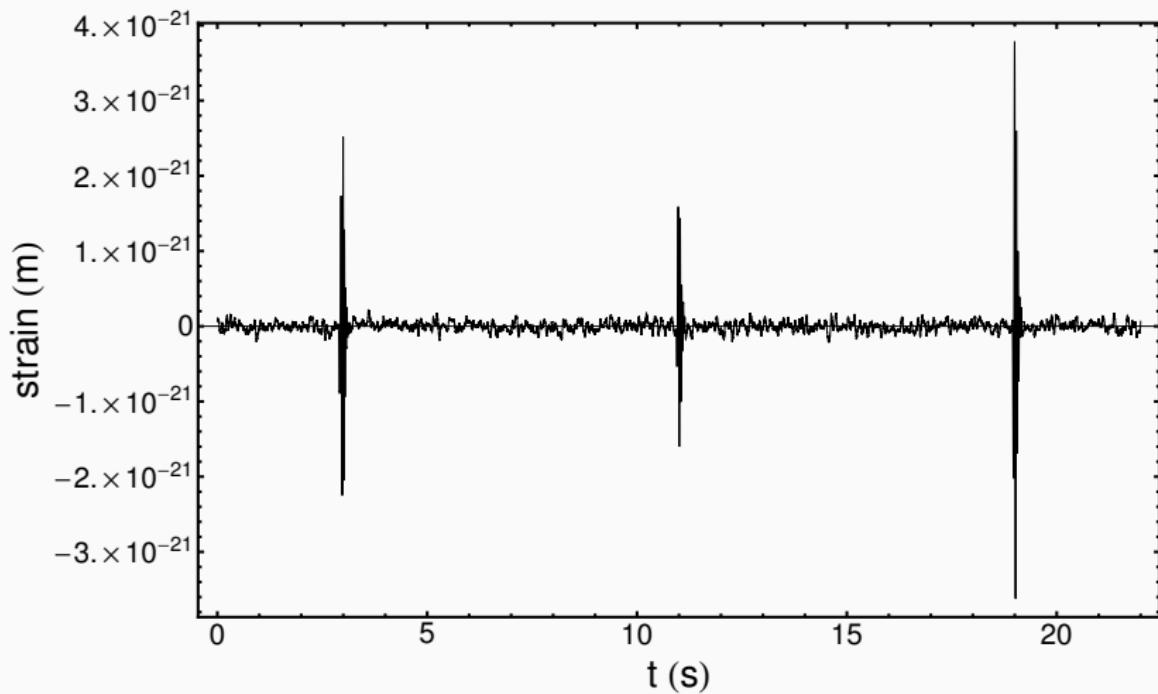
Enough massive binaries can be seen from the bandwidth of space-borne detectors to ground-based ones: Detailed evolution of inspiral, merger and ringdown, crucial to assess the black hole hypothesis.

# Different masses



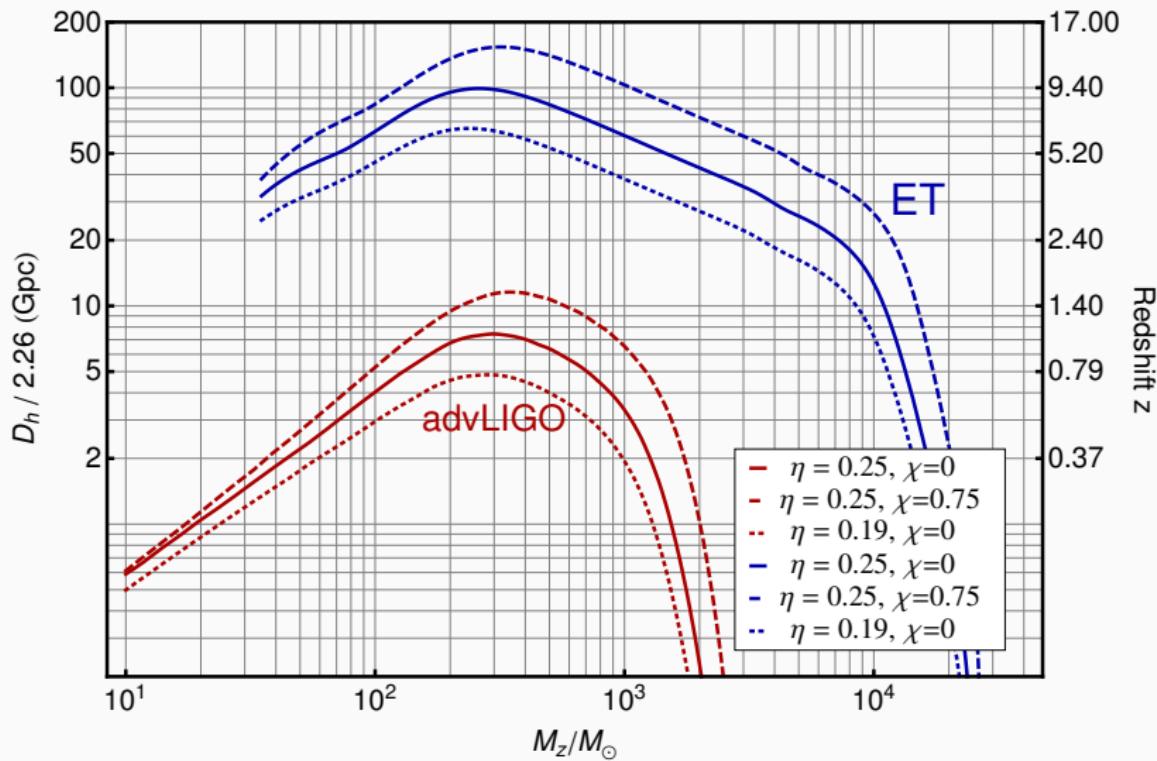
[Amaro-Seoane & Santamaría 2010]

# Three hidden IMBH binaries in LIGO simulated noise



[Amaro-Seoane & Santamaría 2010]

# Cosmology with IMBH binaries



[Amaro-Seoane & Santamaría 2010]

# Conclusions

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# GW Jackets



Seen at the Gangnam Station Underground Shopping Center, next to line 2, Seoul, 23/Dec/2017

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- ✗ Supermassive- and intermediate-mass black holes probably exist:  
It'd be strange that they didn't!
- ✗ "Unfortunately" we do science and such words (probably, strange, etc) don't matter – We must prove their existence

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- To prove them we need to probe their horizon: The capture of a compact object will probe a regime where photons can barely escape
- We have to overcome 10 orders of magnitude to get there: Not exactly trivial, and there will be surprises
- We've just started: The Gravitational Wave Astronomy era is now

Questions?