

# FROM ALGORITHMS TO ASTROPHYSICS: MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

## NIKOLAOS STERGIOULAS

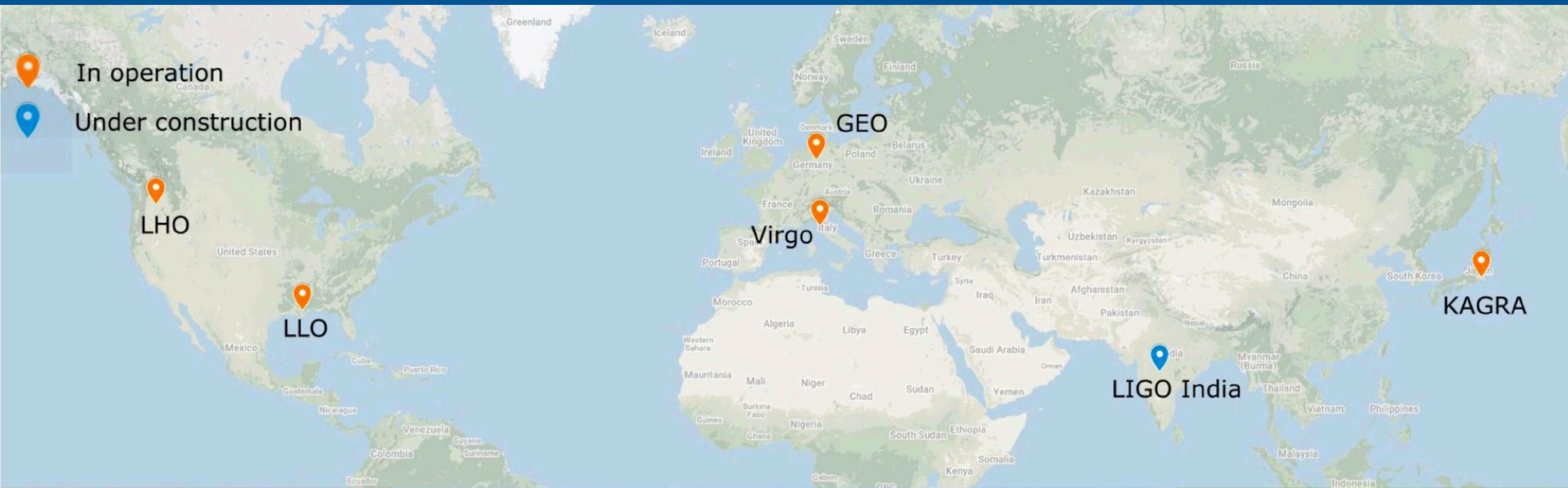
DEPARTMENT OF PHYSICS

ARISTOTLE UNIVERSITY OF THESSALONIKI



# **PART A. BINARY BLACK HOLE MERGERS**

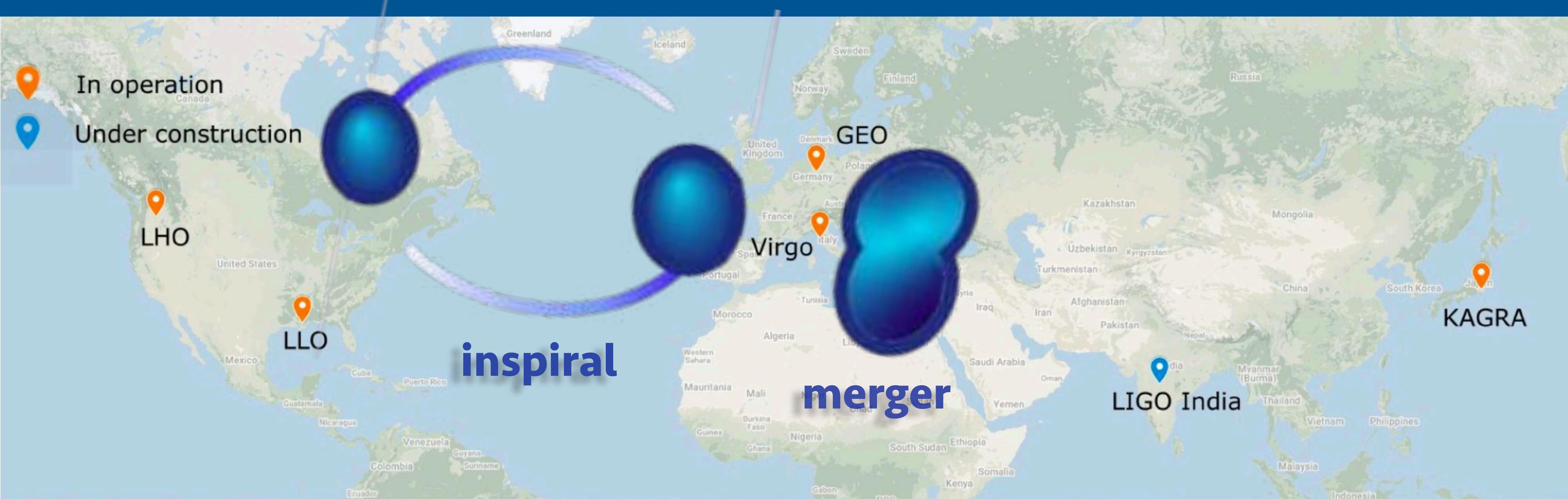
# INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



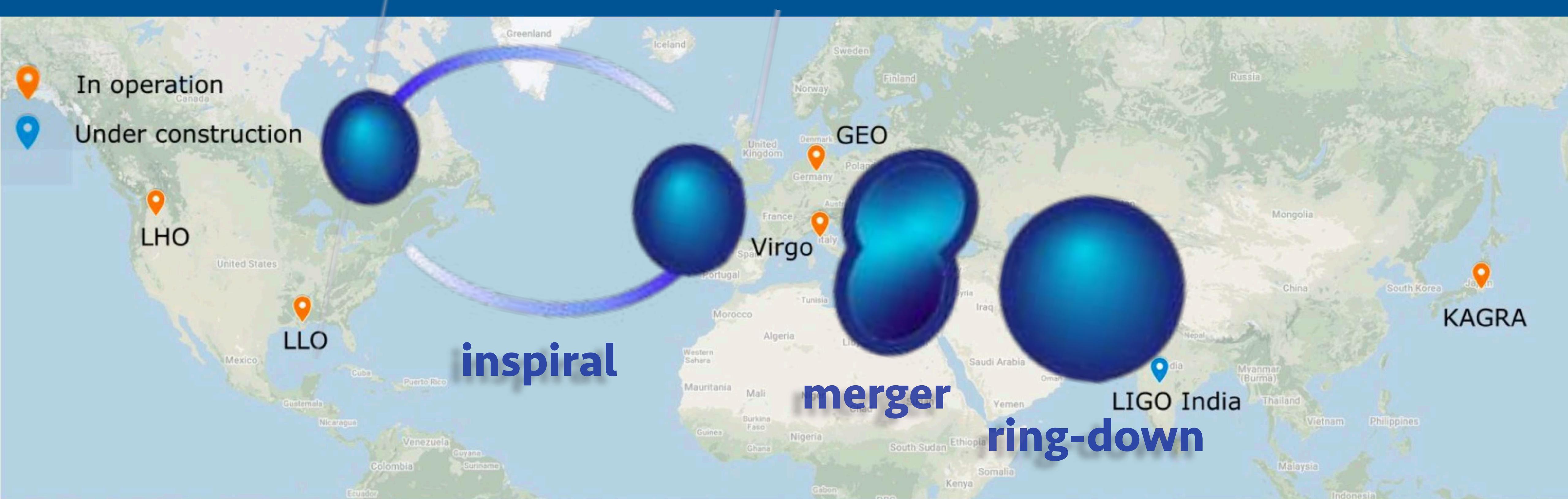
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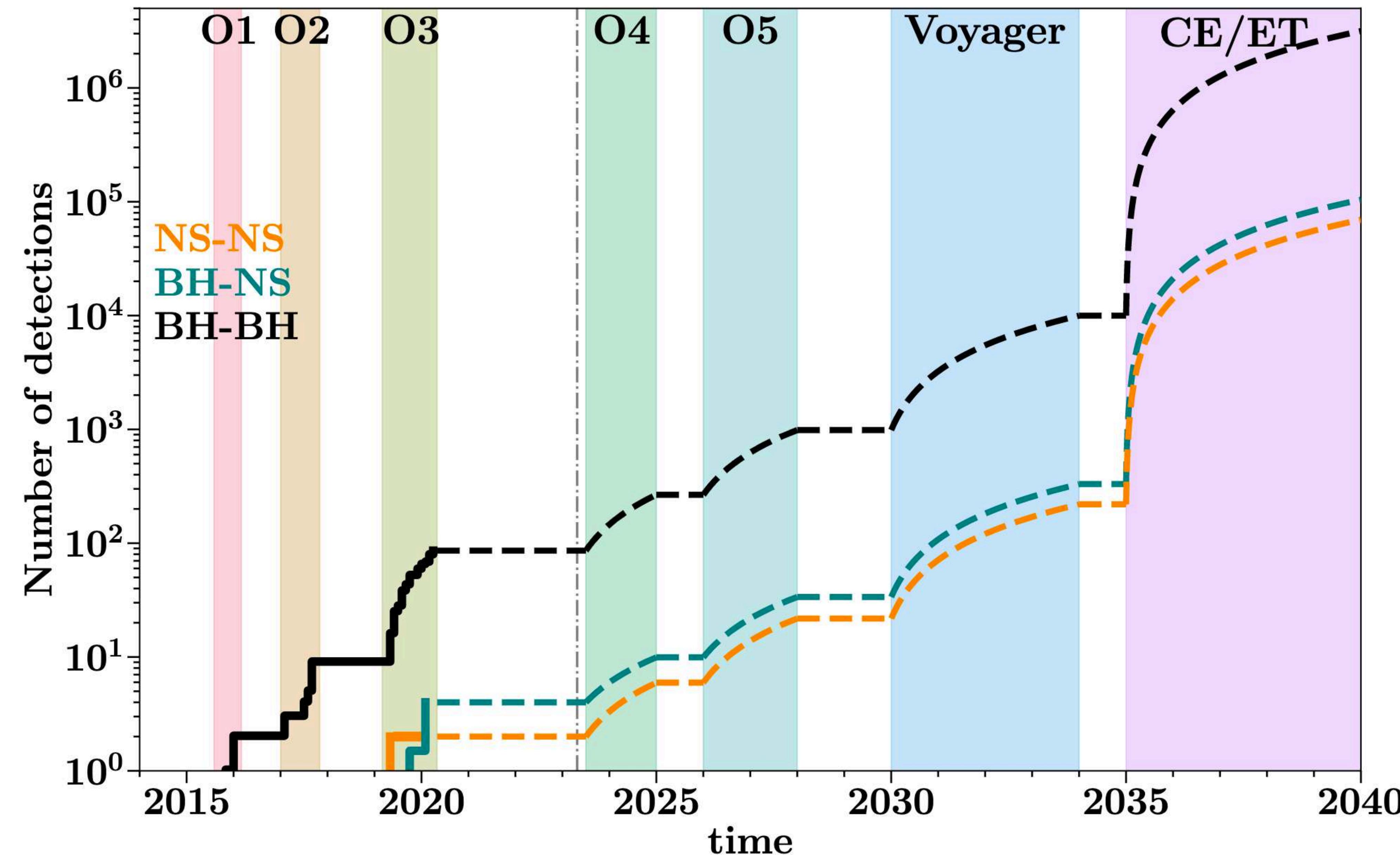
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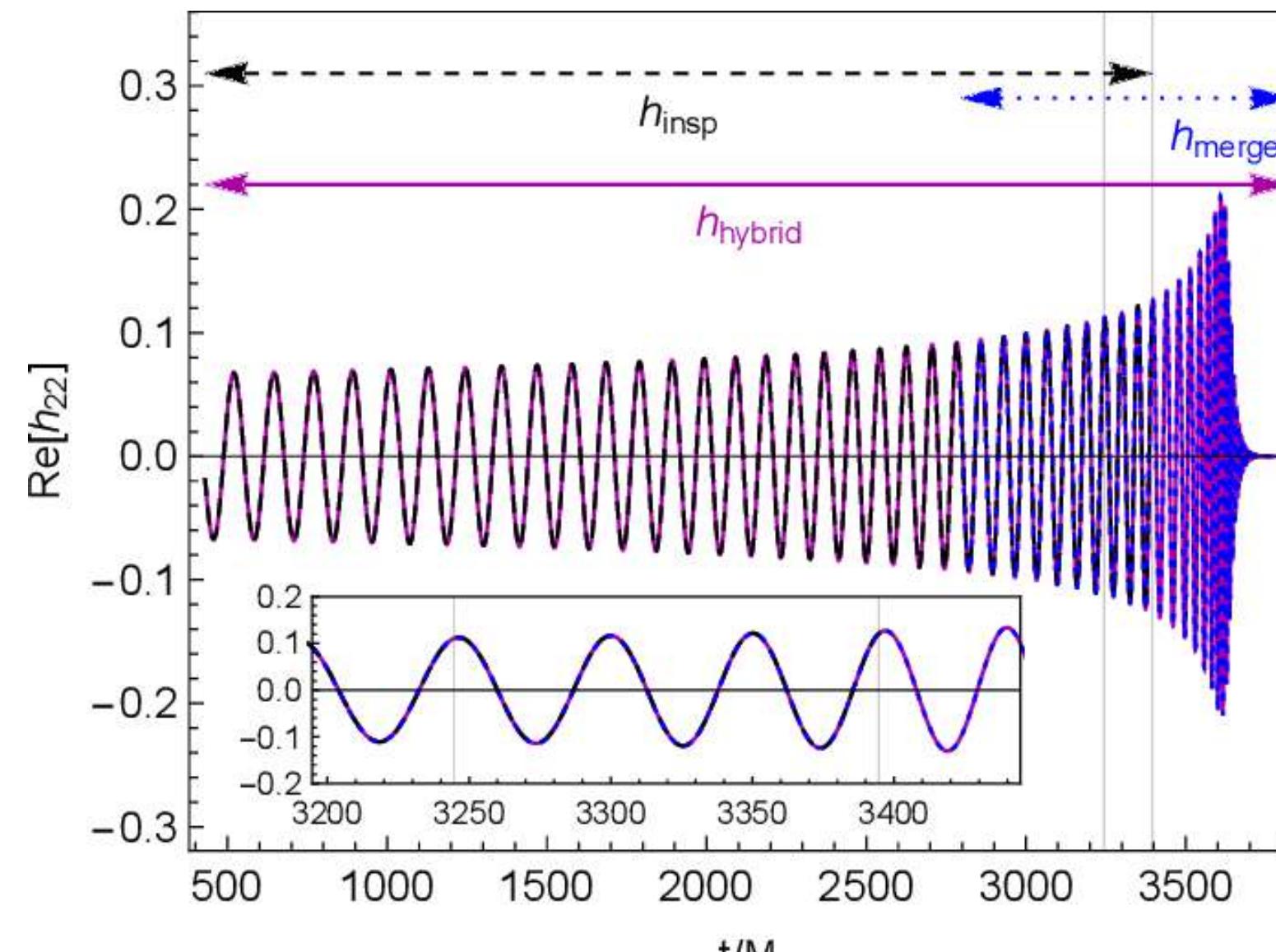


# EXPECTED NUMBER OF DETECTIONS

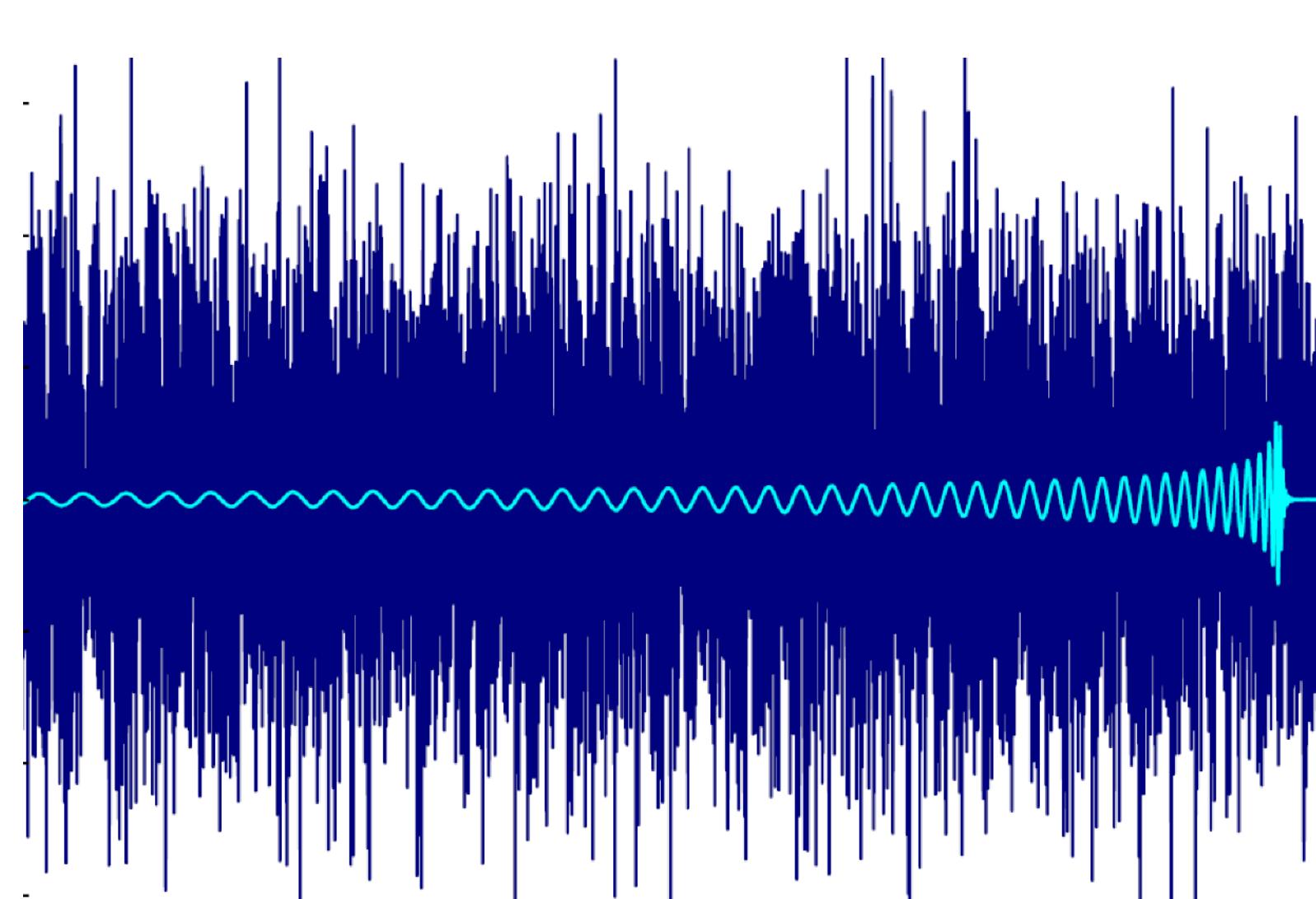


# MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

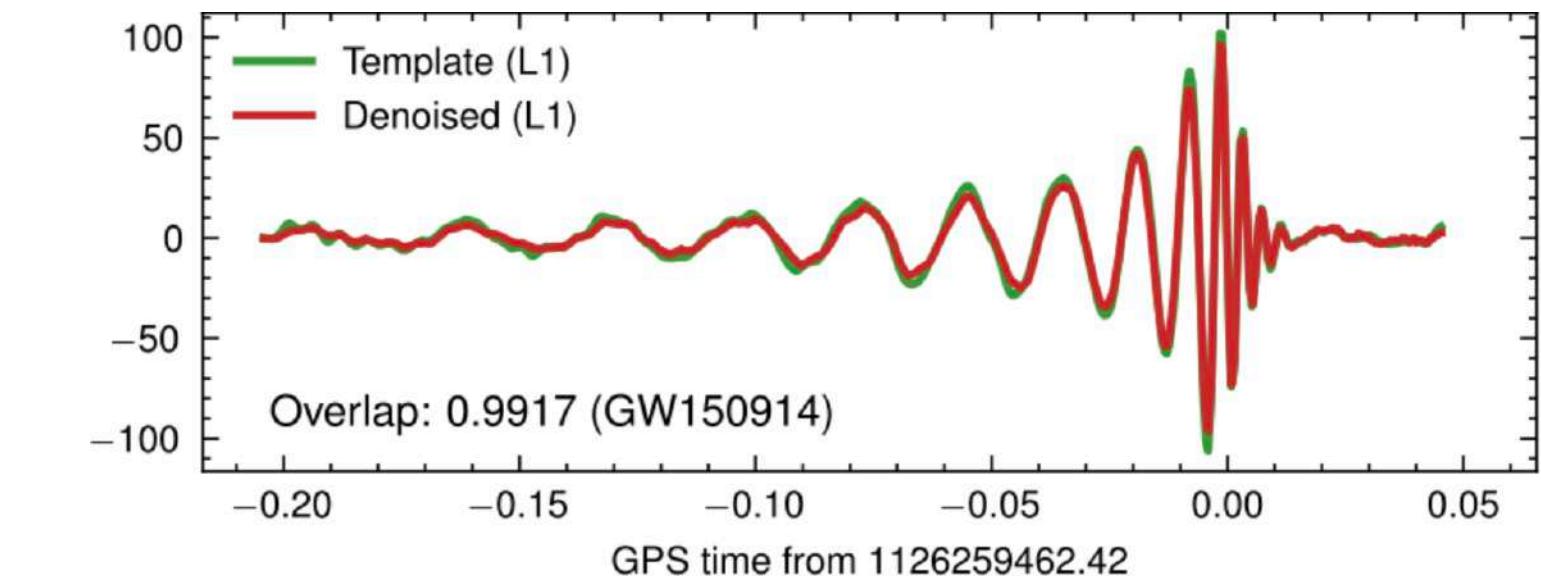
## Waveform Modeling



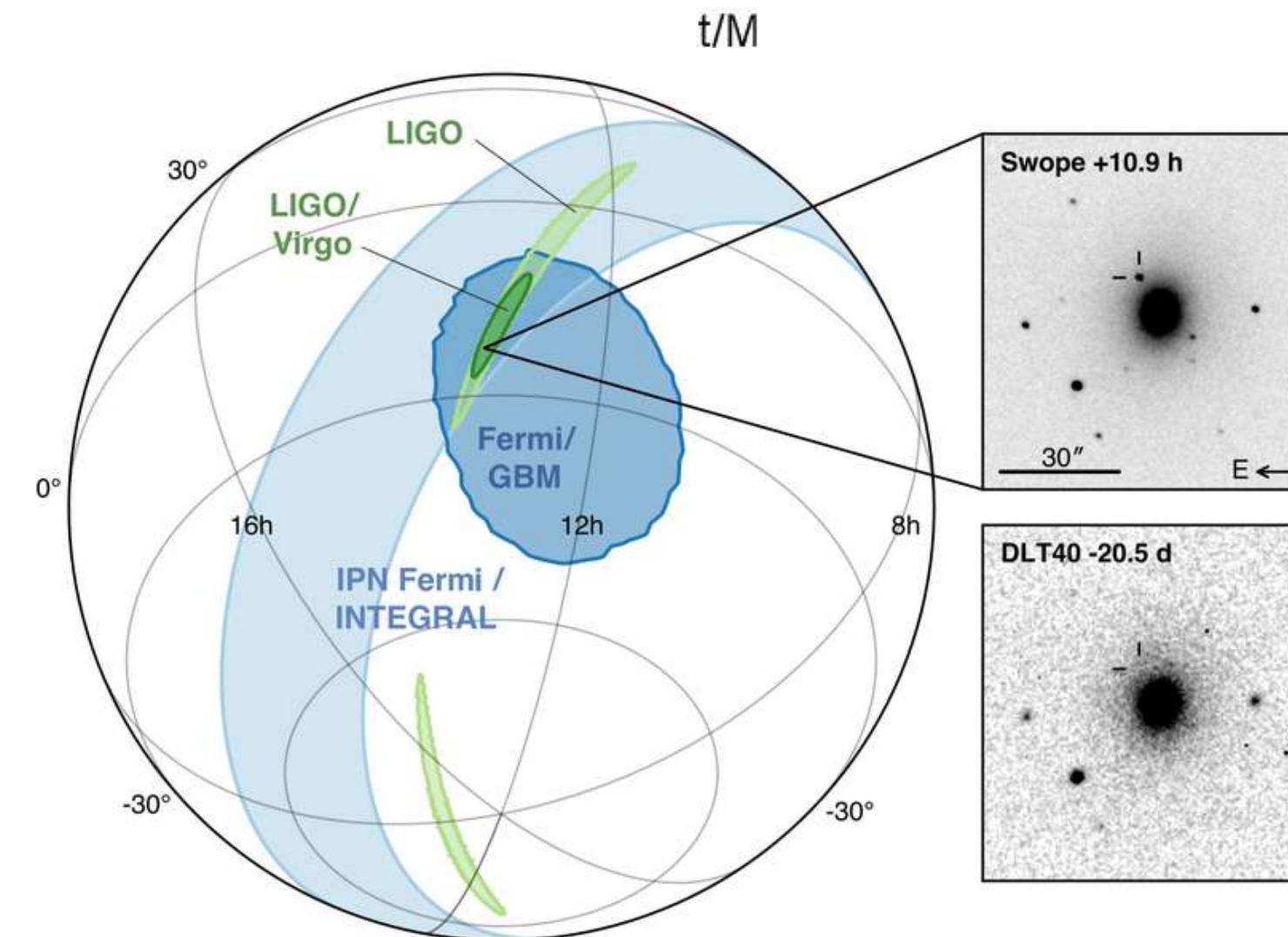
## Detection



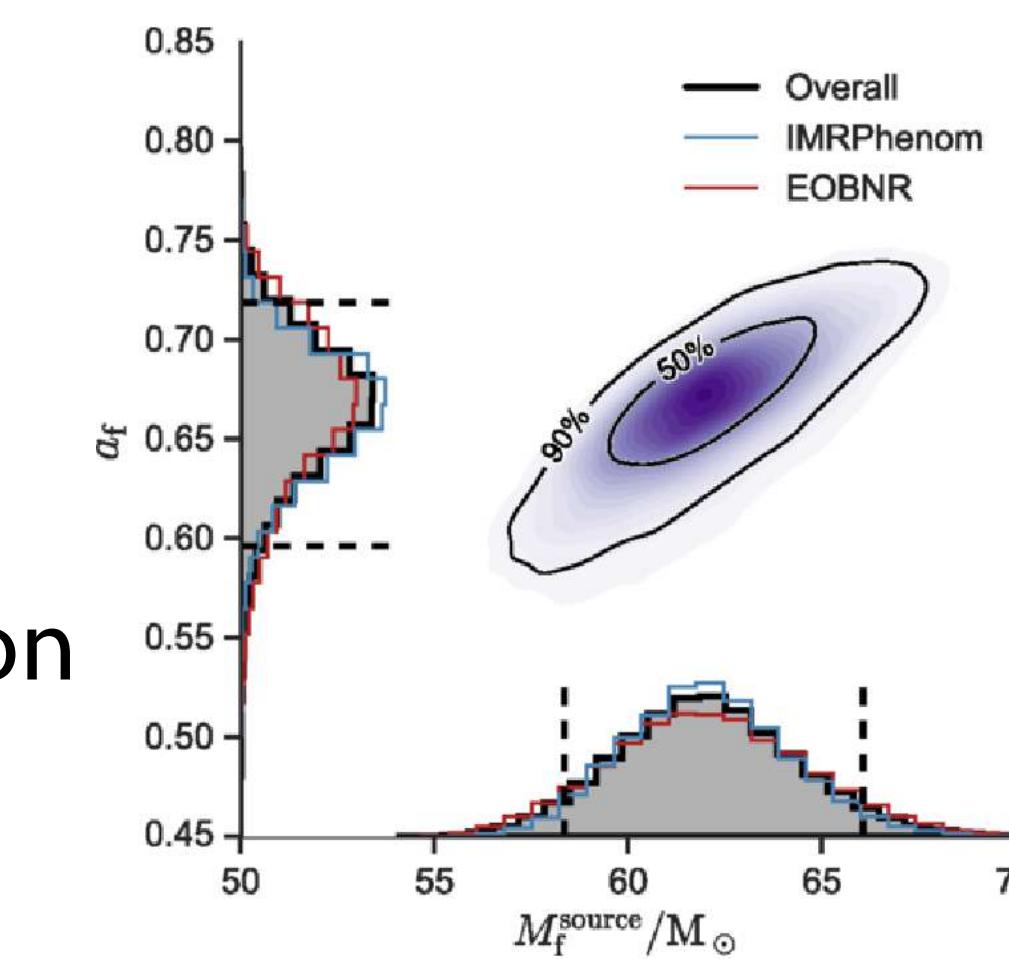
## Denoising



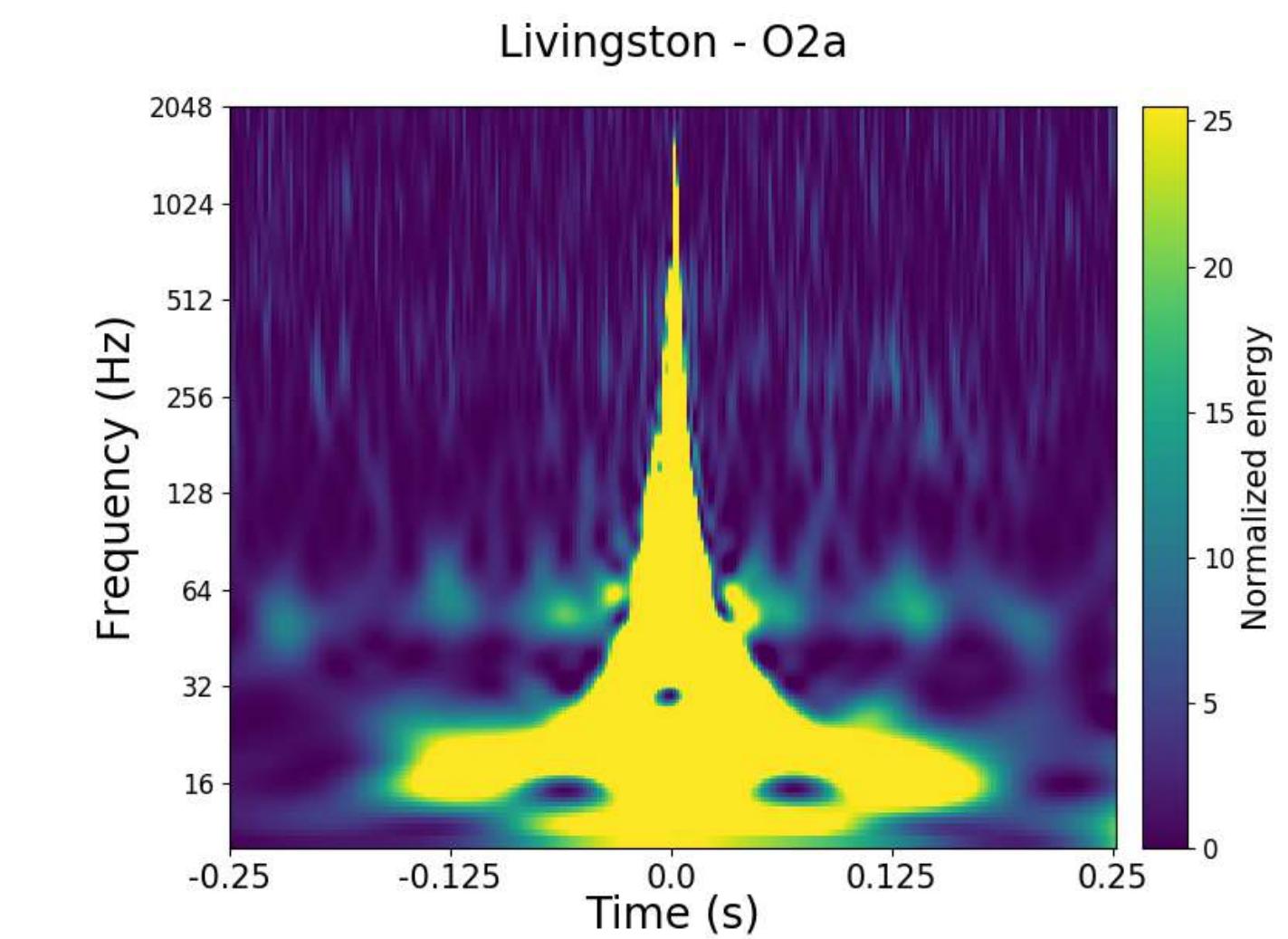
## Glitch Classification



## Parameter Estimation

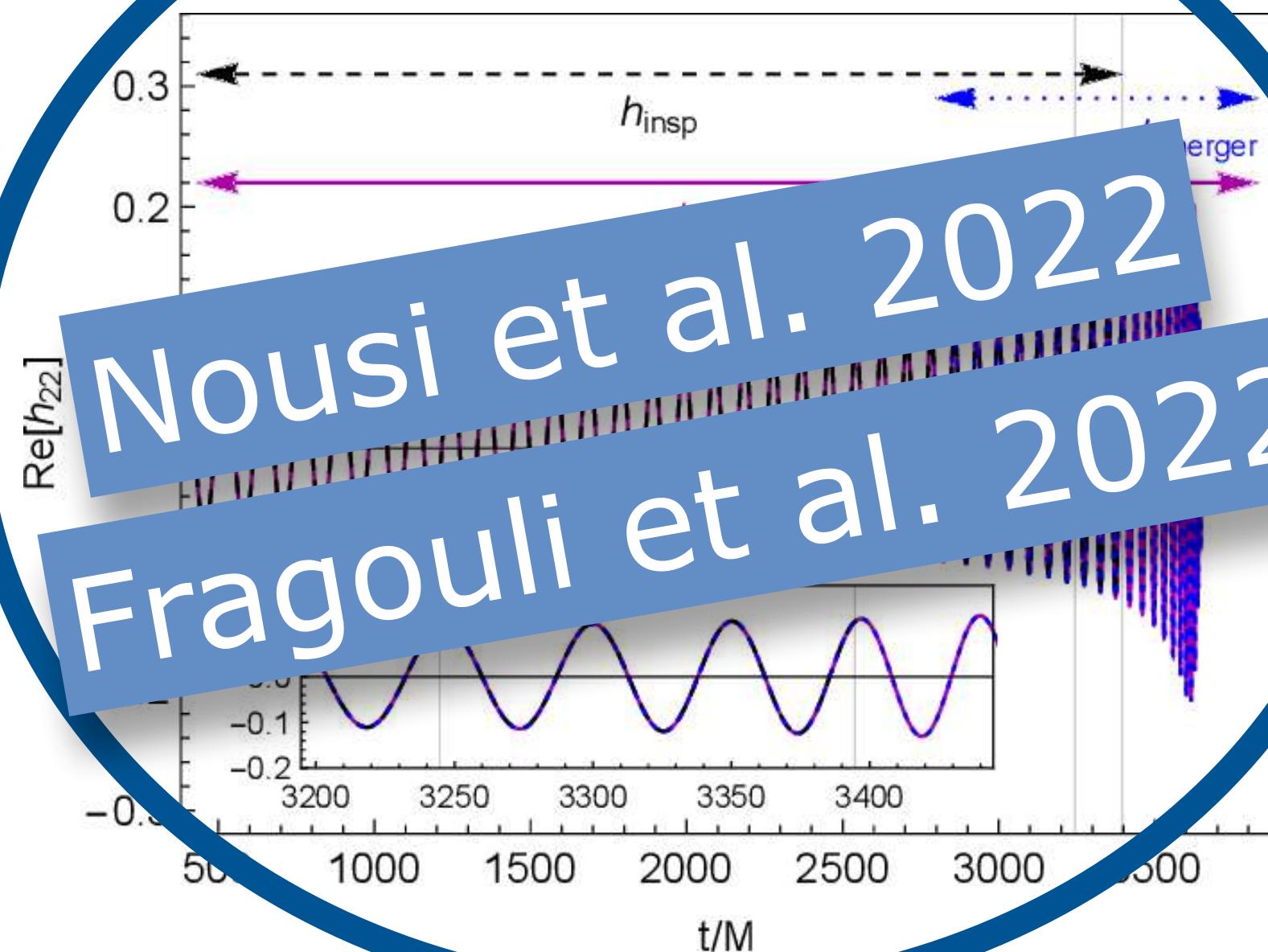


## Sky Localization

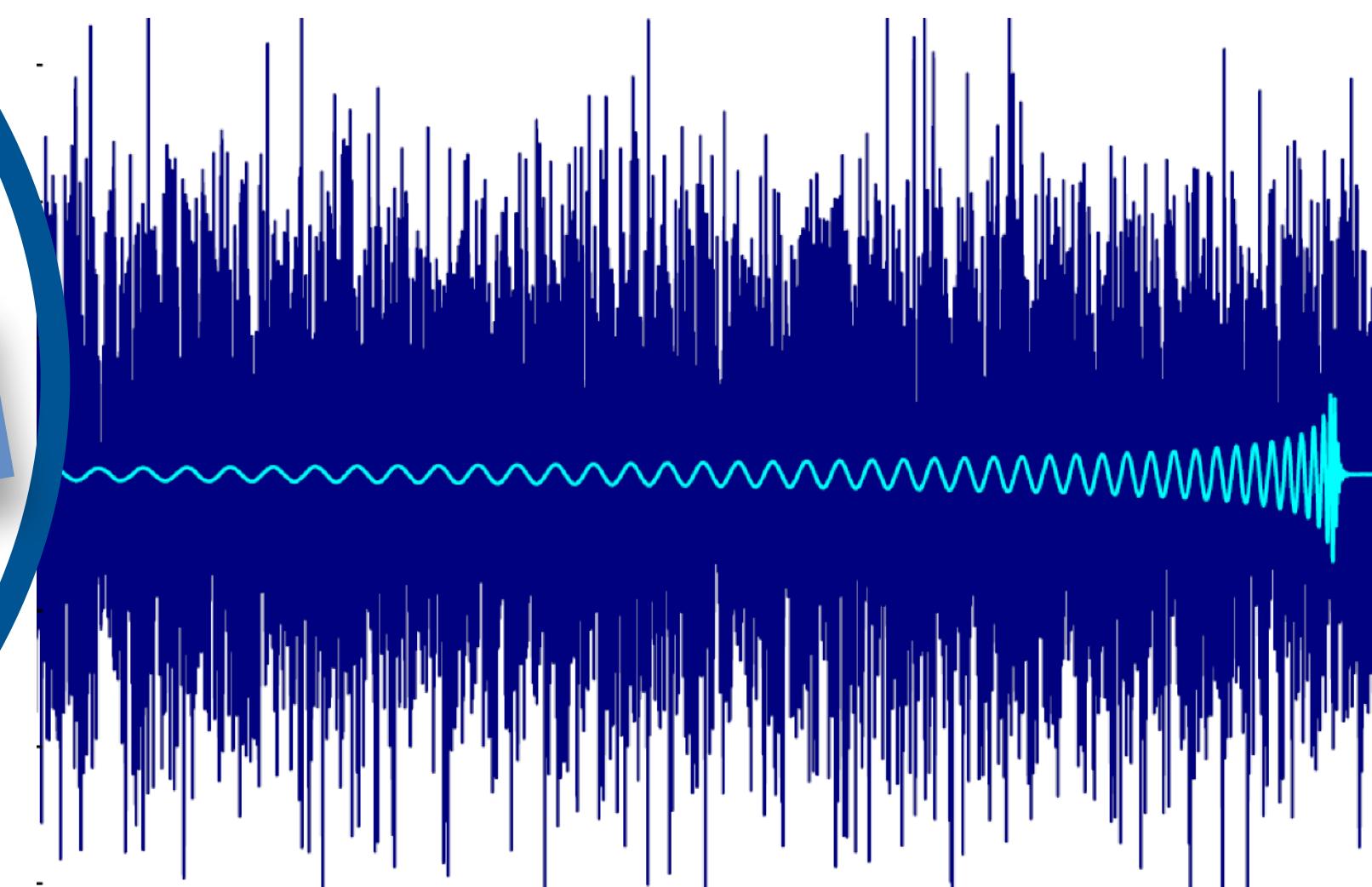


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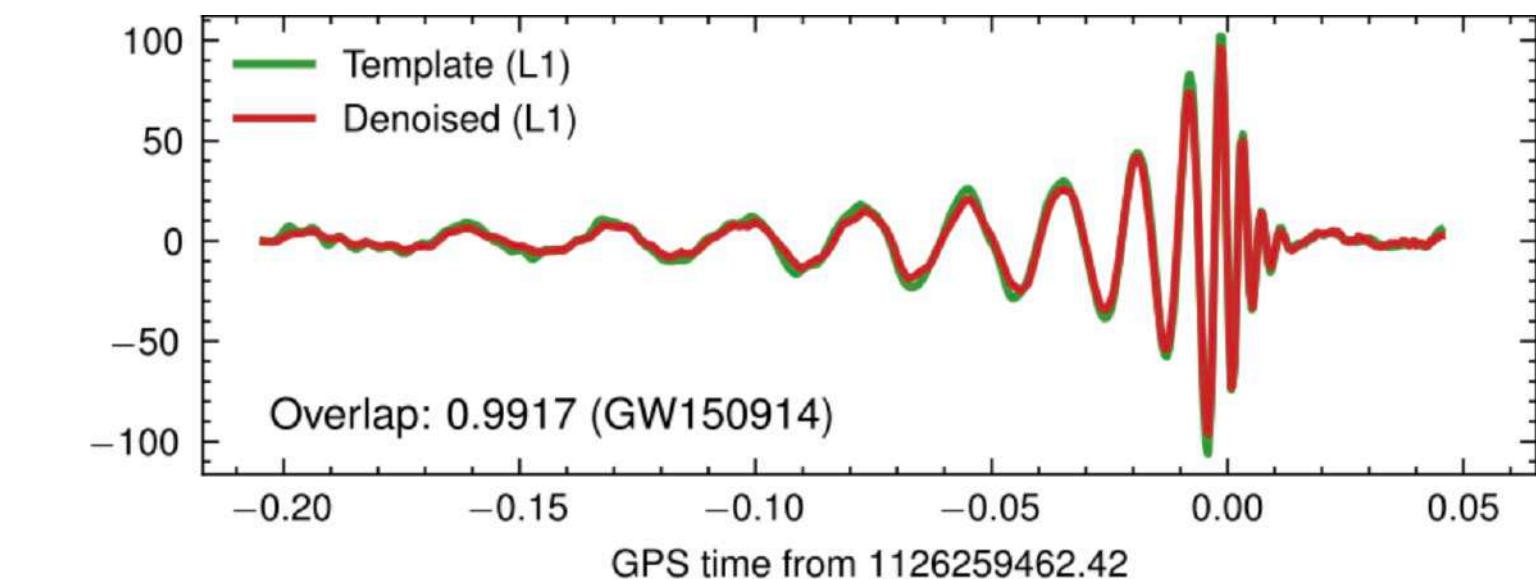
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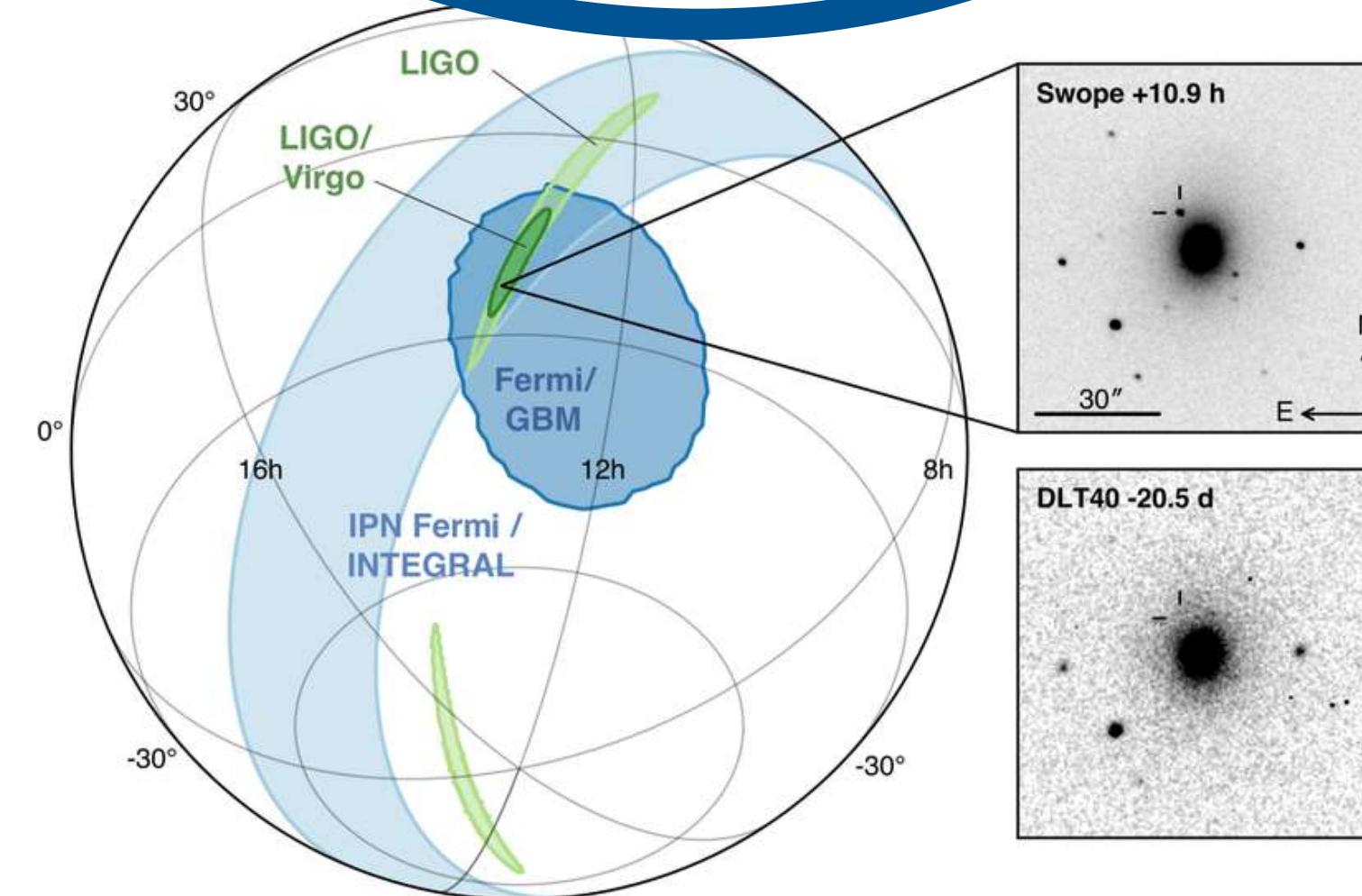
## Detection



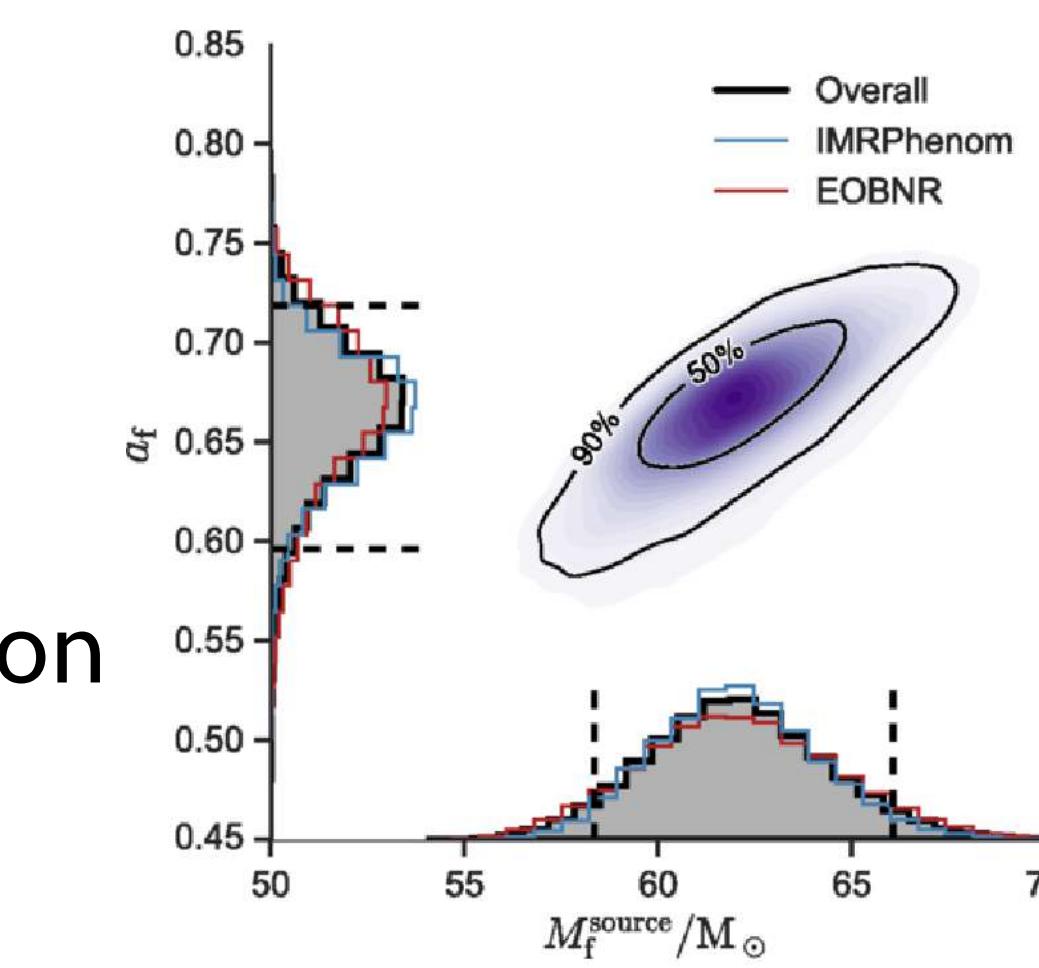
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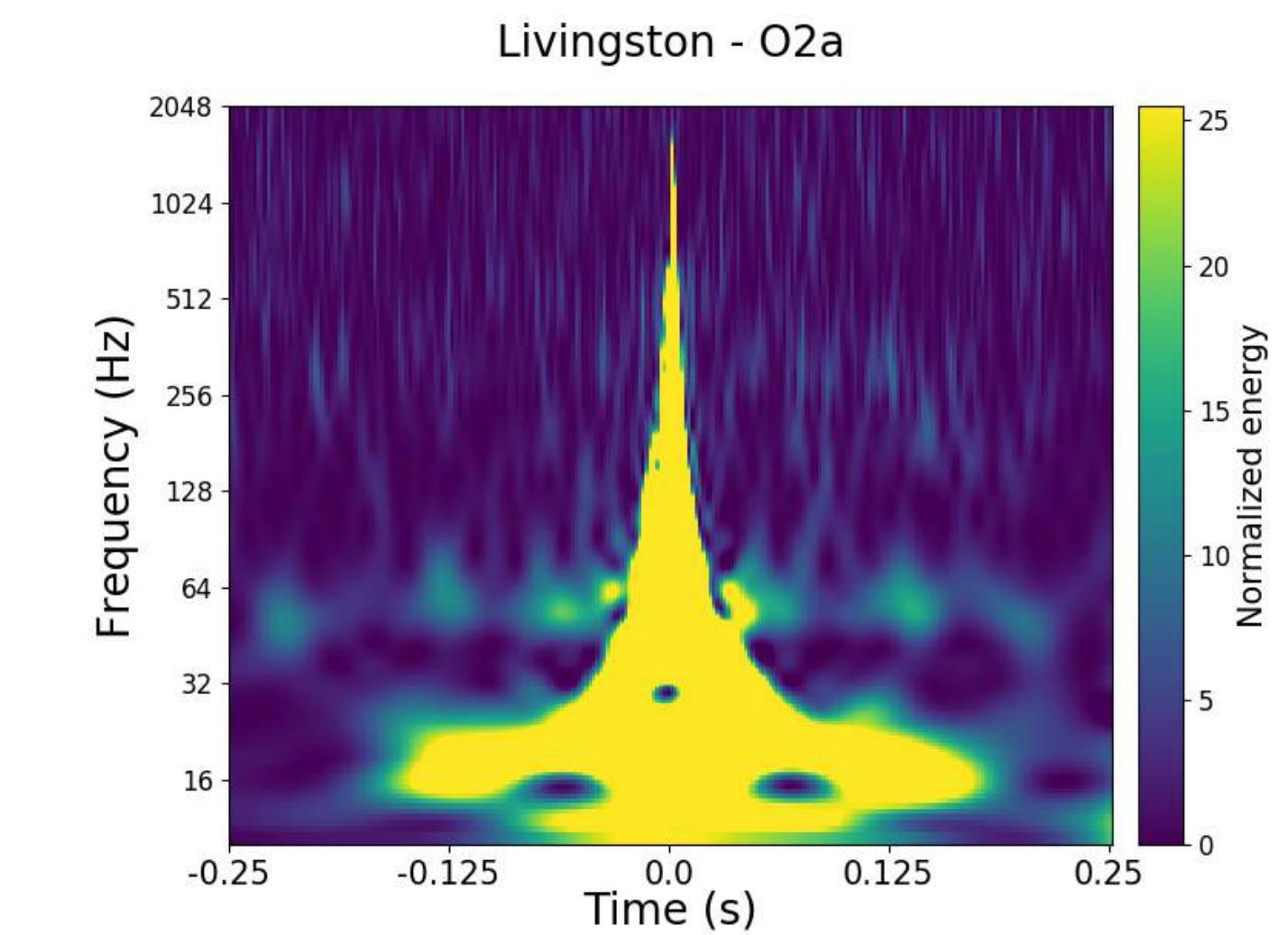
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## Parameter Estimation

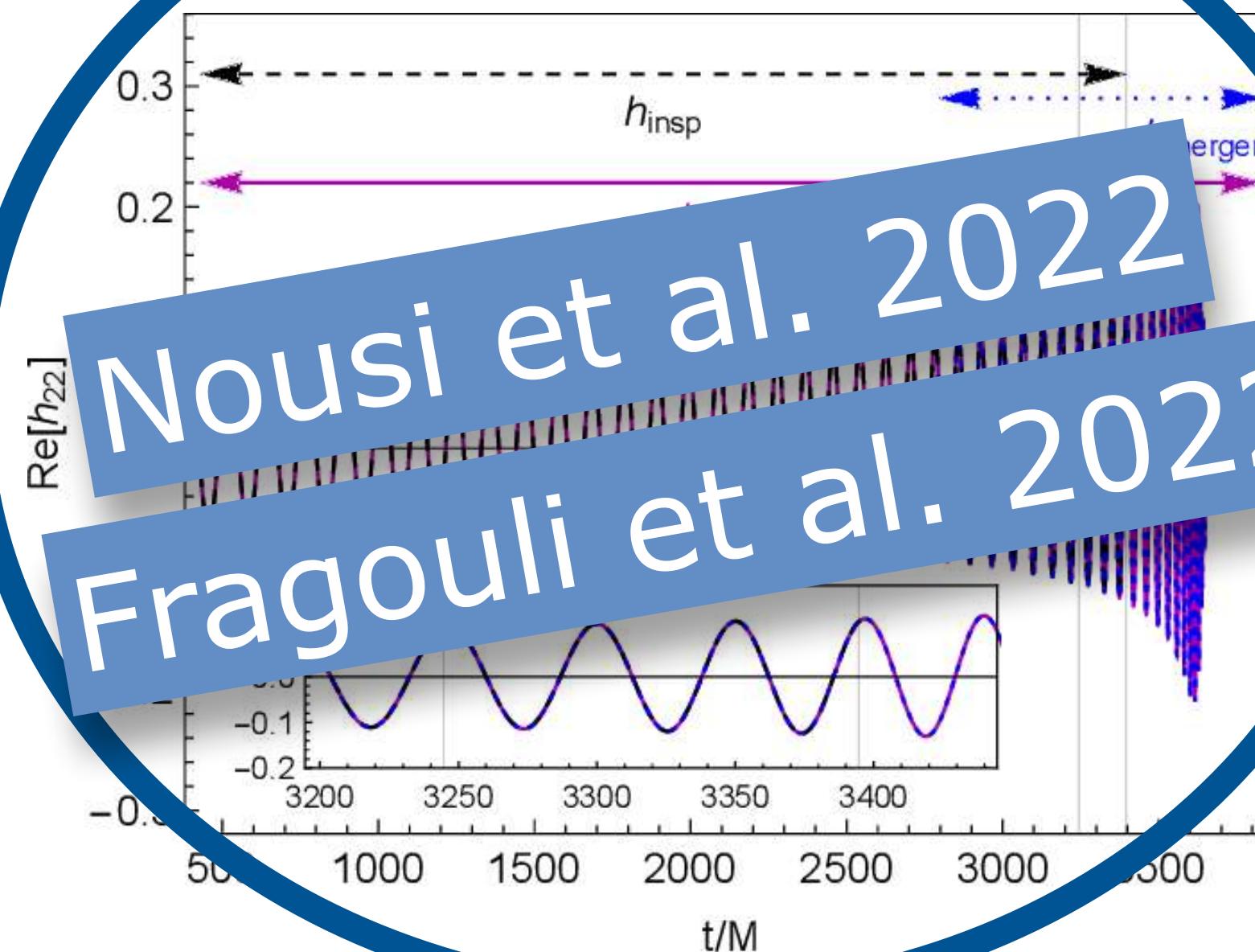


## Sky Localization



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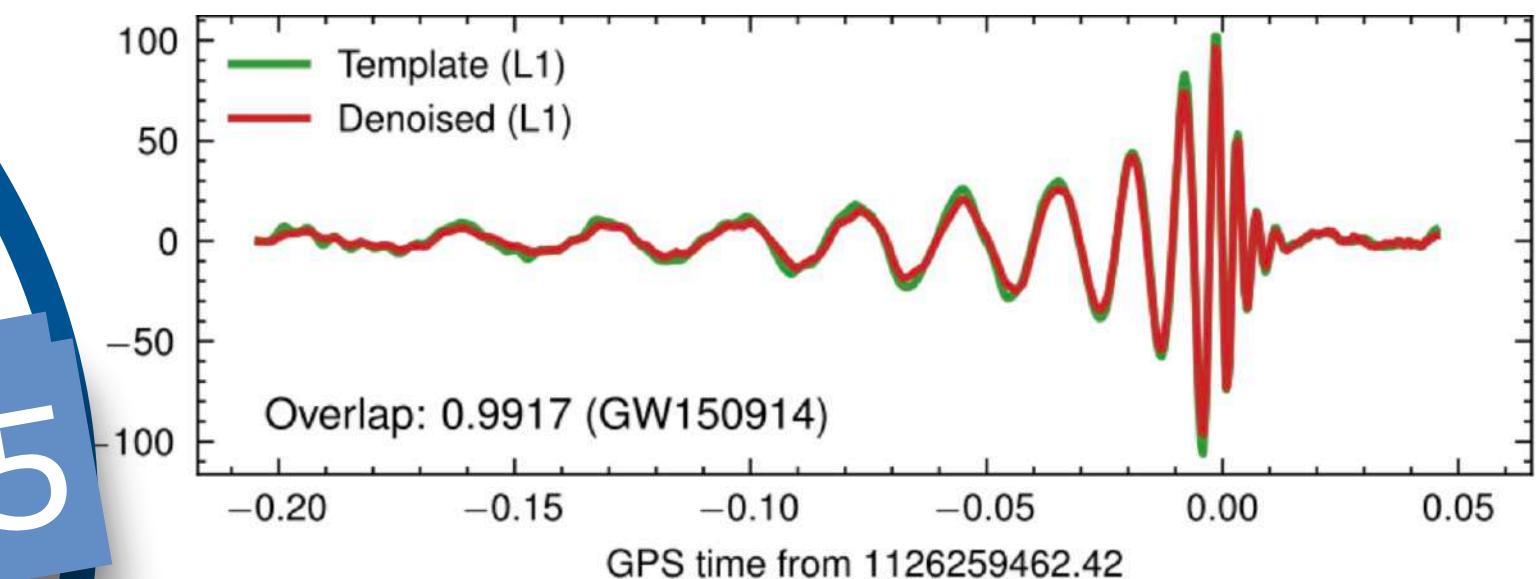
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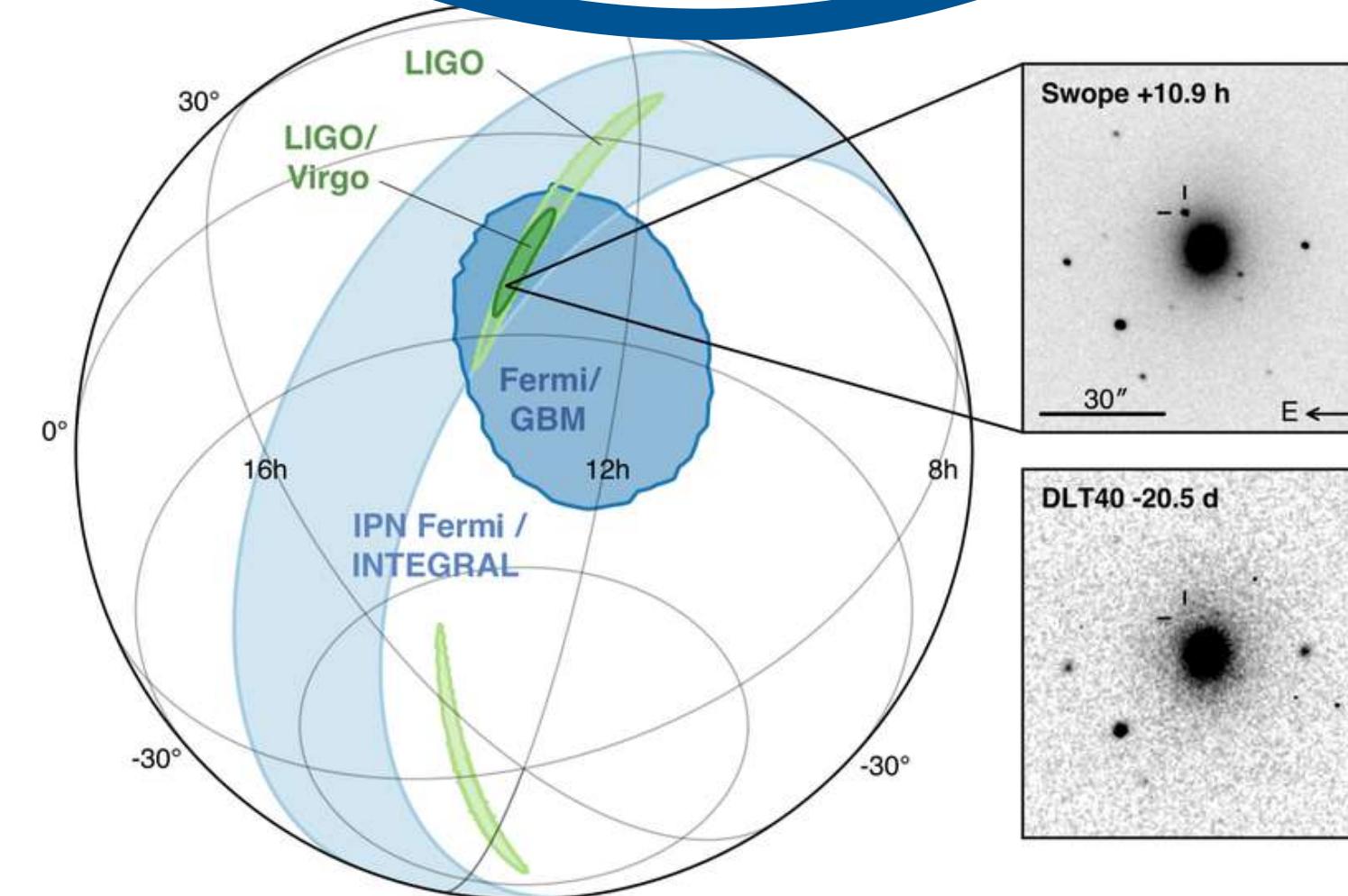
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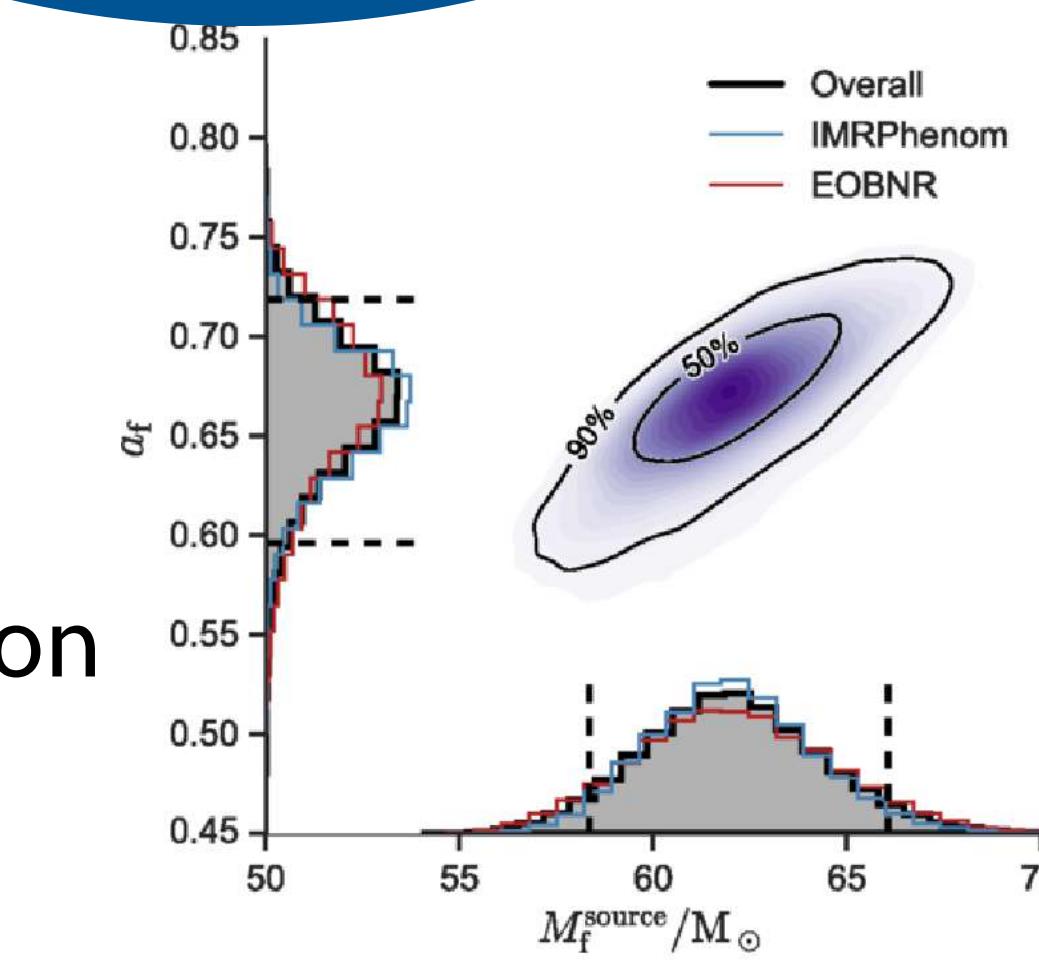
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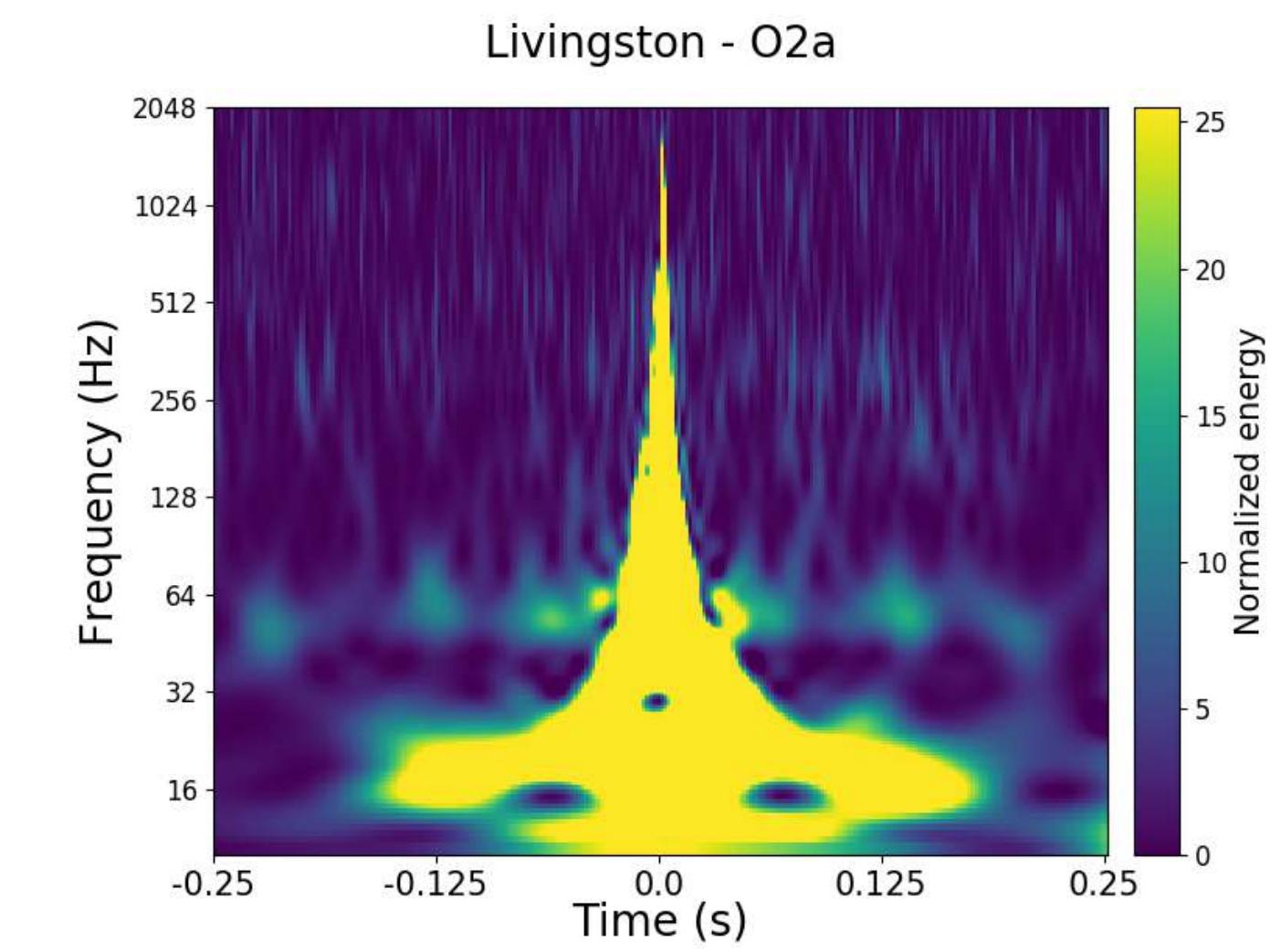
## Glitch Classification



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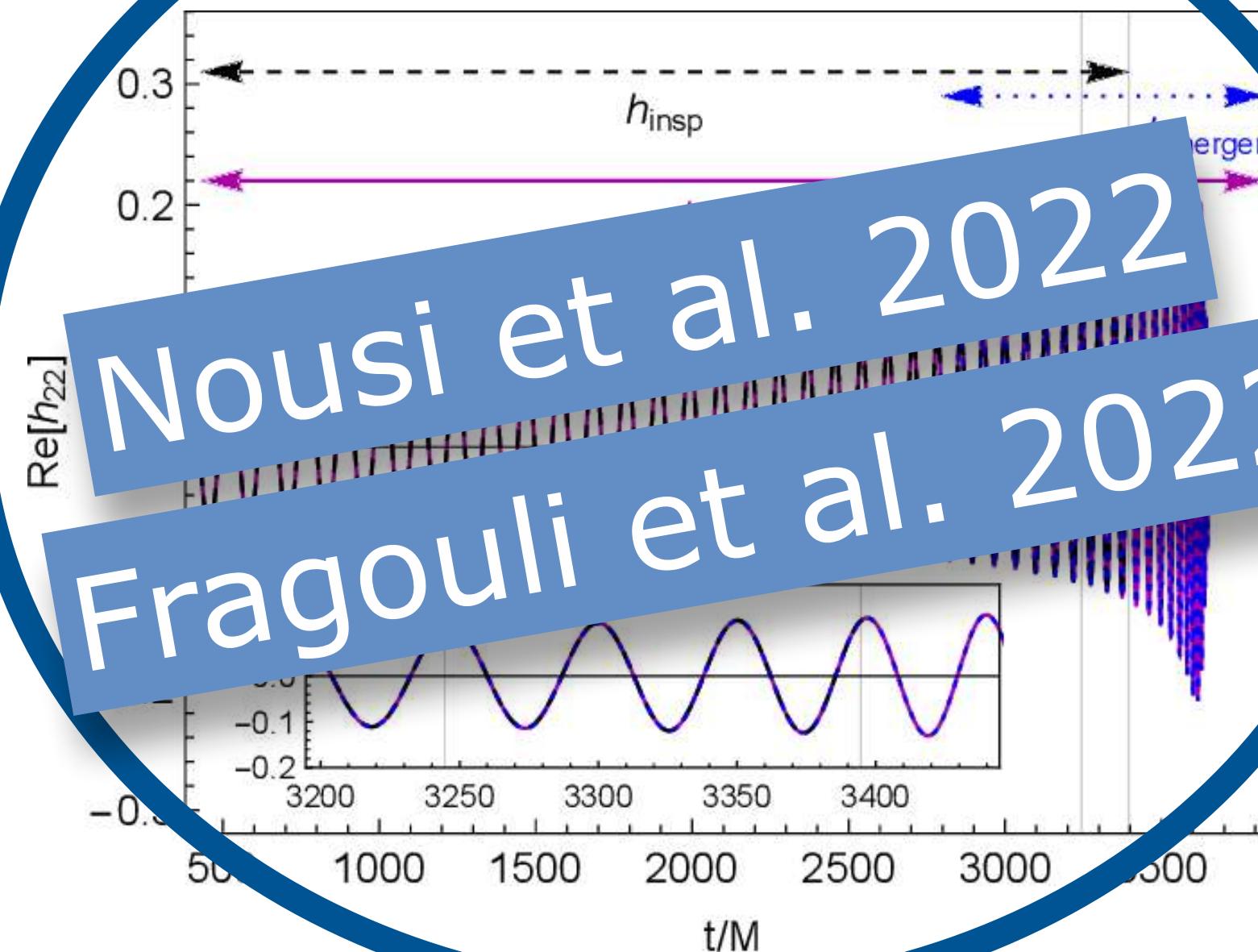


## Sky Localization



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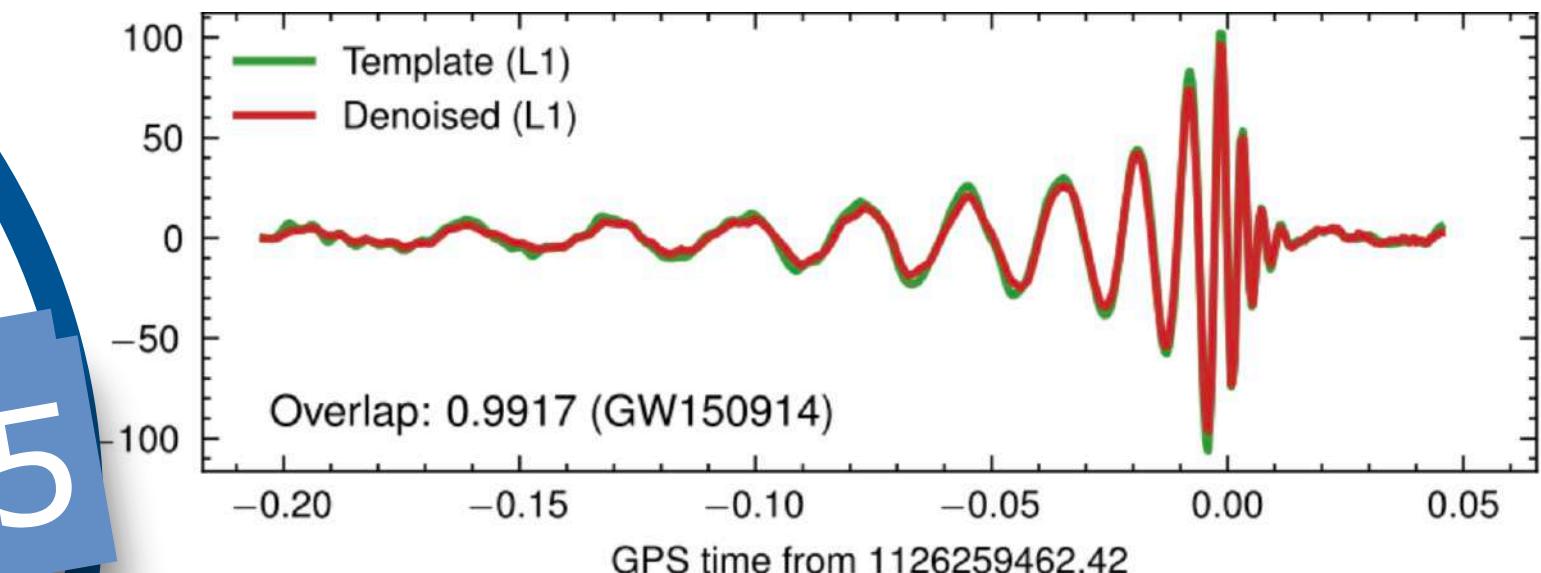
Waveform Modeling



Detection

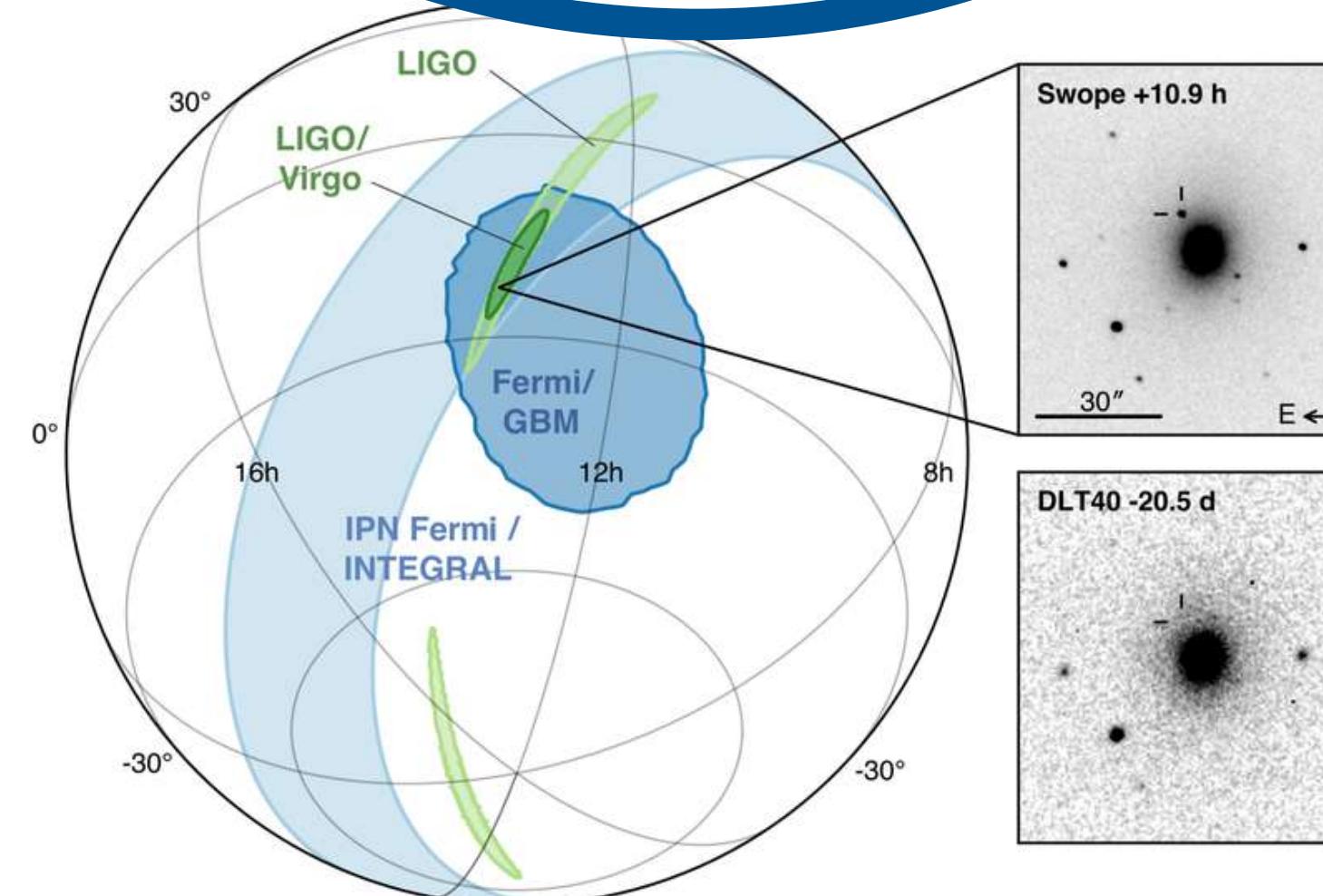


Denoising



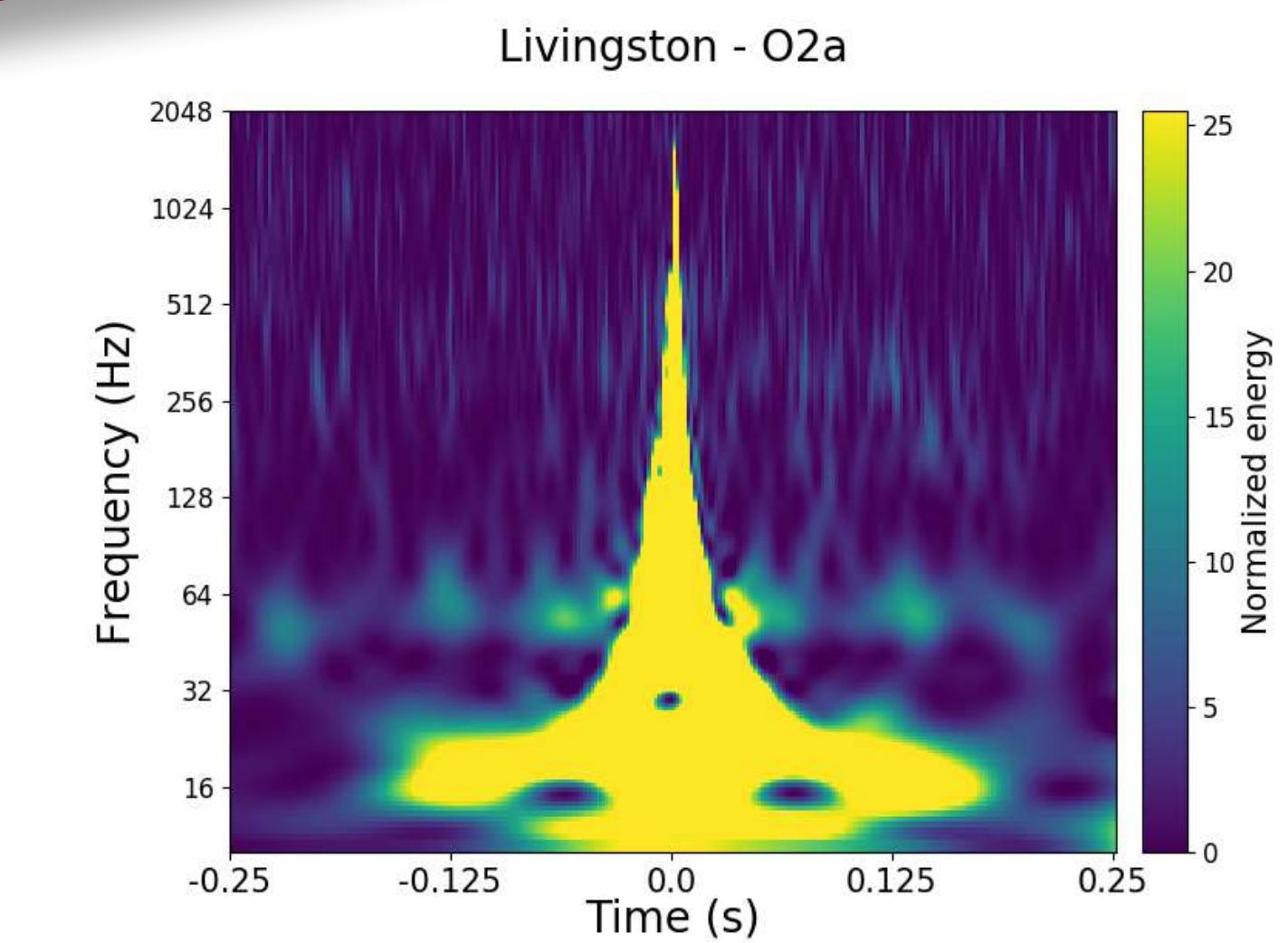
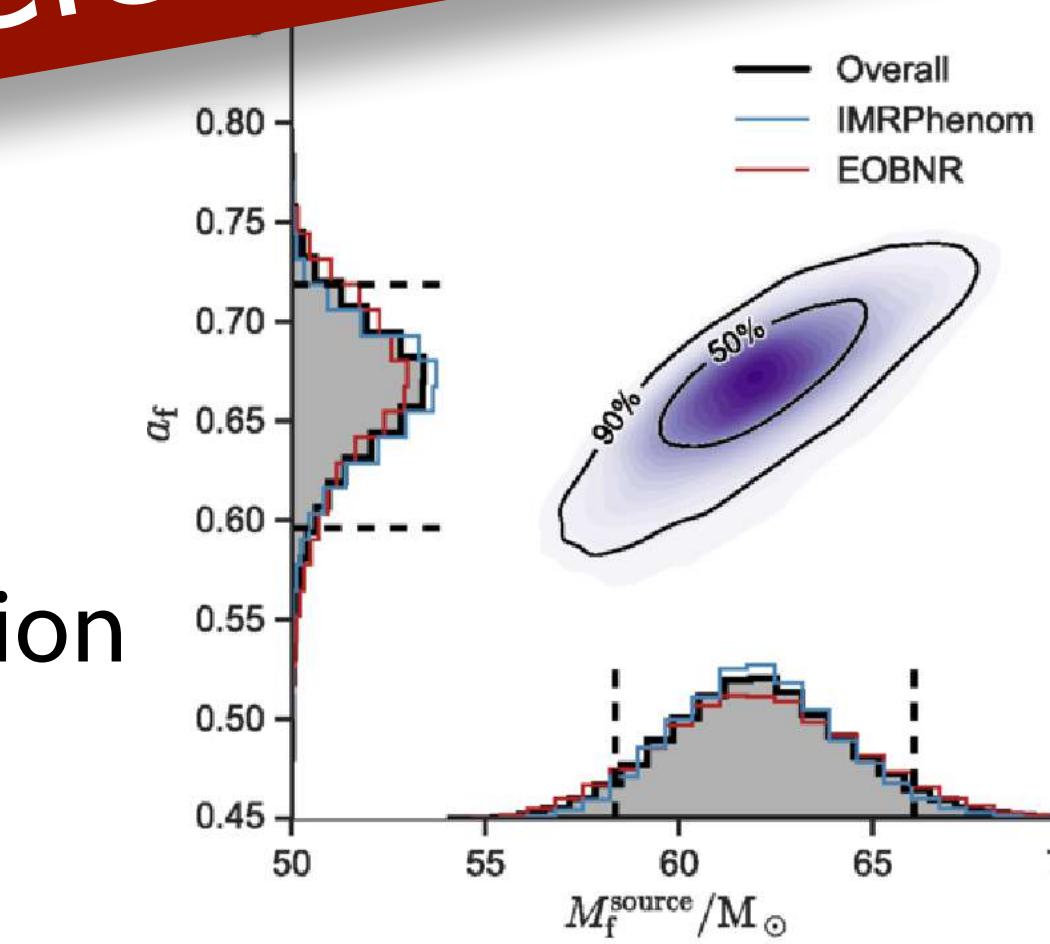
Glitch  
Classification

See also A. Koloniari and  
O. Zelenka talks



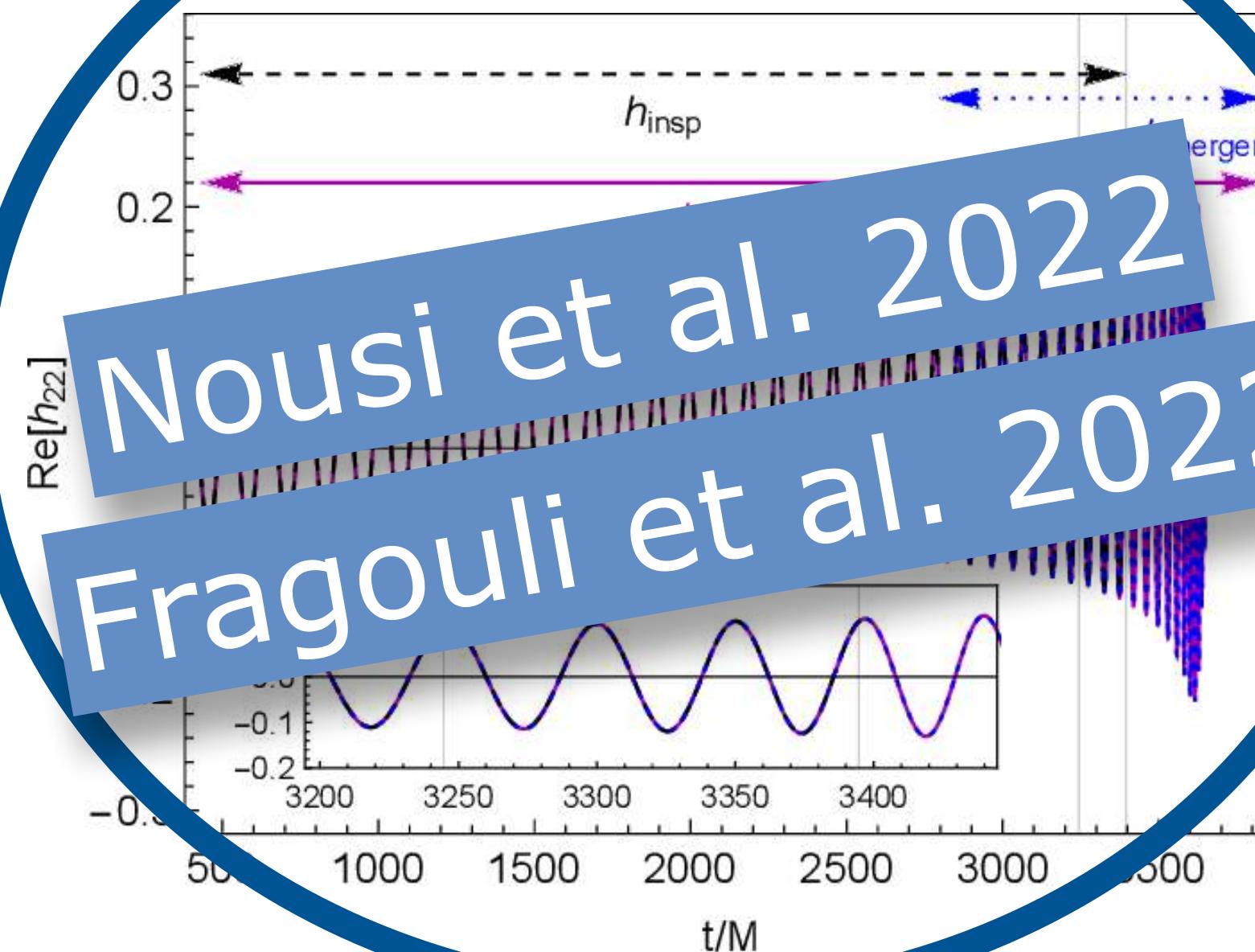
Parameter  
Estimation

Sky Localization



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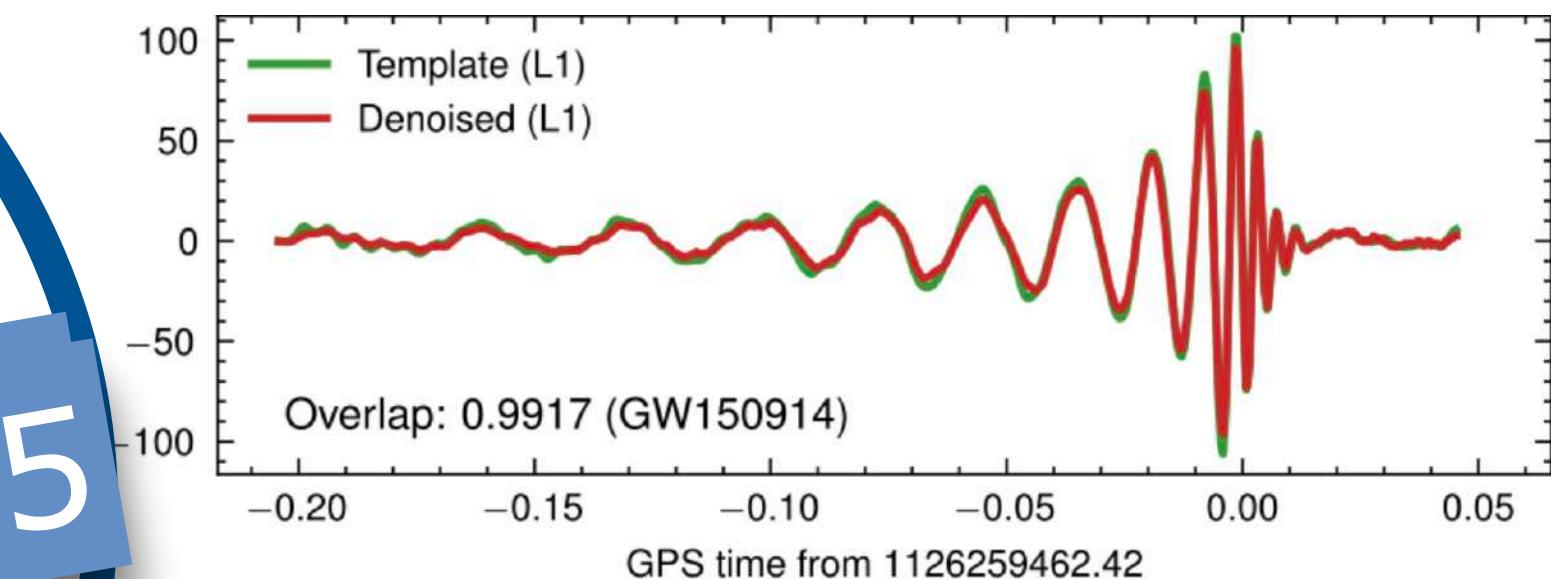
Waveform Modeling



Detection

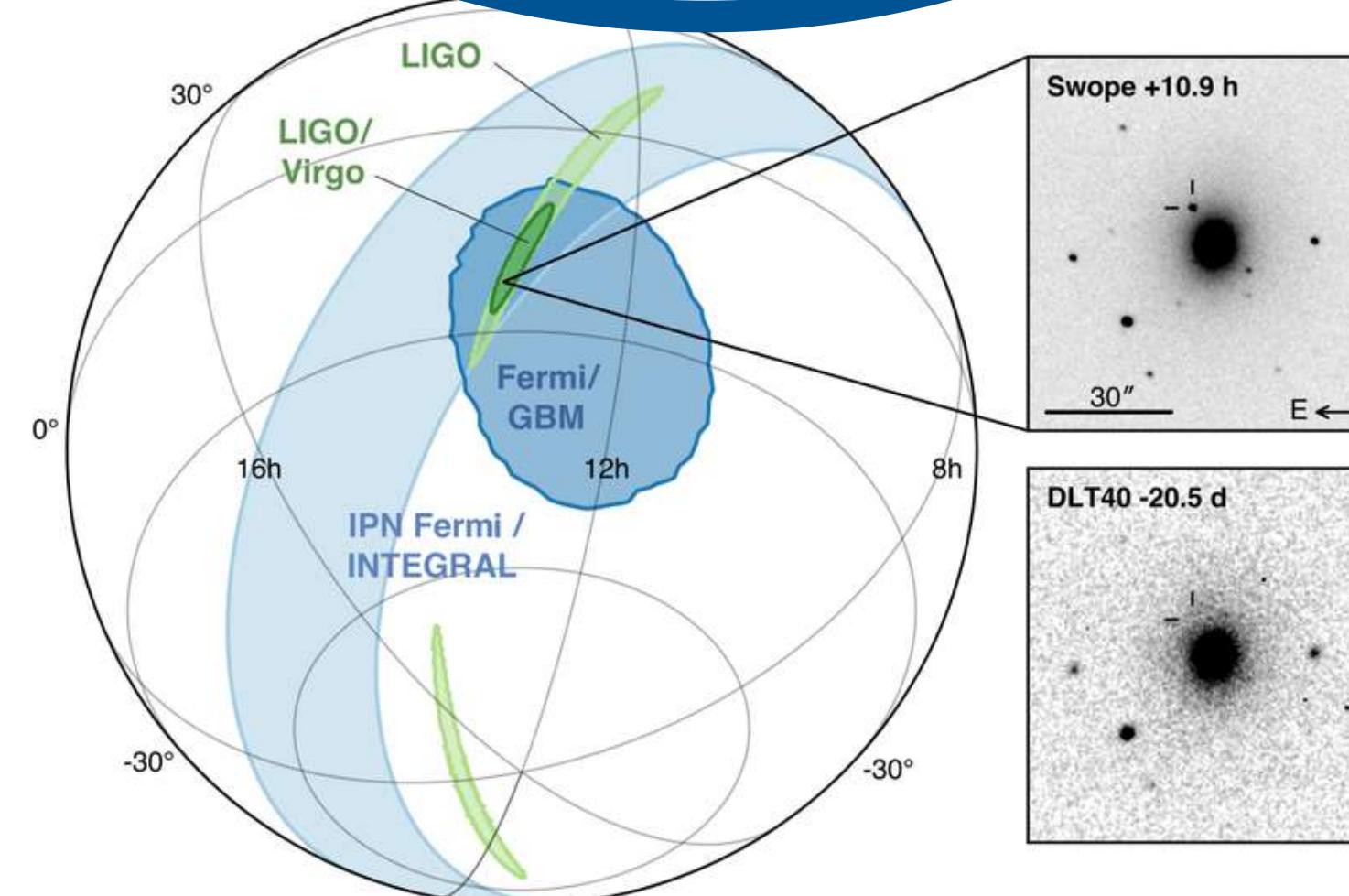


Denoising

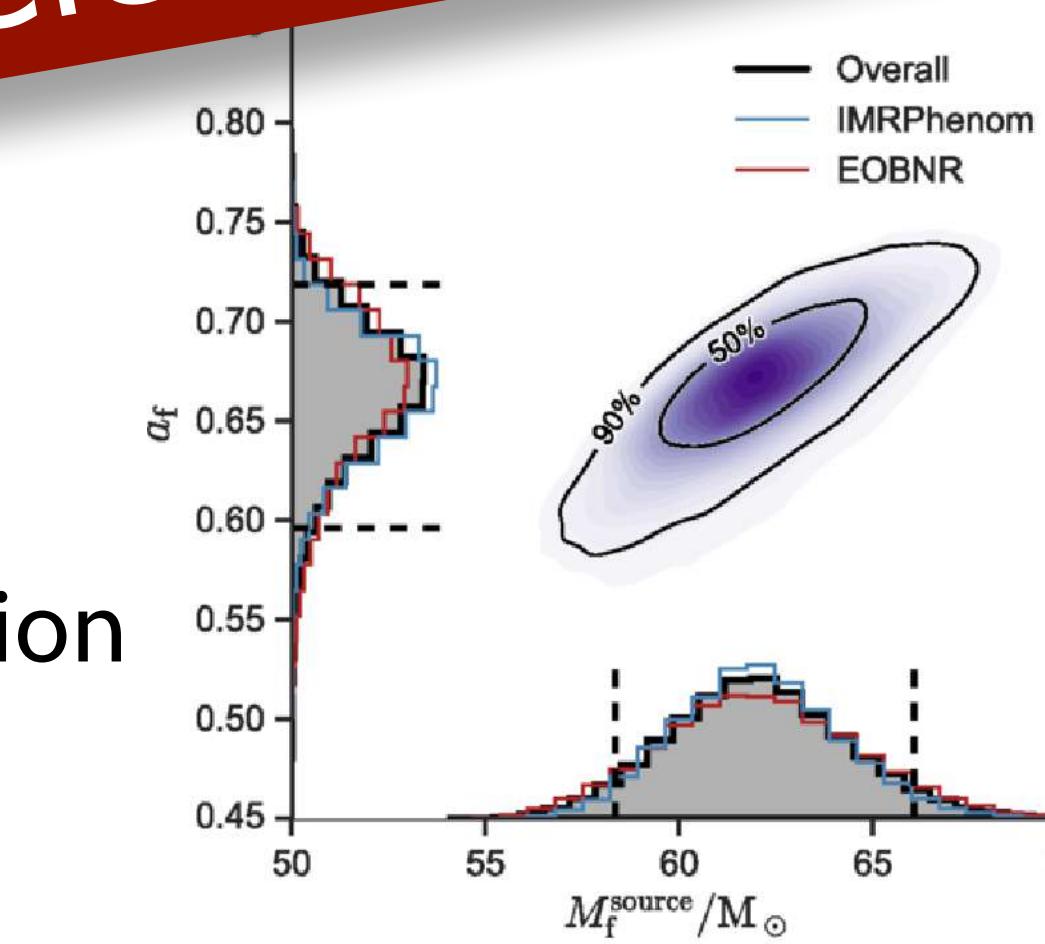


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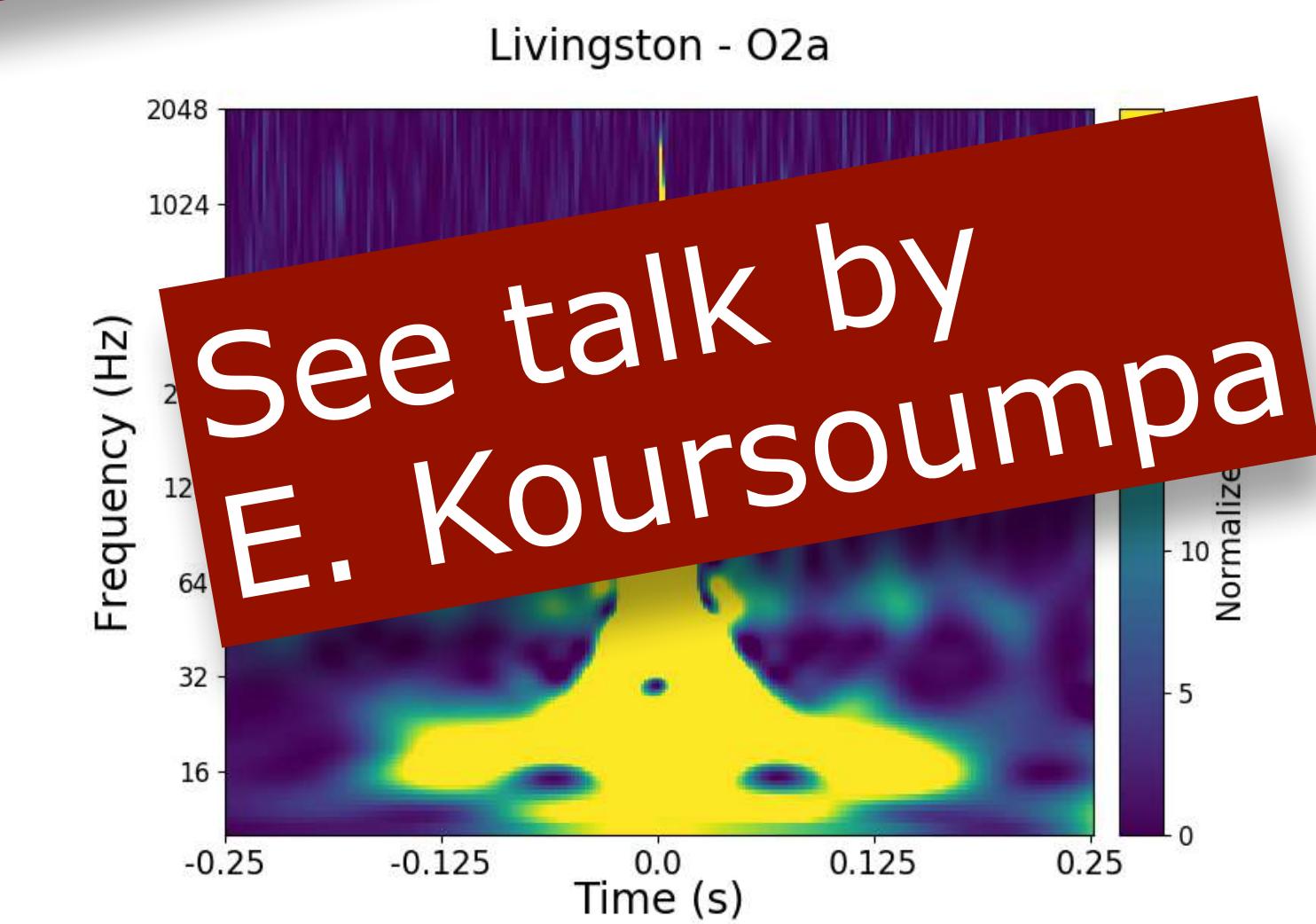
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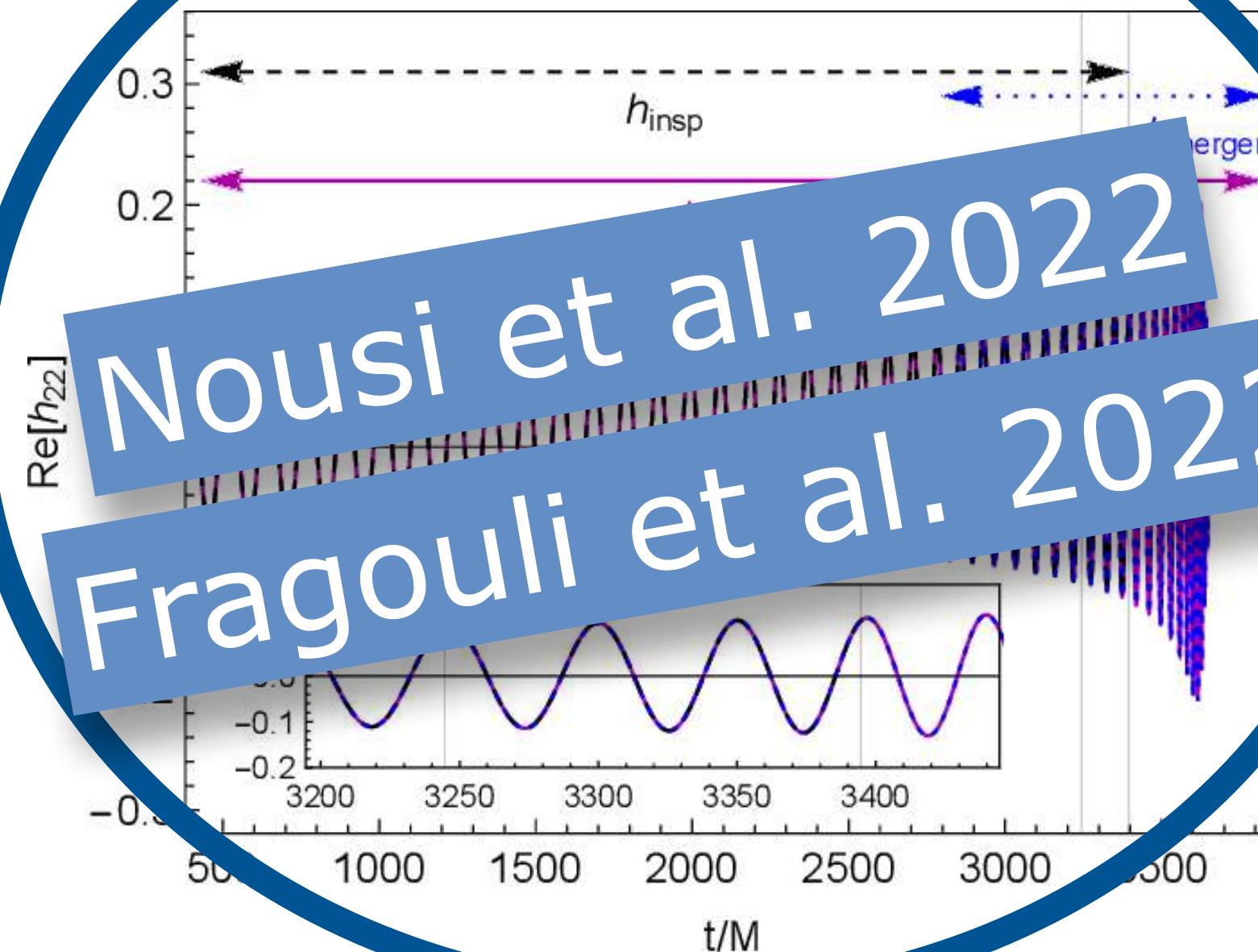


Sky Localization



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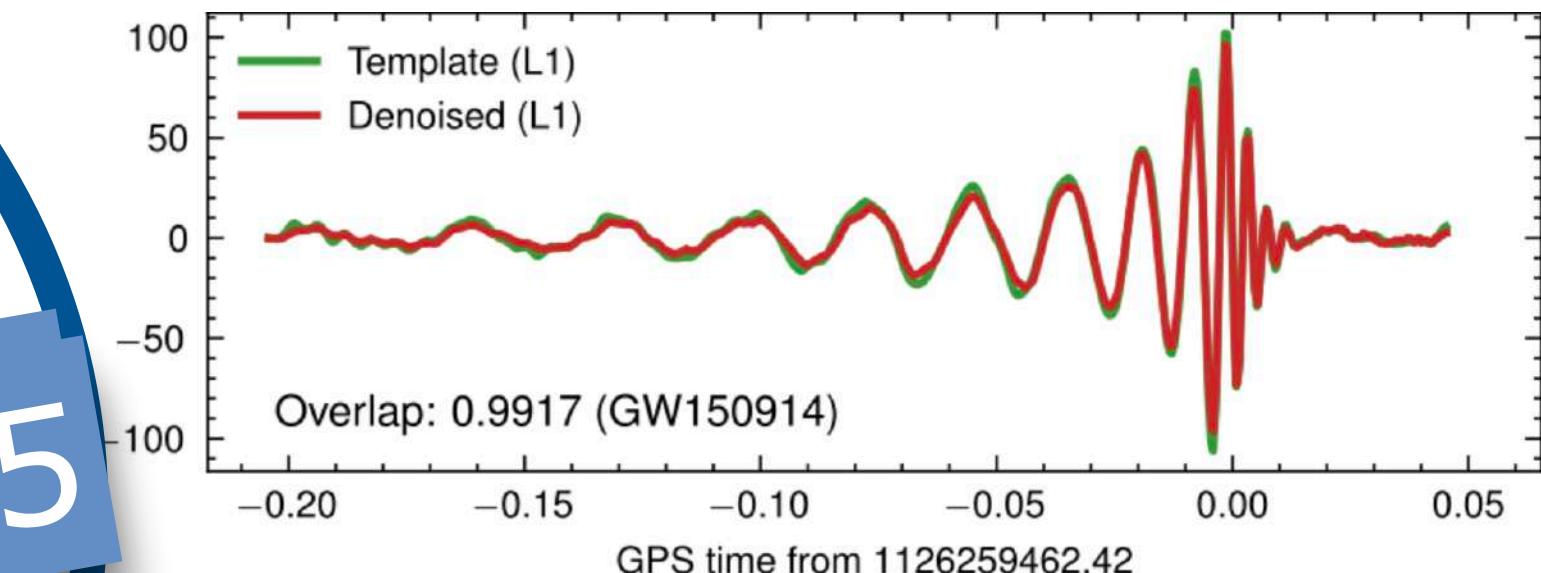
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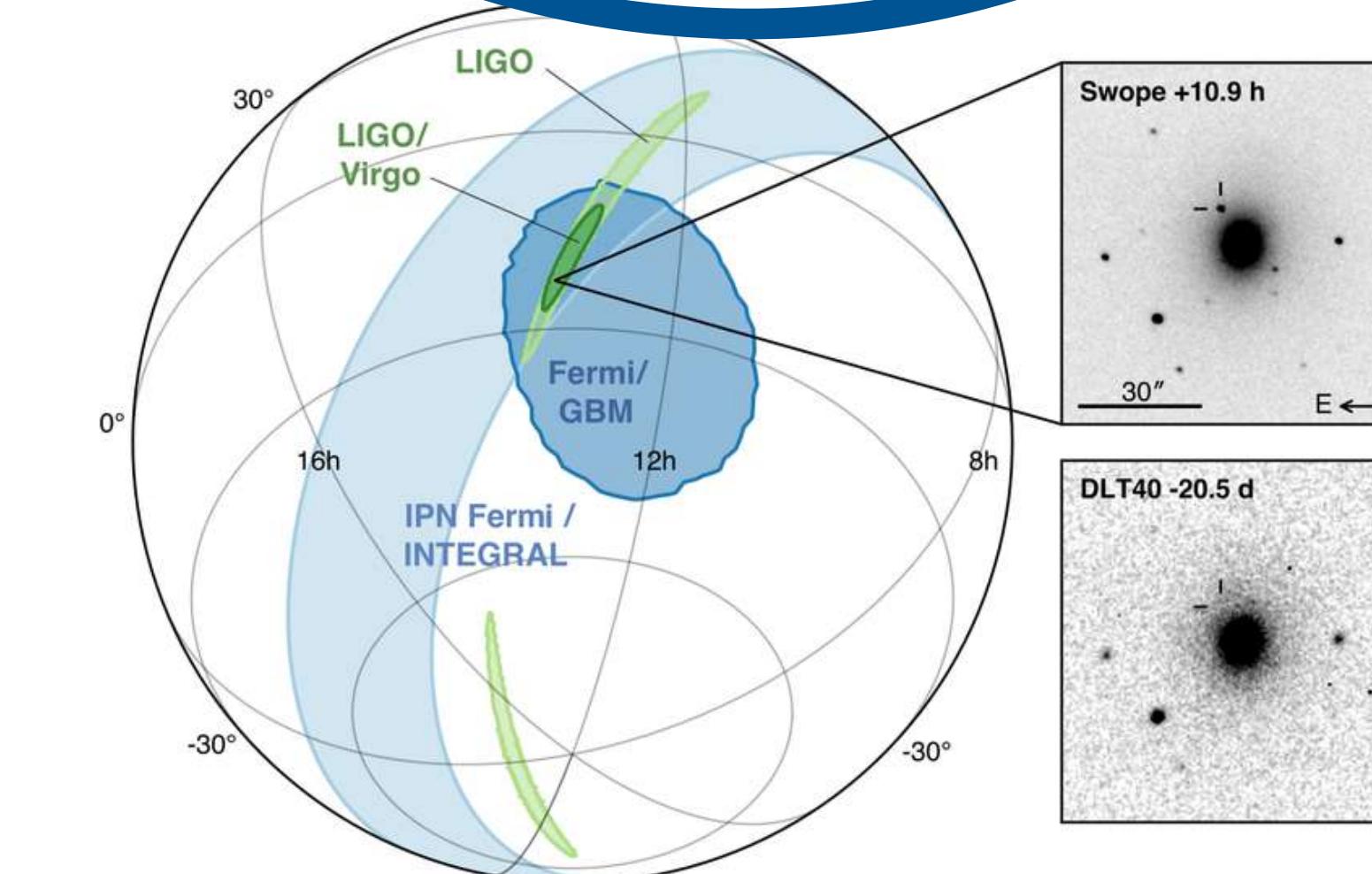
## Detection



## Denoising



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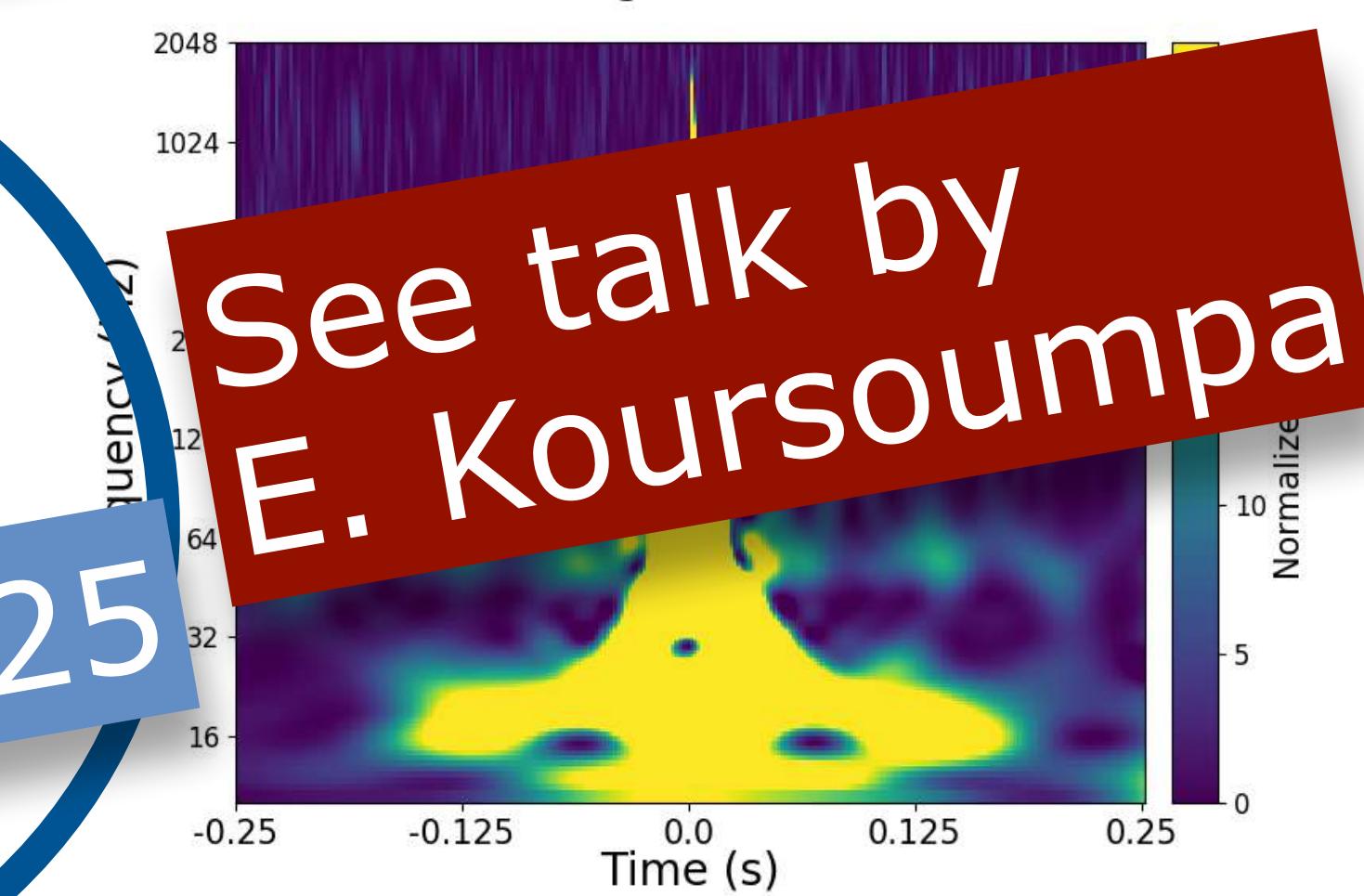


## Parameter Estimation

## Sky Localization



Livingston - O2a



Vretinaris et al. 2025  
See talk by E. Koursoumpa

# GRAVITATIONAL WAVE DETECTION

PHYSICAL REVIEW D 108, 024022 (2023)



## Deep residual networks for gravitational wave detection

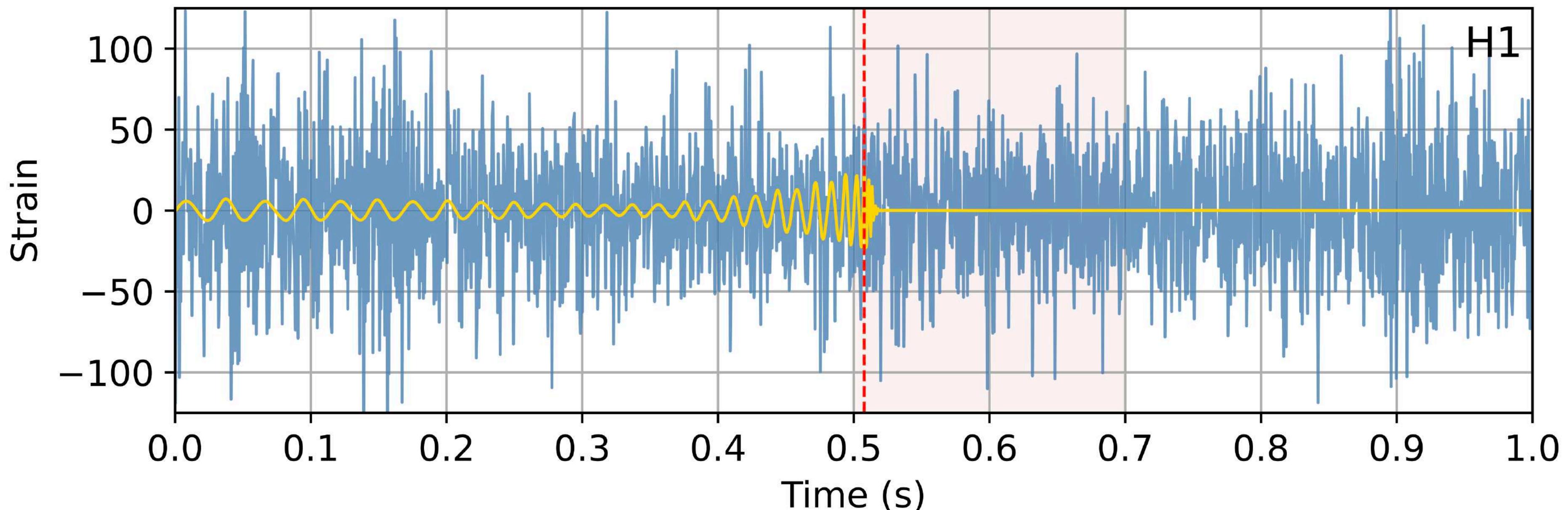
Paraskevi Nousi<sup>ID</sup>,<sup>1</sup> Alexandra E. Koloniari,<sup>2</sup> Nikolaos Passalis,<sup>1</sup> Panagiotis Iosif<sup>ID</sup>,<sup>2</sup>  
Nikolaos Stergioulas<sup>ID</sup>,<sup>2</sup> and Anastasios Tefas<sup>1</sup>

<sup>1</sup>*Department of Informatics, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece*

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## Architecture:

- 54-layer Resnet-1D
- Deep Adaptive Input Normalization
- SNR-based Curriculum Learning
- 30x faster than PyCBC (using a single GPU card)



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**Training:** 1-second segments @2kHz of BBH injections with [IMRPhenomXPHM](#)  
in real O3 noise from L1 and H1

**Mass range:**

$$7M_{\odot} \leq M \leq 50M_{\odot}$$

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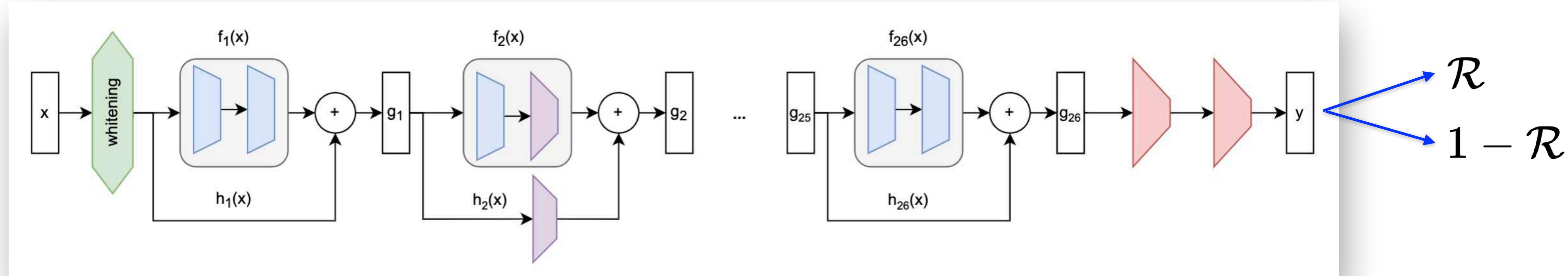
$$7M_{\odot} \leq M \leq 50M_{\odot}$$

**Leading algorithm** (Virgo-AUTH) in the **1st ML GW search challenge** in the most demanding dataset.

<https://github.com/gwastro/ml-mock-data-challenge-1>

# NETWORK ARCHITECTURE OF ARES-GW

**1-D ResNet-54** (27 residual blocks with 2 convolutional layers each and skip connections)!

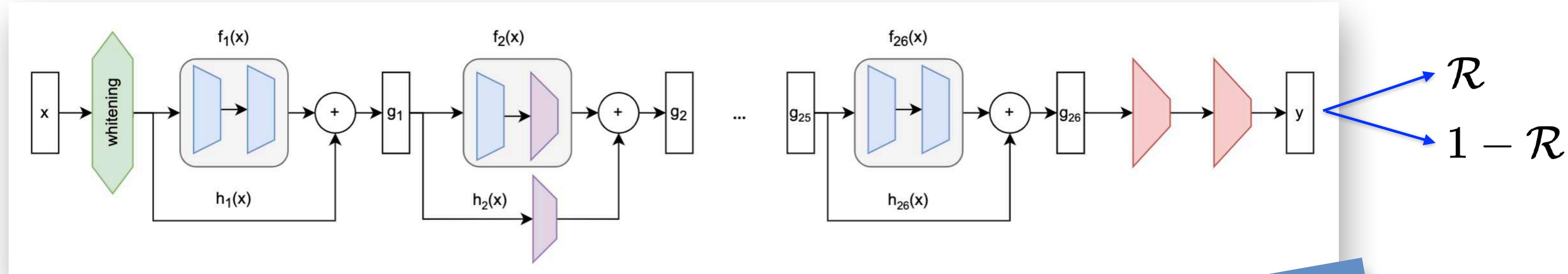


- Residual blocks with skip connections:  $g(\mathbf{x}) = f(\mathbf{x}) + h(\mathbf{x})$
- $h(\mathbf{x}) = \mathbf{x}$  or a strided convolutional layer
- After each convolutional layer: batch normalization + ReLU activation
- Mini-batch size of 400 segments
- Adam optimizer for back propagation
- Objective function = regularized binary cross entropy

Residual blocks	Filters	Strided	Input $D$
4	8		$2 \times 2048$
1	16	✓	$8 \times 2048$
2	16		$16 \times 1024$
1	32	✓	$16 \times 1024$
2	32		$32 \times 512$
1	64	✓	$32 \times 512$
2	64		$64 \times 256$
1	64	✓	$64 \times 256$
2	64		$64 \times 128$
1	64	✓	$64 \times 128$
2	64		$64 \times 64$
5	32		$64 \times 64$
3	16		$32 \times 64$

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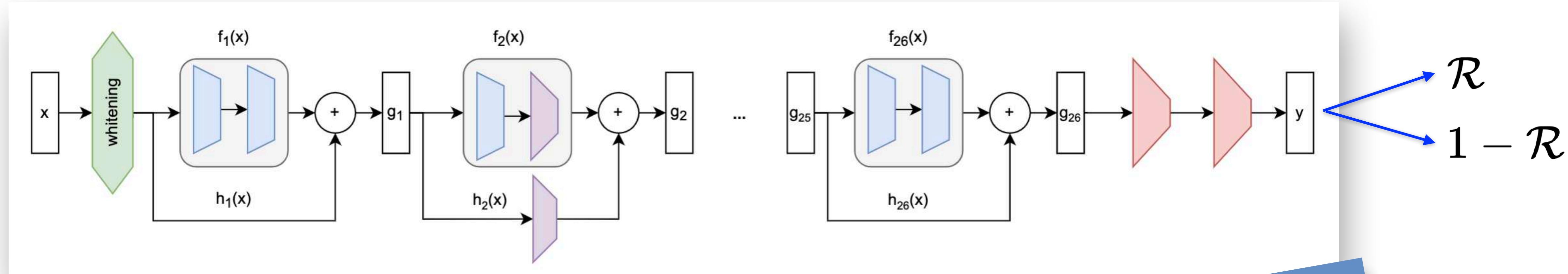
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- Mini-batch size of 400 segments
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- Objective function = regularized binary cross entropy

Gradient problem solved!  
-> much deeper networks

	Input $D$	
10	$2 \times 2048$	✓
16	$8 \times 2048$	
32	$16 \times 1024$	
64	$16 \times 1024$	
1	$32 \times 512$	
2	$32 \times 512$	
1	$64 \times 512$	✓
2	$64 \times 256$	
1	$64 \times 256$	✓
2	$64 \times 128$	
1	$64 \times 128$	✓
2	$64 \times 64$	
5	$64 \times 64$	
3	$32 \times 64$	

# NETWORK ARCHITECTURE OF ARES-GW

**1-D ResNet-54** (27 residual blocks with 2 convolutional layers each and skip connections)!



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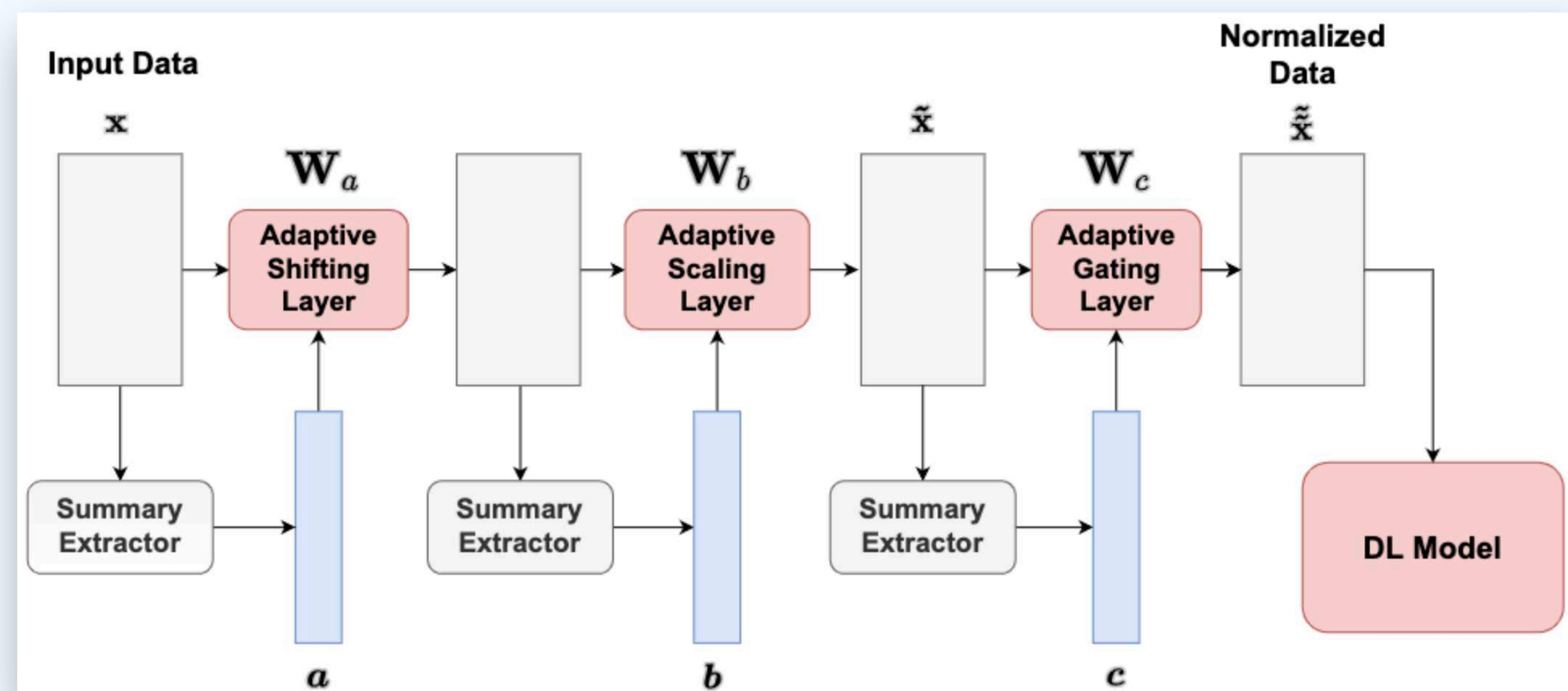
1-D ResNet-54 now used by most  
ML GW detection codes

	Input $D$
1	$2 \times 2048$
2	$8 \times 2048$
3	$16$
4	$32$
5	$64$
6	$64$
7	$64$
8	$64$
9	$64$
10	$64$
11	$64 \times 256$
12	$64 \times 128$
13	$64 \times 128$
14	$64 \times 64$
15	$64 \times 64$
16	$32 \times 64$

# ADAPTIVE INPUT NORMALIZATION

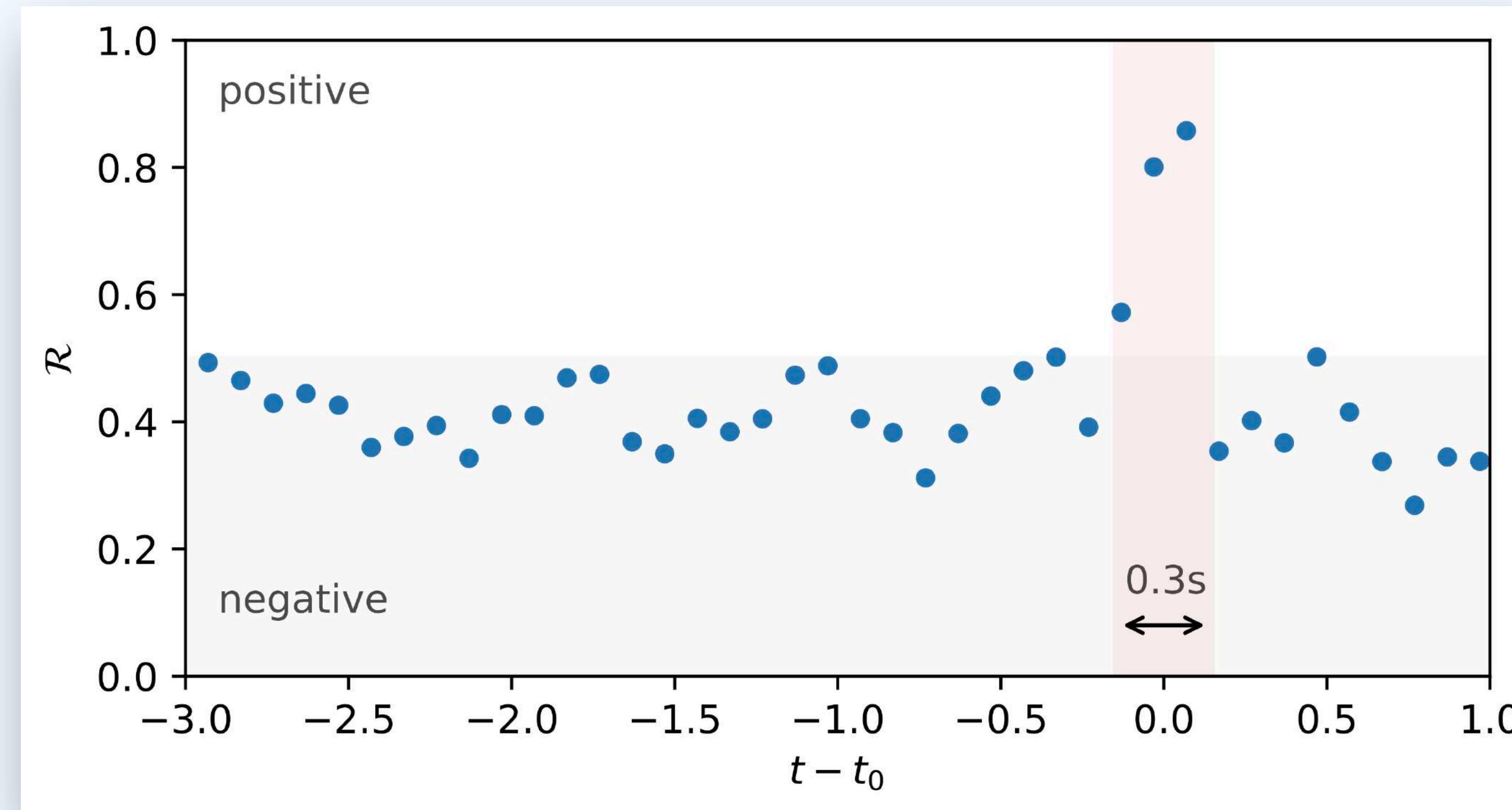
## Deep Adaptive Input Normalization (DAIN) (Passalis et al. 2019)

Is applied during training - weights  $\mathbf{W}_a$ ,  $\mathbf{W}_b$ ,  $\mathbf{W}_c$  are learnable and adapt to input data!



# RANKING STATISTIC

**Neural Network Ranking Statistic**  $R$  is reported every 0.1 s of input data



**Logarithmic Ranking Statistic**

$$\mathcal{R}_s = -\log_{10}(1 - \mathcal{R} + 10^{-16})$$

# ARESGW ON GITHUB

<https://github.com/vivinousi/gw-detection-deep-learning>

vivinousi / gw-detection-deep-learning Public

Code Issues Pull requests Actions Projects Security Insights

master 1 Branch Tags Go to file Code

vivinousi	readme update	dde2791 · 2 years ago	8 Commits
doc	readme update	2 years ago	
modules	training code initial commit	2 years ago	
trained_models	training code initial commit	2 years ago	
utils	training code initial commit	2 years ago	
LICENSE	Initial commit	2 years ago	
README.md	readme update	2 years ago	
run_on_test.sh	training code initial commit	2 years ago	
test.py	training code initial commit	2 years ago	
test_challenge_model.py	training code initial commit	2 years ago	
train.py	readme update	2 years ago	

About

Gravitational wave detection in real noise timeseries using deep residual neural networks

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Releases No releases published

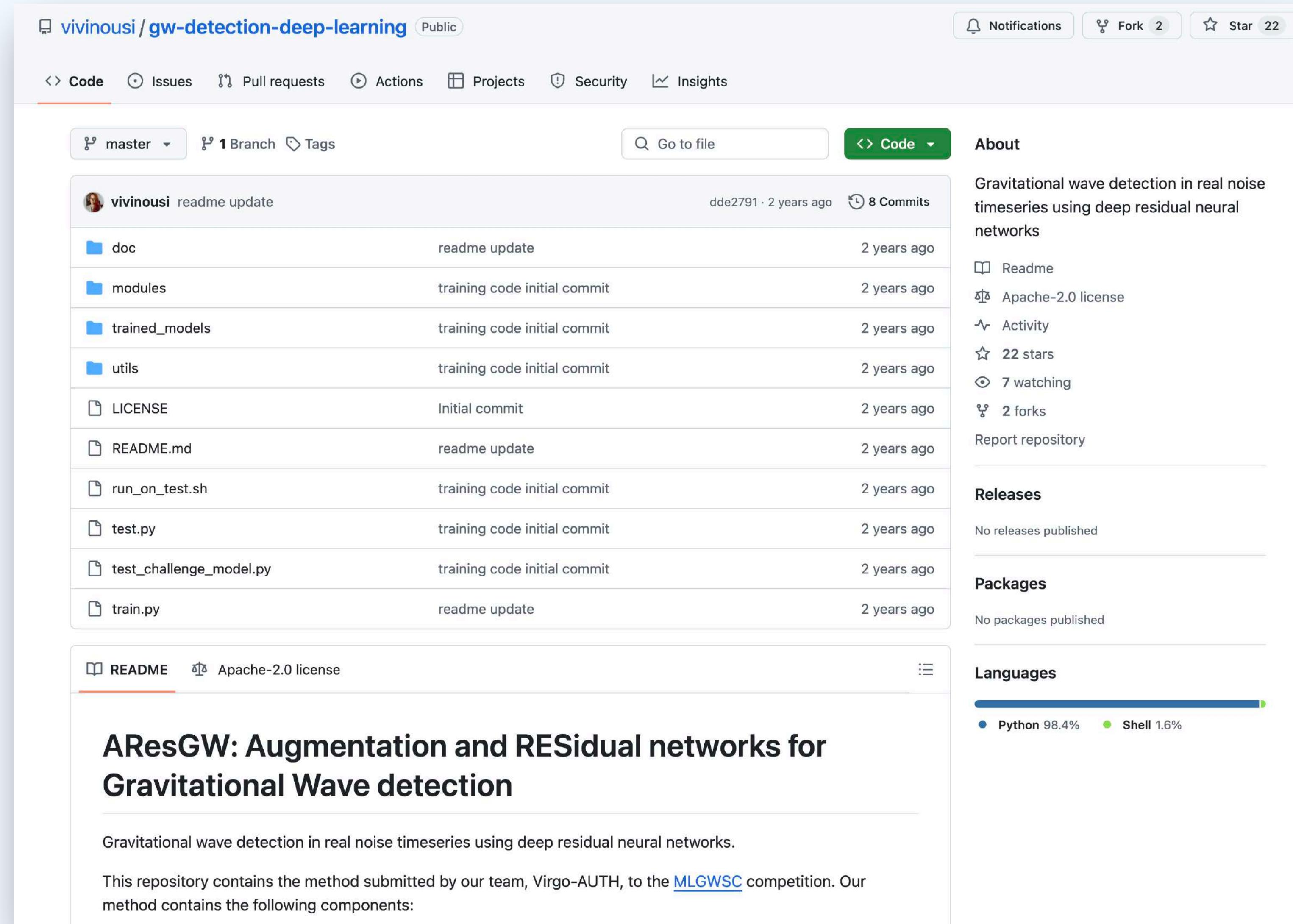
Packages No packages published

Languages Python 98.4% Shell 1.6%

## AResGW: Augmentation and RESidual networks for Gravitational Wave detection

Gravitational wave detection in real noise timeseries using deep residual neural networks.

This repository contains the method submitted by our team, Virgo-AUTH, to the [MLGWSC](#) competition. Our method contains the following components:



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PAPER

## New gravitational wave discoveries enabled by machine learning

Alexandra E Koloniari<sup>1,\*</sup> , Evdokia C Koursoumpa<sup>1</sup> , Paraskevi Nousi<sup>2</sup> , Paraskevas Lampropoulos<sup>1</sup> , Nikolaos Passalis<sup>3</sup> , Anastasios Tefas<sup>4</sup>  and Nikolaos Stergioulas<sup>1</sup> 

<sup>1</sup> Department of Physics, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece

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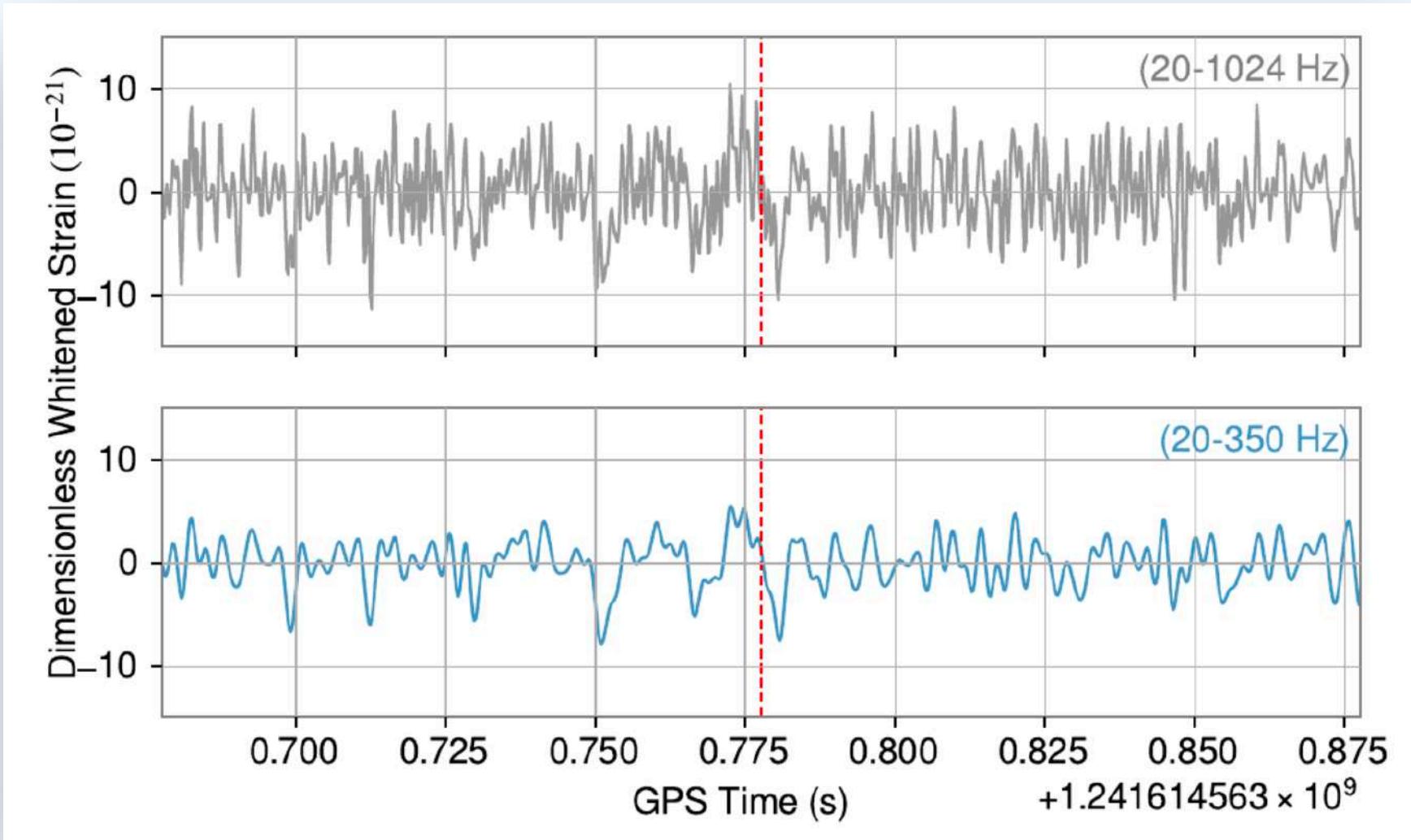
13 February 2025

PUBLISHED

27 February 2025

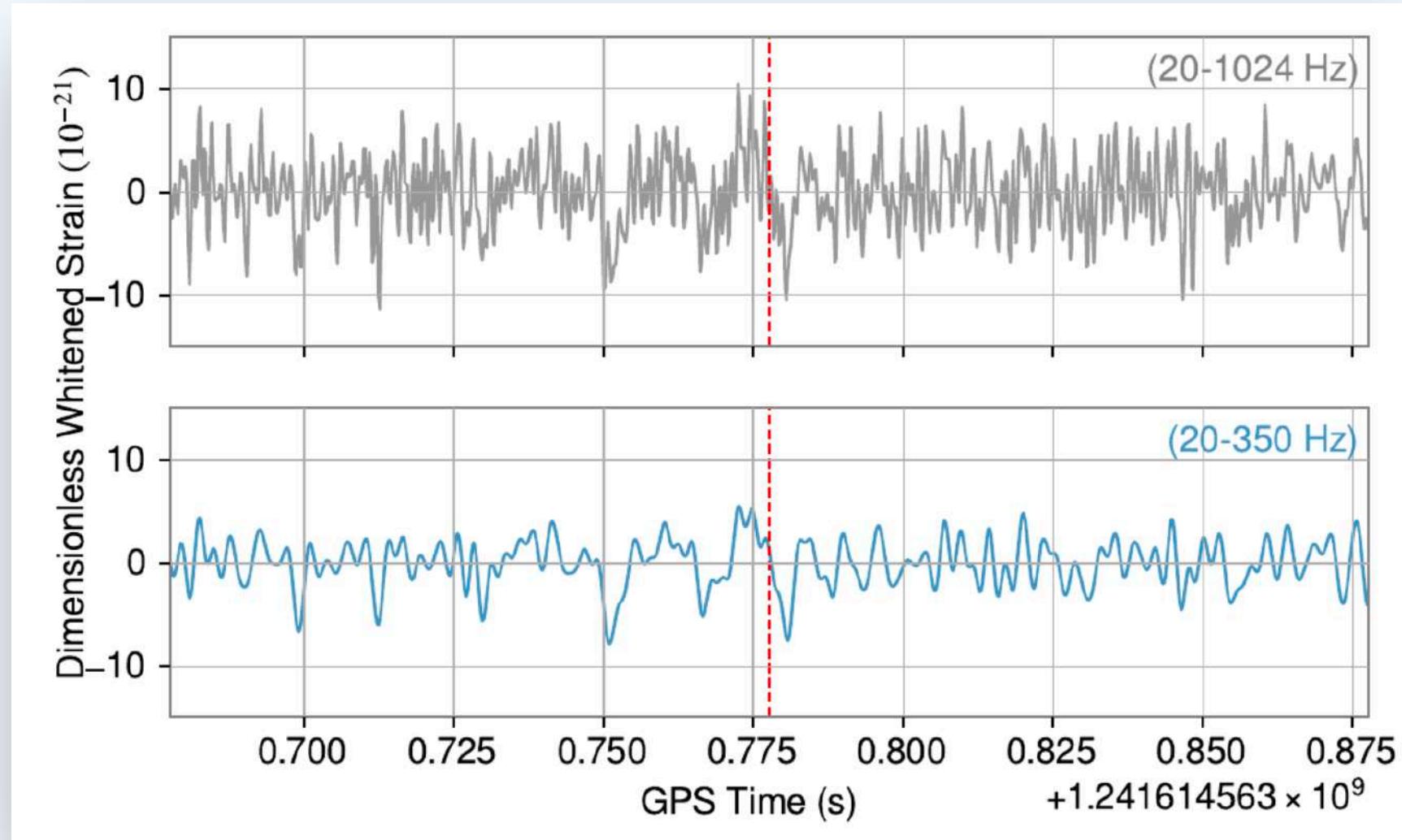
# MAIN ENHANCEMENTS:

## 1) Training on low-pass filtered data

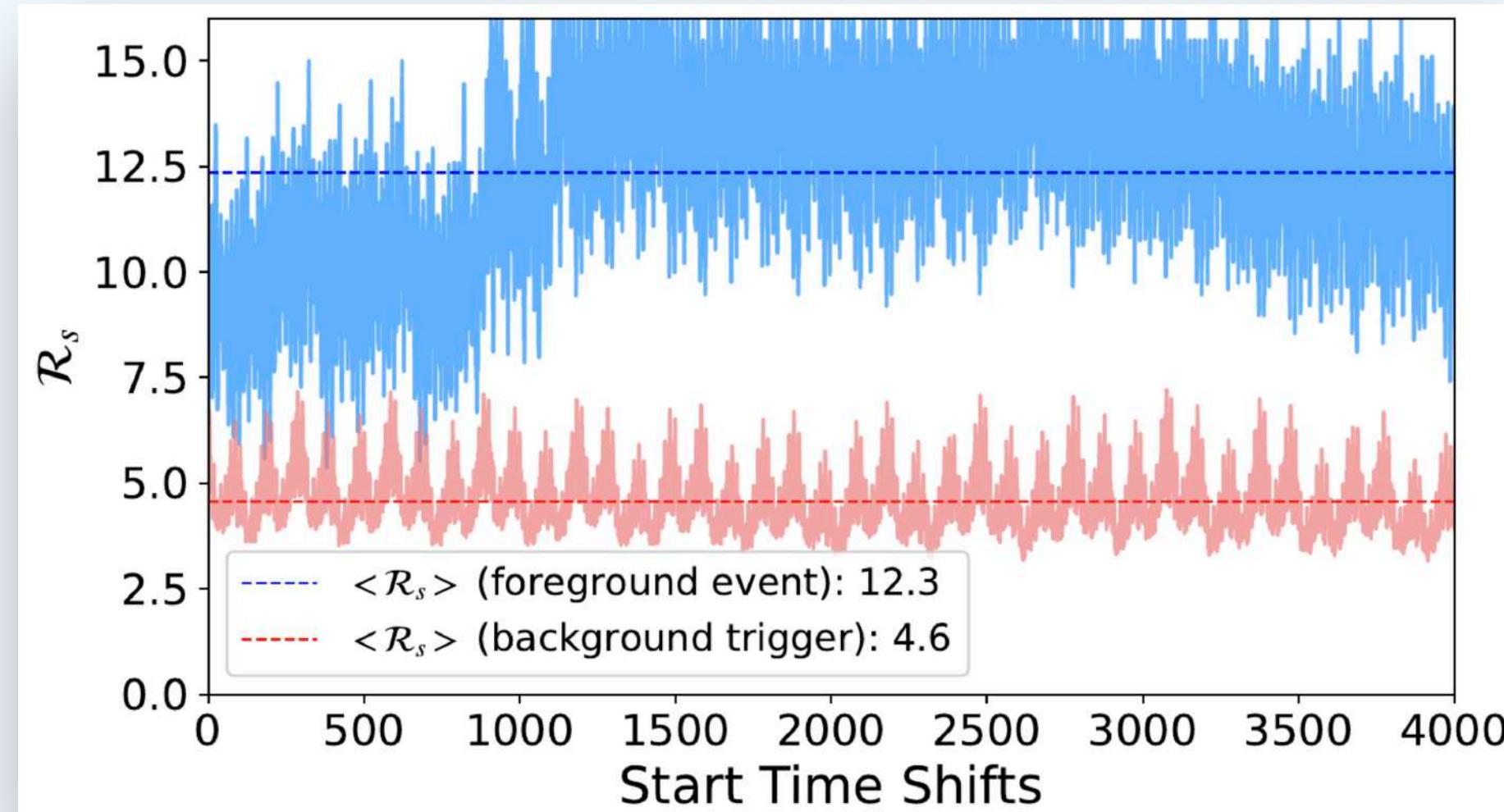


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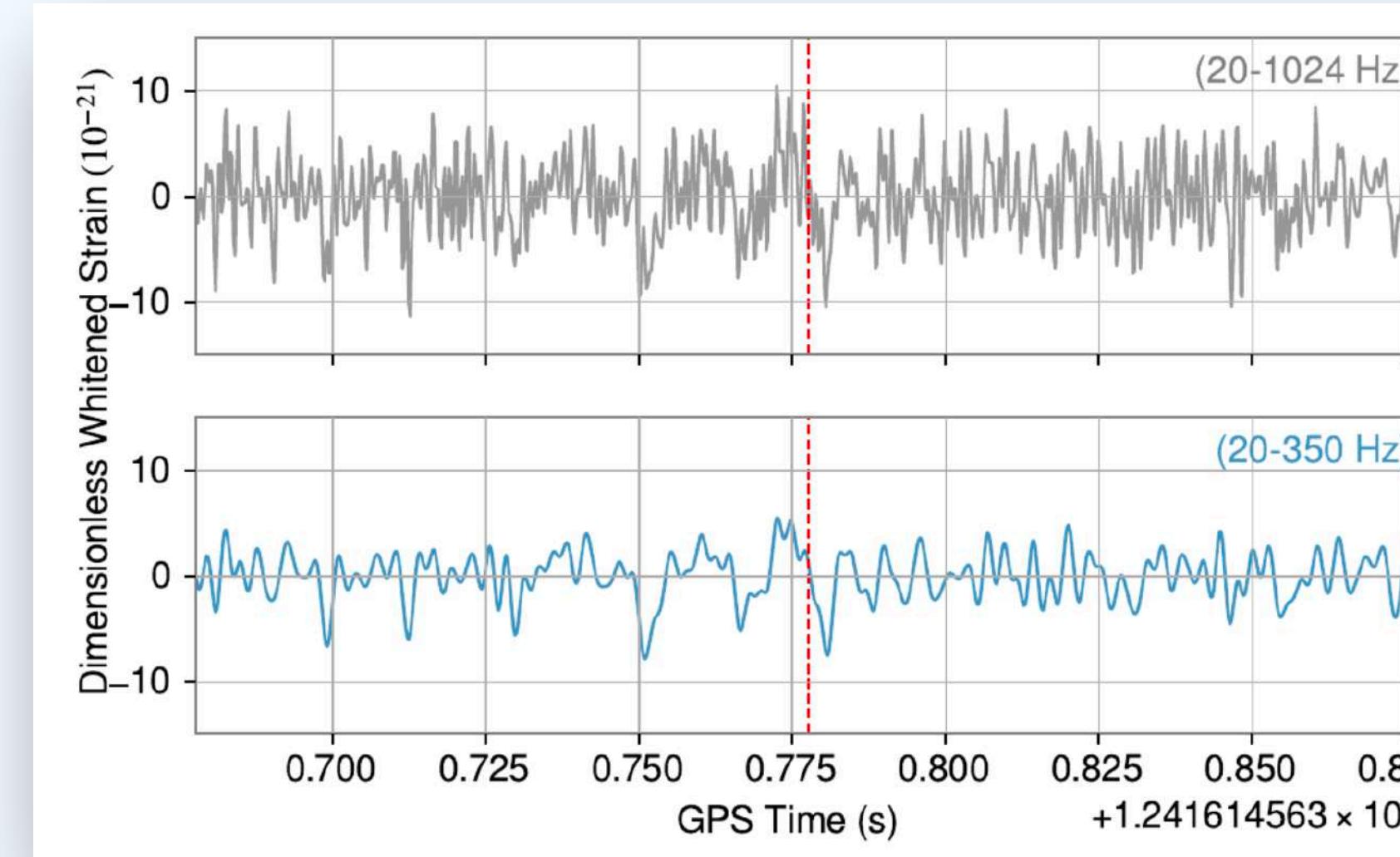


## 2) Ensemble-averaged ranking statistic

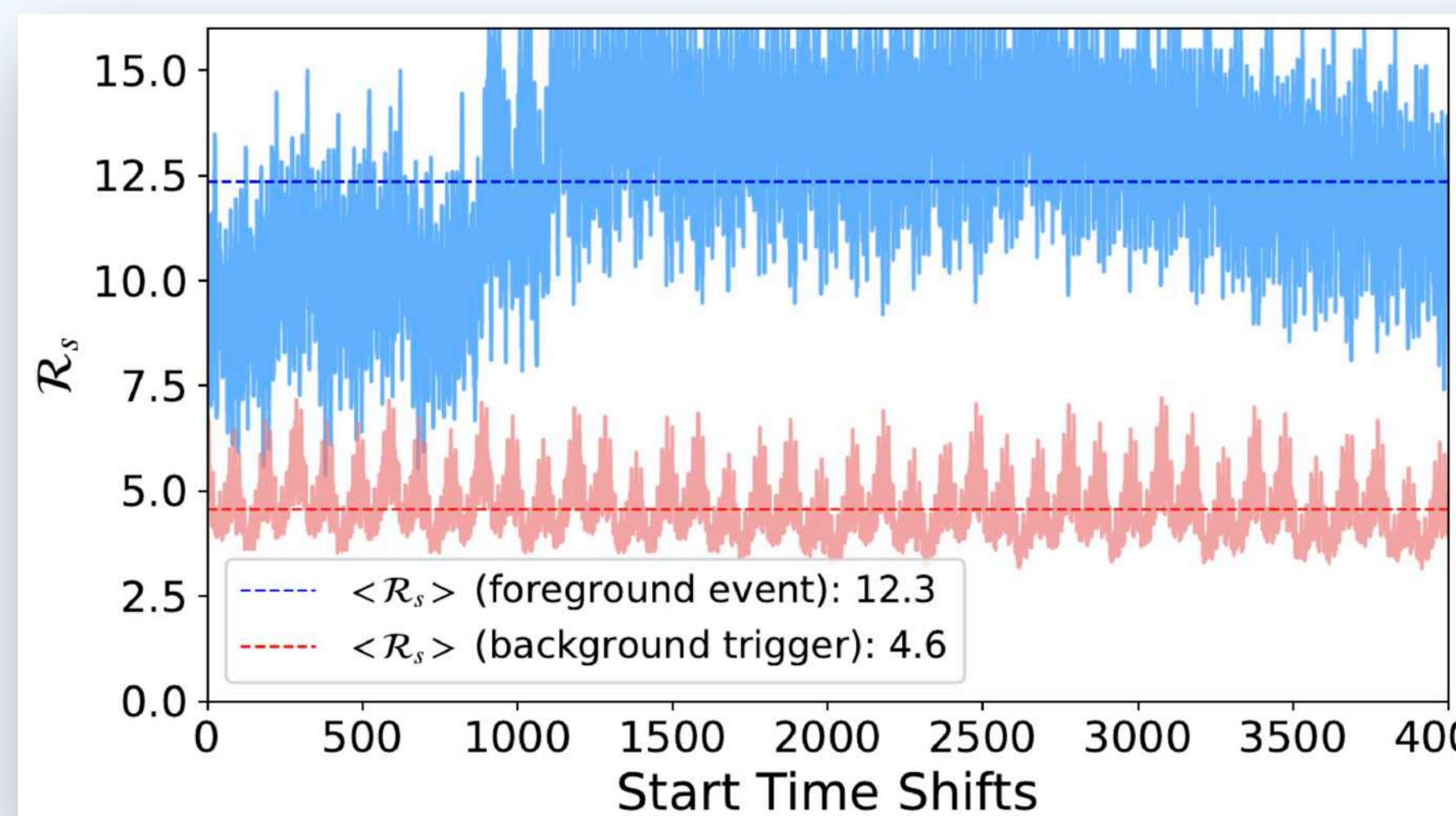


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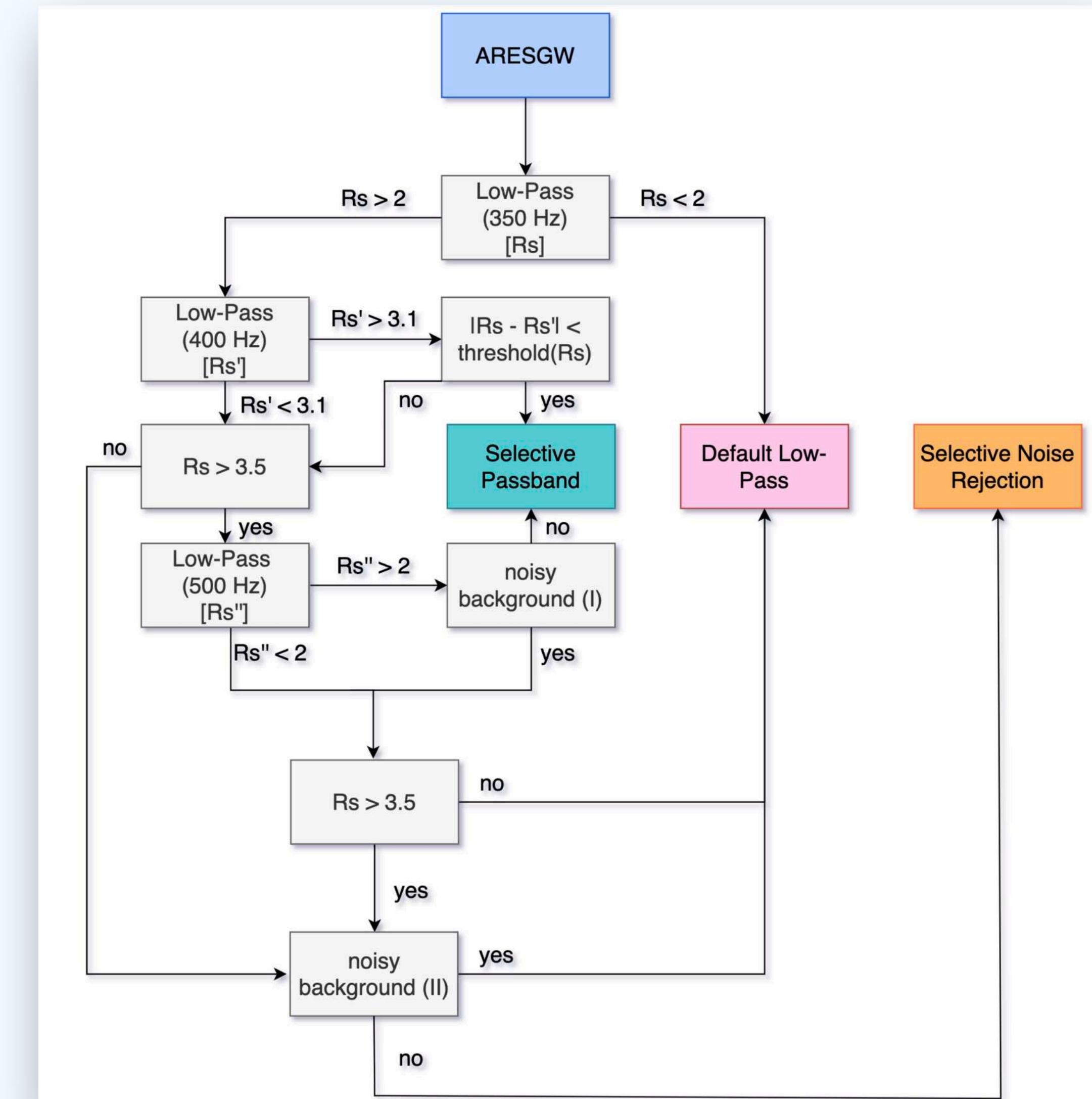
# 1) Training on low-pass filtered data



## 2) Ensemble-averaged ranking statistic



### 3) Application of noise filters to reduce background FAR.



# ASTROPHYSICAL PROBABILITY

**p\_astro** is calculated as

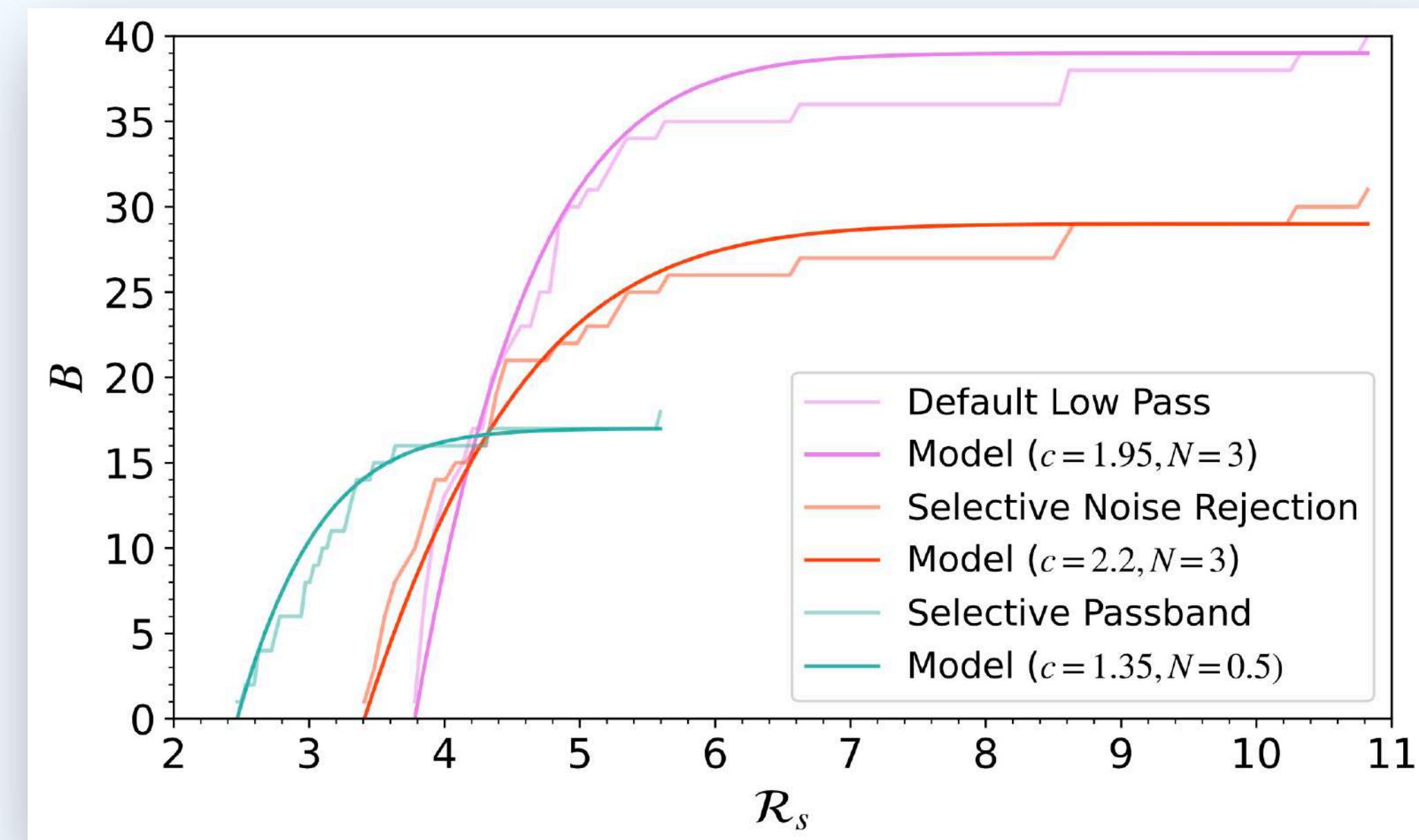
$$p_{\text{astro}} = \frac{f(\mathcal{R}_s)}{b(\mathcal{R}_s) + f(\mathcal{R}_s)}$$

where the **background** and **foreground** differential rates are

The cumulative distribution of the **O3 background** is modeled **analytically** as

$$b(\mathcal{R}_s) = \frac{dB}{d\mathcal{R}_s} \quad f(\mathcal{R}_s) = \frac{dF}{d\mathcal{R}_s}$$

$$\hat{B}(x) = \frac{\left(1 + \operatorname{erf}\left(\frac{x}{\sqrt{2}}\right)\right)^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}{2^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}$$

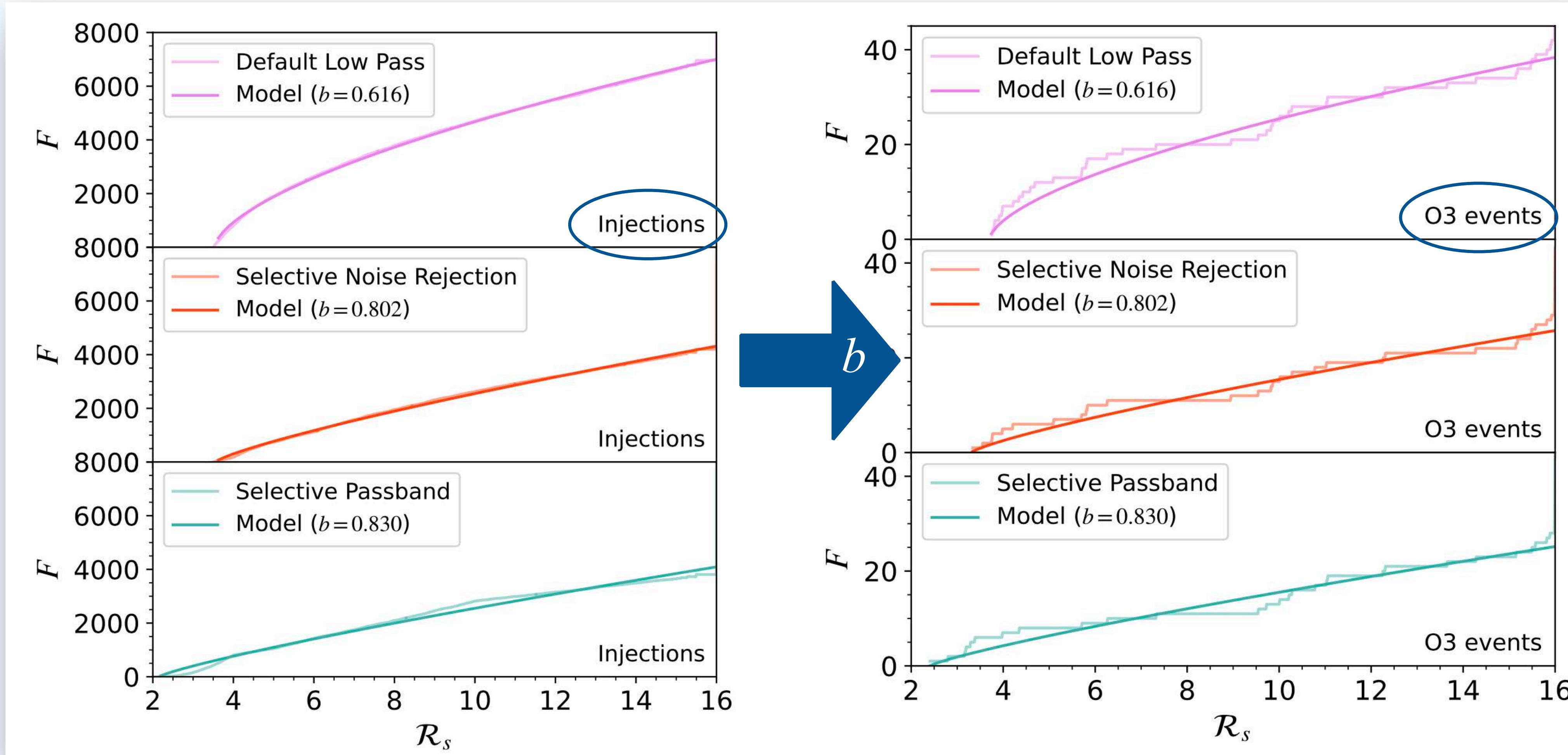


# ASTROPHYSICAL PROBABILITY

Analytic model of cumulative **foreground** distribution:

$$F(x) = a(x - x_{\min})^b$$

Coefficient **b** determined through injections in O3 noise:



# NEW GW DETECTIONS WITH AresGW IN O3 DATA

**AresGW** detects **42 out of 51** known O3 events (*most sensitive pipeline in this mass range*)

We found **8 new gravitational wave candidates** with  $p_{\text{astro}} > 50\%$  (3  $p_{\text{astro}} > 99\%$ ).

TABLE VII: New candidate events identified by AresGW.

#	Event Name	GPS Time (s)	$p_{\text{astro}}$	FAR (1/yr)	$\langle \mathcal{R}_s \rangle$	Time delay (s)	$\chi_L^2$	$\chi_H^2$	Class
1	GW190511_125545	1241614563.77	1.00	0.27	9.54	0.0027	1.16	1.46	Selective Passband
2	GW190614_134749	1244555287.93	0.99	4.6	5.80	0.0012	0.65	0.80	Selective Passband
3	GW190607_083827	1243931925.99	0.99	6.5	8.95	0.0056	0.90	0.48	Selective Noise Rejection
4	GW190904_104631	1251629209.01	0.72	14	4.35	0.0002	0.38	0.71	Selective Passband
5	GW190523_085933	1242637191.44	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
6	GW200208_211609	1265231787.68	0.55	18	4.0	0.0063	0.69	0.98	Selective Passband
7	GW190705_164632	1246380410.88	0.51	49	5.82	0.0103	1.05	0.98	Default Low-Pass*
8	GW190426_082124	1240302101.93	0.50	20	3.91	0.0007	1.48	0.53	Selective Passband

# NEW GW DETECTIONS WITH AresGW IN O3 DATA

AresGW detects **42 out of 51** known O3 events (*most sensitive pipeline in this mass range*)

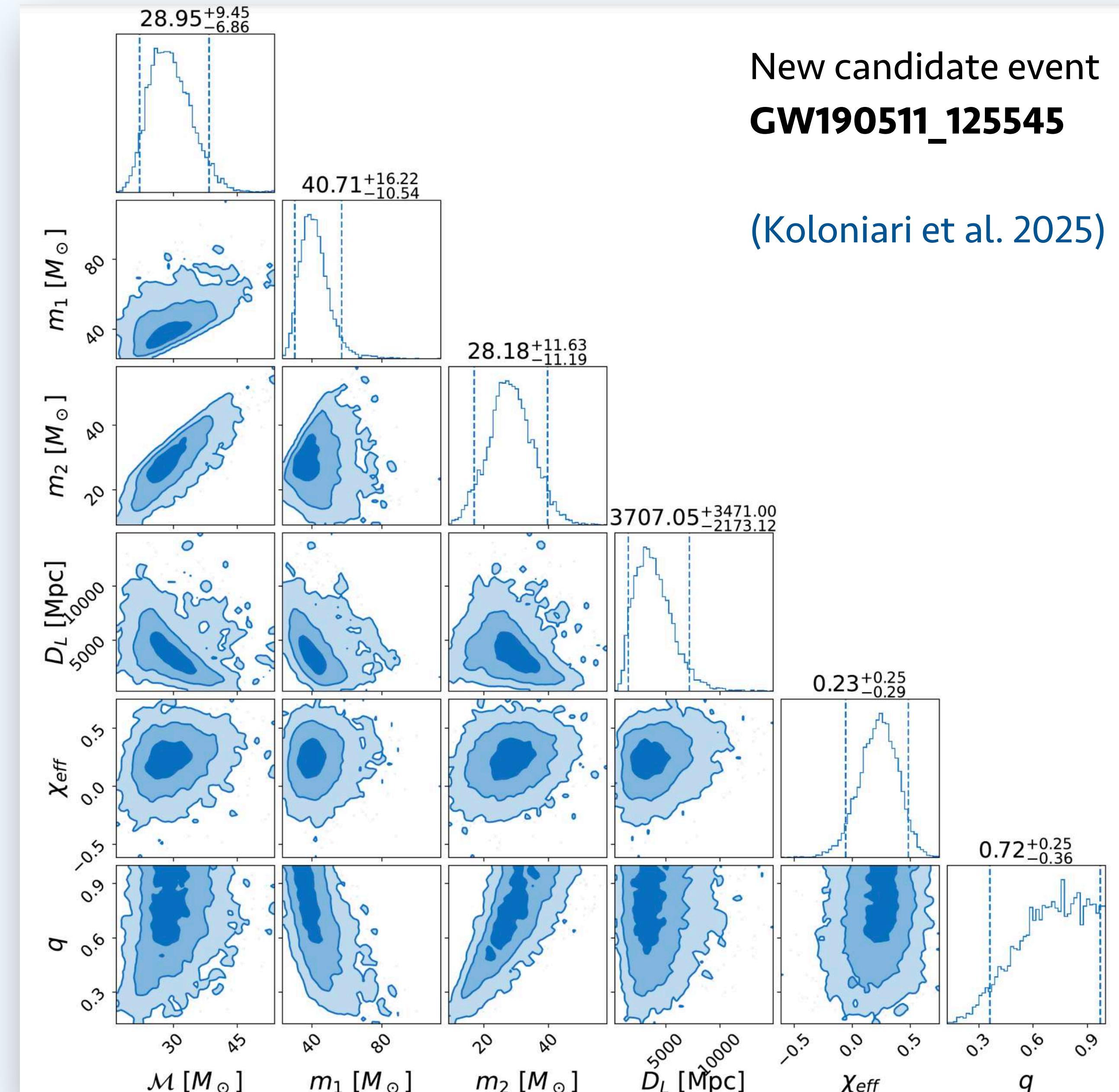
We found **8 new gravitational wave candidates** with  $p_{\text{astro}} > 50\%$  (3  $p_{\text{astro}} > 99\%$ ).

TABLE VII: New candidate events identified by AresGW.

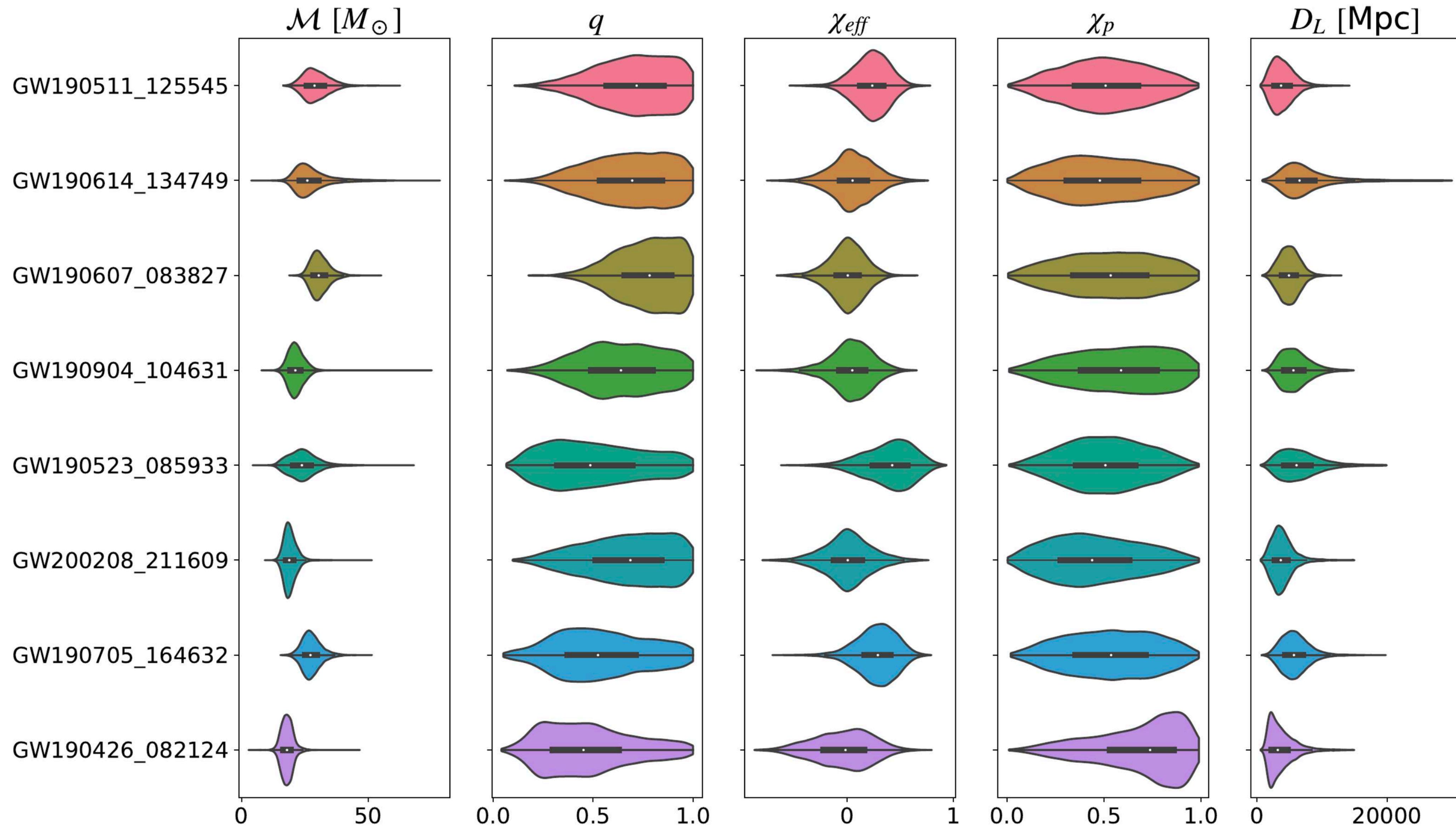
#	Event Name	GPS Time (s)	$p_{\text{astro}}$	FAR (1/yr)	$\langle \mathcal{R}_s \rangle$	Time delay	$\chi^2$	S	Class
1	GW190511_125545	1241614563.77	1.00	1.00	0.55	0.0056	0.90	0.48	Selective Passband
2	GW190614_134749	1242637191.44	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
3	GW190607_083151	1242637191.44	0.72	14	4.35	0.0002	0.38	0.71	Selective Passband
4	GW190904_104151	1241614563.77	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
5	GW200208_211609	1265231787.68	0.55	18	4.0	0.0063	0.69	0.98	Selective Passband
7	GW190705_164632	1246380410.88	0.51	49	5.82	0.0103	1.05	0.98	Default Low-Pass*
8	GW190426_082124	1240302101.93	0.50	20	3.91	0.0007	1.48	0.53	Selective Passband

First GW events identified  
using a machine-learning algorithm

# PARAMETER ESTIMATION USING BILBY



# PARAMETER ESTIMATION USING BILBY



# RECONSTRUCTED WAVEFORMS FOR NEW EVENTS

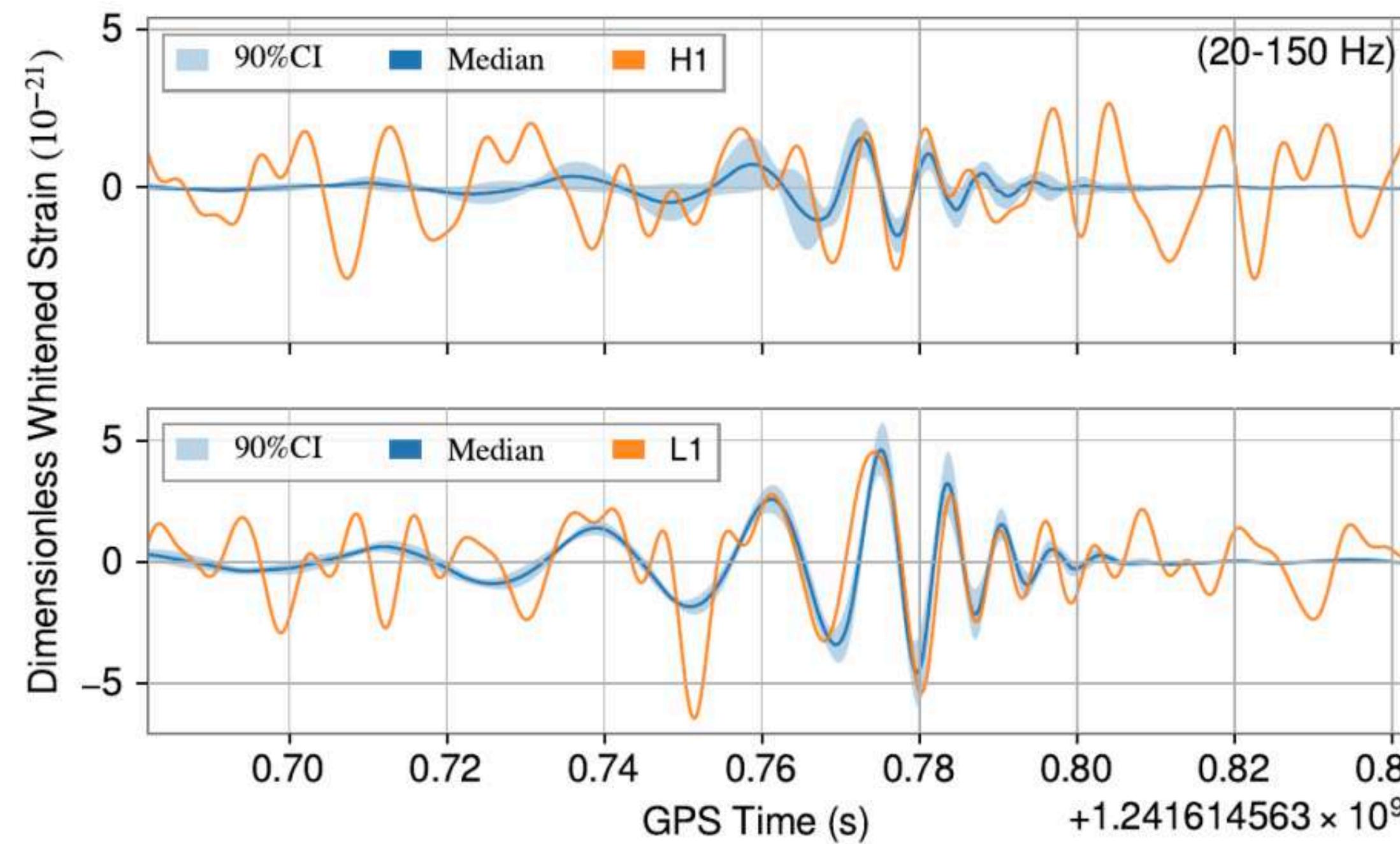


FIG. 35: Whitened, bandpassed strain data and reconstructed waveform for the new event GW190511\_125545 identified by AresGW.

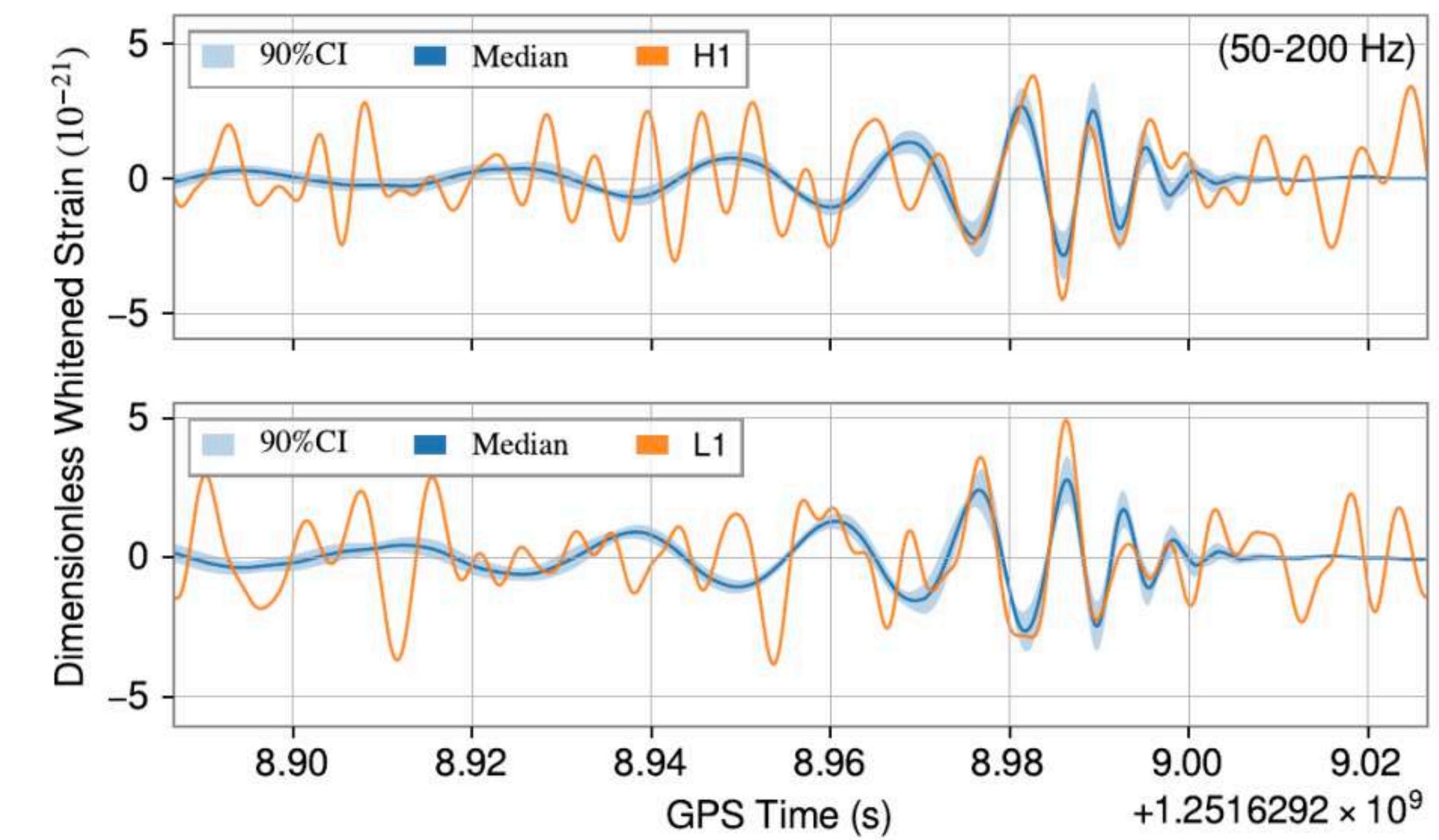
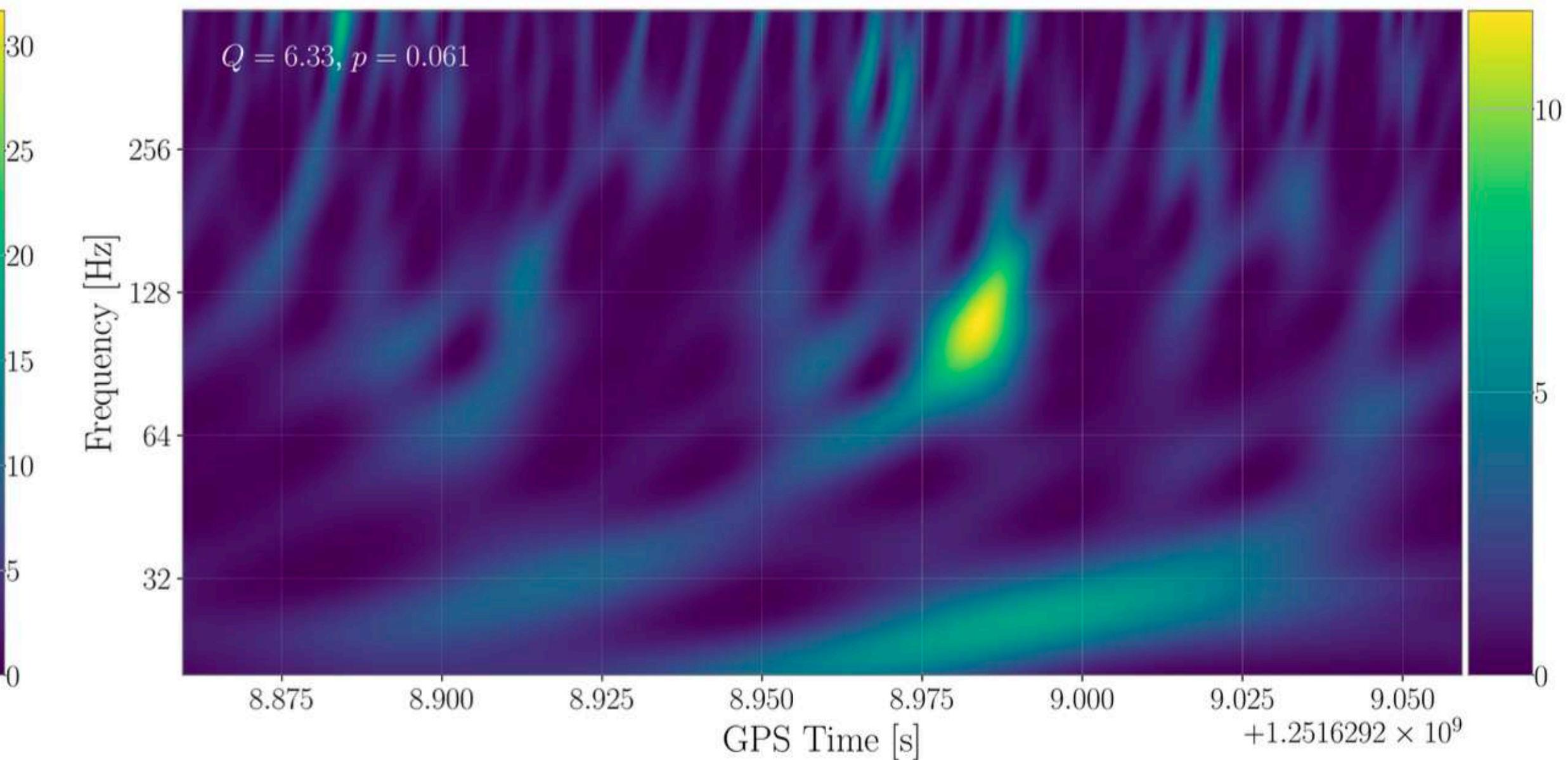
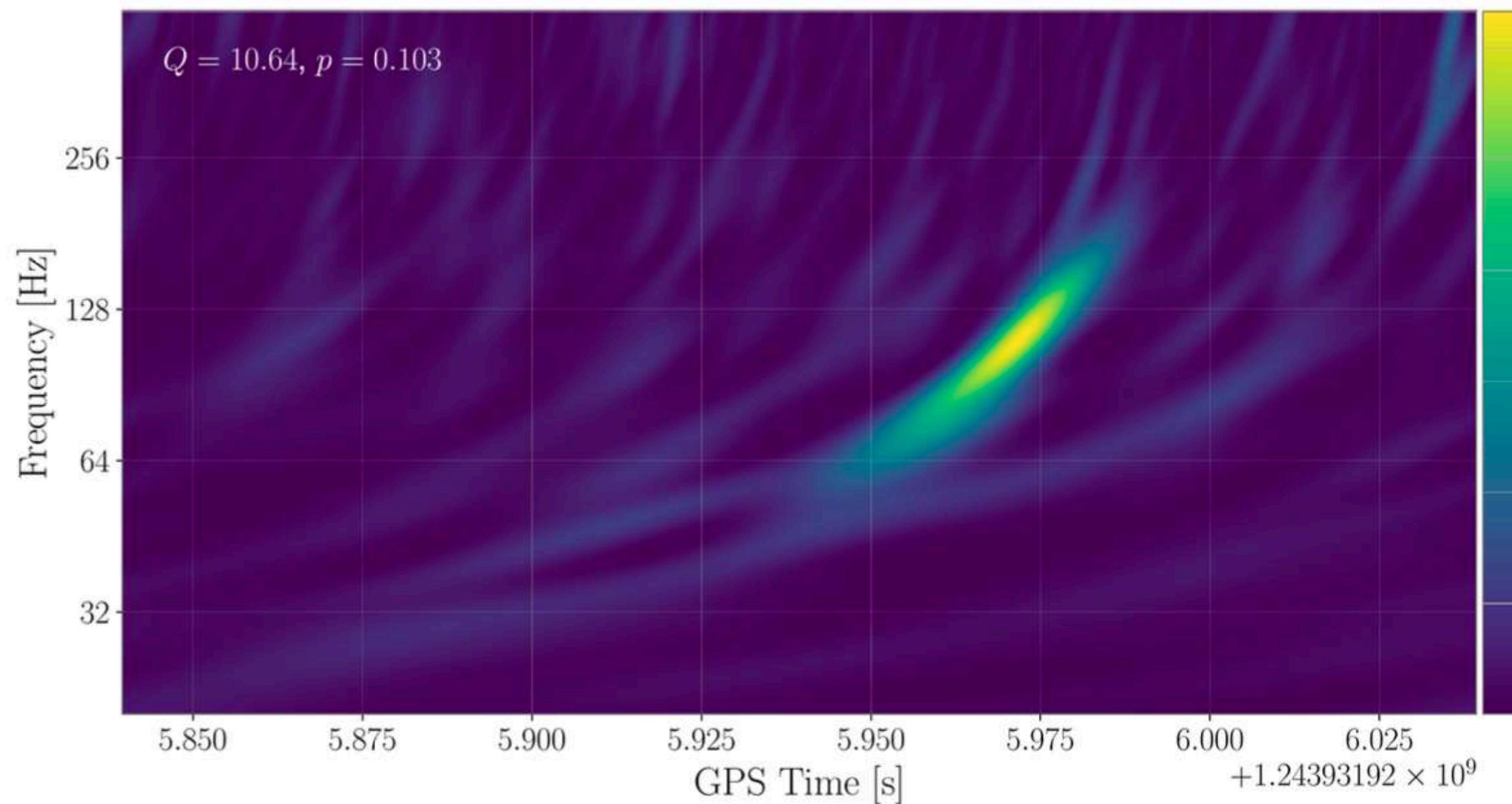
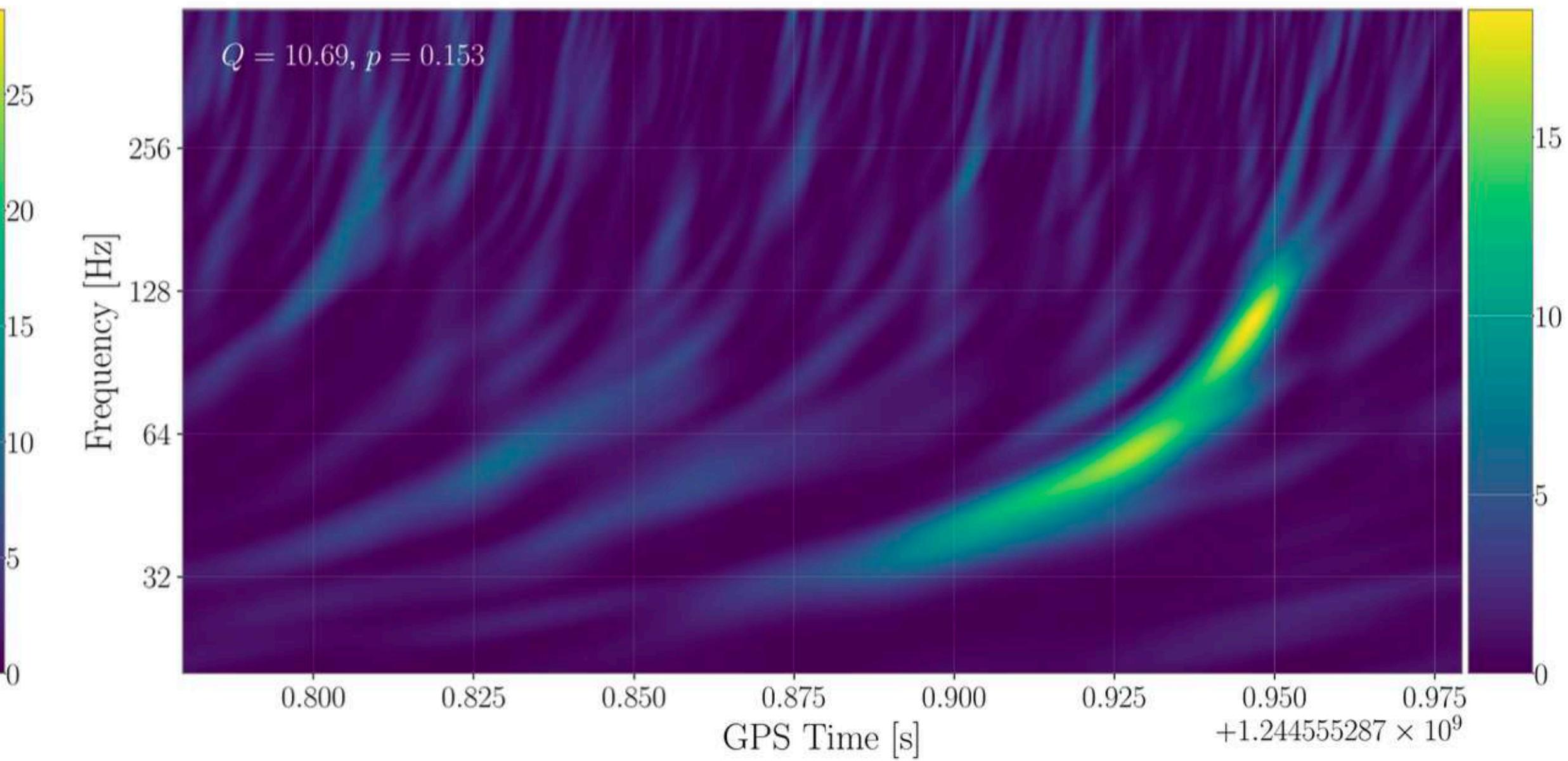
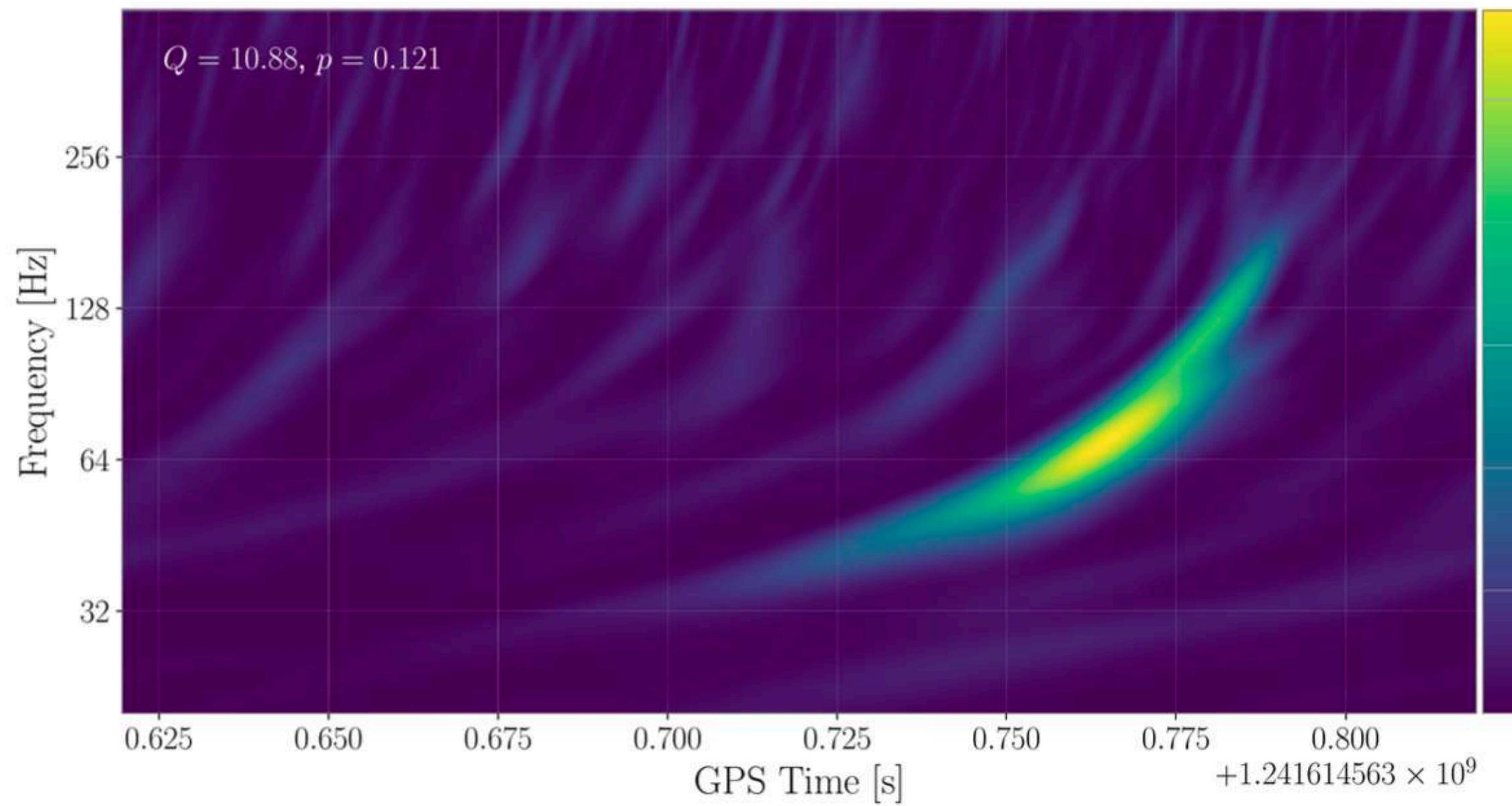
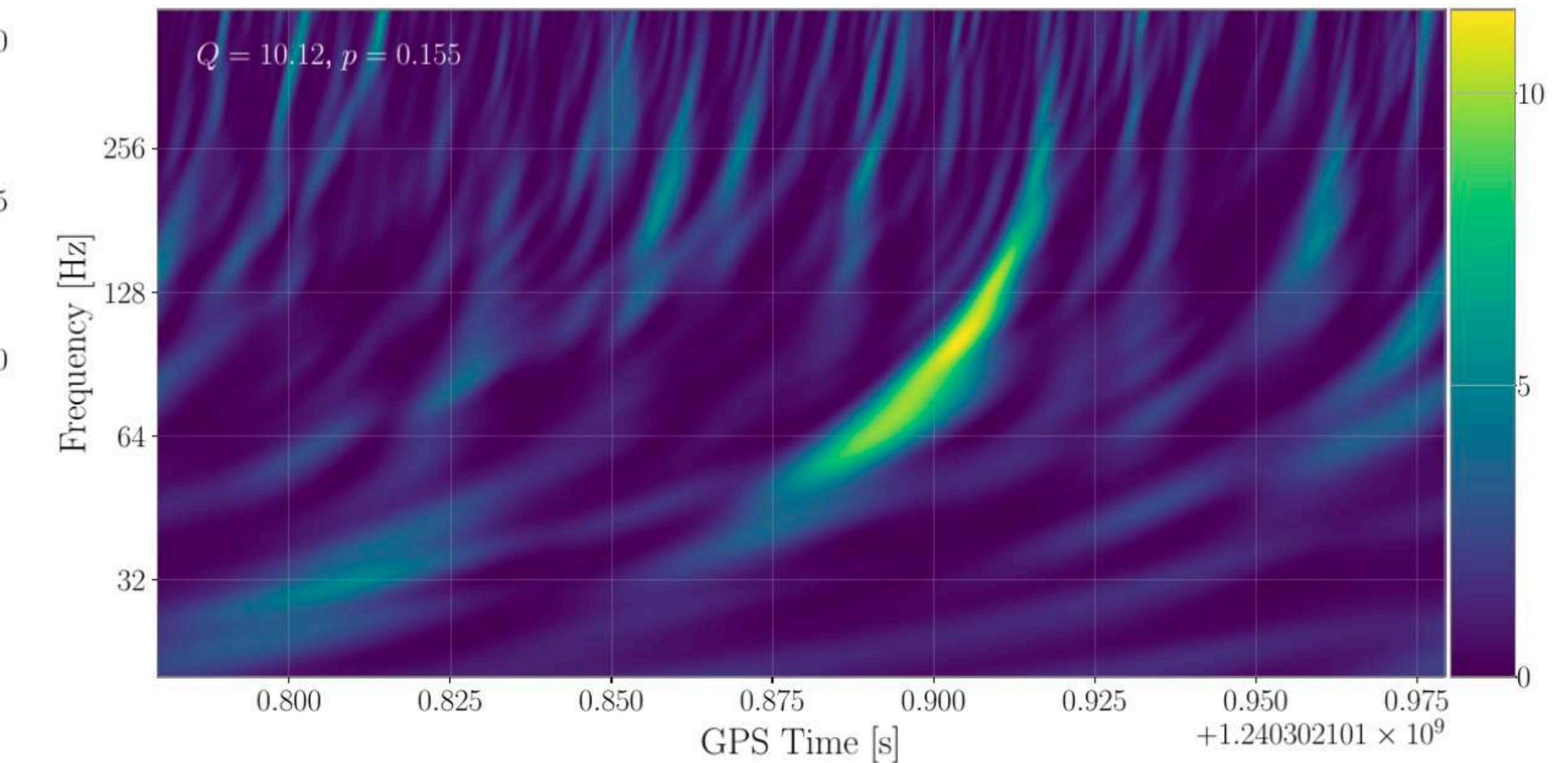
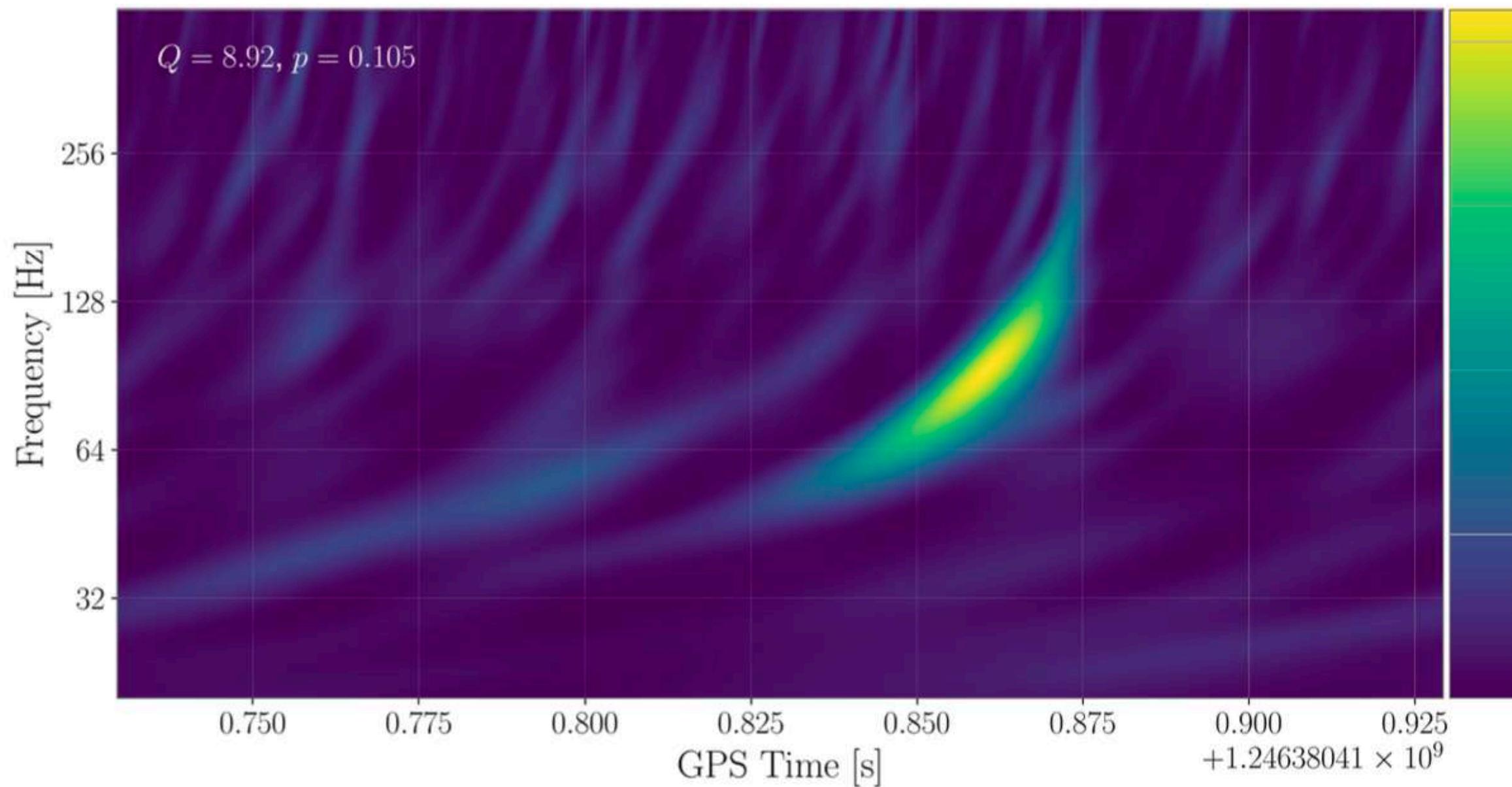
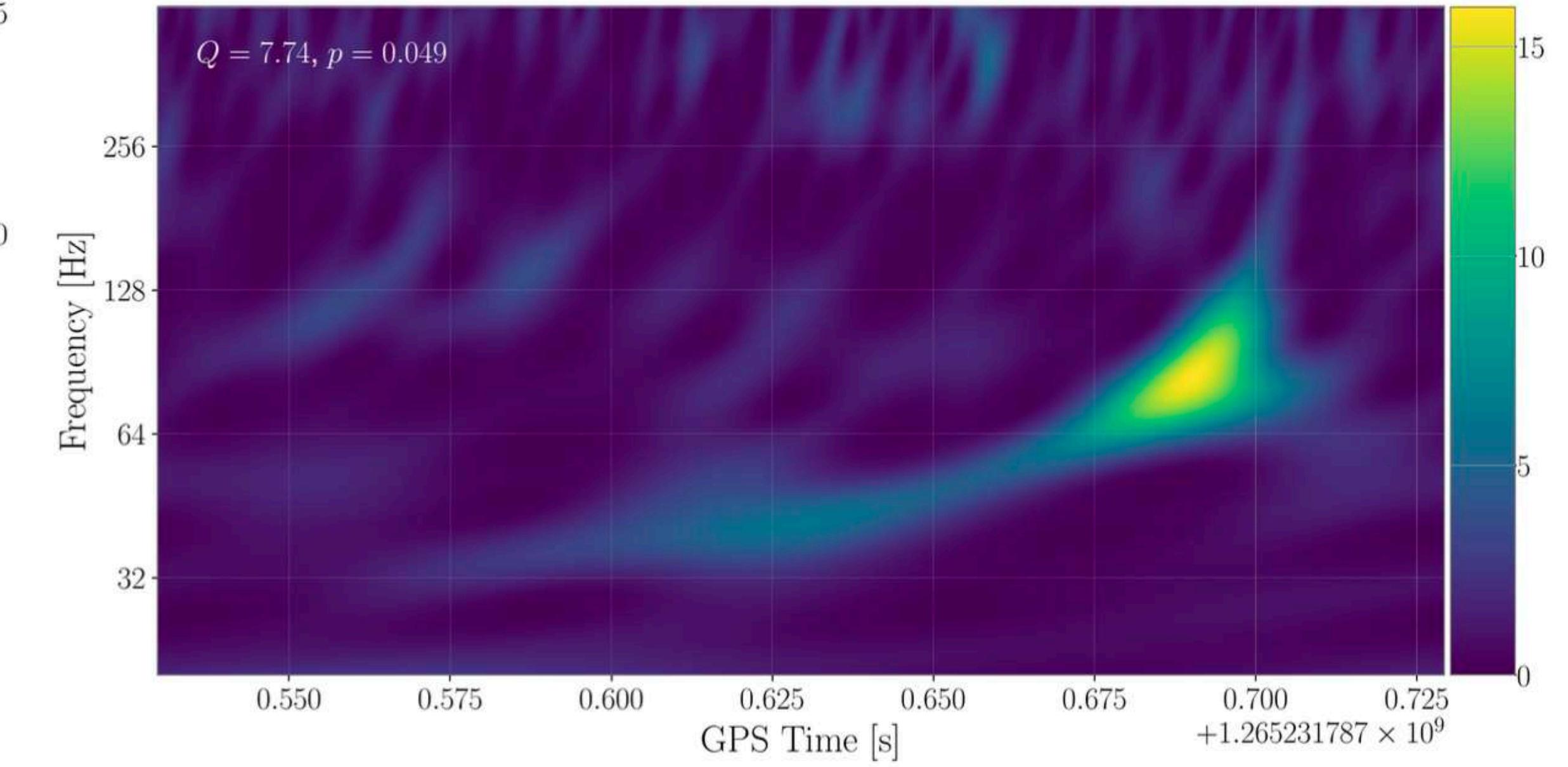
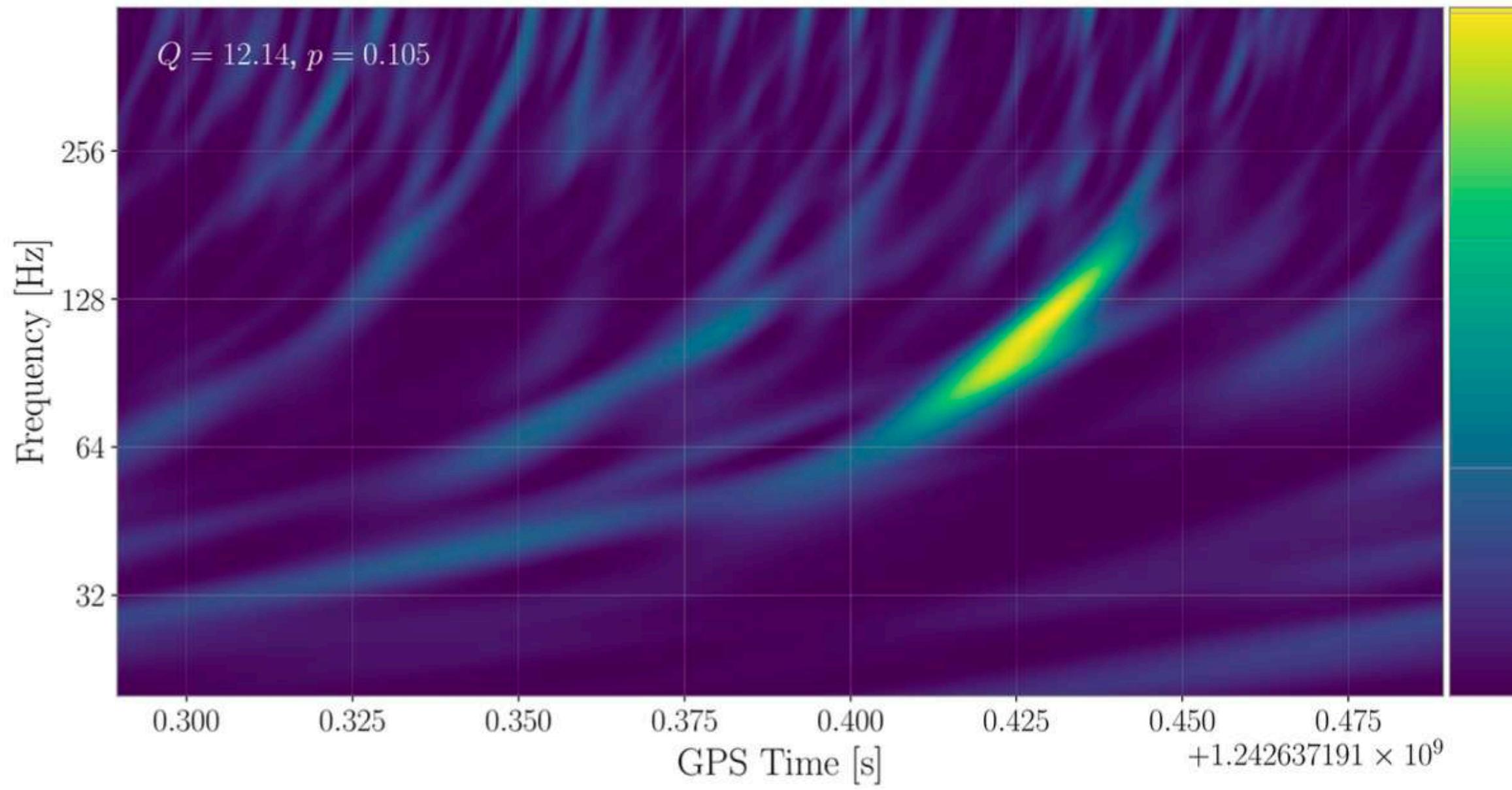


FIG. 38: Same as Fig. 35, but for the new event GW190904\_104631.

# ARESGW NEW CANDIDATE EVENTS



# ARESGW NEW CANDIDATE EVENTS



**PART B.**  
**BINARY NEUTRON STAR POST-MERGER PHASE**

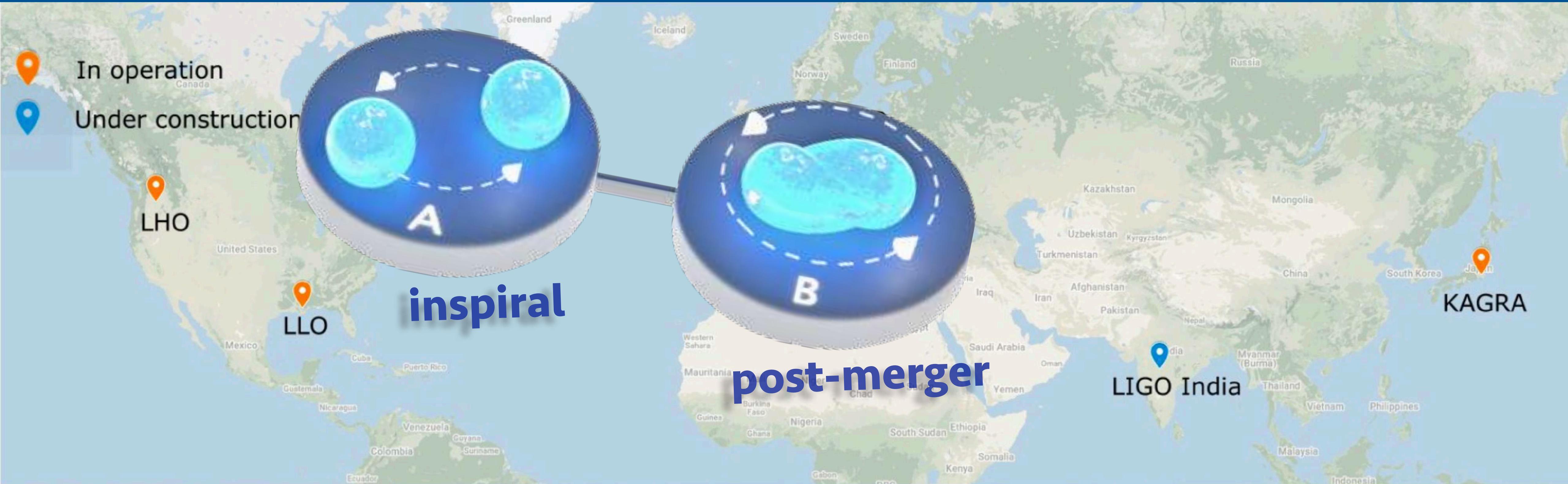
# INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



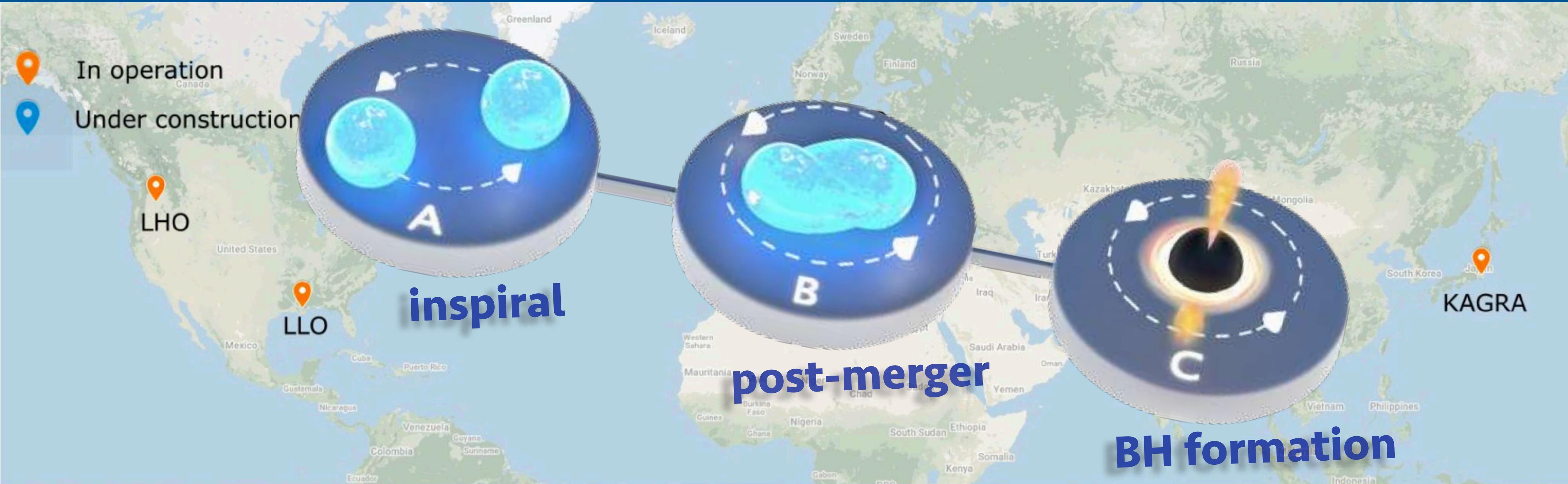
# INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



# INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)

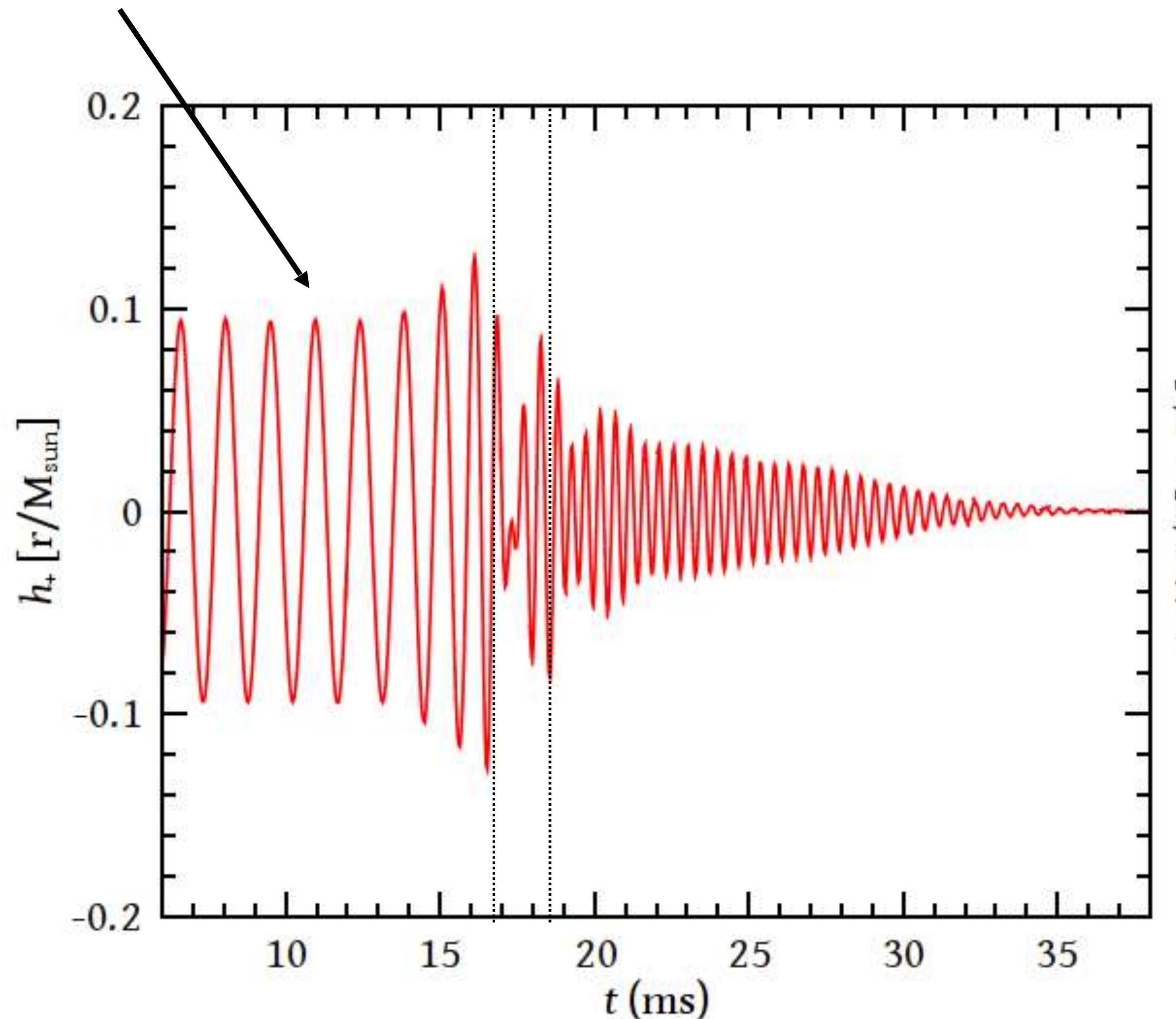


# INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



# POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:  
*inspiral*, *merger* and *post-merger oscillations*.

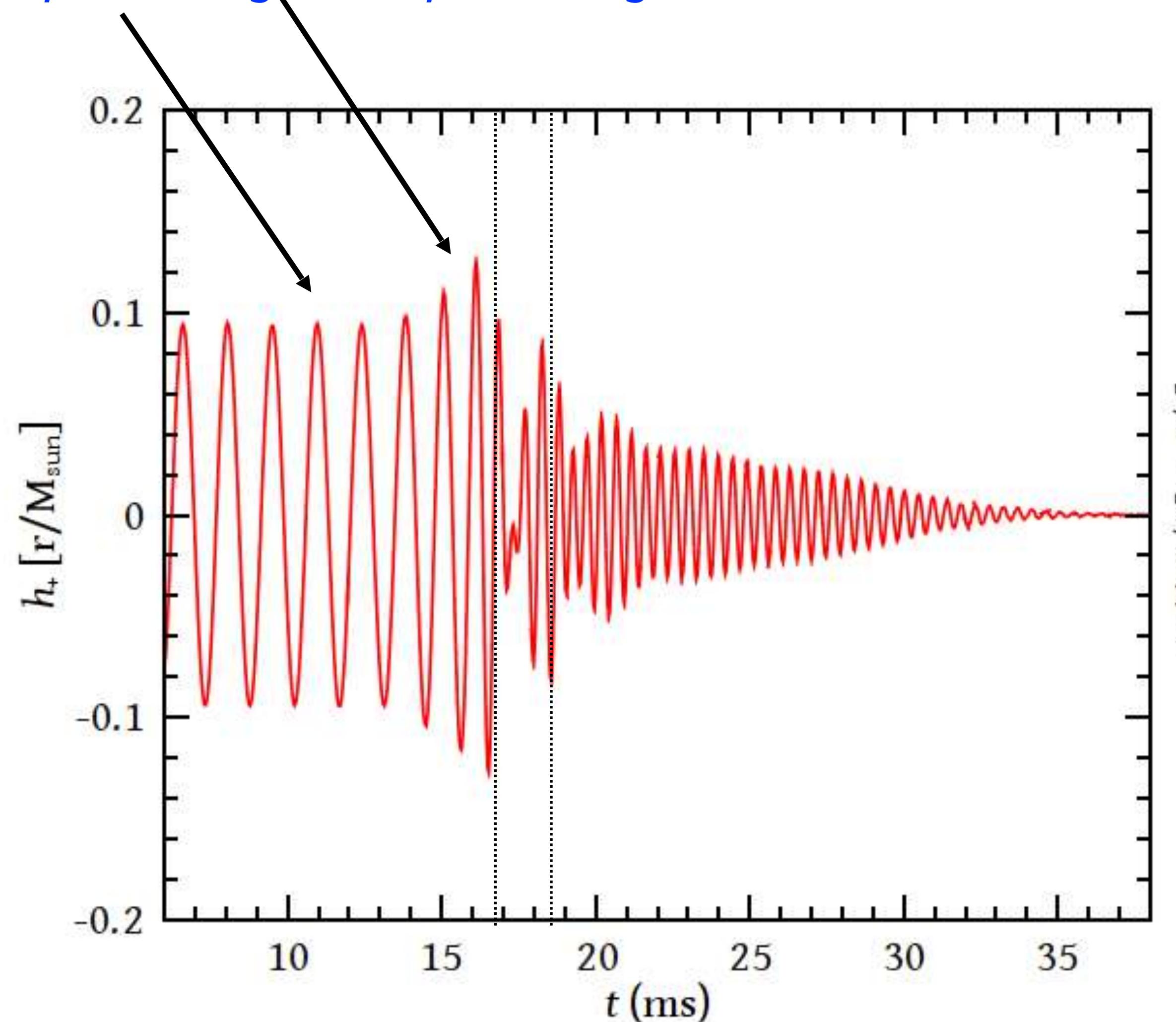


Stergioulas et al. (2011)

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Time domain: three distinct phases of the GW signal:

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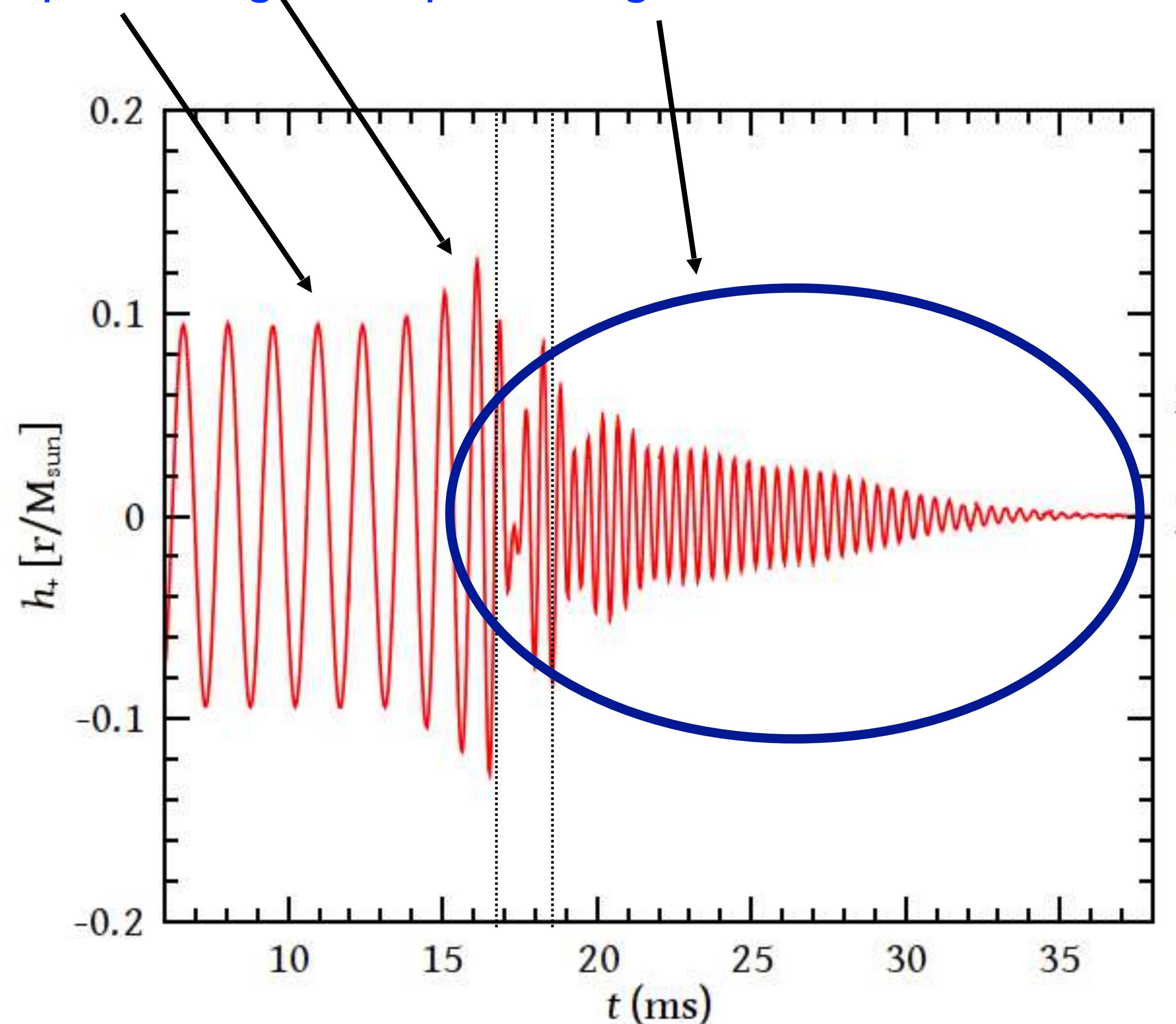


Stergioulas et al. (2011)

# POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:

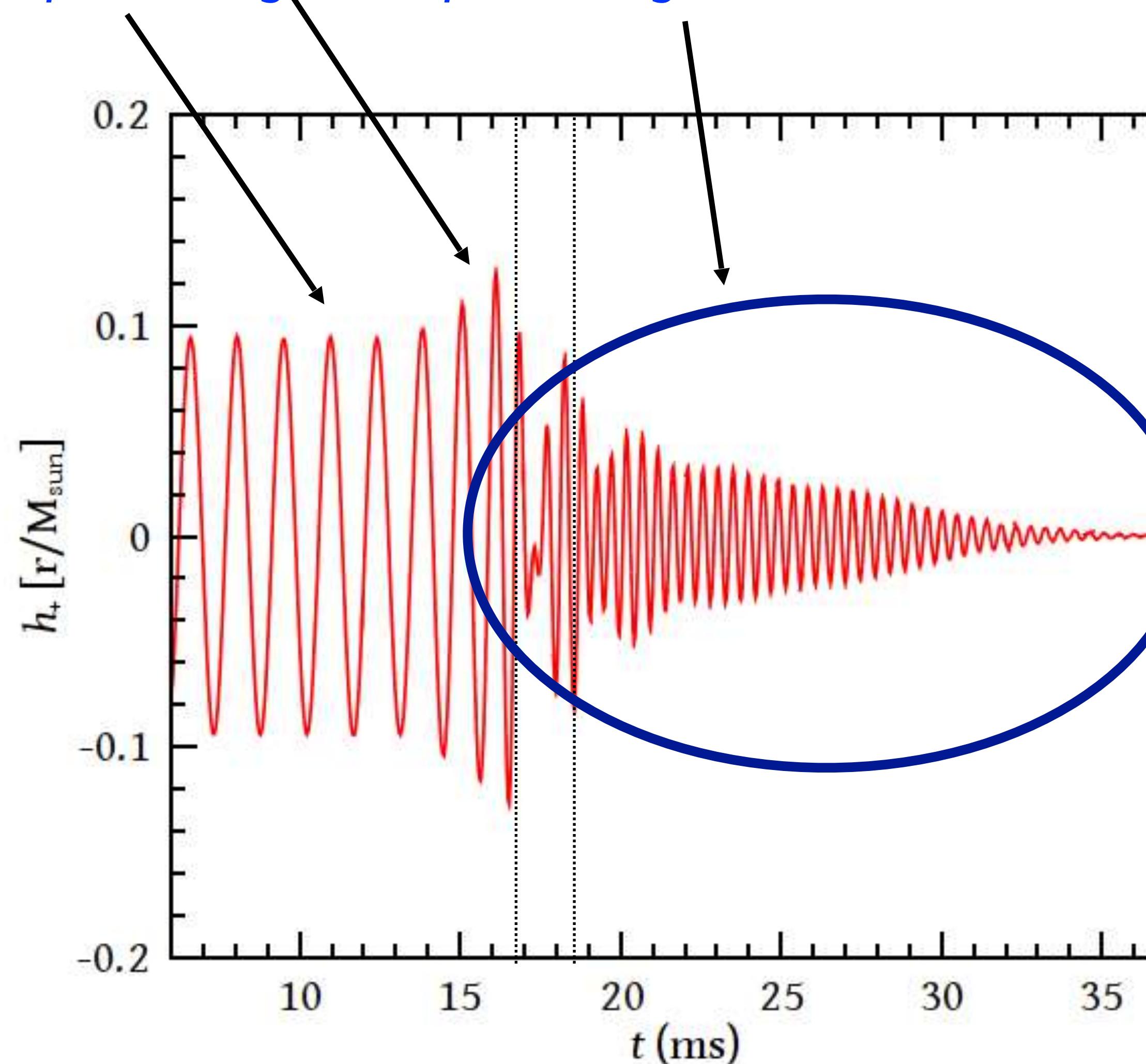
*inspiral*, *merger* and *post-merger oscillations*.



Stergioulas et al. (2011)

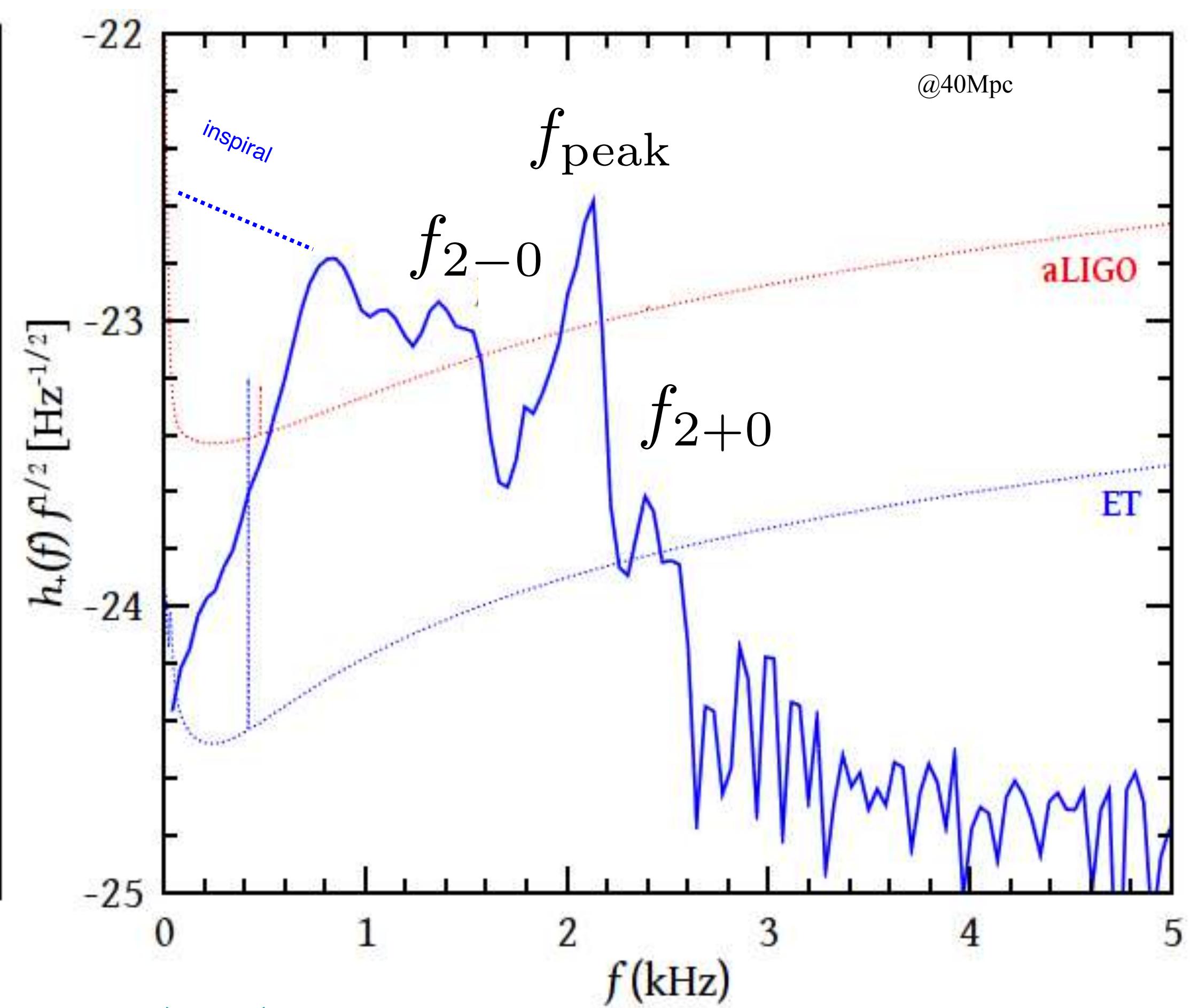
# POST-MERGER PHASE IN BNS MERGERS

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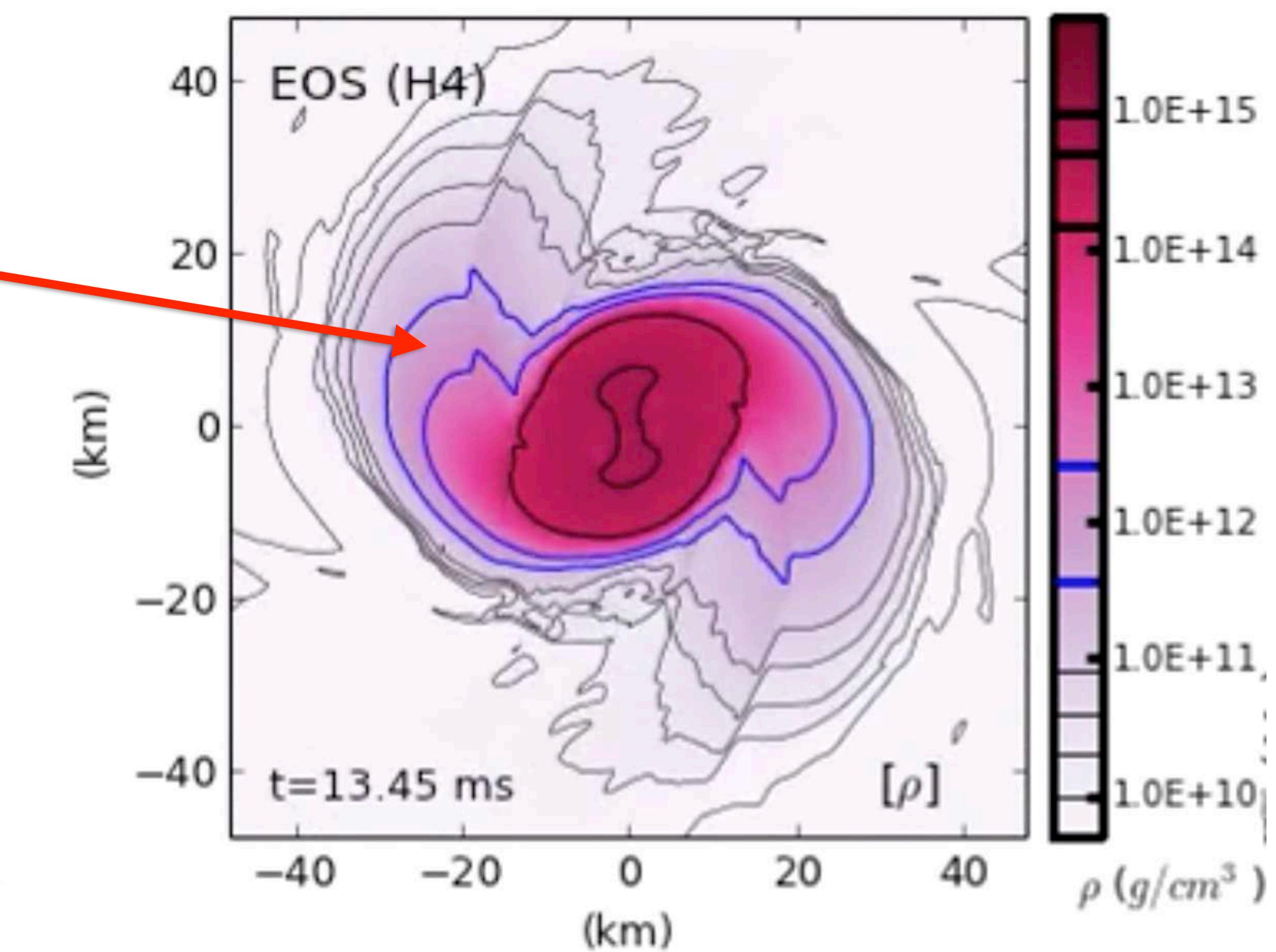
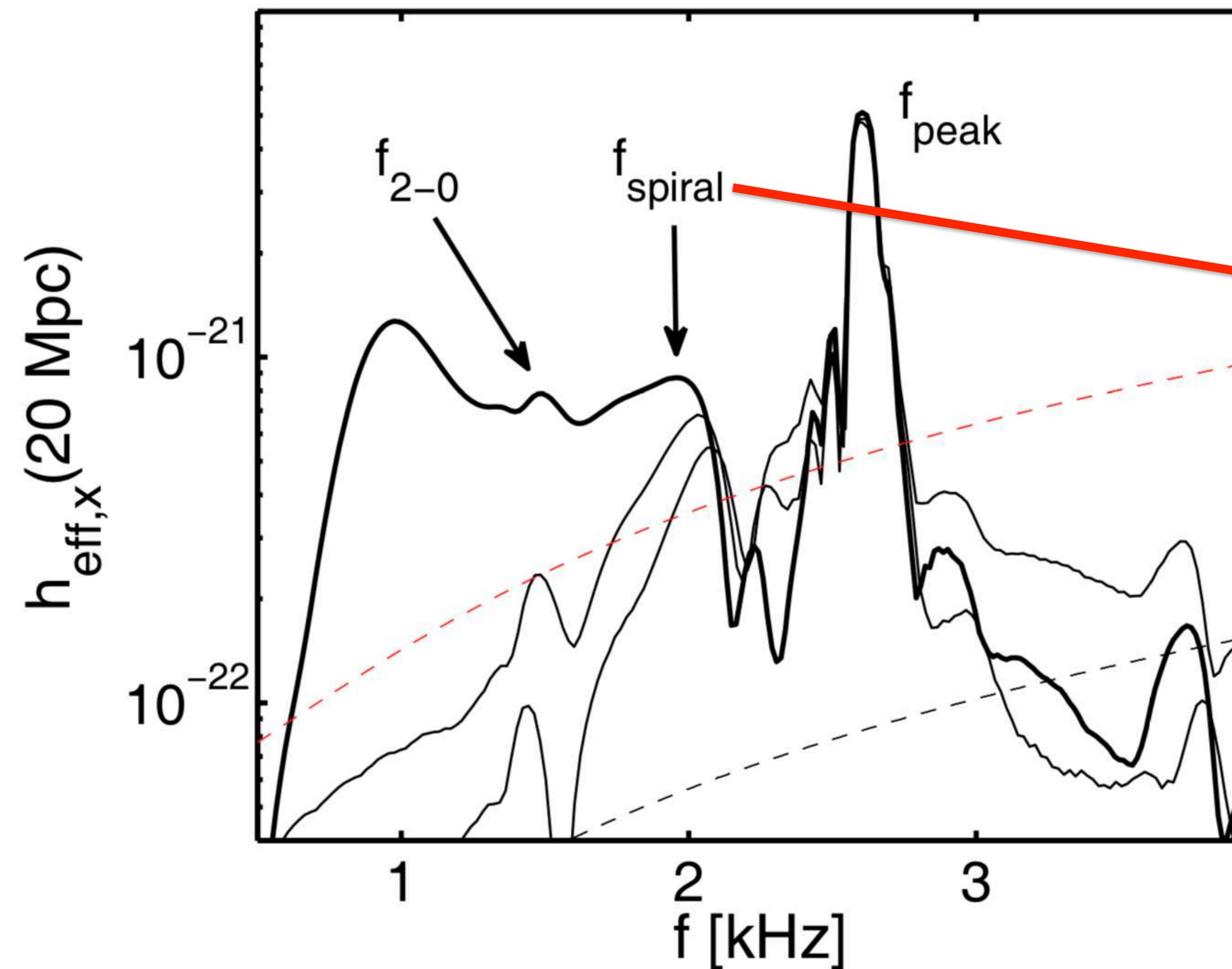
Frequency domain:  
 $f_{\text{peak}}$  :  $l=m=2$  fundamental mode.

$f_{2-0}, f_{2+0}$  : nonlinear combination tones

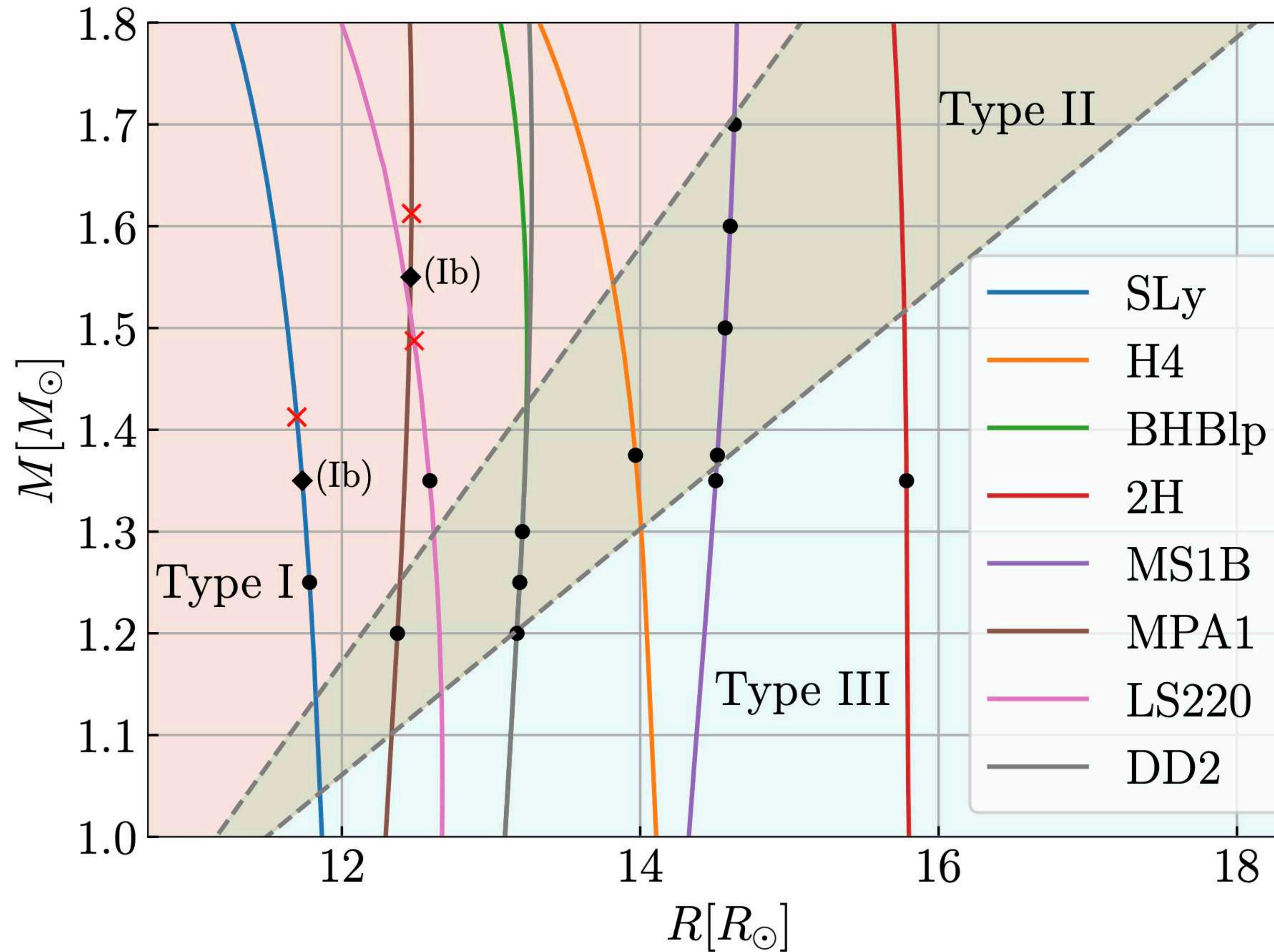


# POST-MERGER PHASE IN BNS MERGERS

Orbiting spiral arms also lead to a distinct frequency  $f_{\text{spiral}}$



# CLASSIFICATION OF POST-MERGER WAVEFORMS



Vretinaris et al. (2025)

Bauswein & Stergioulas (2015)

Vretinaris, Bauswein & Stergioulas (2020)

**Type I:**

$f_{2-0}$  stronger than  $f_{\text{spiral}}$

**Type II:**

$f_{2-0}$  comparable to  $f_{\text{spiral}}$

**Type III:**

$f_{\text{spiral}}$  stronger than  $f_{2-0}$

**Type Ib:**

(close to  $M_{\text{thres}}$ )

# EMPIRICAL RELATIONS OF POST-MERGER FREQUENCIES

$$f_{\text{peak}} M_{\text{chirp}} = 1.392 - 0.108 M_{\text{chirp}} + 51.70 \tilde{\Lambda}^{-1/2}$$

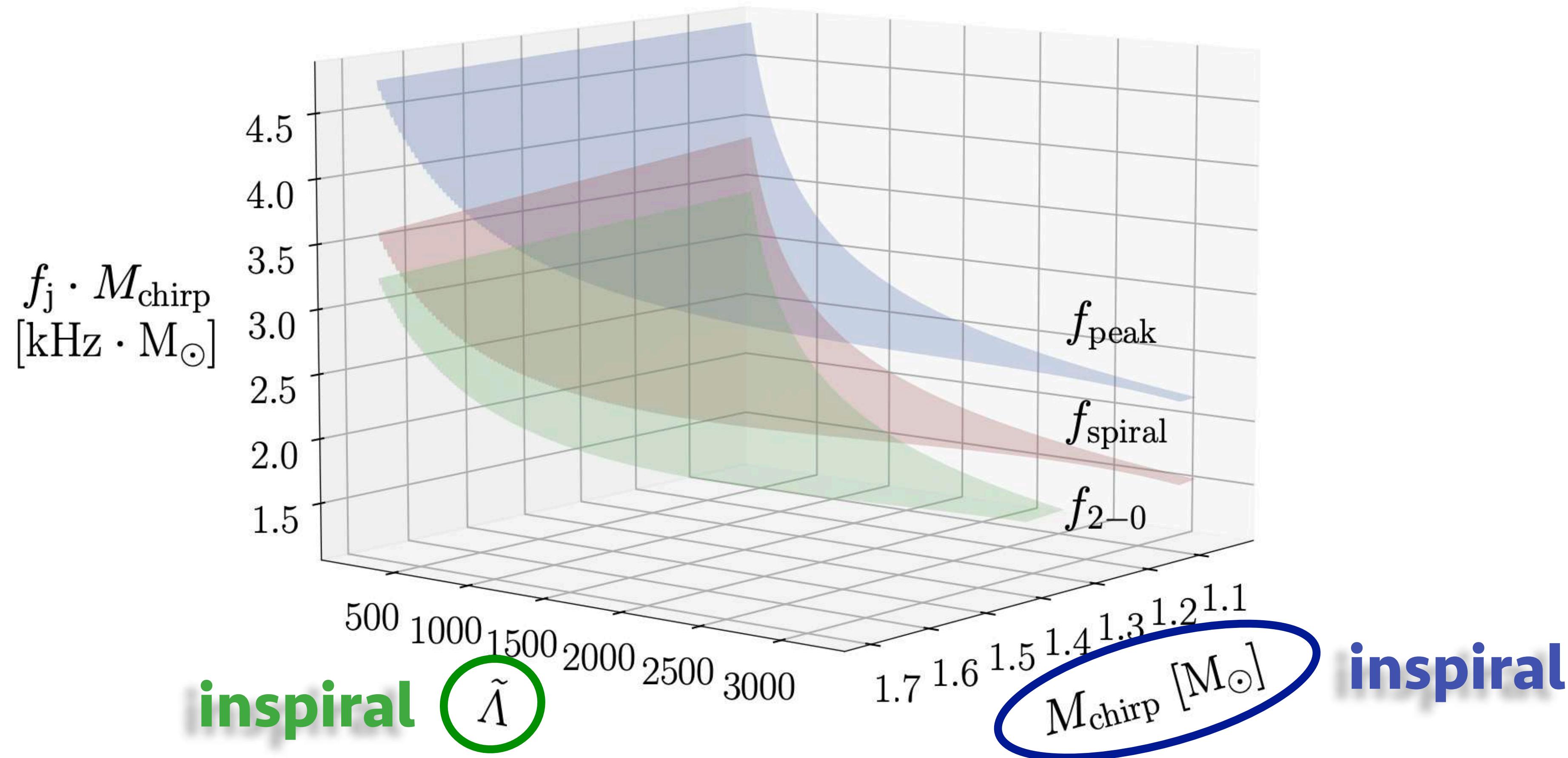
Vretinaris, Bauswein & Stergioulas (2020)

$$f_{2-0} M_{\text{chirp}} = 0.558 - 0.406 M_{\text{chirp}} + 48.696 \tilde{\Lambda}^{-1/2}$$

Vretinaris et al. (2025)

$$f_{\text{spiral}} M_{\text{chirp}} = 1.2 - 0.442 M_{\text{chirp}} + 45.819 \tilde{\Lambda}^{-1/2}$$

Vretinaris et al. (2025)



# EMPIRICAL RELATIONS OF POST-MERGER FREQUENCIES

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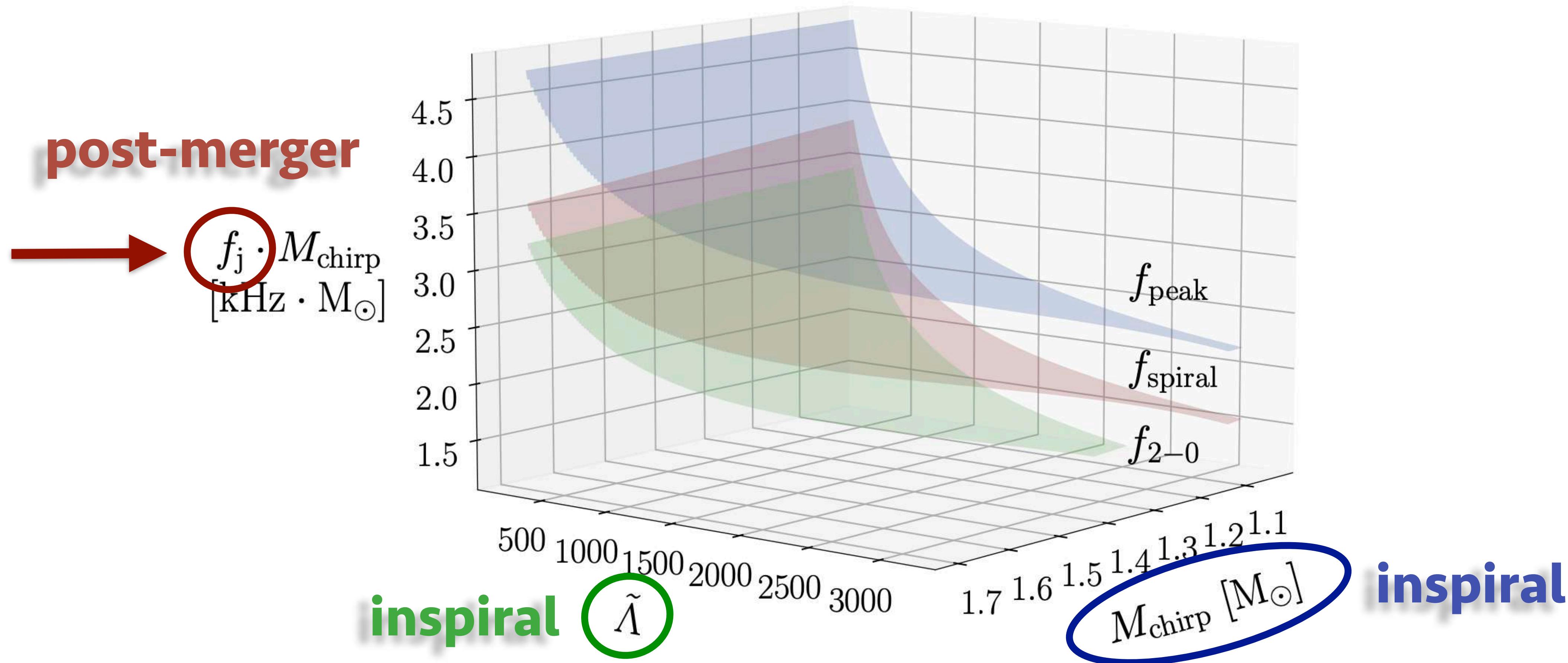
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Vretinaris et al. (2025)



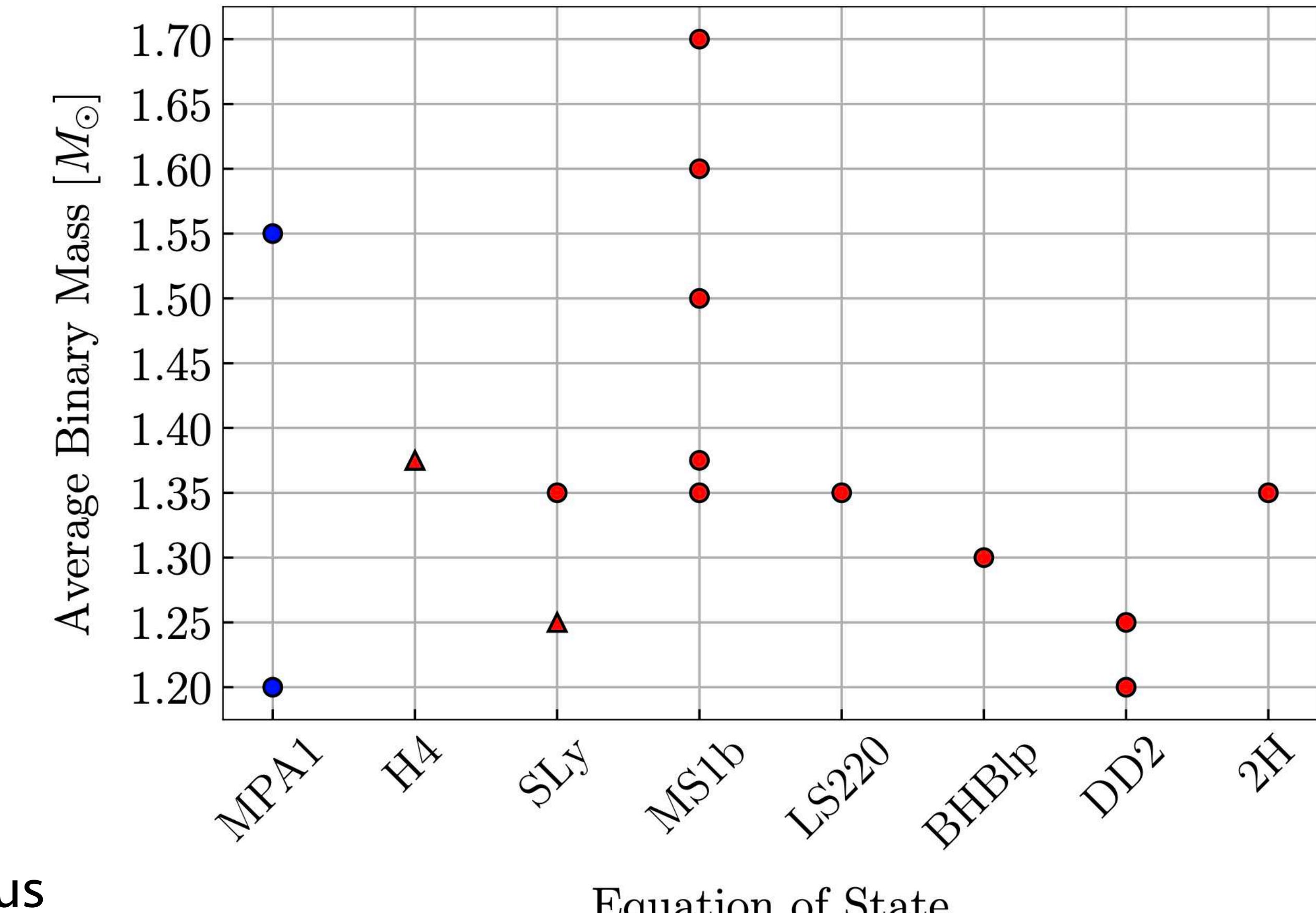
# ACCELERATION OF POST-MERGER INFERENCE

13 numerical waveforms from the CoRe database (Gonzalez et al. 2022)

+2 numerical waveforms from Soultanis, Bauswein & Stergioulas (2022)

Label	EOS	q	(Average) Mass	References
THC:0036:R03	SLy	1.0	1.350	[47]
THC:0019:R05	LS220	1.0	1.350	[101, 102]
BAM:0088:R01	MS1b	1.0	1.500	[99, 100]
THC:0002:R01	BHBlp	1.0	1.300	[101, 102]
THC:0011:R01	DD2	1.0	1.250	[101, 102]
BAM:0070:R01	MS1b	1.0	1.375	[103]
BAM:0065:R03	MS1b	1.0	1.350	[104]
THC:0010:R01	DD2	1.0	1.200	[101, 102]
BAM:0002:R02	2H	1.0	1.350	[104]
BAM:0053:R01	H4	1.5	1.375	[105]
BAM:0124:R01	SLy	1.5	1.250	[103]
BAM:0090:R02	MS1b	1.0	1.600	[99, 100]
BAM:0092:R02	MS1b	1.0	1.700	[99, 100]
Soultanis et al.	MPA1	1.0	1.200	[67]
Soultanis et al.	MPA1	1.0	1.550	[67]

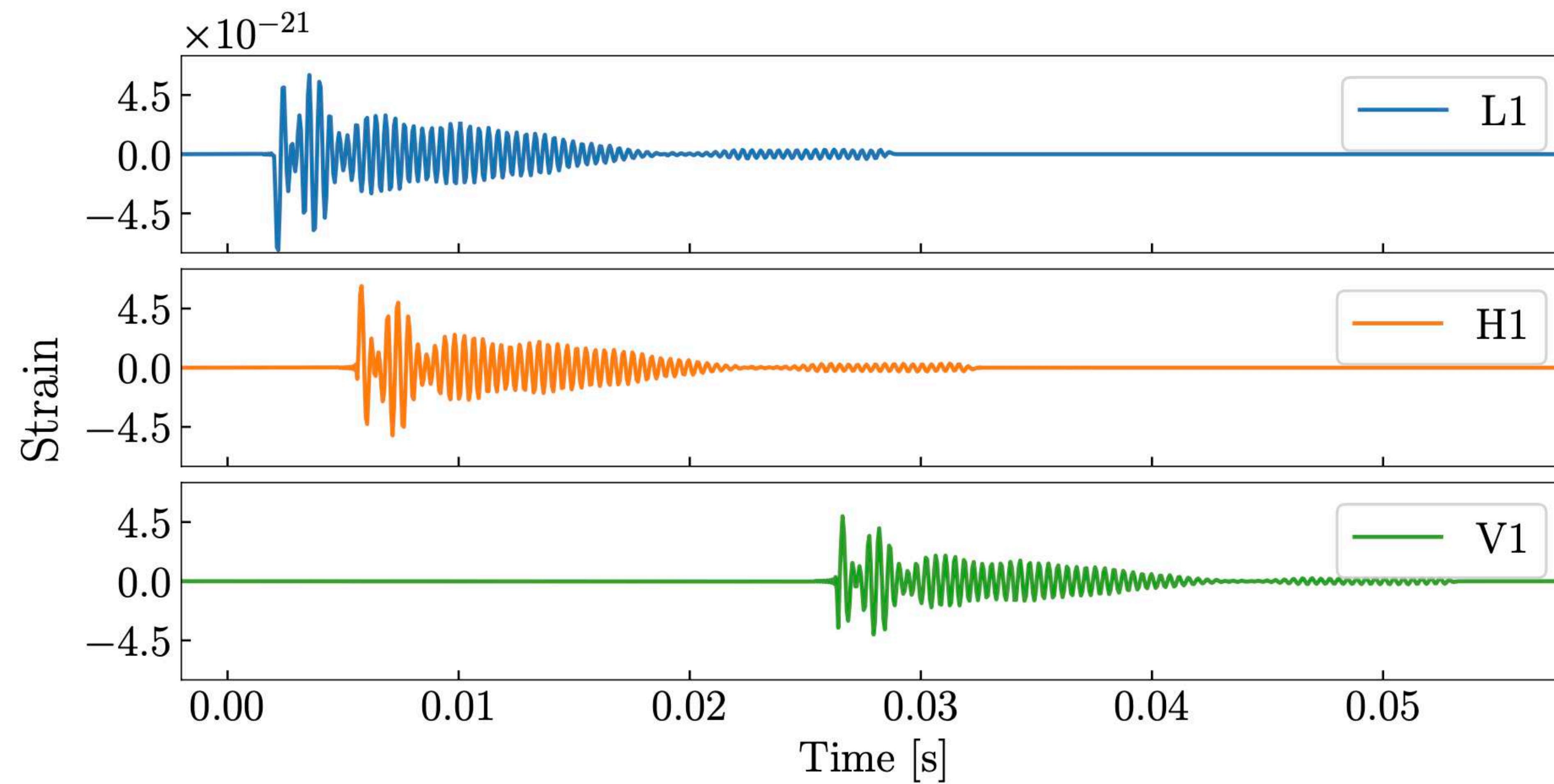
Extension of the set of 9 waveforms used in previous work by Easter et al. (2020)



# INJECTIONS IN 3-DETECTOR NETWORK

Waveforms are injected in 3-detector HLV network at design sensitivity, using BILBY (Ashton et al. 2019)

We choose post-merger SNR of 8, 16 and 50, to simulate detection by 3G network (ET/CE) at distances as close as 200Mpc.



# ANALYTIC BNS POST-MERGER WAVEFORM MODELS

Several analytic models exist in the time- and frequency-domains.

Here, we extend the analytic model of Easter et al. (2020) as follows:

$$\begin{aligned} h(\boldsymbol{\theta}, t) &= h_+(\boldsymbol{\theta}, t) - i h_{\times}(\boldsymbol{\theta}, t) \\ &= \sum_{j=1}^4 [h_{j,+}(\boldsymbol{\theta}, t) - i h_{j,\times}(\boldsymbol{\theta}, t)] \\ h_{j,+}(\boldsymbol{\theta}, t) &= A_j \exp \left[ -\frac{t}{T_j} \right] \cos [2\pi f_j t (1 + a_j t) + \psi_j] \end{aligned}$$

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Intrinsic parameters  $\boldsymbol{\theta} = \{A_j, T_j, f_j, a_j, \psi_j\}$  for  $j \in [1, 4]$

$h_{j,\times}(\boldsymbol{\theta}, t)$  is obtained by applying a  $\pi/2$  phase shift to  $h_{j,+}(\boldsymbol{\theta}, t)$

- We have added a 4th oscillator at high frequencies  $> f_{\text{peak}}$  (e.g.  $f_{2+0}$ )
- Amplitudes  $A_j$  are free parameters

# INFORMED PRIORS

In Easter et al. (2020) flat priors in a wide frequency range of 1-5 kHz for every oscillator were used.

- Here, we take advantage of the empirical relations to set Gaussian priors in a narrow frequency range around each expected frequency.
- In addition, the priors differ, according to the type of the post-merger waveform:
  - Type I: Gaussian priors,  $\mathcal{N}(f_{2-0}, \sigma^2)$  for  $f_{2-0}$  and uniform priors  $\mathcal{U}(1, 5)[\text{kHz}]$  for  $f_{\text{spiral}}$ .
  - Type II: Gaussian priors,  $\mathcal{N}(f_{2-0}, \sigma^2)$  for  $f_{2-0}$  and  $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$  for  $f_{\text{spiral}}$ .
  - Type III: Gaussian priors,  $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$  for  $f_{\text{spiral}}$  and uniform priors  $\mathcal{U}(1, 5)[\text{kHz}]$  for  $f_{2-0}$ .

where  $\sigma = 3 \times \text{max error of empirical relations}$ . For  $f_{\text{peak}}$ : Gaussian ; for  $f_4$ : flat in  $[f_{\text{peak}} + 0.3\text{kHz}, 5\text{kHz}]$ .

priors for  $A_j$ : uniform in [-24, -19]

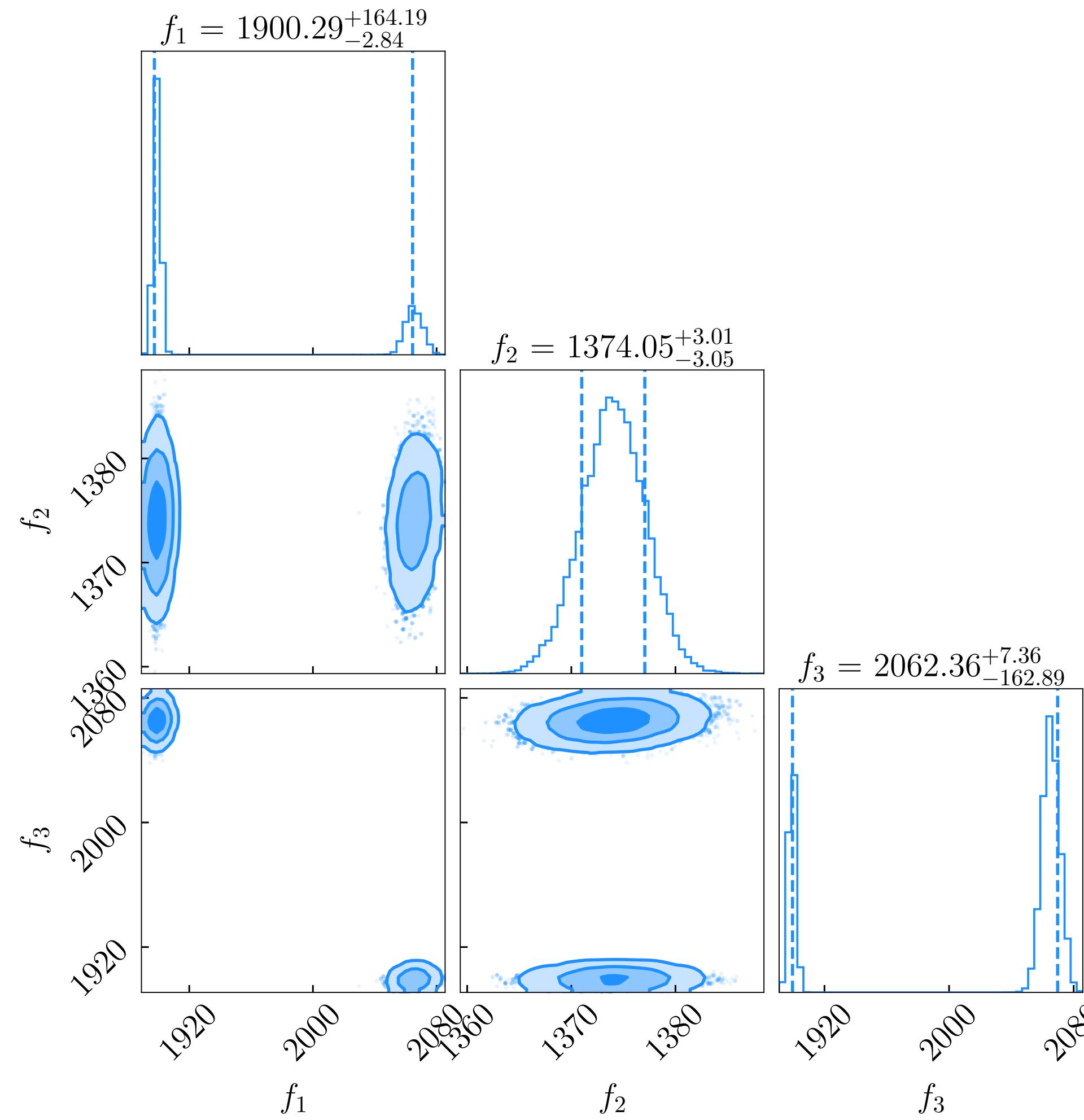
priors for  $a_j$ : uniform in [-6.4, 6.4]

priors for remaining parameters: as in Easter et al. (2020)

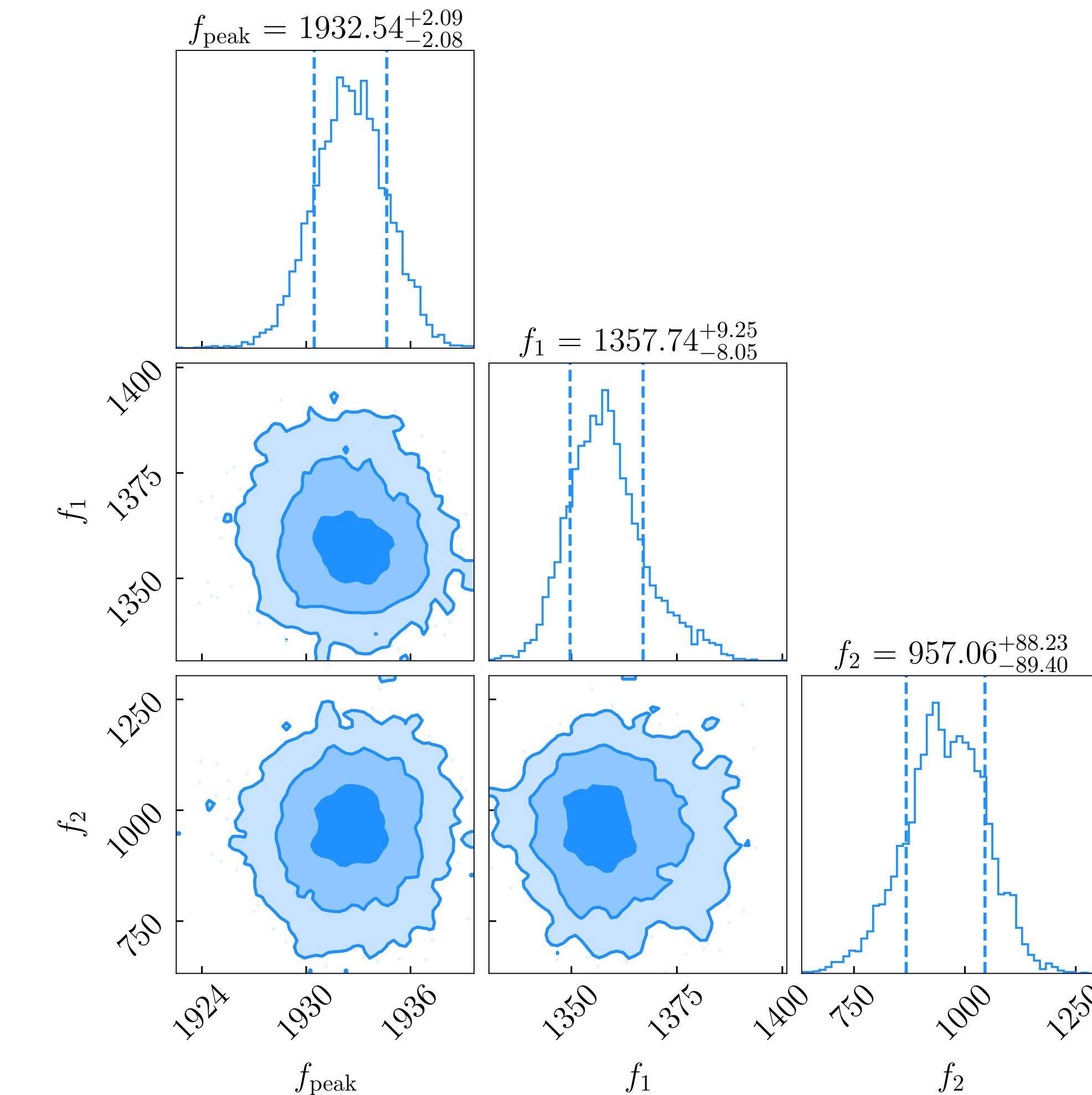
# POSTERIOR DISTRIBUTIONS

EOS 2H 1.35+1.35, SNR = 50

**using flat priors**



**using informed priors (through empirical relations)**

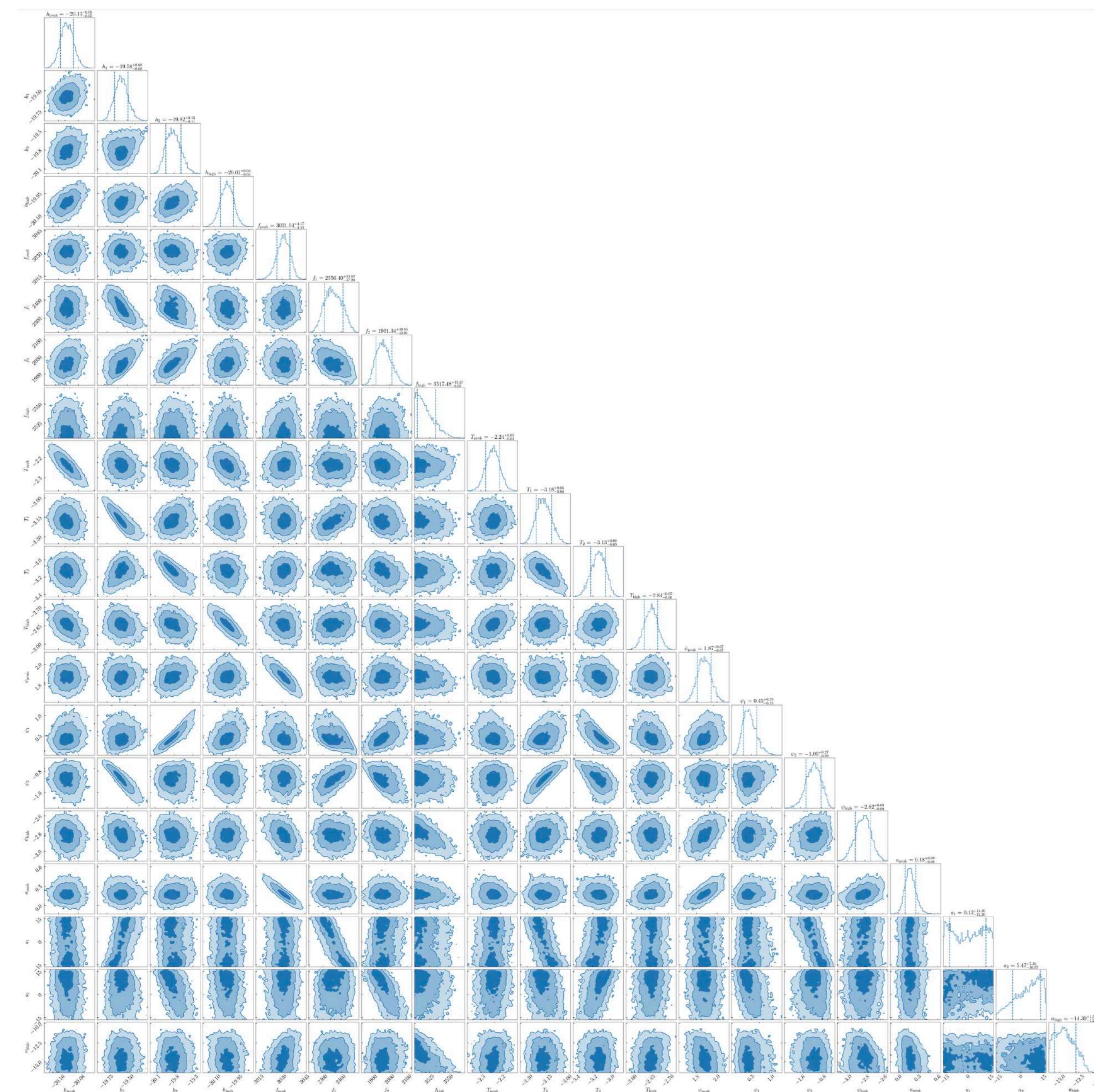


# POSTERIOR DISTRIBUTIONS

EOS MPA 1.55+1.55, SNR = 50

using informed priors

**all parameters**



# POCOMC: PRECONDITIONED MONTE CARLO SAMPLER

**Preconditioned Monte Carlo Sampling** (Karamanis et al. 2022)

PMC targets an **annealed version of the posterior**, with density given by

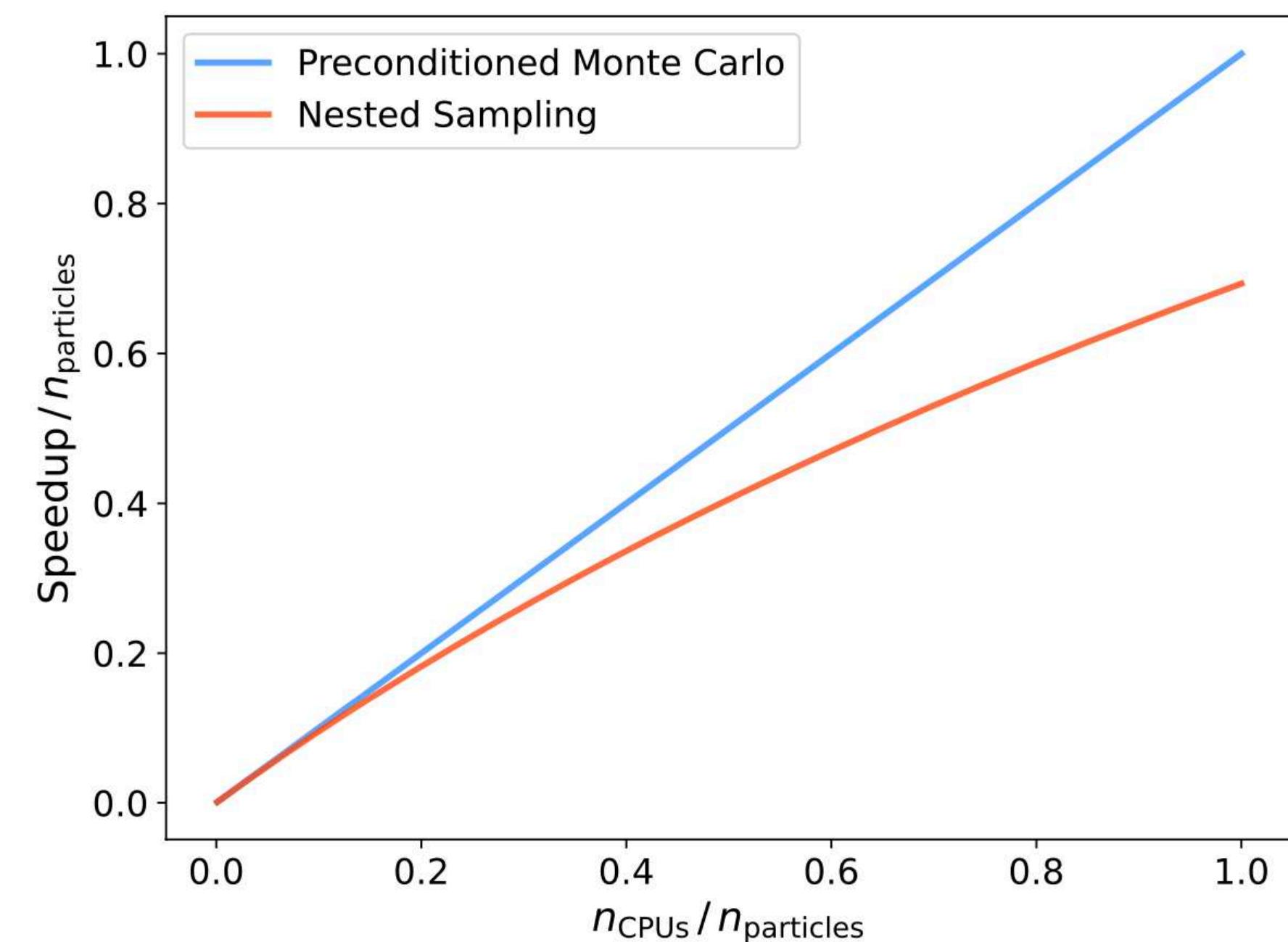
$$p_t(\boldsymbol{\theta} \mid d) \propto \mathcal{L}^{\beta_t}(\boldsymbol{\theta} \mid d)\pi(\boldsymbol{\theta})$$

where  $\beta_t$  a parameter (inverse temperature).

We use 2000 particles that transition from the prior ( $\beta_0 = 0$ ) to the posterior distribution ( $\beta_T = 1$ ), through a sequence of reweighting, resampling and mutation steps.



<https://github.com/minaskar/pocomc>



PocoMC is highly parallelizable

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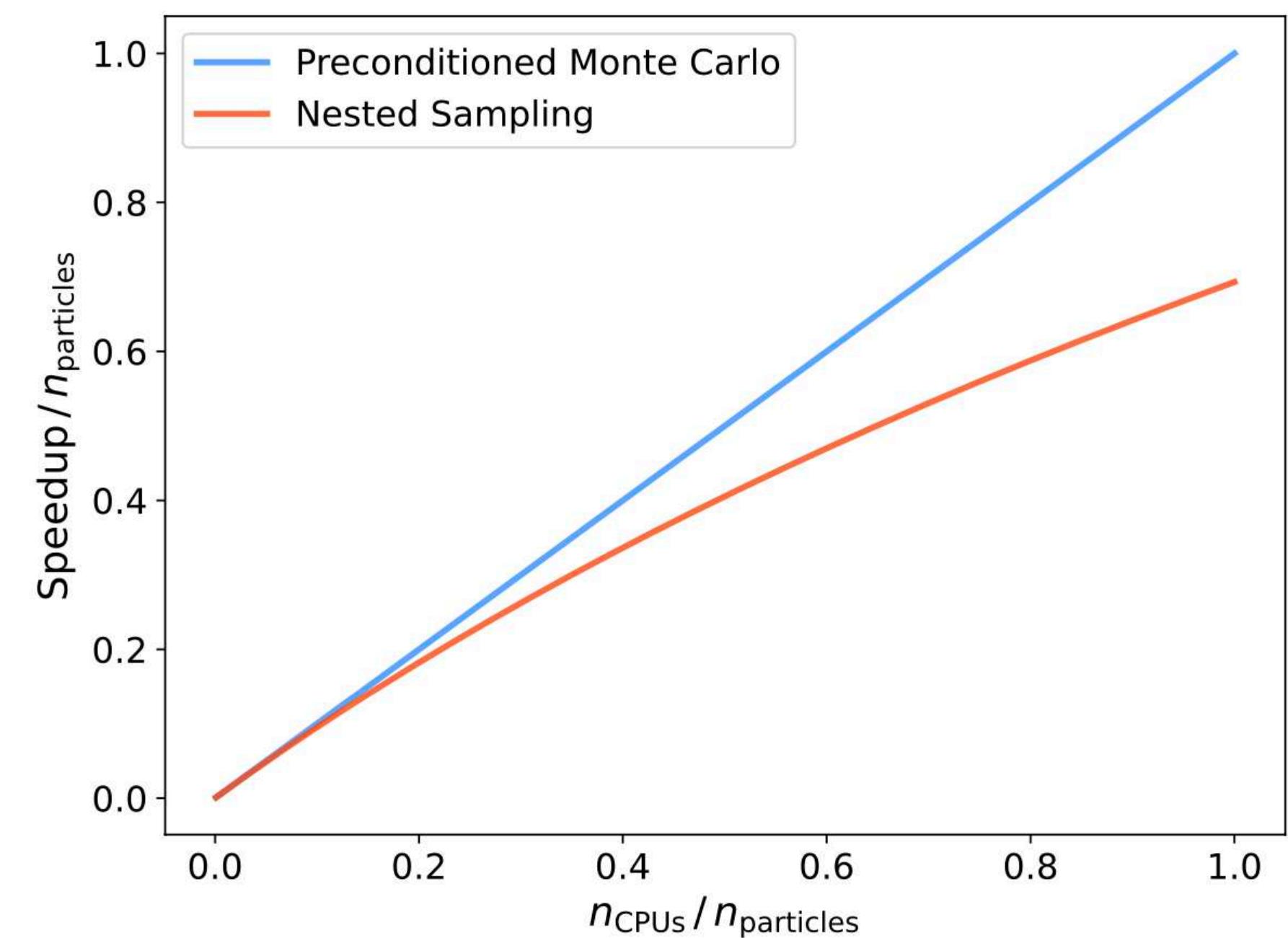
We use 2000 particles that **transition from the prior ( $\beta_0 = 0$ ) to the posterior distribution ( $\beta_T = 1$ )**, through a sequence of reweighing, resampling and mutation steps.

After each iteration, a **normalizing flow** transforms the distribution to a simpler one (almost Gaussian), decorrelating the parameters. This allows for a much faster sampling.

On same number of CPUs: pocoMC is **~10 times faster** than dynesty.

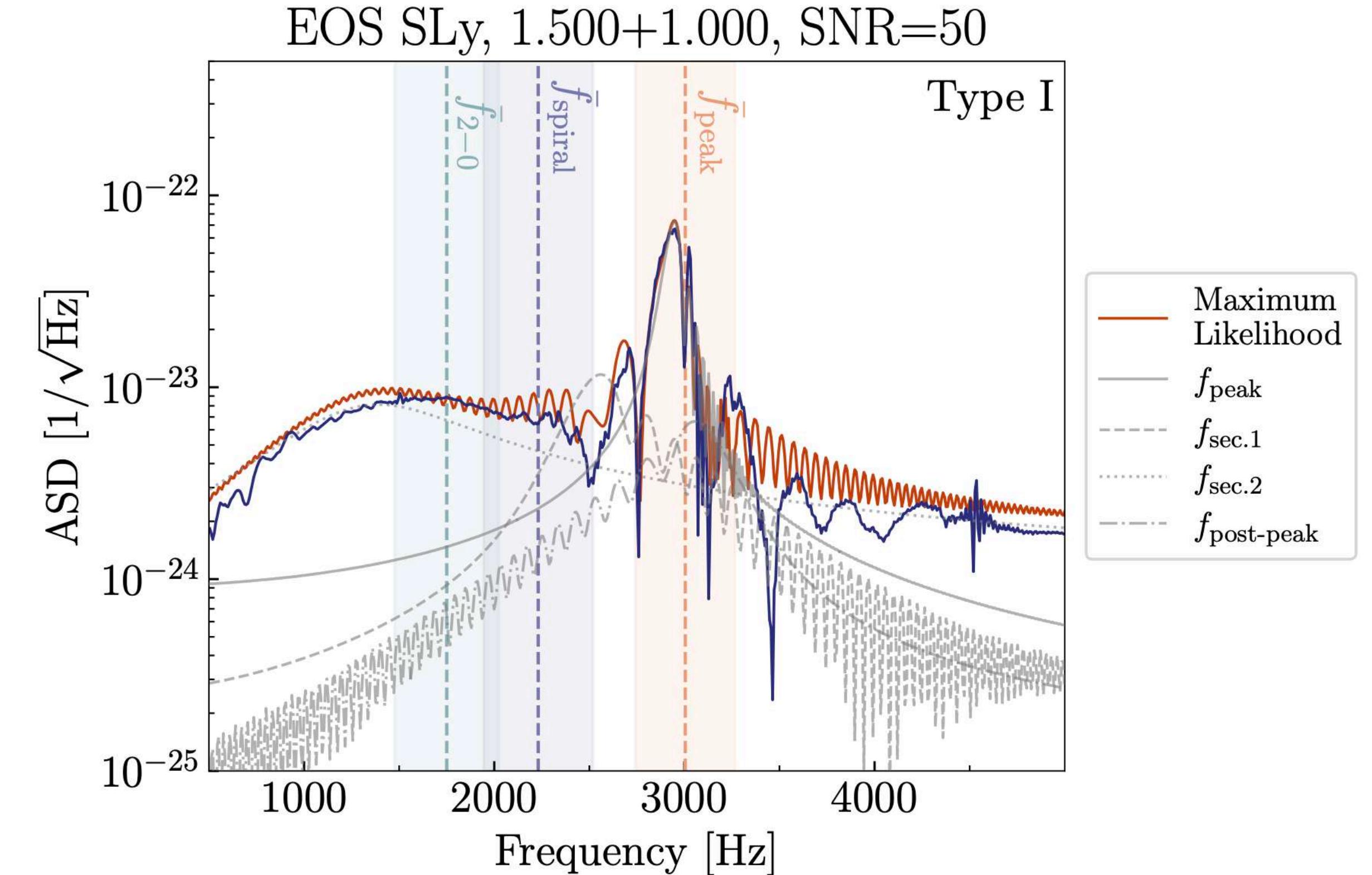
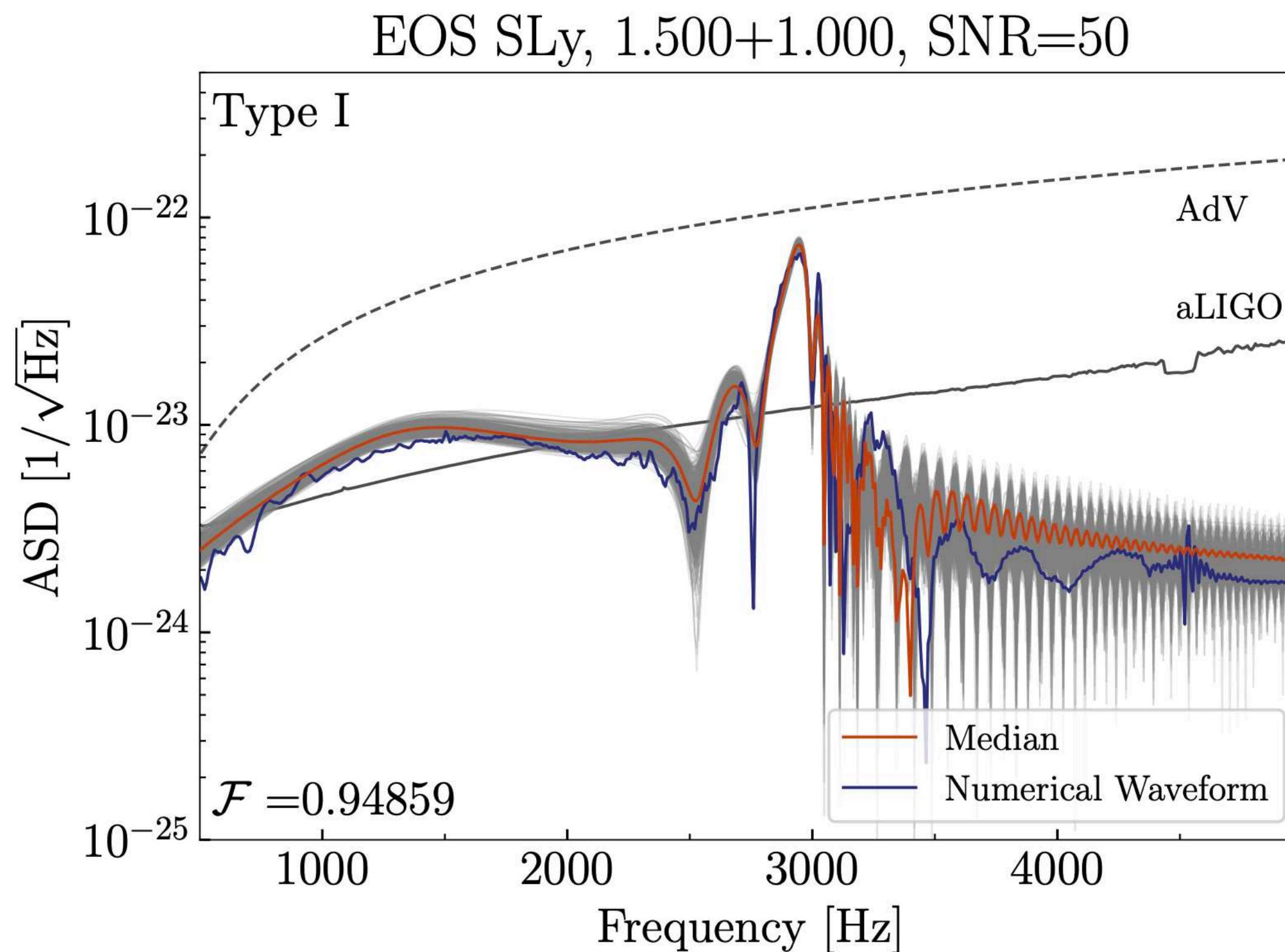


<https://github.com/minaskar/pocomc>



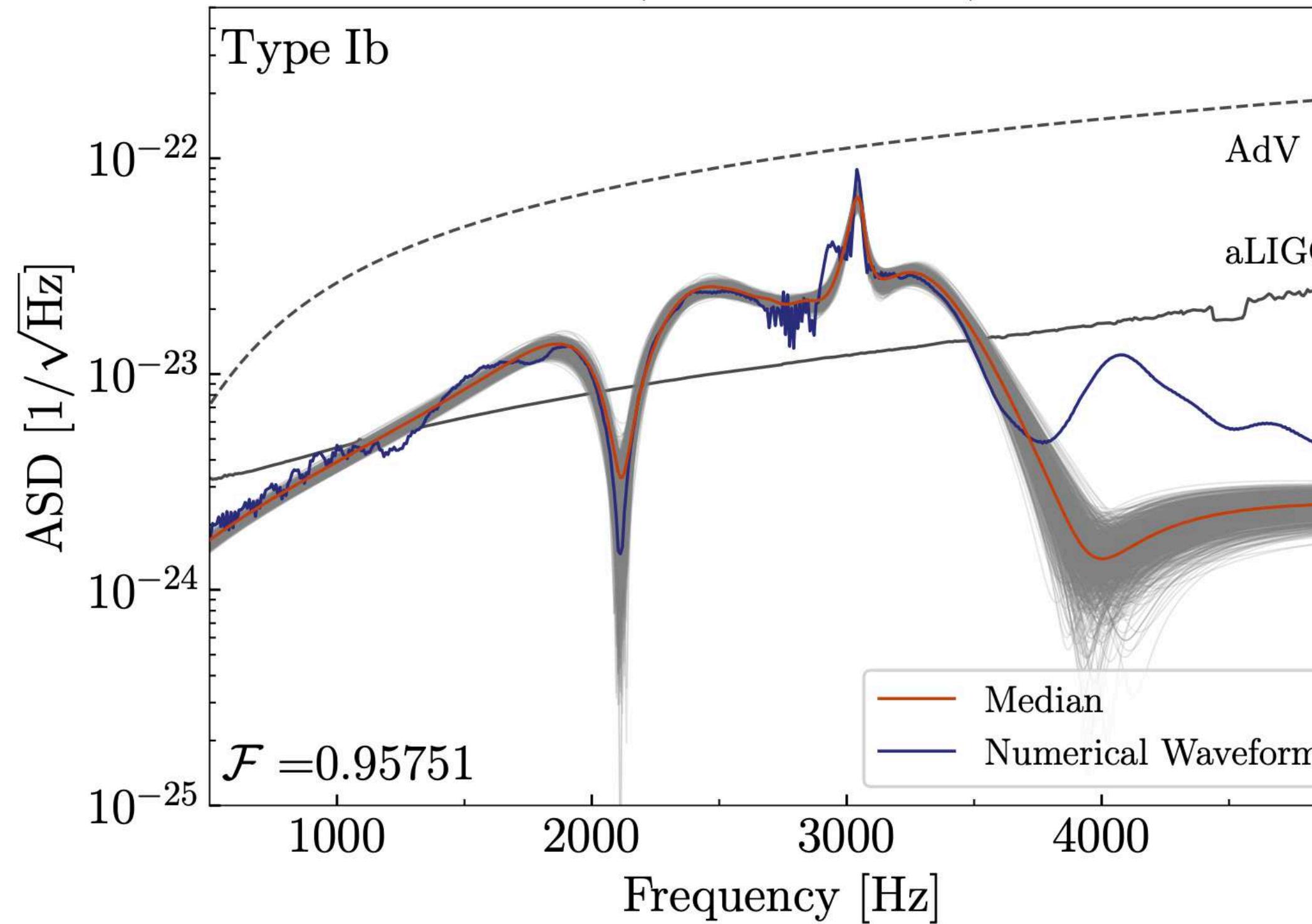
PocoMC is highly parallelizable

# RECONSTRUCTION IN THE FREQUENCY DOMAIN

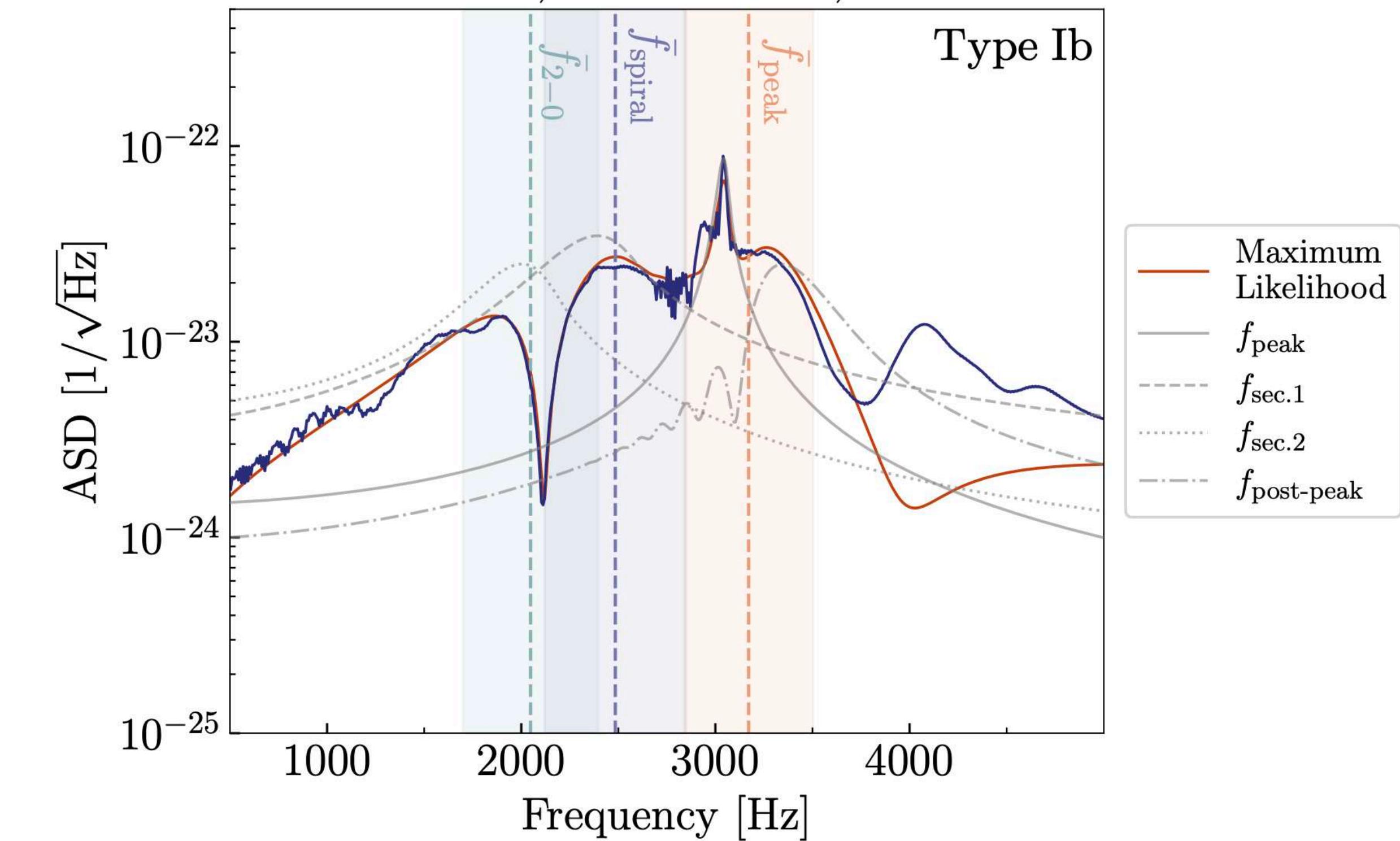


# RECONSTRUCTION IN THE FREQUENCY DOMAIN

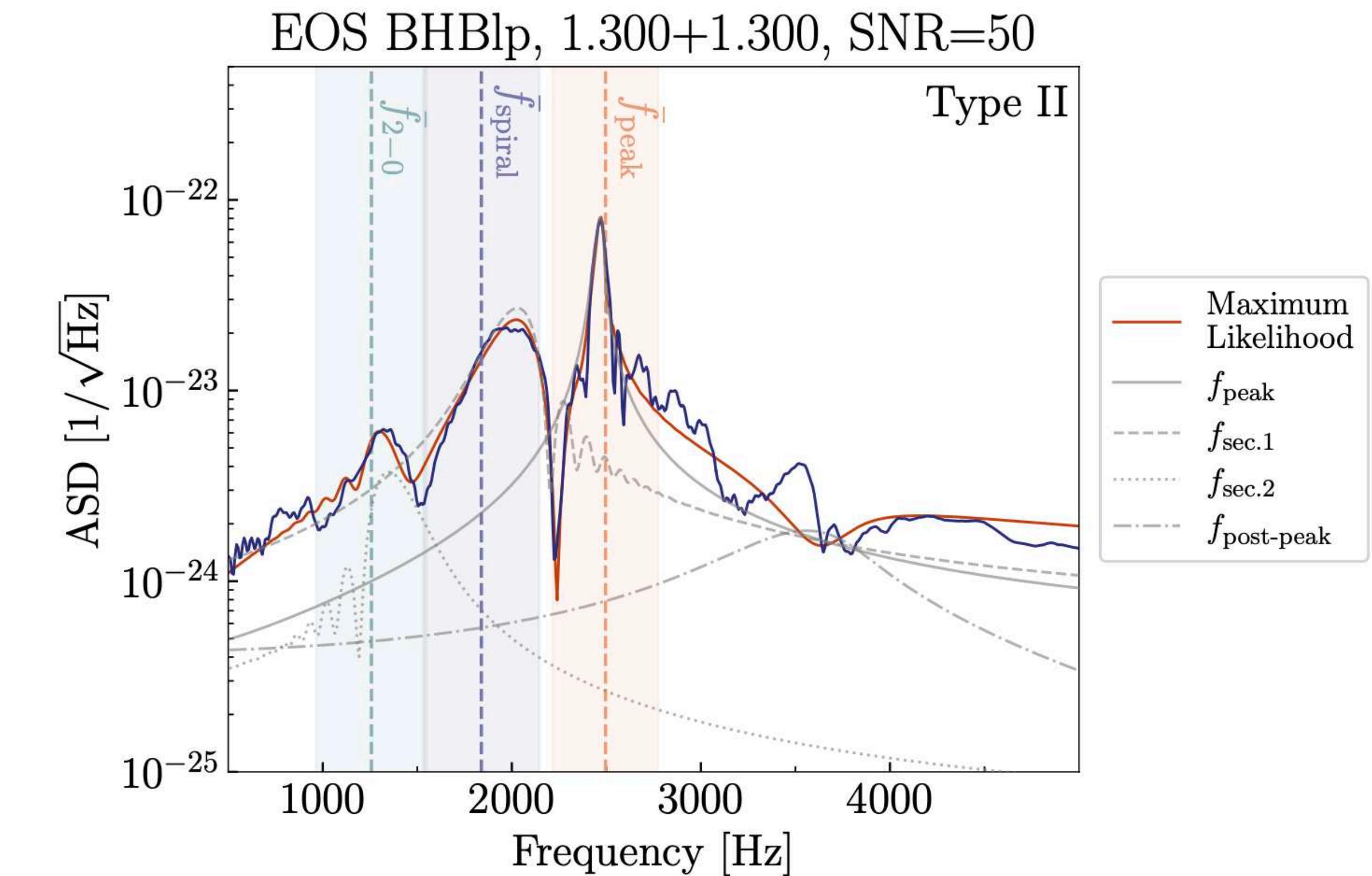
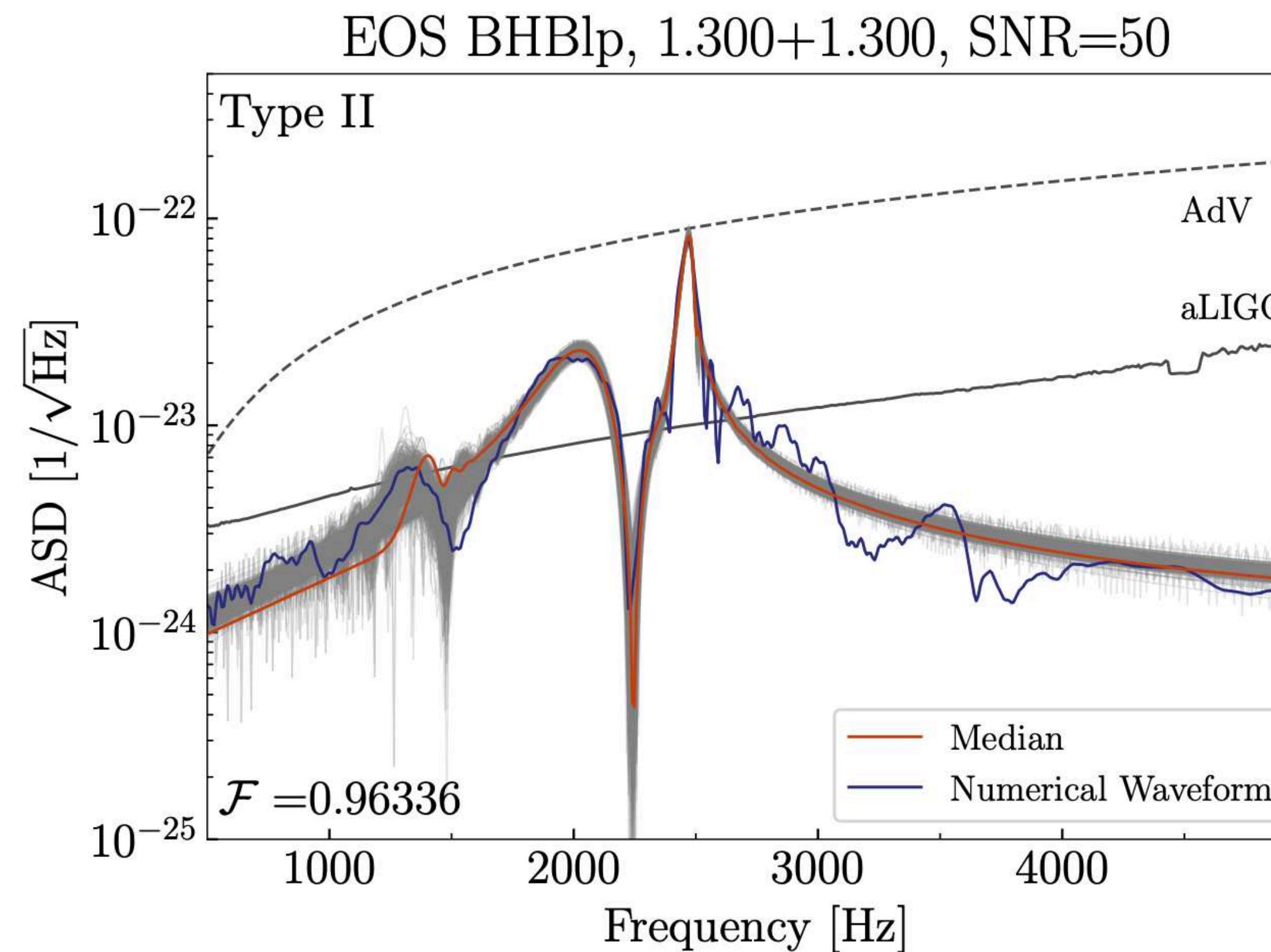
EOS MPA1, 1.550+1.550, SNR=50



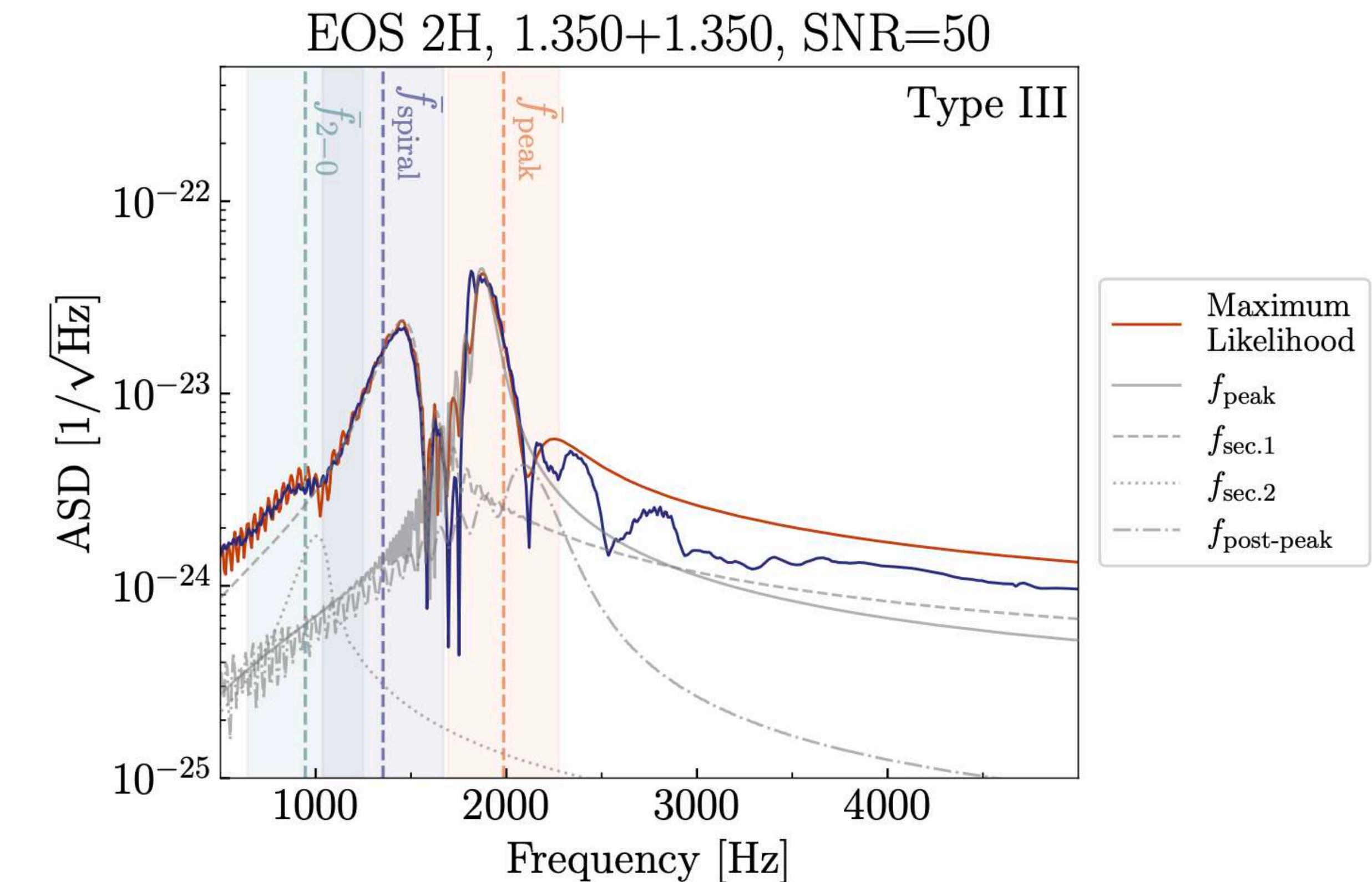
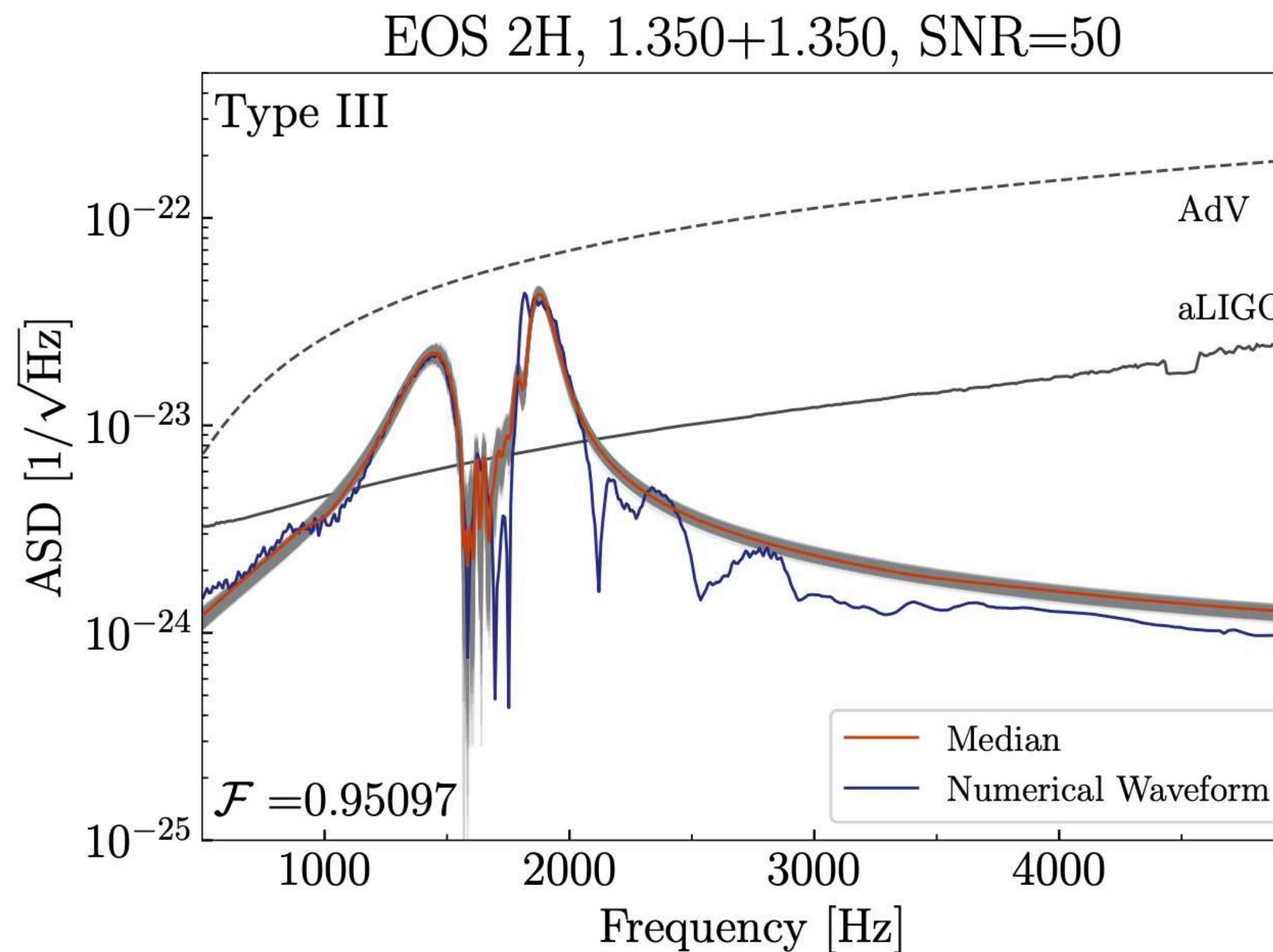
EOS MPA1, 1.550+1.550, SNR=50



# RECONSTRUCTION IN THE FREQUENCY DOMAIN



# RECONSTRUCTION IN THE FREQUENCY DOMAIN

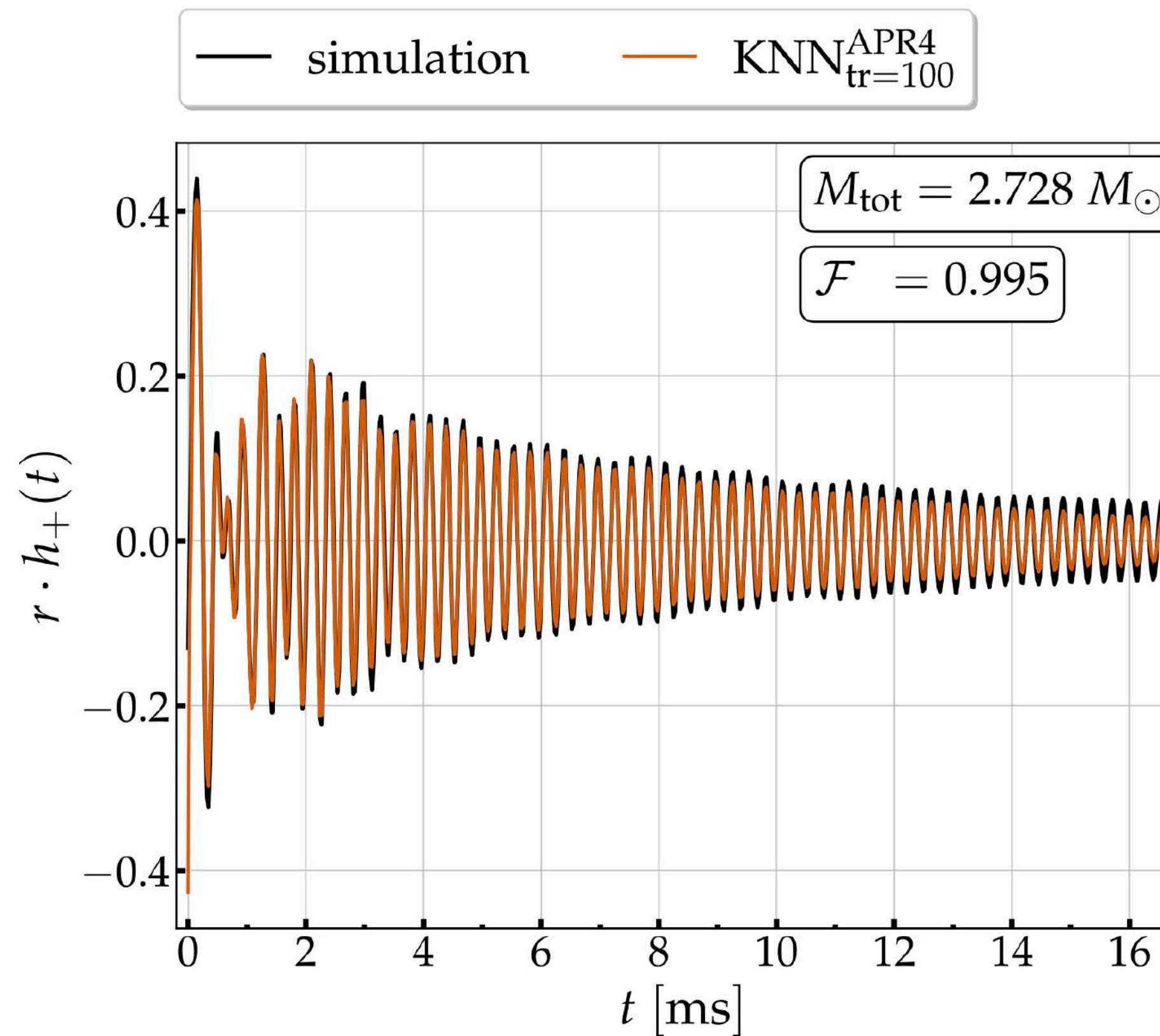


# APPLICATION OF MACHINE LEARNING TO THE POST-MERGER PHASE

**Problem:** Only  $O(200)$  substantially different numerical BNS simulations are currently available.

**Solution:** Construct surrogate model of post-merger GWs as function of e.g.  $M$ ,  $q$ ,  $\text{EOS}(\Lambda)$

**Time domain surrogate** model using  
**K-Nearest Neighbor (KNN) regression:**

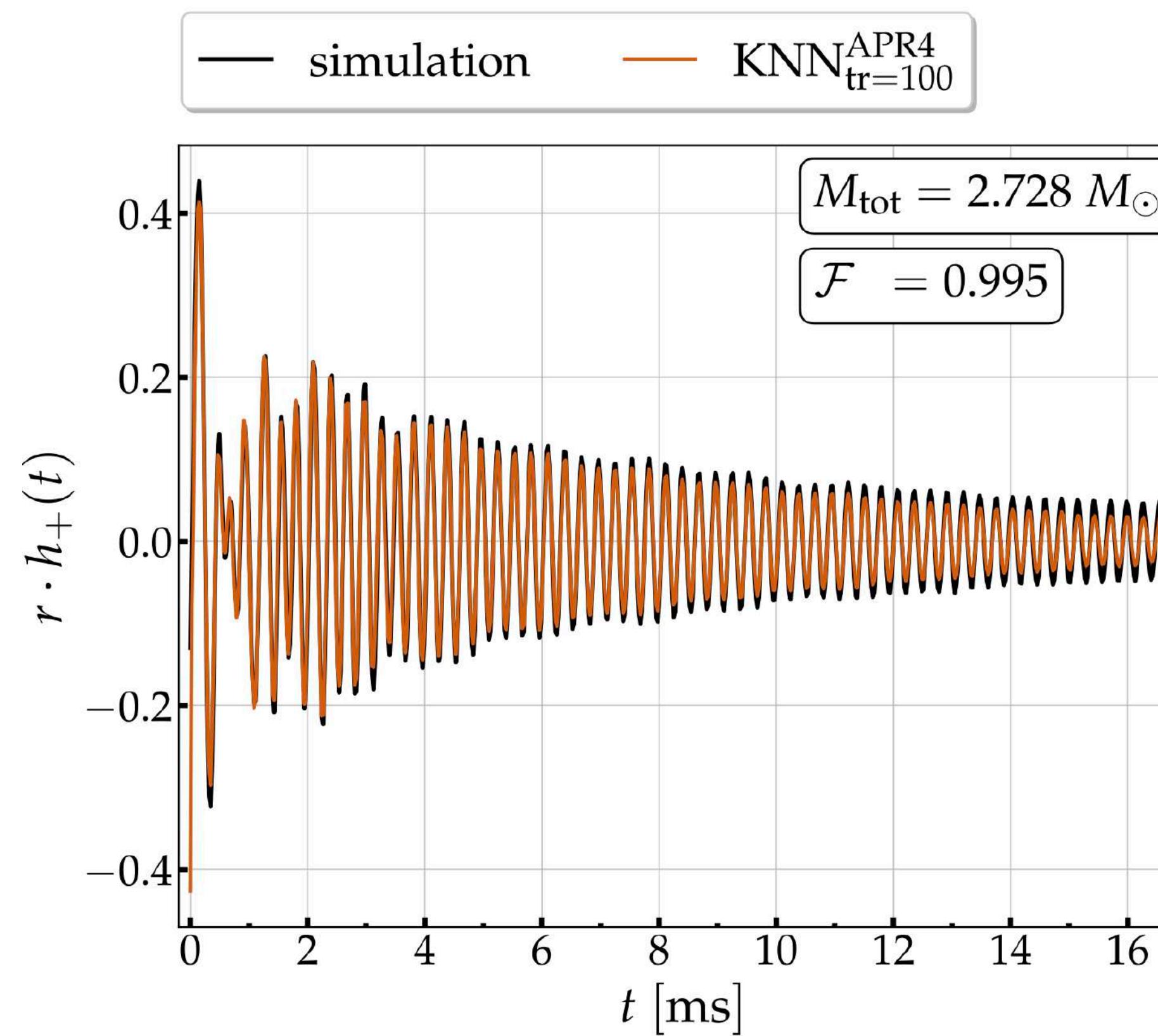


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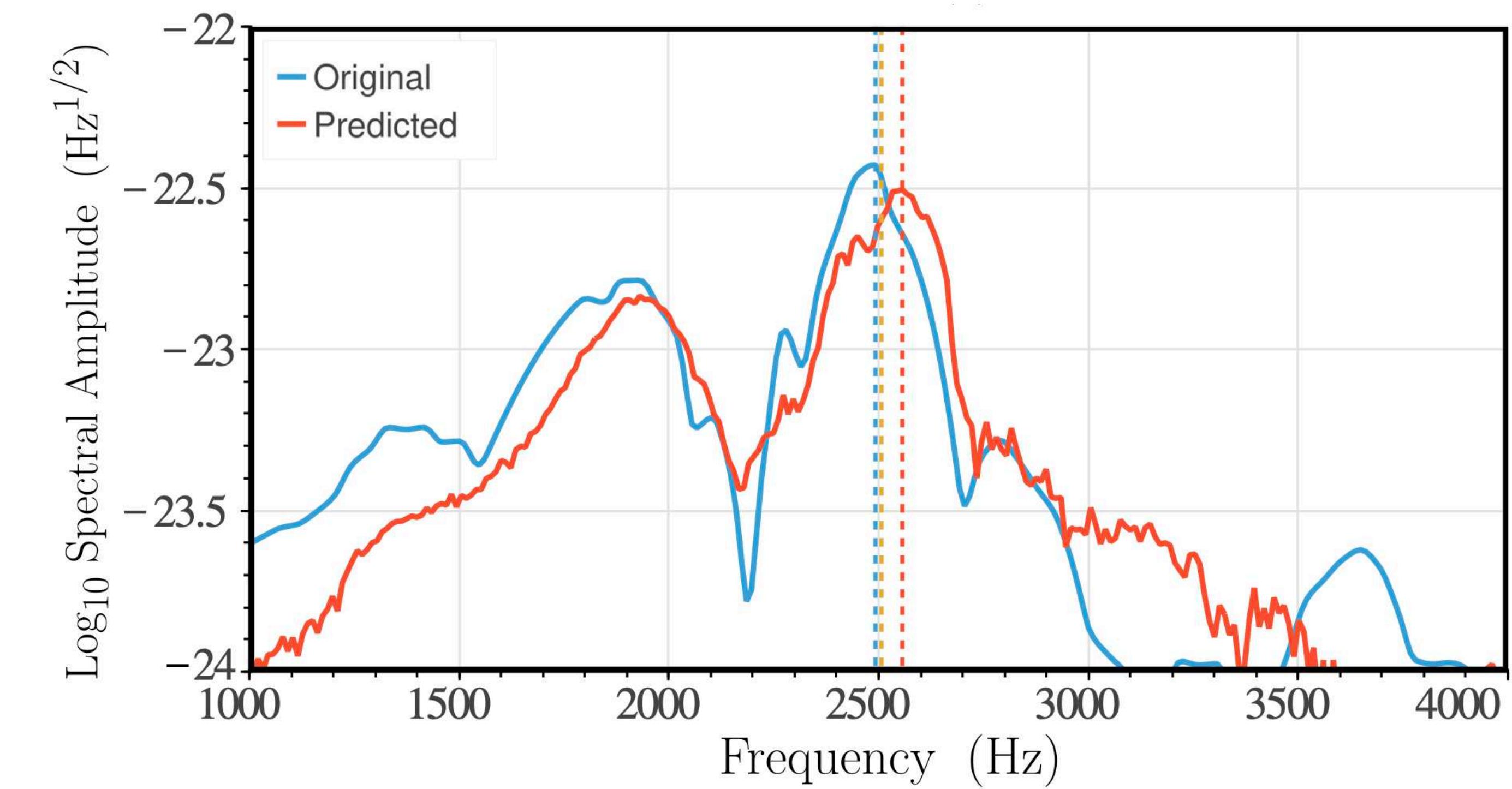
**Solution:** Construct surrogate model of post-merger GWs as function of e.g.  $M$ ,  $q$ ,  $\text{EOS}(\Lambda)$

**Time domain surrogate** model using  
K-Nearest Neighbor (KNN) regression:



Soultanis et al. (2025)

**Frequency domain surrogate** model using  
Artificial Neural Networks (ANN) regression:



Pesios et al. (2024)

# K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

**Training set:** 20-100 different  $M_{\text{tot}}$  ( $q=1$ ) between 2.4 and 2.8  $M_{\text{sun}}$ .

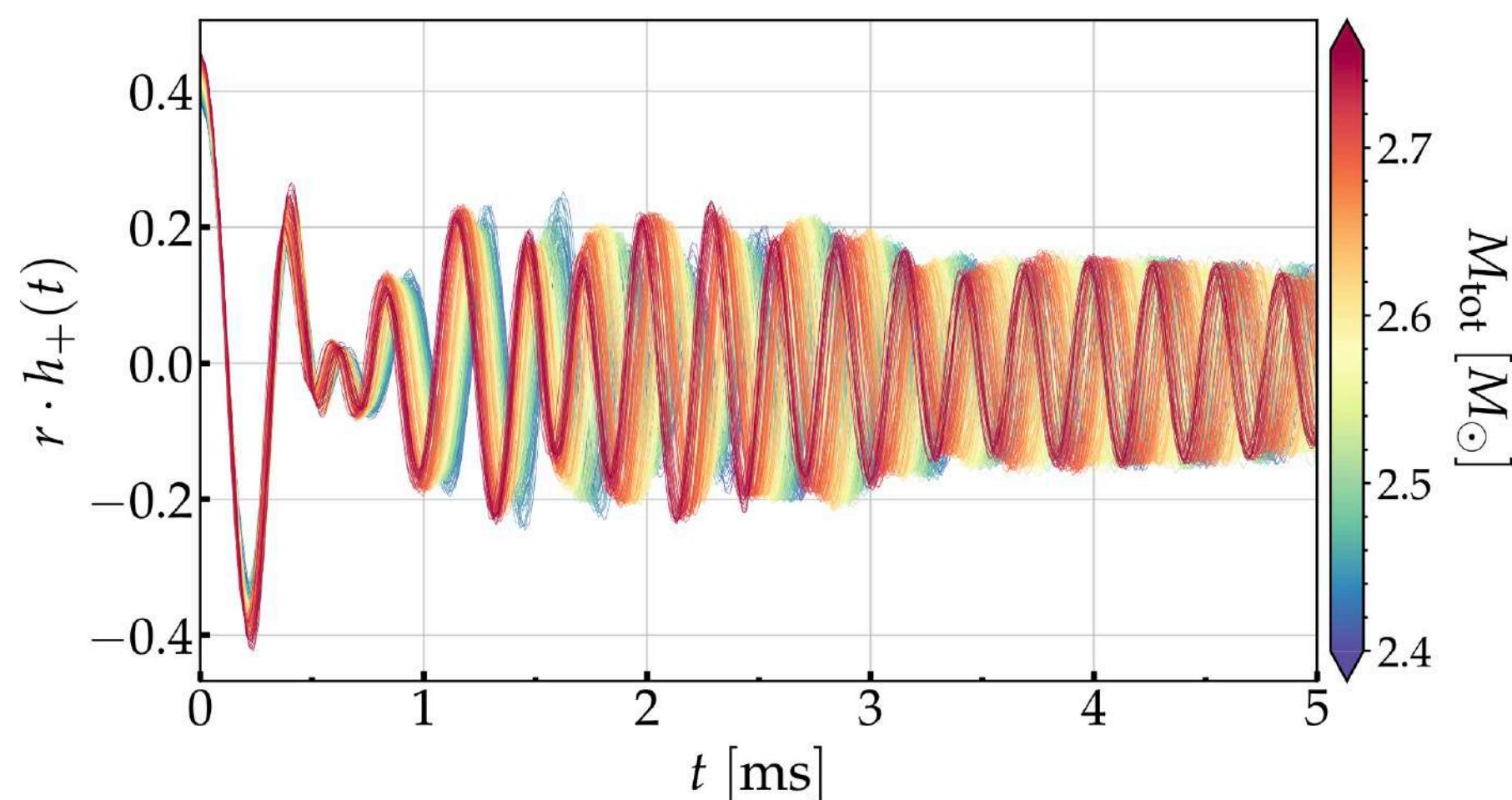
Choose specific EOS (APR4; SFHX).

Complex GW strain:

$$h(t) = h_+(t) + i h_\times(t)$$

$$= |h(t)| \cdot e^{+i\phi(t)},$$

**Signals are aligned at merger time:**



# K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

**Training set:** 20-100 different  $M_{\text{tot}}$  ( $q=1$ ) between 2.4 and 2.8  $M_{\odot}$ .

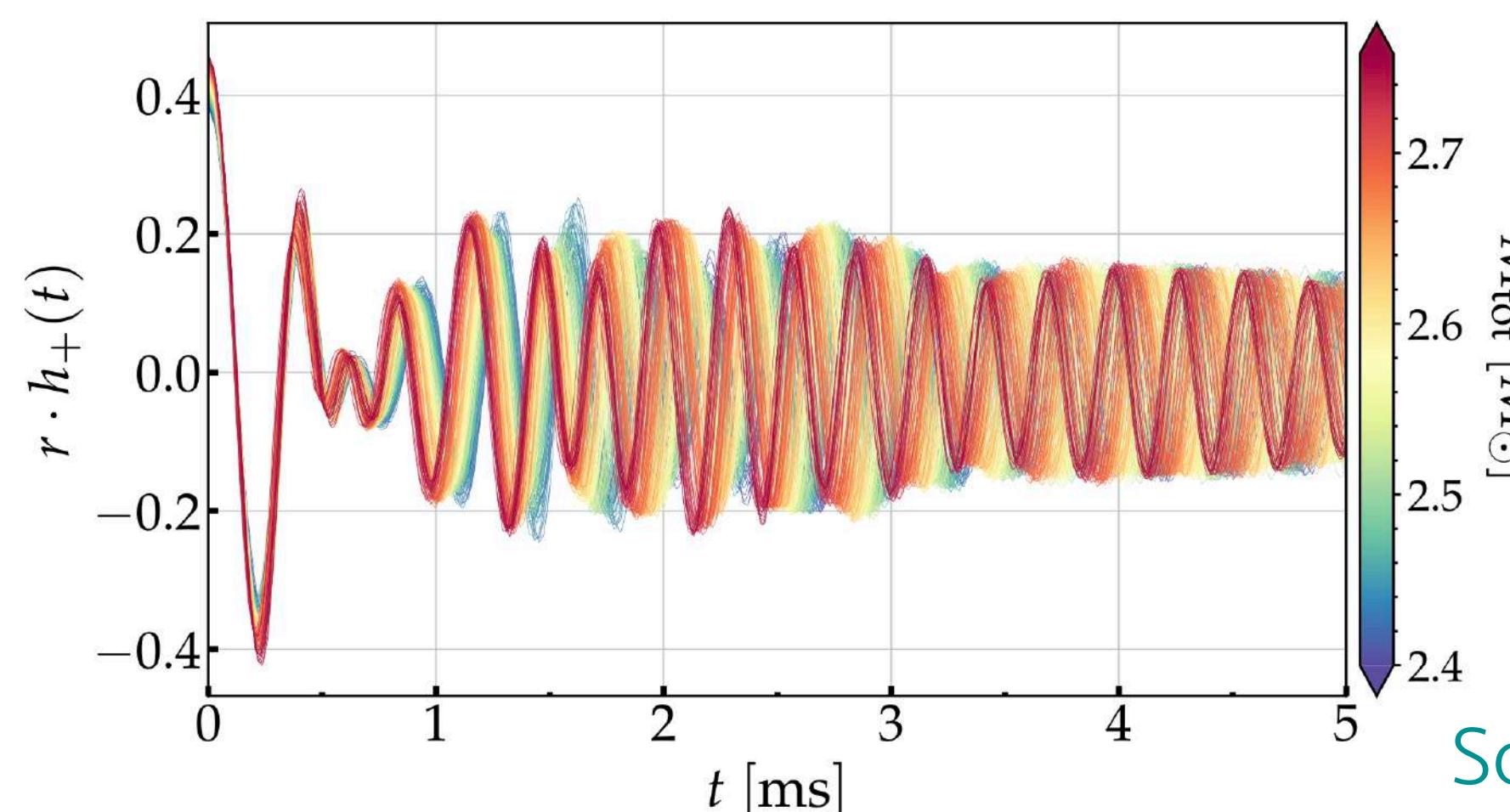
Choose specific EOS (APR4; SFHX).

Complex GW strain:

$$h(t) = h_+(t) + i h_\times(t)$$

$$= |h(t)| \cdot e^{+i\phi(t)},$$

**Signals are aligned at merger time:**



**Input features:**

$$\vec{X}_i = \{M_{\text{tot}}, t_j\}$$

**Predictions:**

$$\vec{Y}_i = \text{strain data}$$

**KNN algorithm:**

For given input  $\vec{X}_0$ , find set  $N_0$  of K nearest neighbors

The prediction is a weighted average

$$\vec{Y}_0 = \frac{1}{K} \sum_{\vec{X}_i \in N_0} \frac{w_i \cdot \vec{Y}_i}{W}, \quad \text{where } W = \sum_{\vec{X}_i \in N_0} w_i$$

and  $w_i = 1/d_i$  where  $d_i$  is the distance between  $\vec{X}_0$

and  $\vec{X}_i$ .

**Hyperparameters:**  $K$  and  $w_i$

(tuned to optimal choices using a validation set)

# K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

**Noise-weighted inner product for two signals:**

$$\langle h_1(t), h_2(t) \rangle \equiv 4 \operatorname{Re} \int_0^\infty df \frac{\tilde{h}_1(f) \cdot \tilde{h}_2^*(f)}{S_h(f)}$$

**Overlap:**

$$\mathcal{O} \equiv \frac{\langle h_1(t), h_2(t) \rangle}{\sqrt{\langle h_1(t), h_1(t) \rangle \langle h_2(t), h_2(t) \rangle}}$$

**Faithfulness (maximized overlap)**

$$\mathcal{F} \equiv \max_{\phi_0, t_0} \frac{\langle h_1(t), h_2(t) \rangle}{\sqrt{\langle h_1(t), h_1(t) \rangle \langle h_2(t), h_2(t) \rangle}}$$

# K-NEAREST NEIGHBOR REGRESSION IN THE TIME DOMAIN

**Noise-weighted inner product for two signals:**

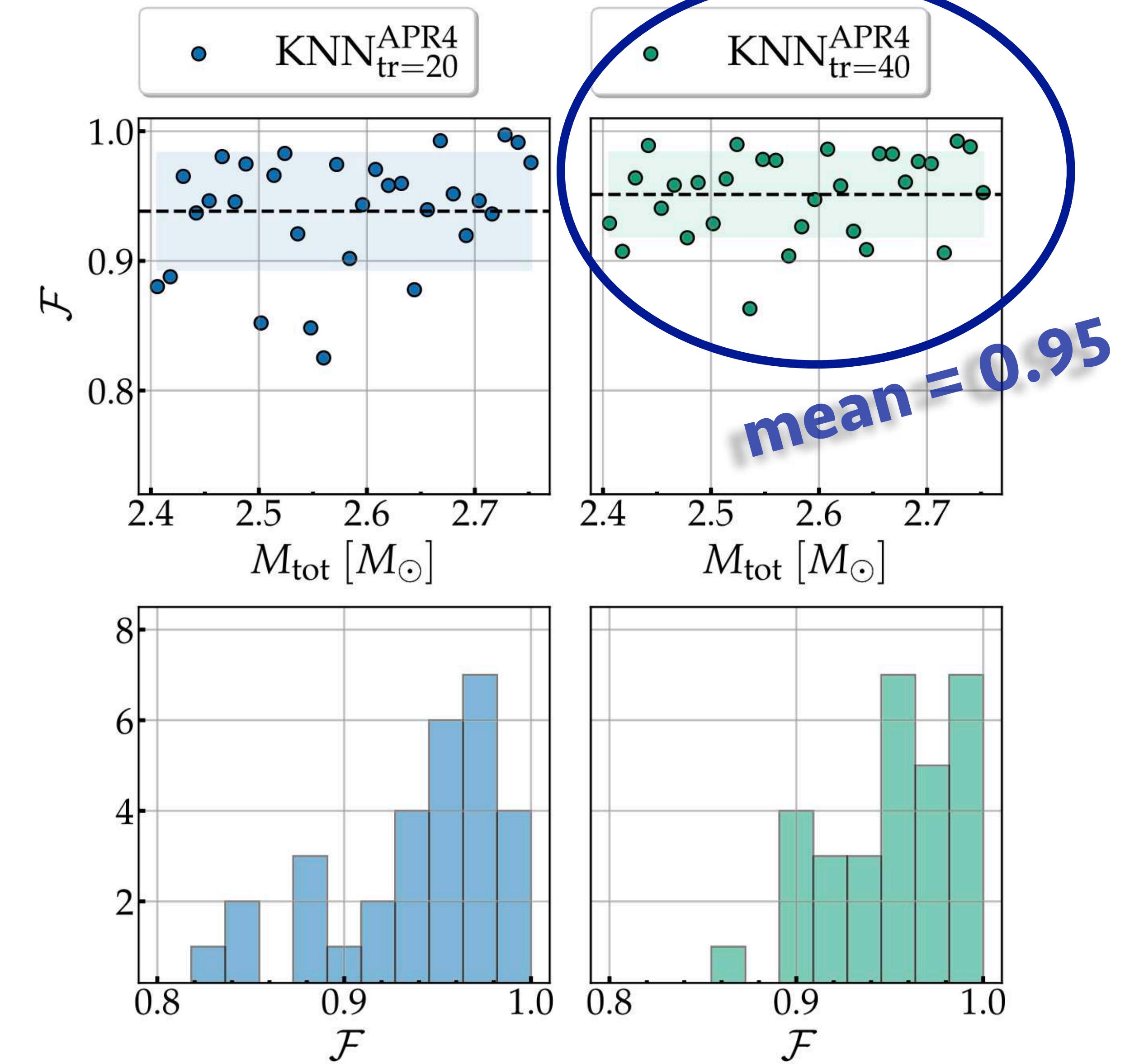
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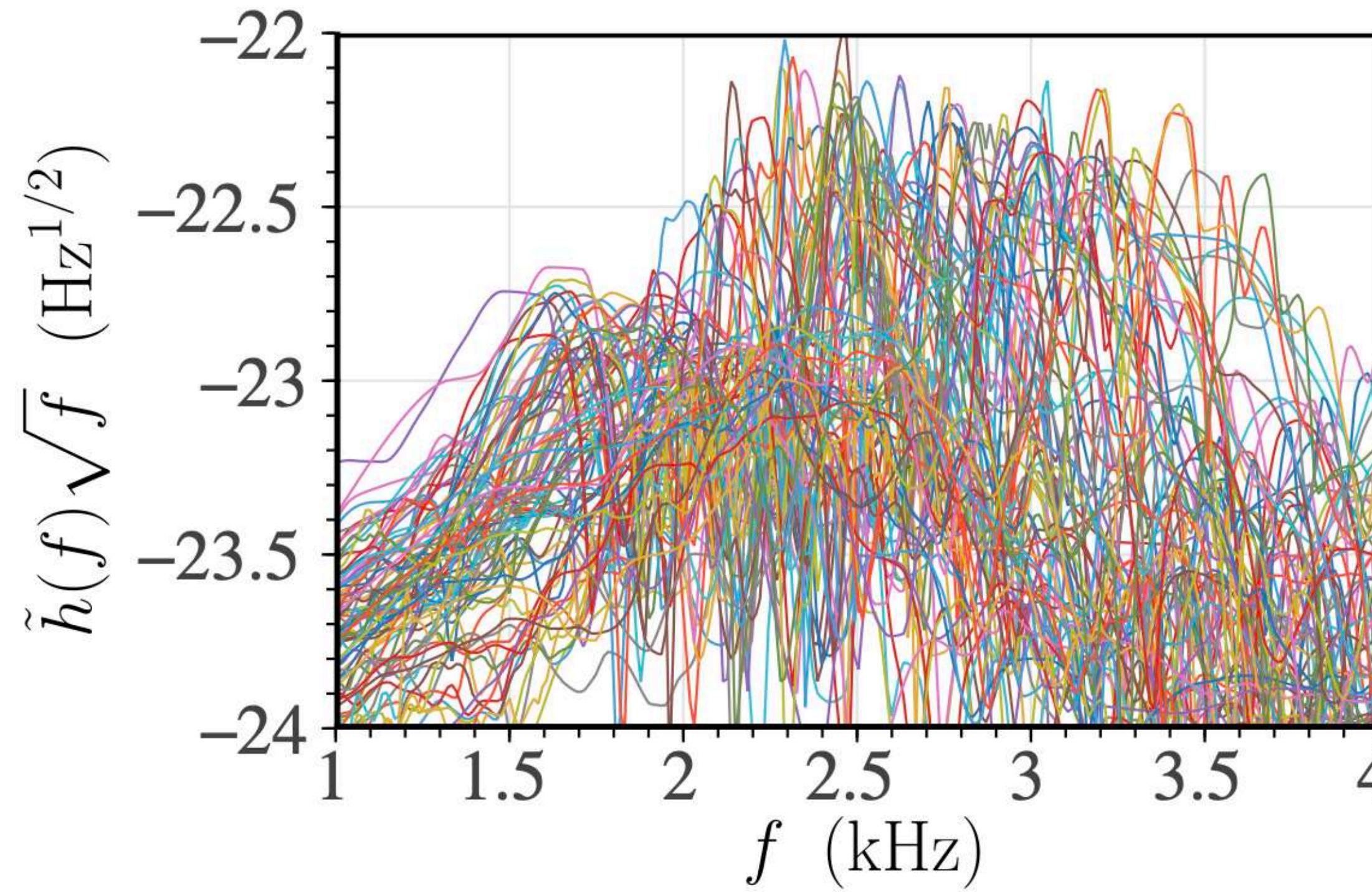
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# ANN REGRESSION IN THE FREQUENCY DOMAIN

**Expanded training set:** 87 equal-mass models using 14 different EOS

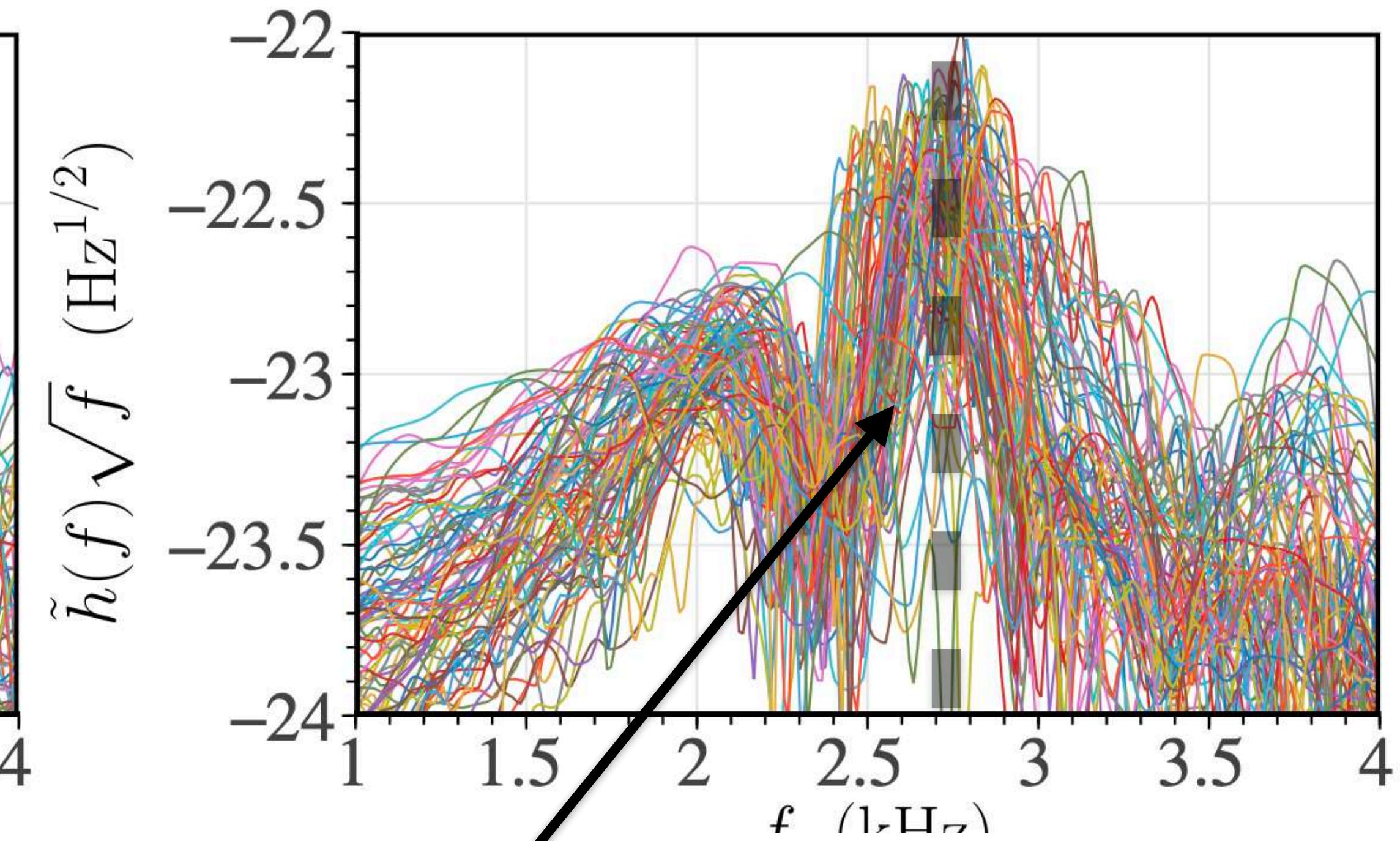
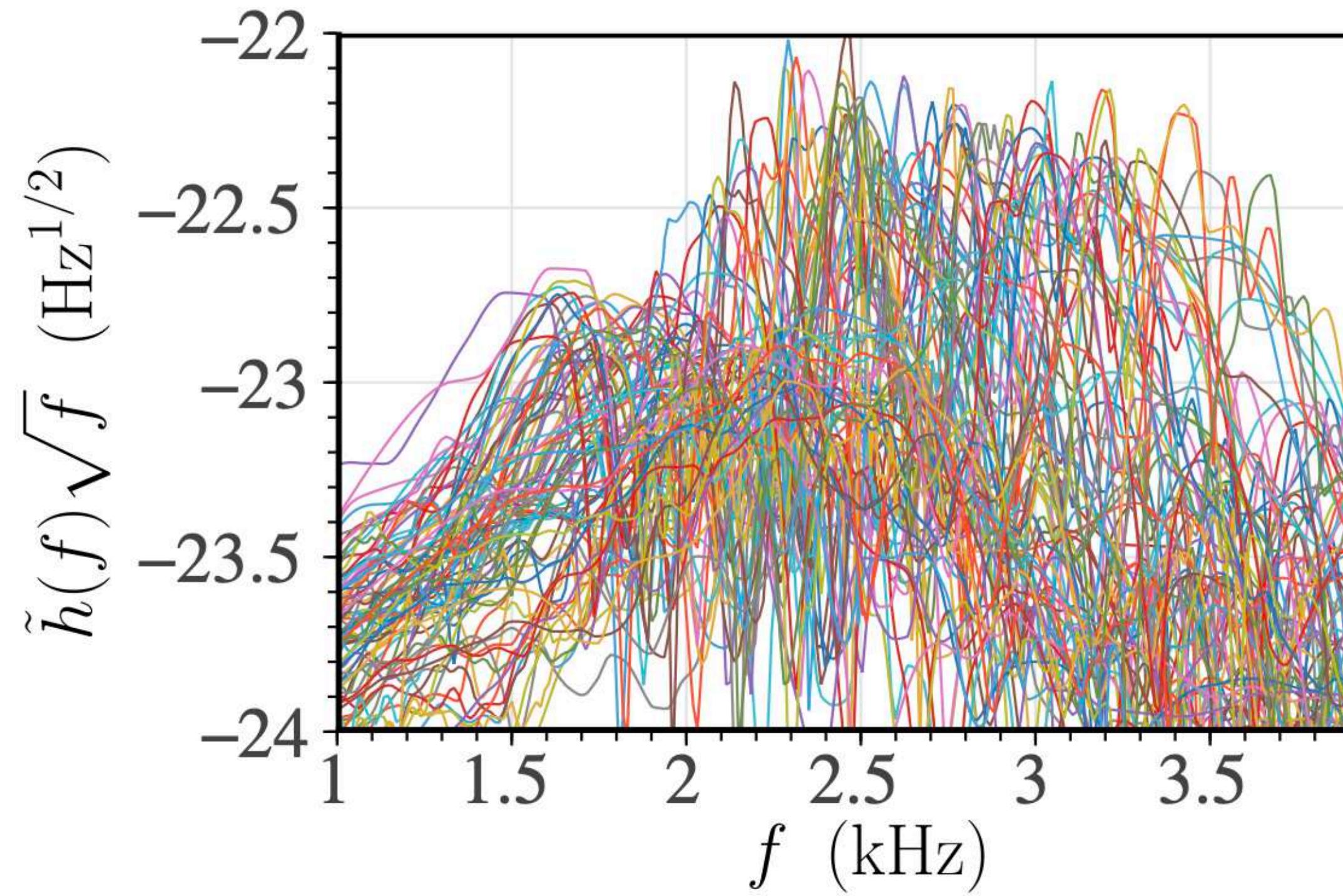
**Surrogate model** now depends on both mass and tidal deformability.



# ANN REGRESSION IN THE FREQUENCY DOMAIN

**Expanded training set:** 87 equal-mass models using 14 different EOS

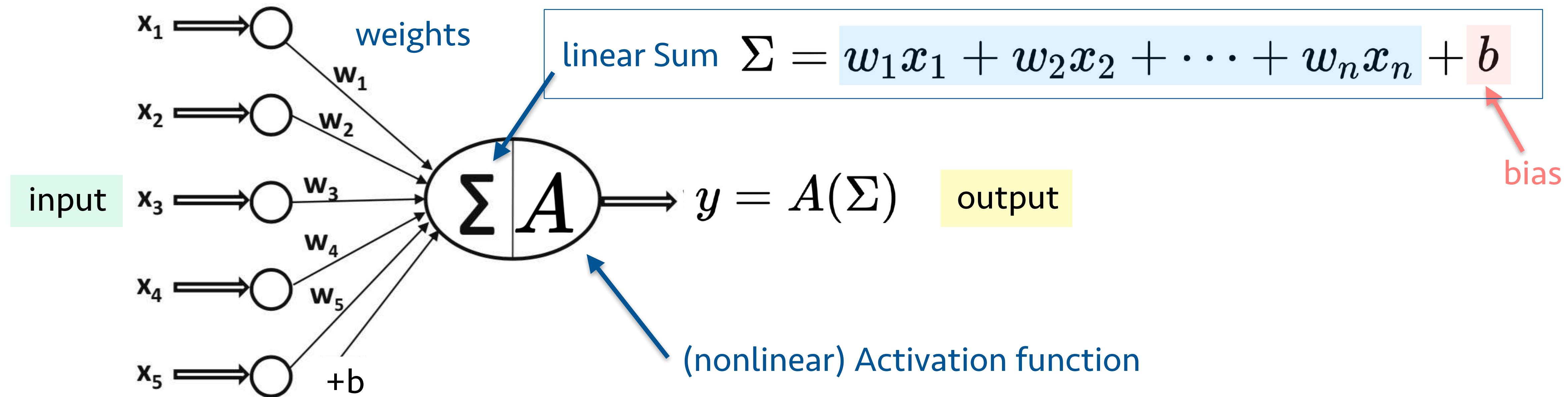
**Surrogate model** now depends on both mass and tidal deformability.



**Partial alignment of spectra** using empirical relation: 
$$f_{\text{peak}}(\kappa_2^\tau, M) = 4 \frac{\beta_1}{M} \ln \left( \frac{\beta_0}{8\kappa_2^\tau} \right)$$

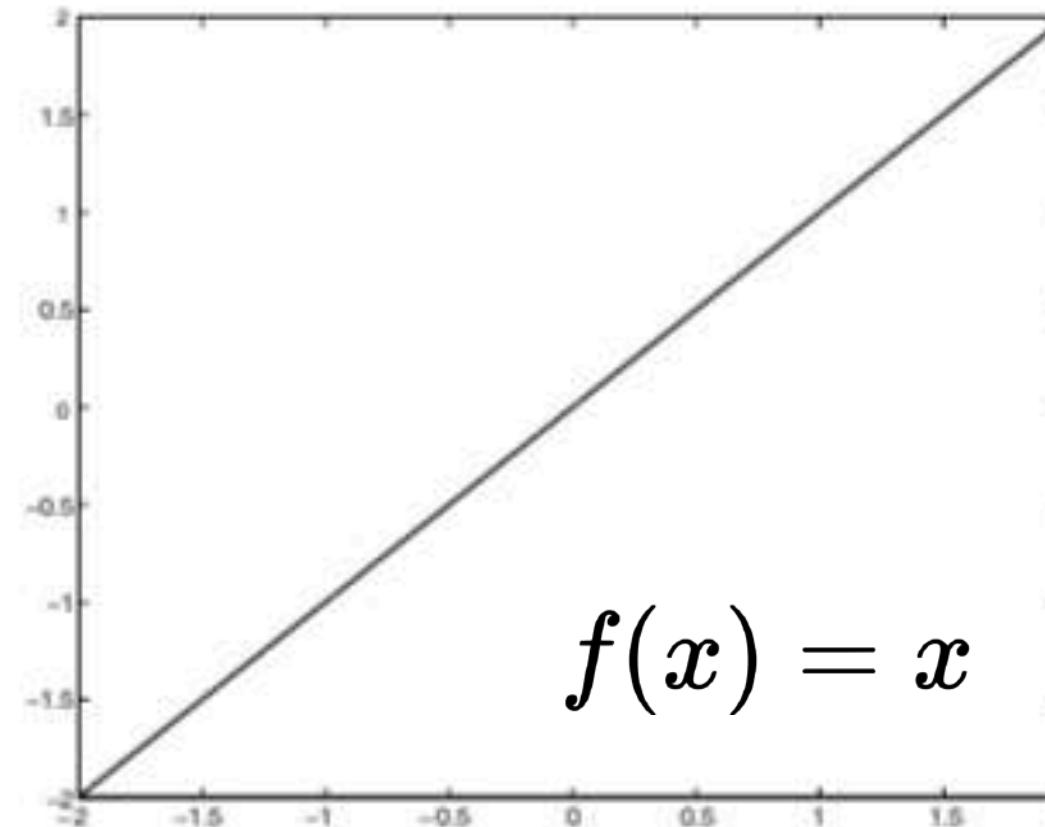
# ARTIFICIAL NEURON

- Each neuron in the network maps several **input values**  $x_1, \dots, x_n$  to an **output value**  $y$

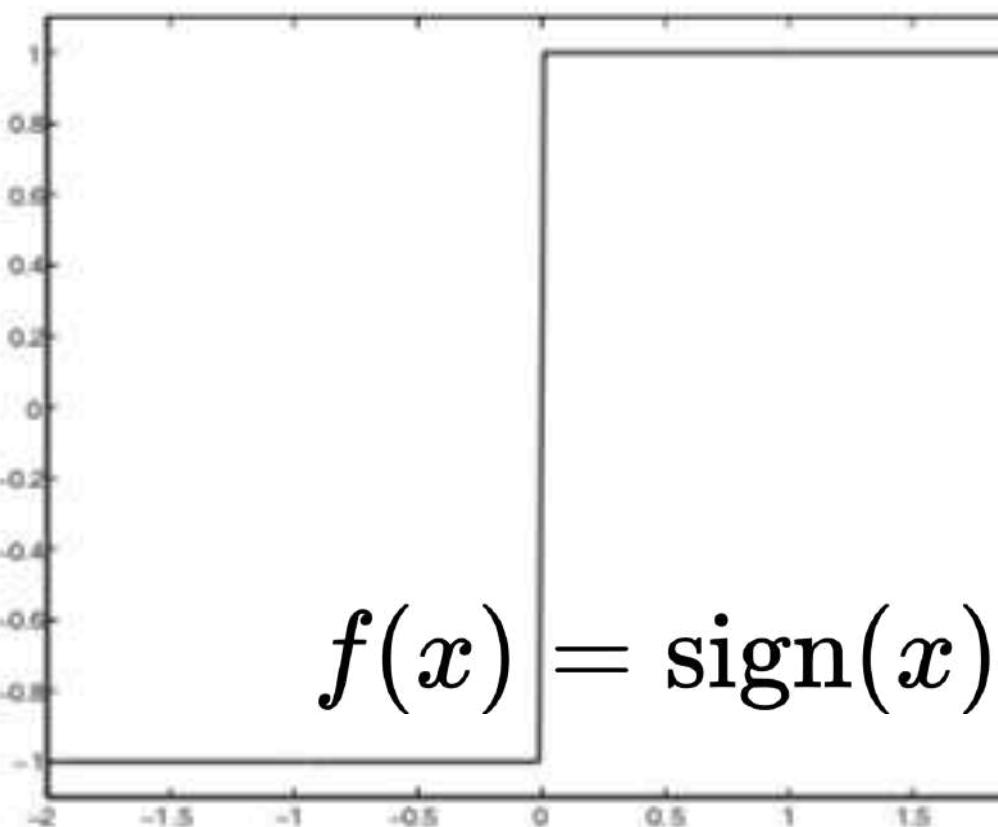


# ACTIVATION FUNCTIONS

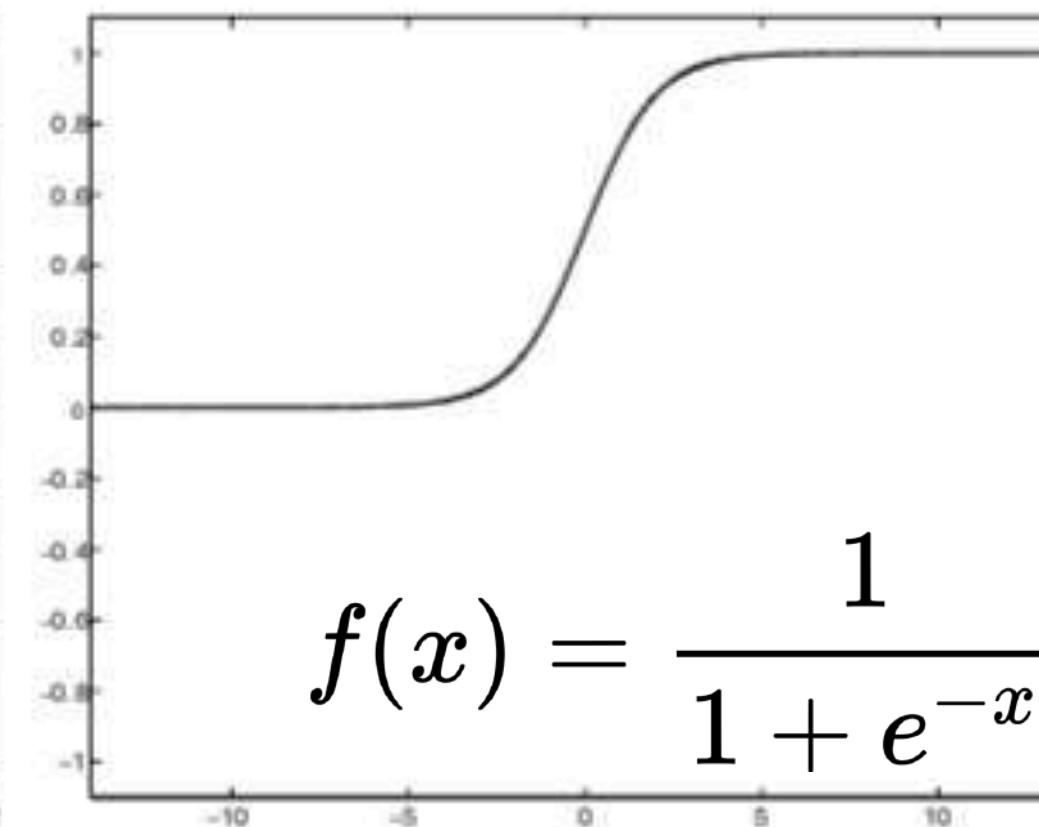
- Different common activation functions:



(a) Identity

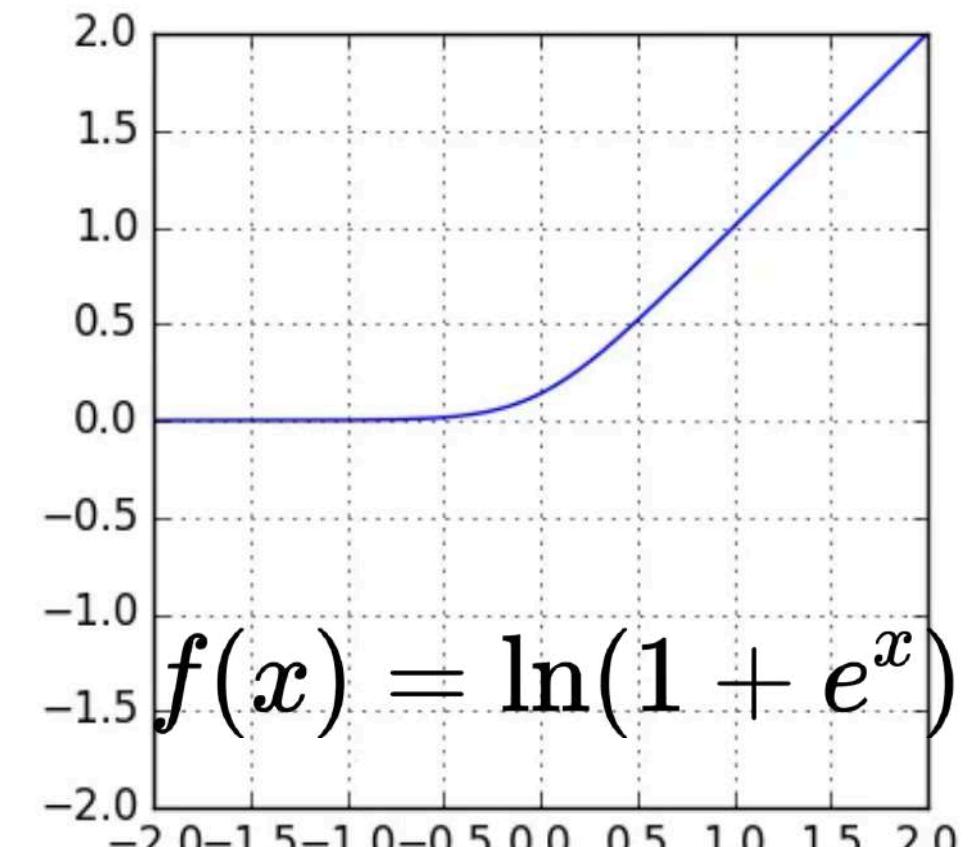


(b) Sign

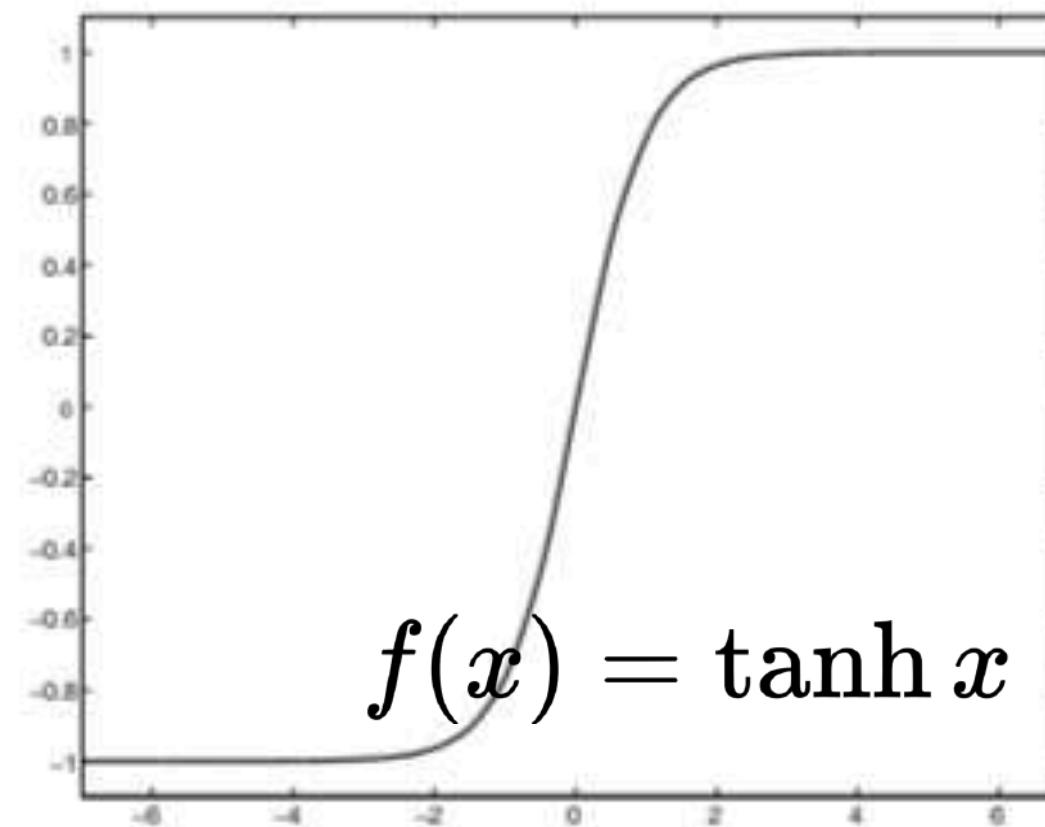


$$f(x) = \frac{1}{1 + e^{-x}}$$

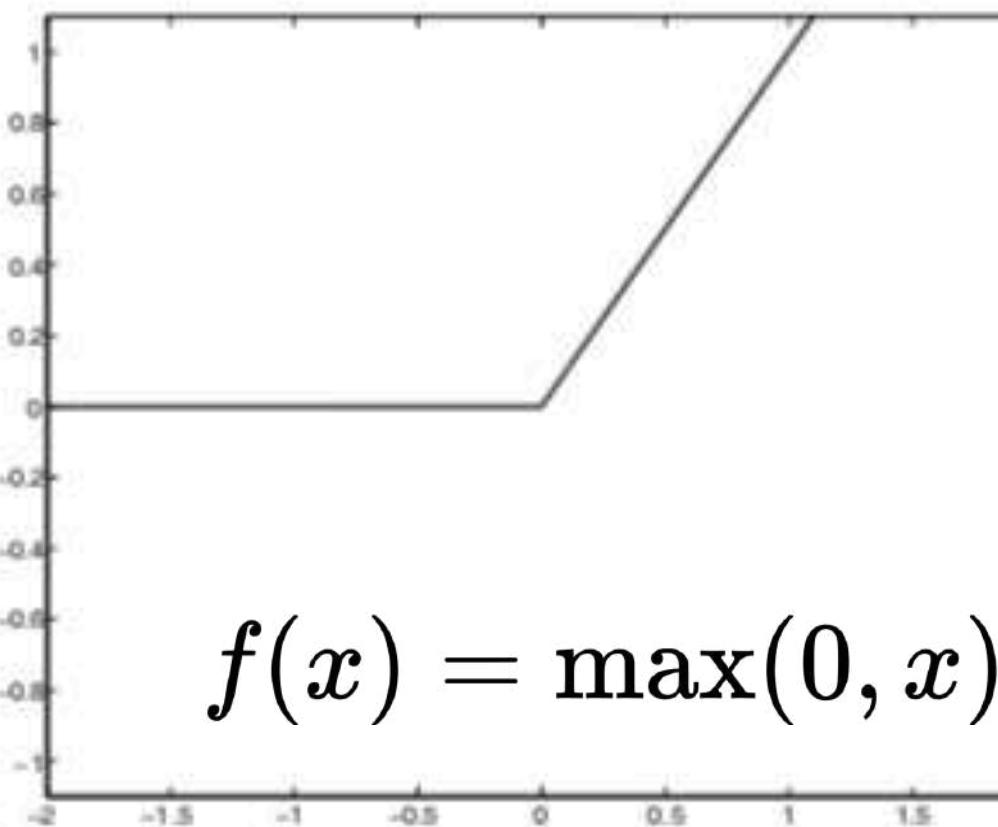
(c) Sigmoid (logistic function)



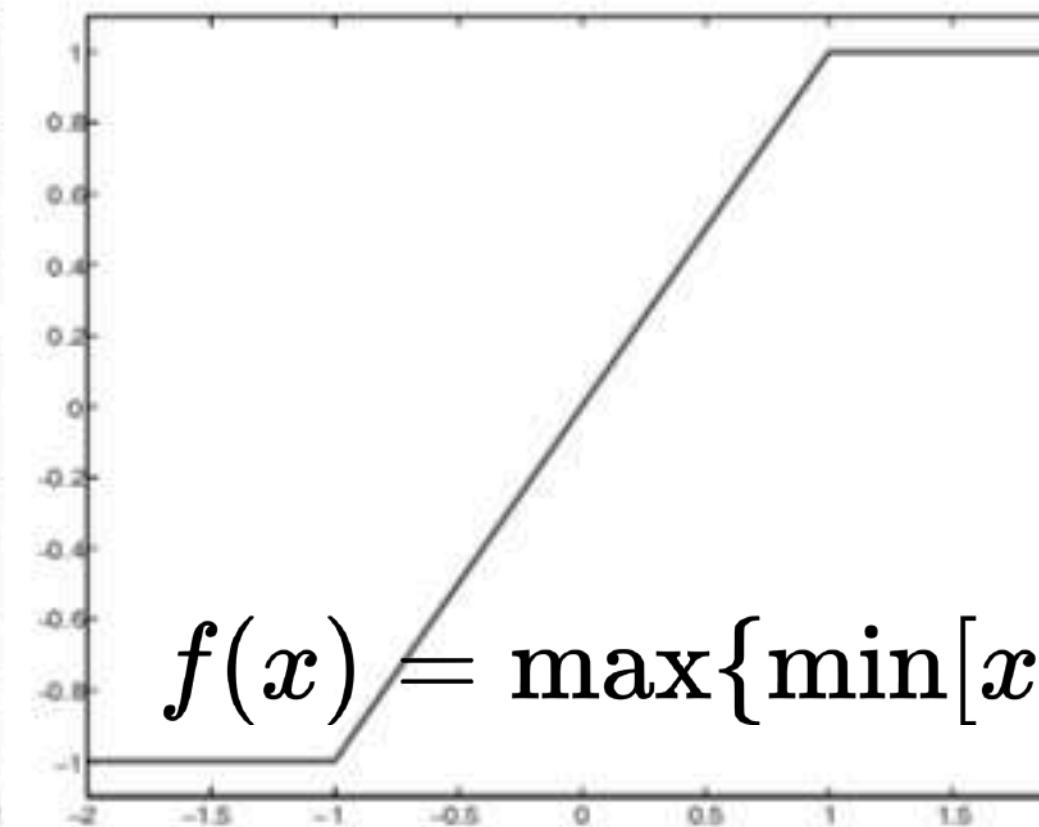
Softplus



(d) Tanh



(e) ReLU



(f) Hard Tanh

(Rectified Linear Unit)

# ANN SURROGATE IN THE FREQUENCY DOMAIN

**Input features:**

- 1) Mass, 2) tidal coupling constant, 3)  $dR/dM$

**Prediction:**

Magnitude of GW spectrum (1-4 kHz).

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**4-layer feed-forward ANN**

**Added Gaussian noise and dropout layers**

**Adam optimizer**

Layer	Type	Shape	Activation	Params
1	Gaussian noise (0.1)	(None, 3)	...	0
2	Dense	(None, 200)	Linear	800
3	Gaussian noise (0.05)	(None, 200)	...	0
4	Dropout (0.15)	(None, 200)	...	0
5	Dense	(None, 400)	Sigmoid	80400
6	Gaussian noise (0.1)	(None, 400)	...	0
7	Dropout (0.15)	(None, 400)	...	0
8	Dense	(None, 400)	Sigmoid	160400
9	Gaussian noise (0.1)	(None, 400)	...	0
10	Dropout (0.05)	(None, 400)	...	0
11	Dense	(None, 370)	Linear	148370

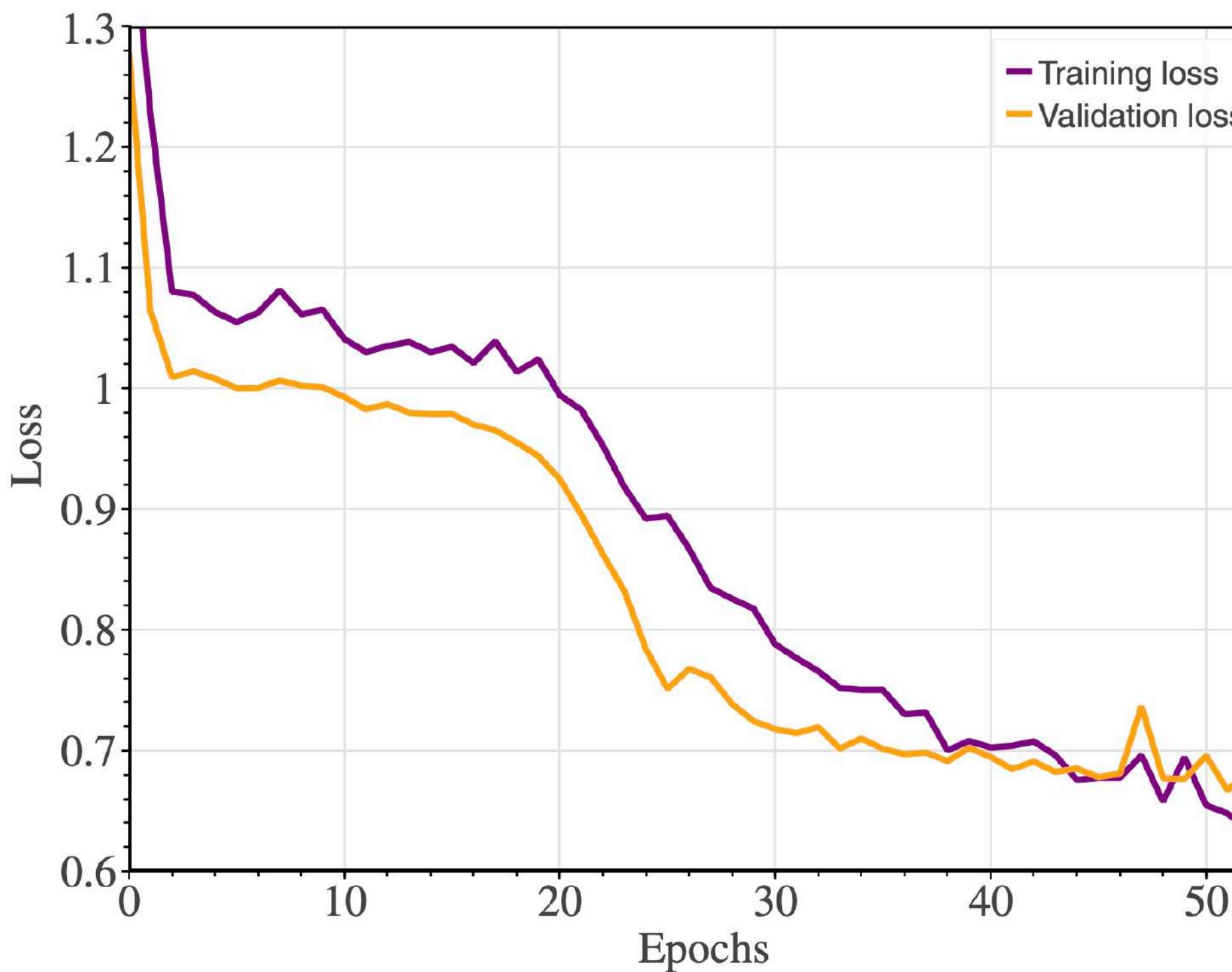
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# ANN SURROGATE IN THE FREQUENCY DOMAIN

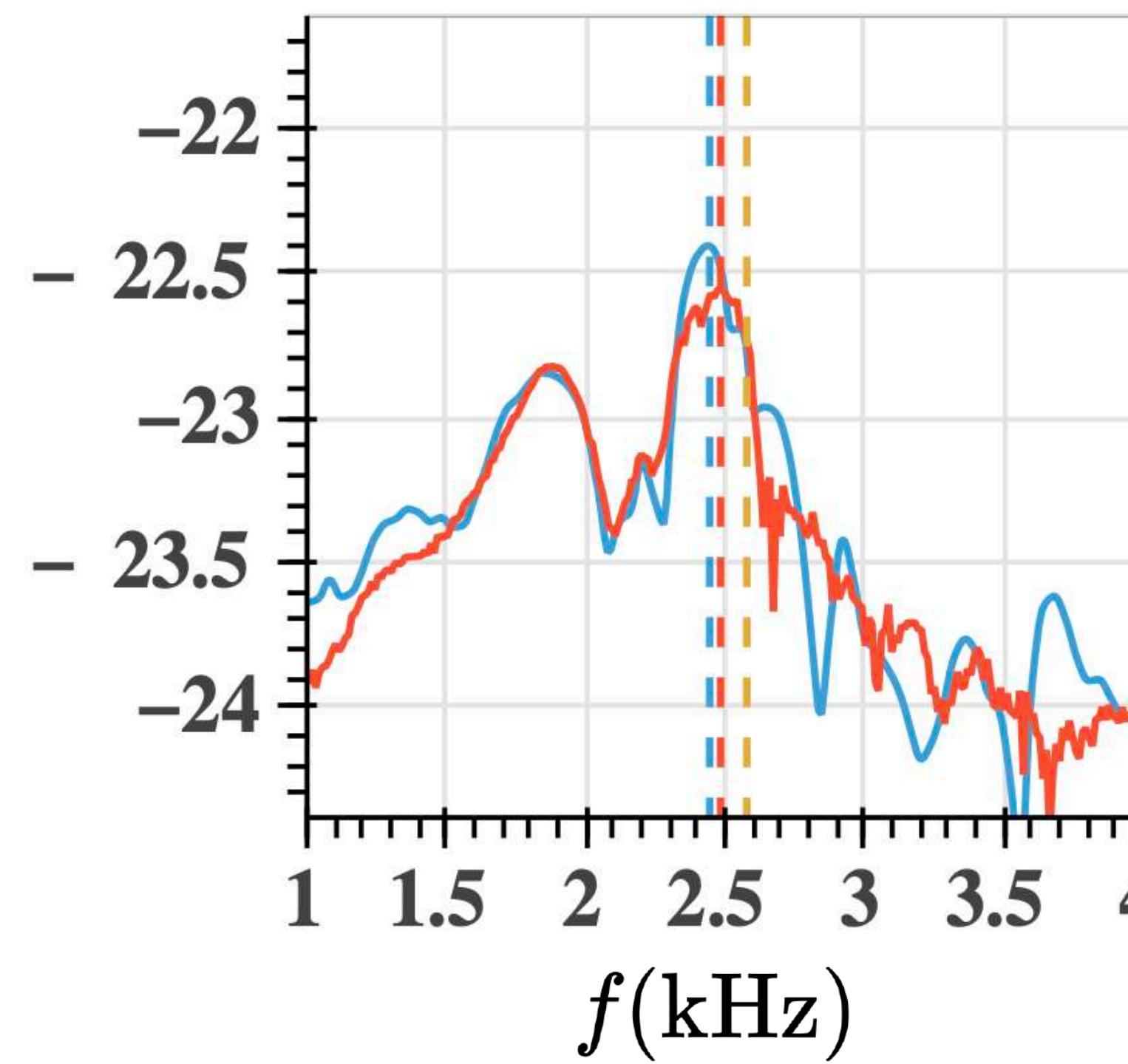
**Typical examples** of predicted magnitudes of GW spectra

**FF = O = overlap**

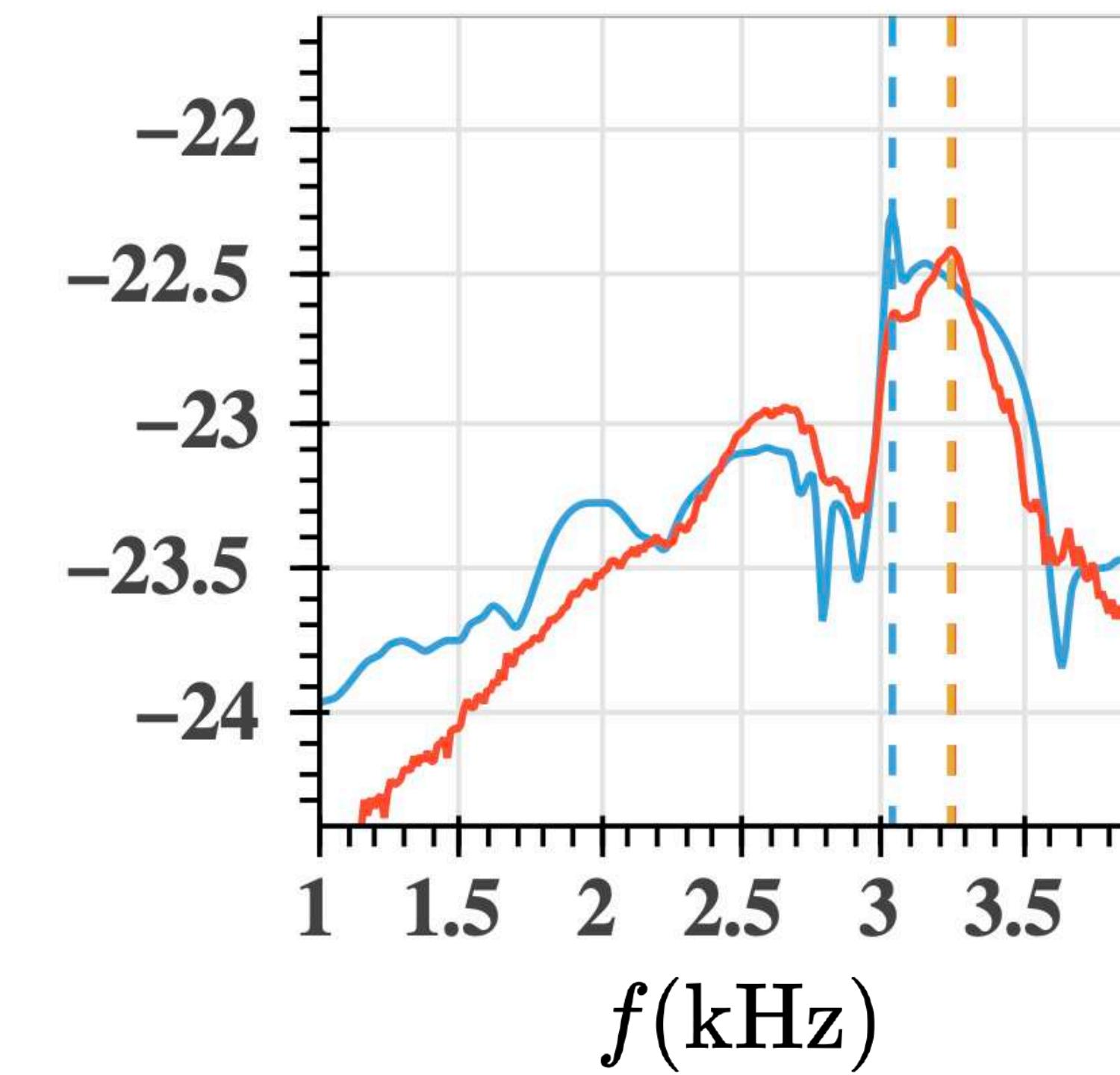
Impact of uncertainty in empirical relation offset by re-calibration of spectra.

**ANN outperforms multivariate linear regression.**

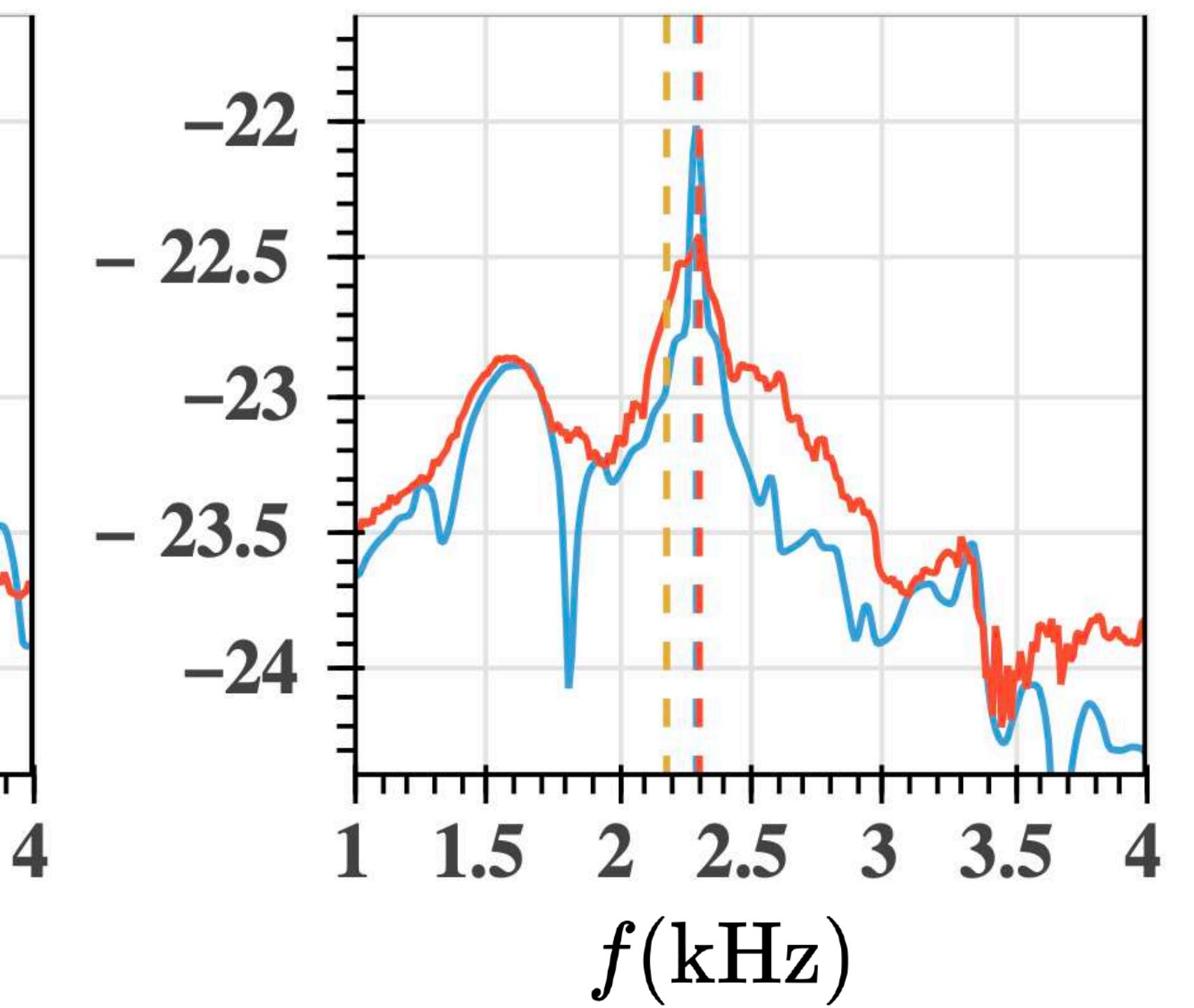
**ALF2, M12500, FF: 0.971**



**APR4, M12500, FF: 0.94**

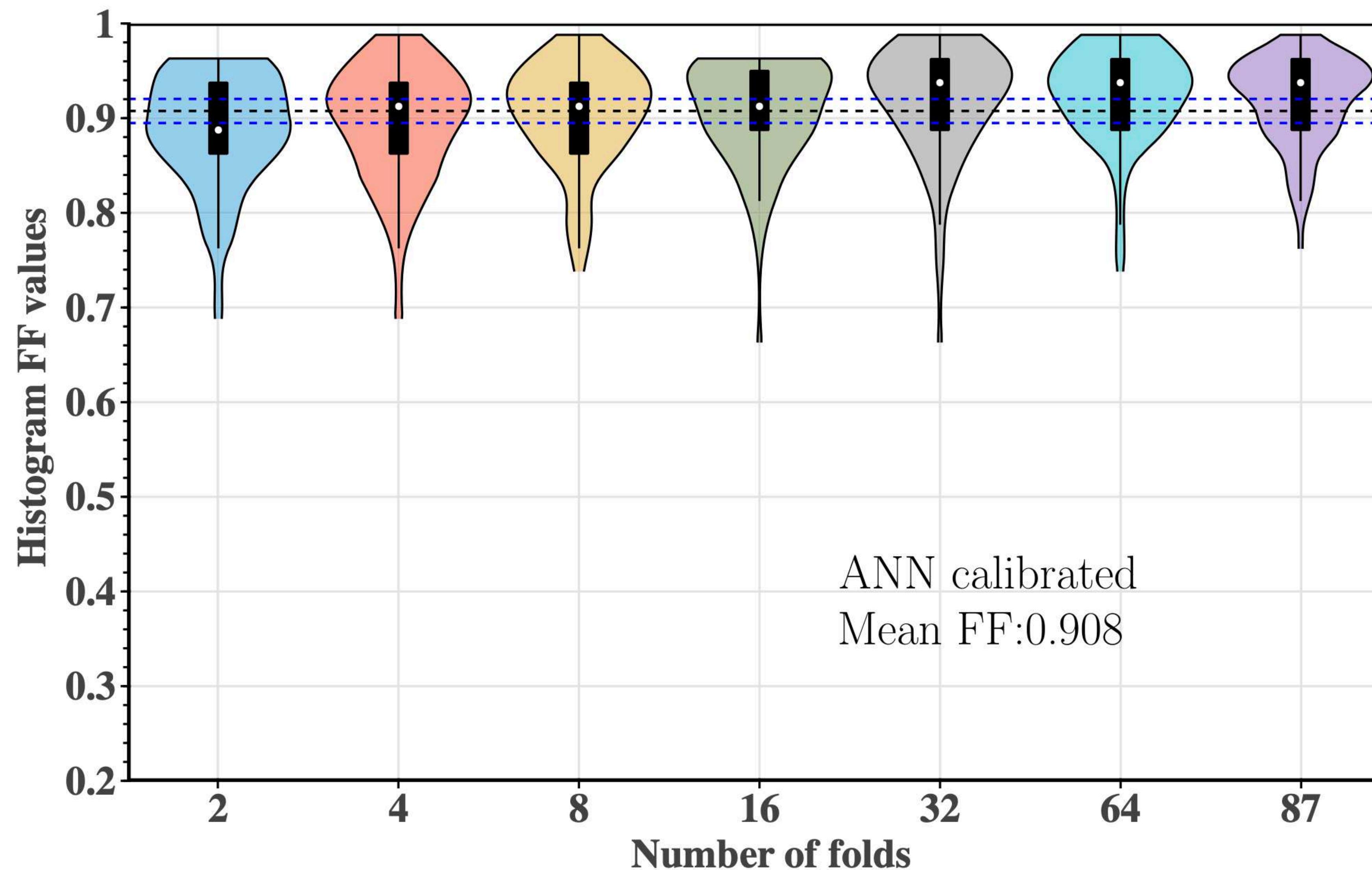


**GNH3, M12500, FF: 0.862**



# ANN SURROGATE IN THE FREQUENCY DOMAIN

## Cross-validation study of fitting factors distribution:

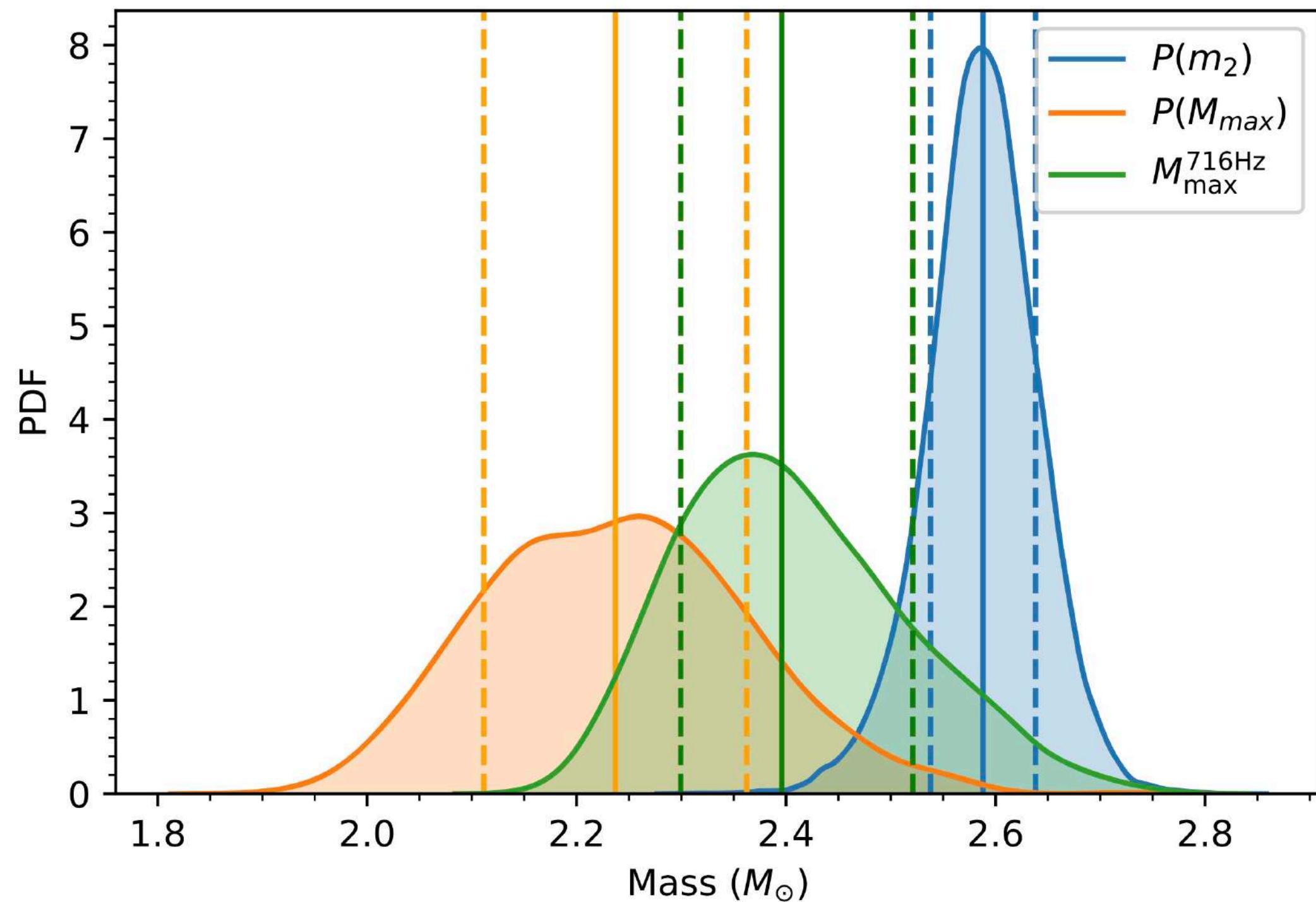


**PART C.**

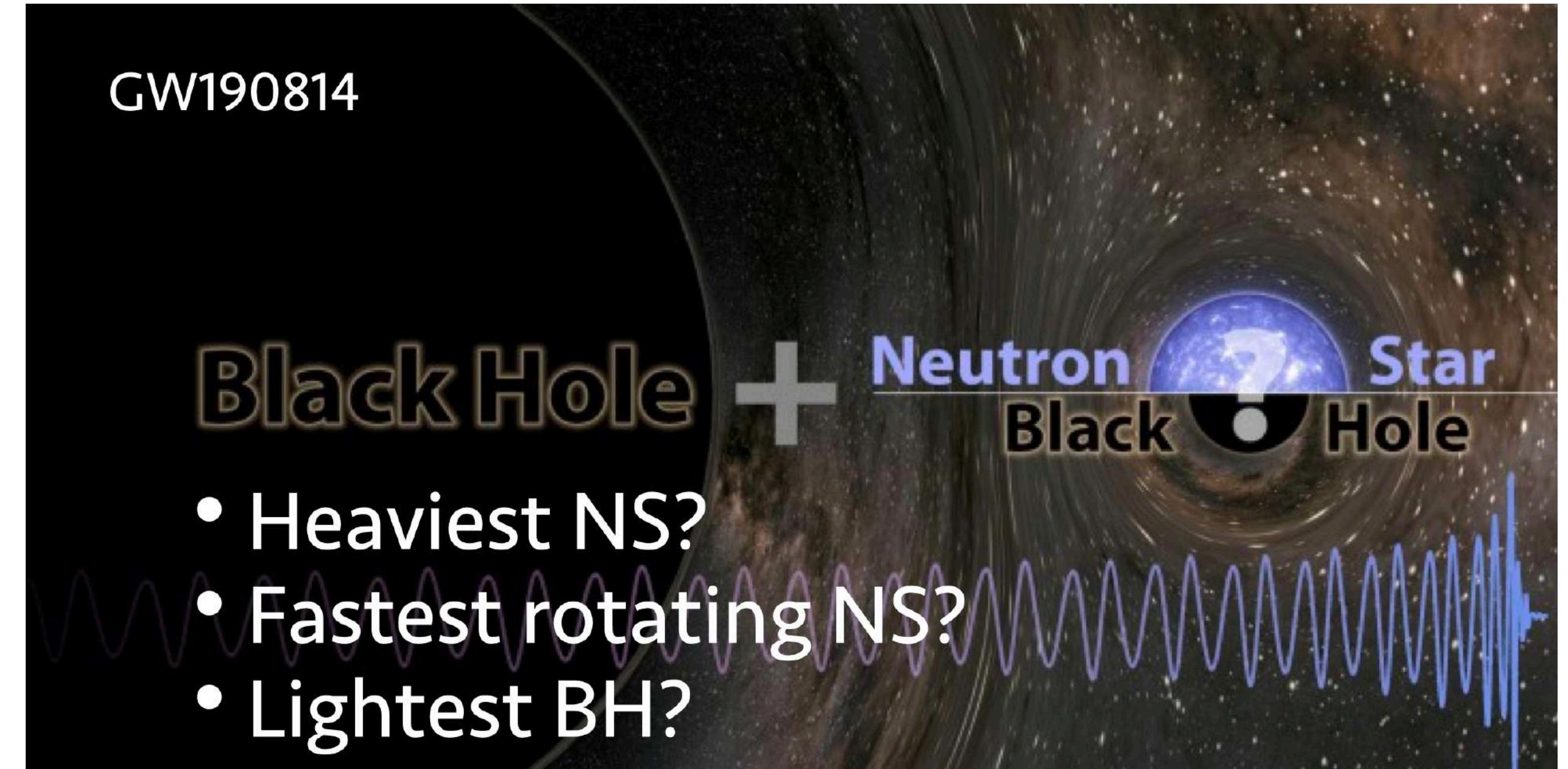
**NEUTRON STAR MODELS IN ALTERNATIVE  
THEORIES OF GRAVITY**

# HIGH MASS NEUTRON STARS?

What was the nature of the lighter component in GW190814?

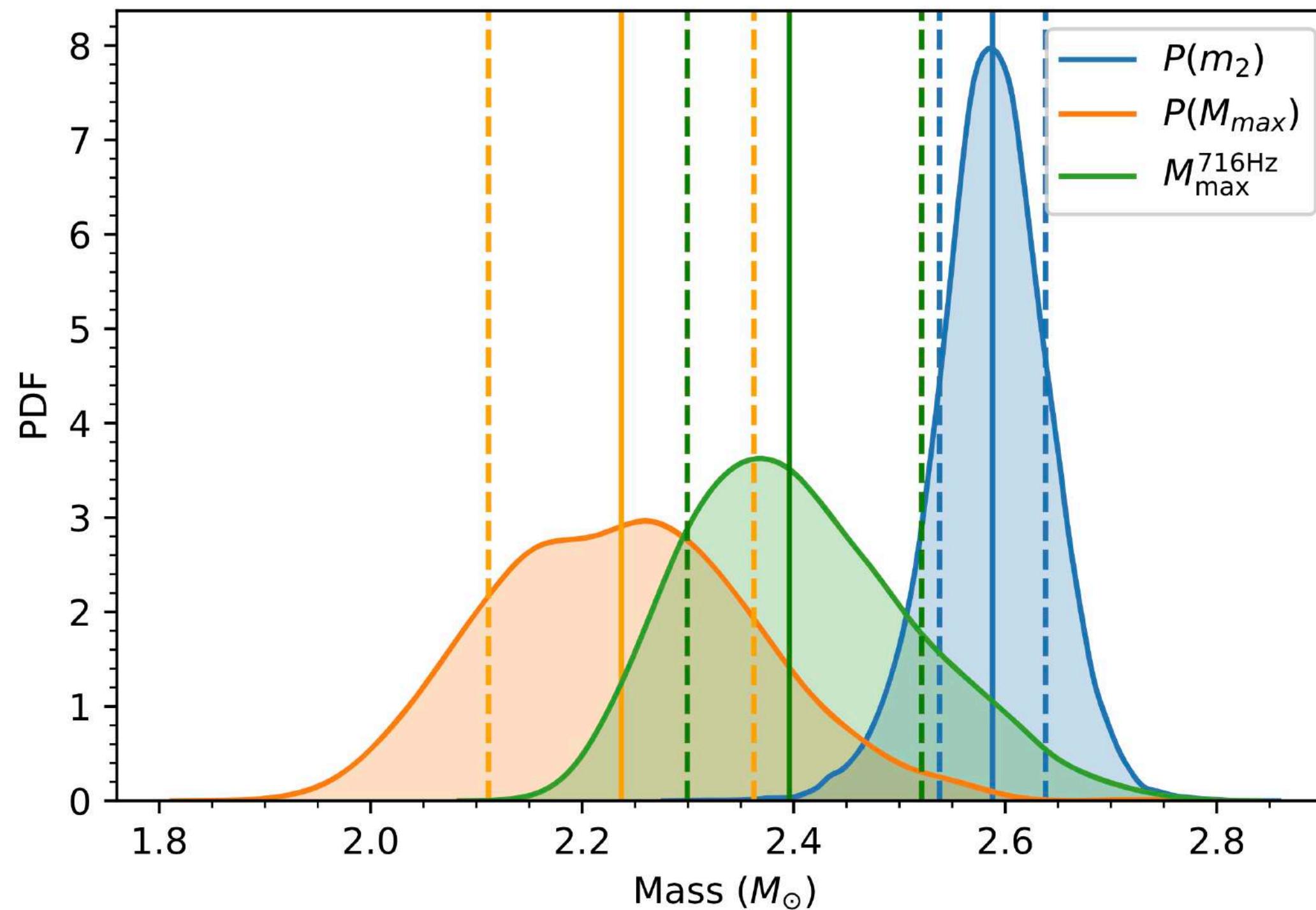


Biswas, Nandi, Char, Bose, Stergioulas (2021)

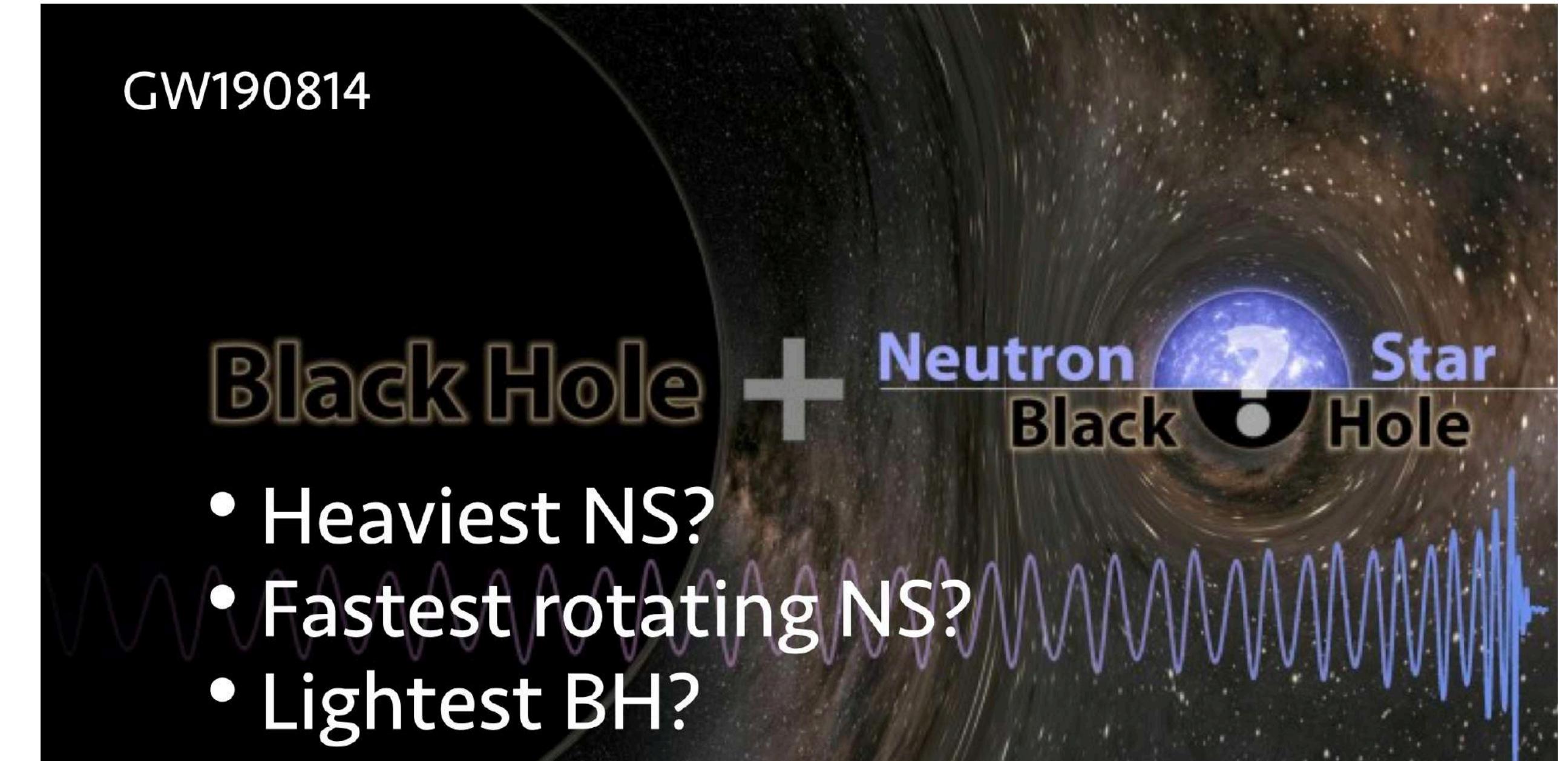


# HIGH MASS NEUTRON STARS?

What was the nature of the lighter component in GW190814?



Biswas, Nandi, Char, Bose, Stergioulas (2021)



Another possibility: if the correct theory of gravity is not GR, then heavier NS might exist!

How can this degeneracy be resolved?

# NS IN 4D EINSTEIN-GAUSS-BONNET GRAVITY

We consider the action

$$S = \frac{1}{2\kappa} \int d^4x \sqrt{-g} \{ R + \alpha [\phi \mathcal{G} + 4G_{\mu\nu} \nabla^\mu \phi \nabla^\nu \phi - 4(\nabla \phi)^2 \square \phi + 2(\nabla \phi)^4] \} + S_m$$

where  $\kappa = 8\pi G/c^4$ ,  $\mathcal{G} = R^2 - 4R_{\mu\nu}R^{\mu\nu} + R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma}$  is the Gauss-Bonnet scalar and  $S_m$  is the matter Lagrangian.

This theory possesses an exact vacuum solution describing nonrotating, static black holes with line element

$$ds^2 = -h(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\Omega^2$$

where

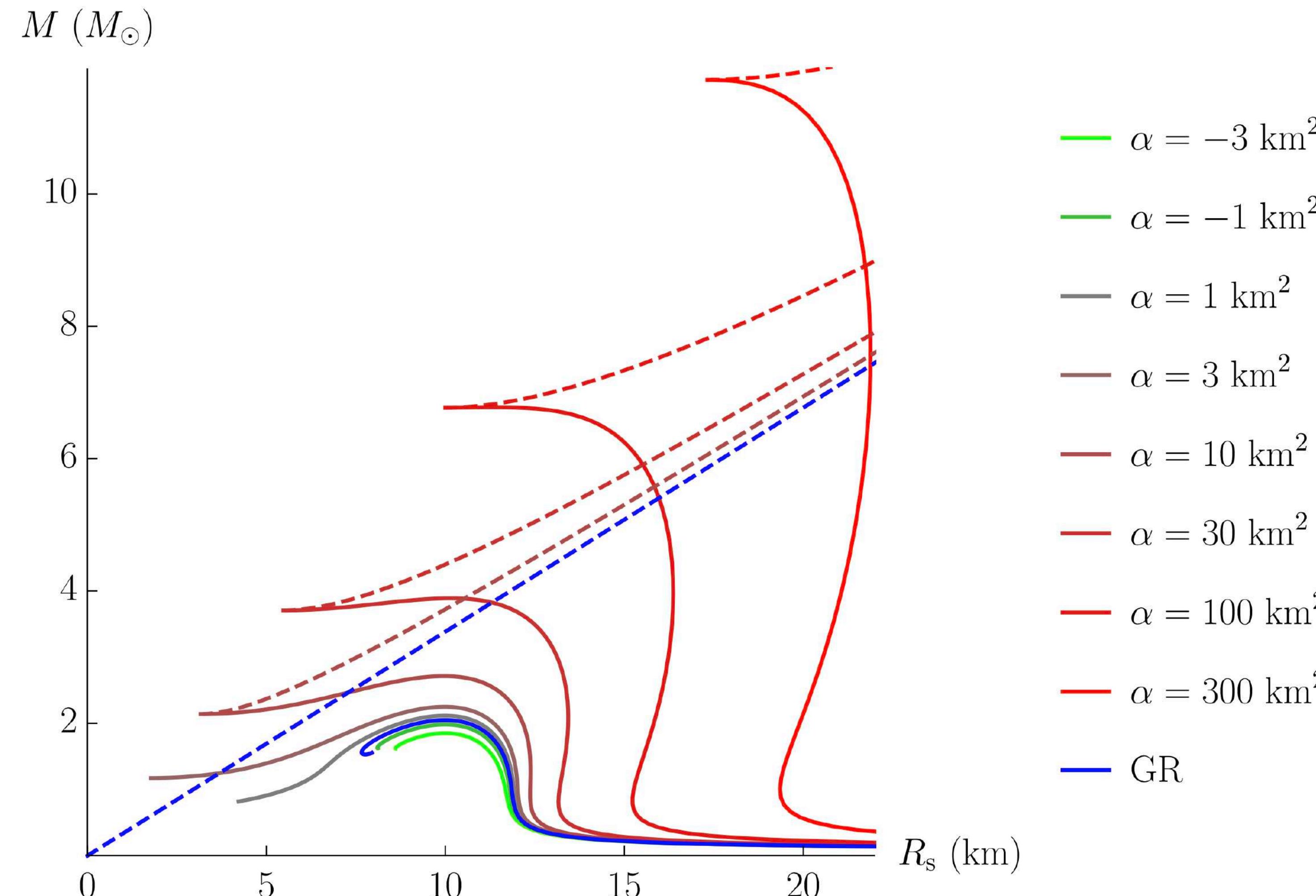
$$h(r) = f(r) = 1 + \frac{r^2}{2\alpha} \left( 1 - \sqrt{1 + \frac{8\alpha M}{r^3}} \right) \quad (M \rightarrow \text{ADM mass})$$

and the shift-symmetric scalar field is

$$\phi(r) = \int dr \frac{\sqrt{f-1}}{r\sqrt{f}}$$

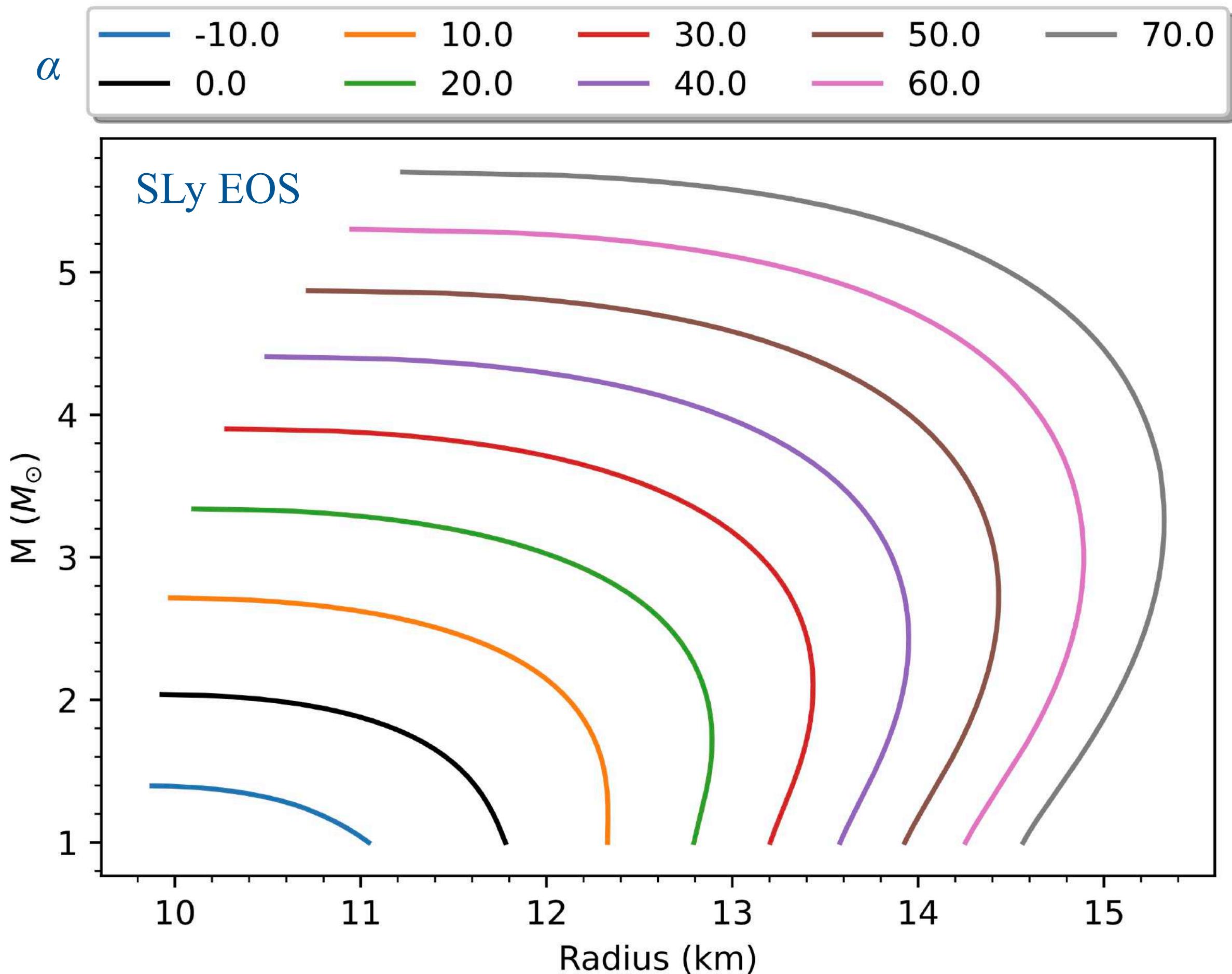
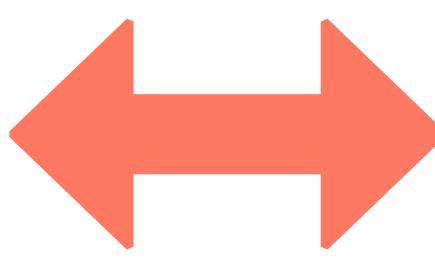
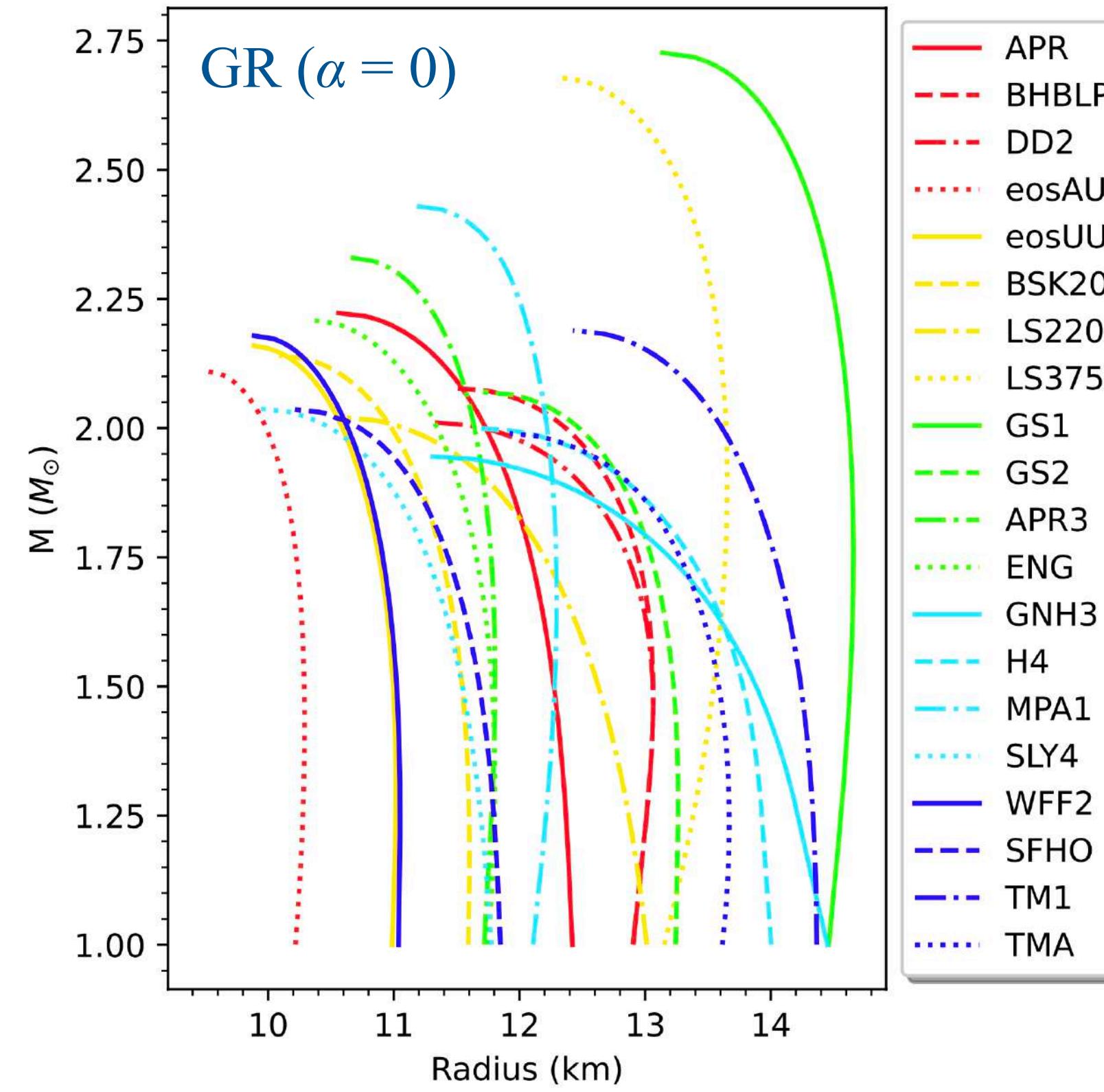
# SEQUENCES OF EQUILIBRIUM MODELS

For the **SLy EOS**, we show representative cases of sequences of NS equilibrium models (solid lines) and BHs (dashed lines). For  $\alpha > 0$ , the NS solutions merge with the minimum mass BH solution.



# EOS-GRAVITY DEGENERACY

In this theory, constructing equilibrium sequences for the same EOS, but different  $\alpha$ , mimics the effect of using different EOS in GR.



Need to use a large number of observations to break the degeneracy!

# ANN SURROGATE MODELS FOR NUMERICAL SOLUTIONS

## EOS collection

Name	Number #
APR	1
BHBLP	2
DD2	3
eosAU	4
eosUU	5
BSk20	6
LS220	7
LS375	8
GS1	9
GS2	10
APR3 (PP)	11
ENG (PP)	12
GNH3 (PP)	13
H4 (PP)	14
MPA1 (PP)	15
SLy4 (PP)	16
WFF2 (PP)	17
SFHo	18
TM1	19
TMA	20

## Surrogate models

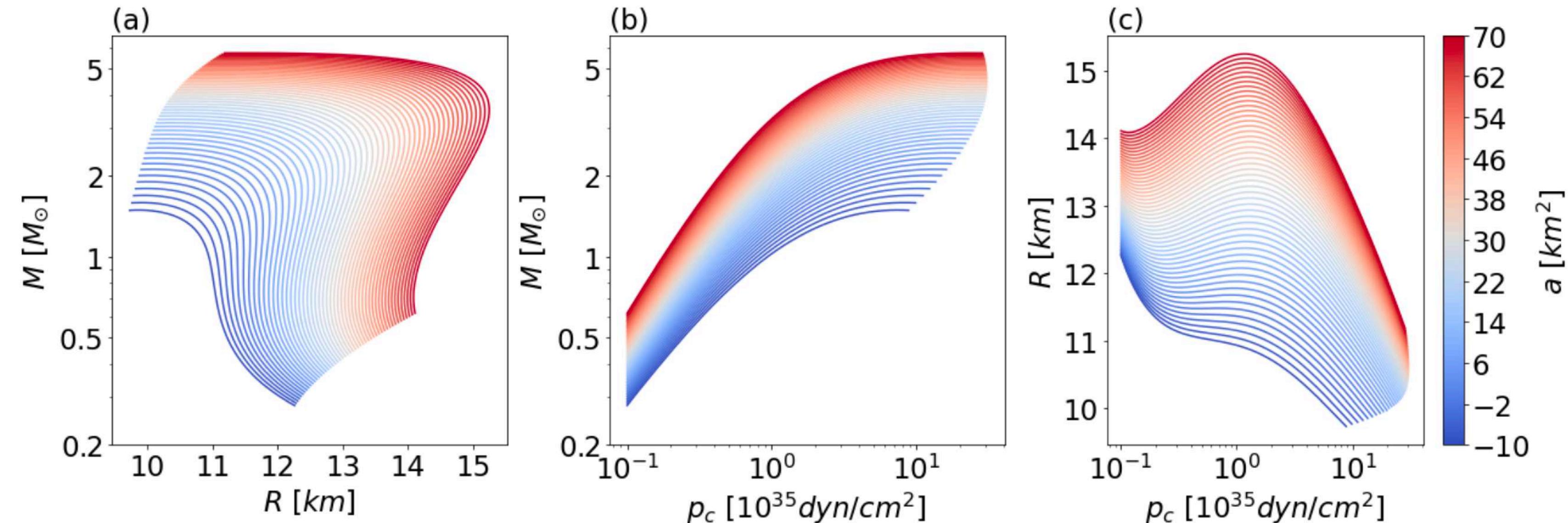
$$f_1(\text{EoS}; \alpha, p_c) \rightarrow (M, R)$$

$$f_2(\text{EoS}; \alpha, M) \rightarrow R$$

## Network architecture for each EOS

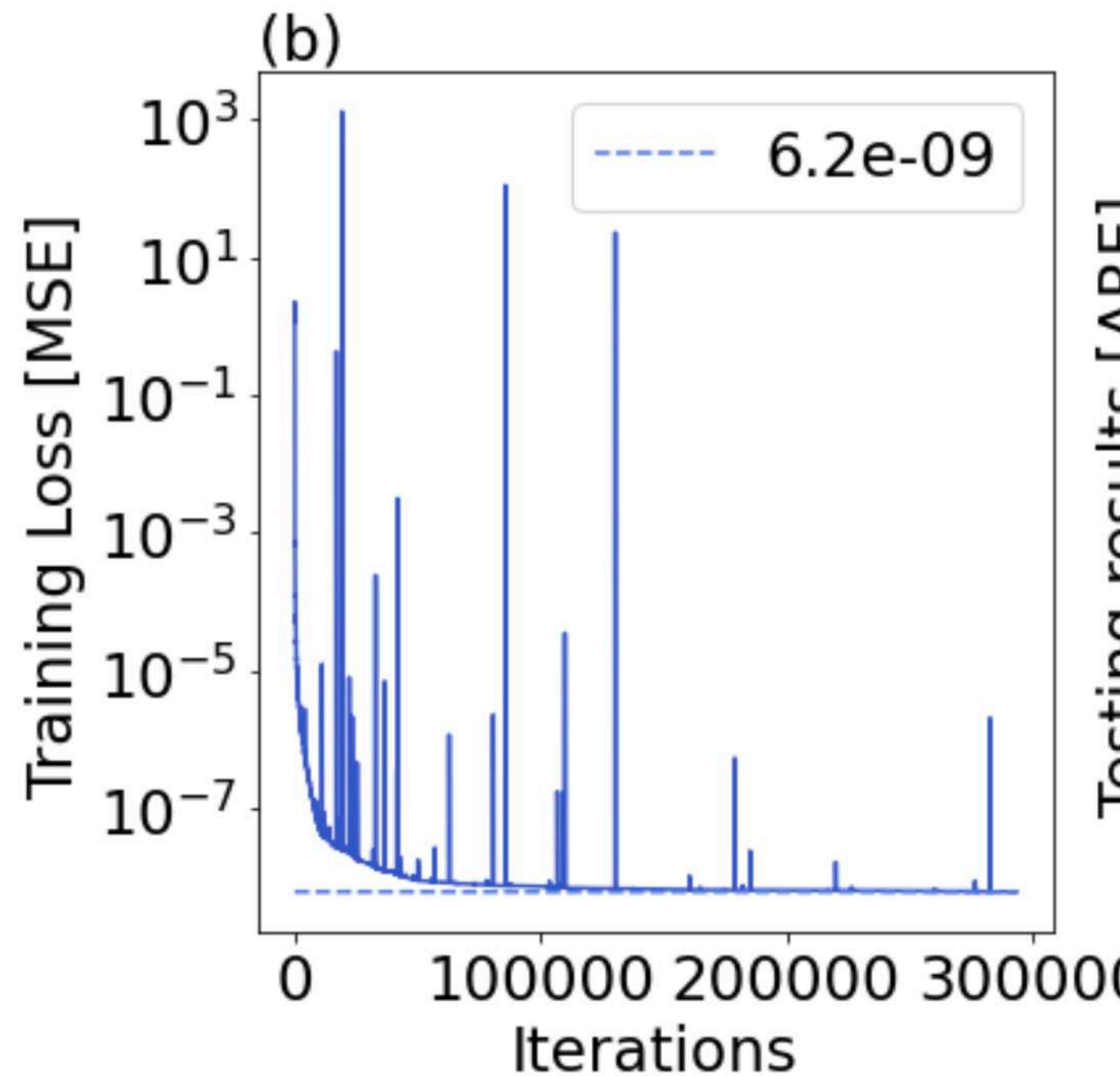
Layer	Type $f_1$	Type $f_2$
Input layer	$(\alpha, p_c)$	$(\alpha, M)$
Hidden layer 1	25-tanh	25-tanh
Hidden layer 2	35-relu	35-relu
Hidden layer 3	25-tanh	25-tanh
Output layer	$(M, R)$	$R$

Training set for each EOS:  $200 (p_c) \times 51 (\alpha) = 10200$  equilibrium models

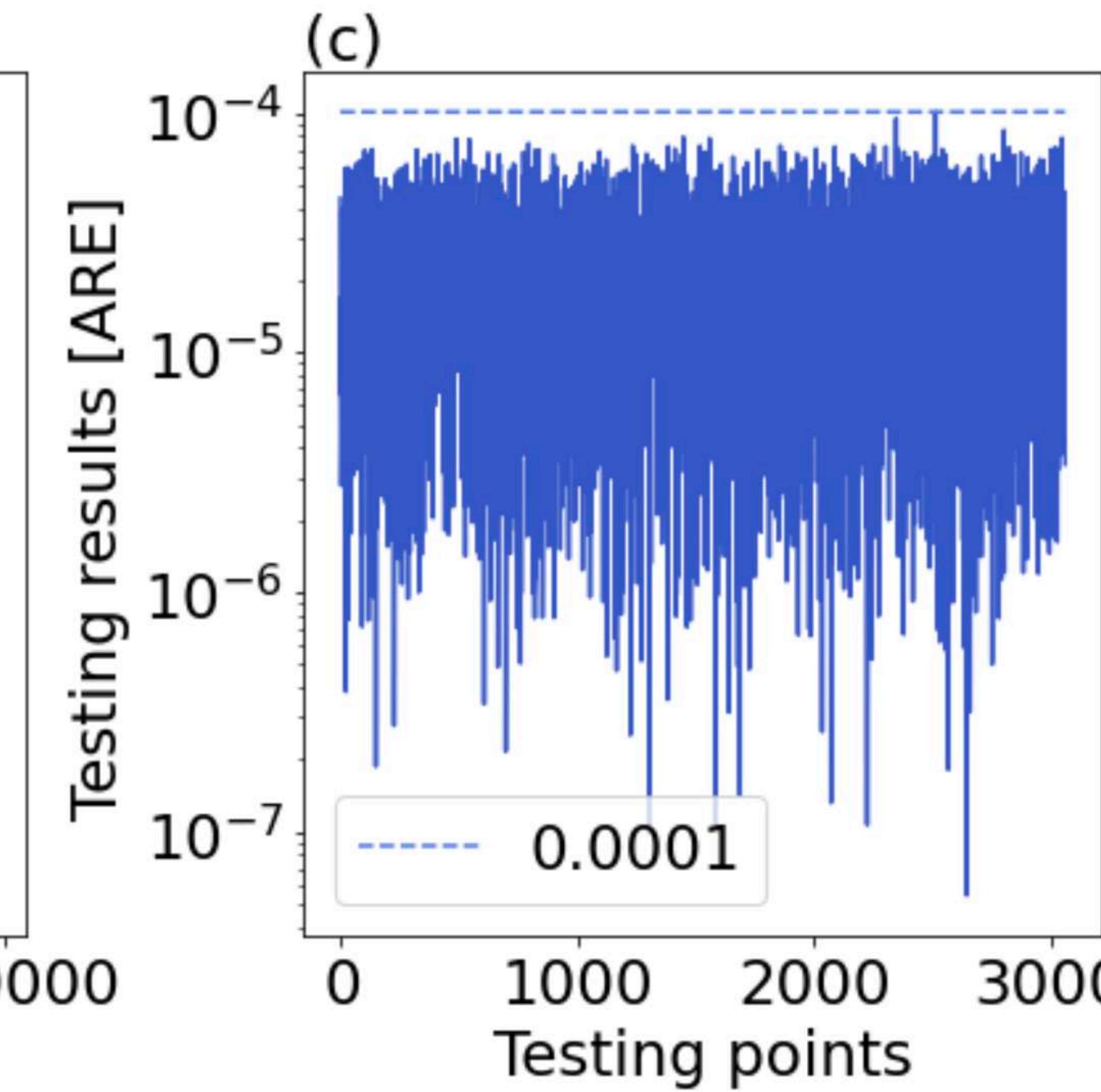


# ACCURACY OF $f_1$ ANN SURROGATE MODEL FOR EOS BSk20

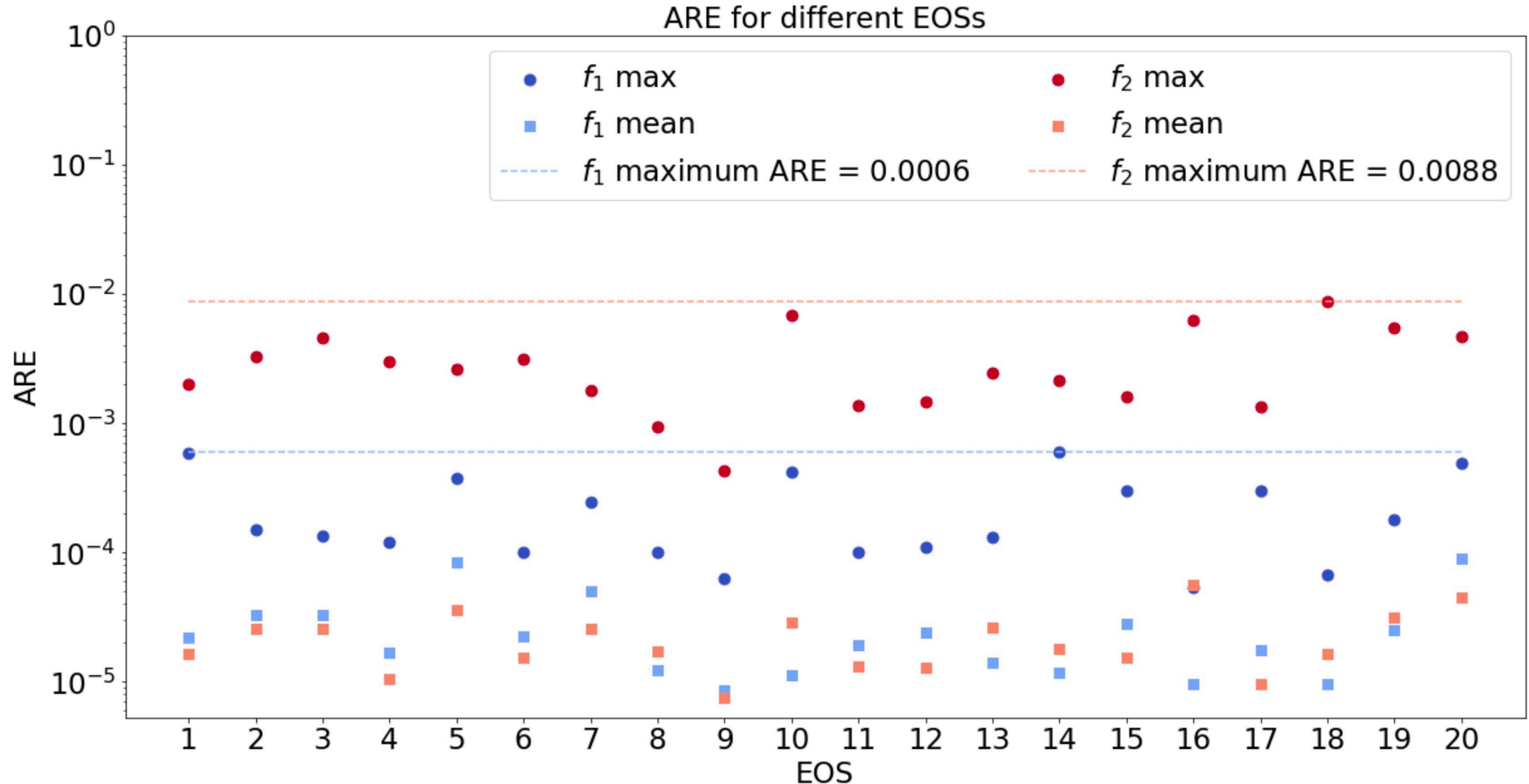
Loss function:  
Mean Square Error (MSE)



Accuracy test:  
Absolute Relative Error

$$ARE_i = \frac{1}{m} \sum_{j=1}^m \left| \frac{Y_i^j - Y_{i,\text{true}}^j}{Y_{i,\text{true}}^j} \right|$$


# ACCURACY OF ANN SURROGATE MODELS FOR ALL EOS



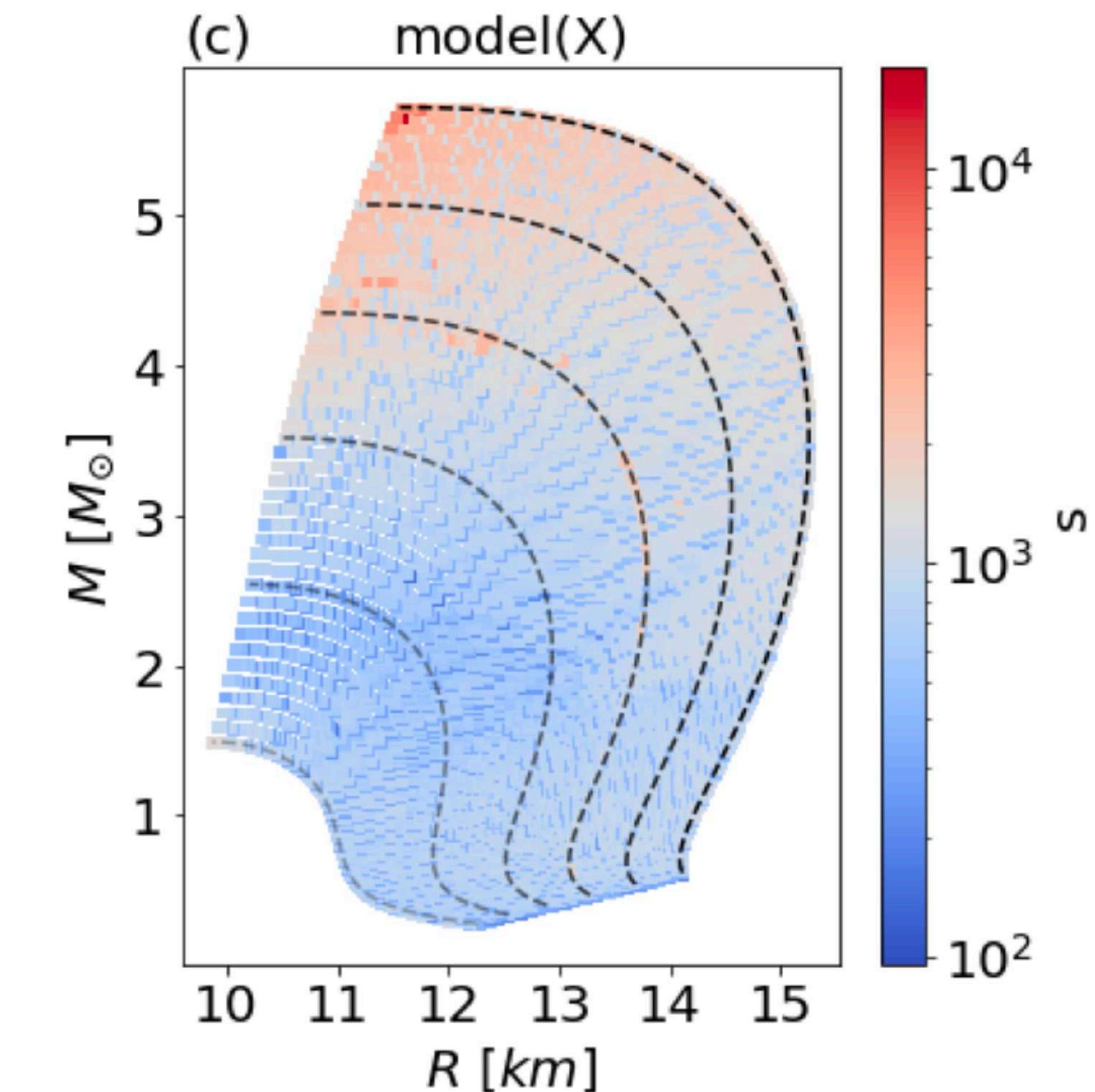
# SPEED-UP ACHIEVED WITH THE ANN SURROGATE MODELS

Speed-up of ANN surrogate model compared to original numerical code

$$s = \frac{\Delta t_{\text{ANN}}}{\Delta t_{\text{num}}}$$

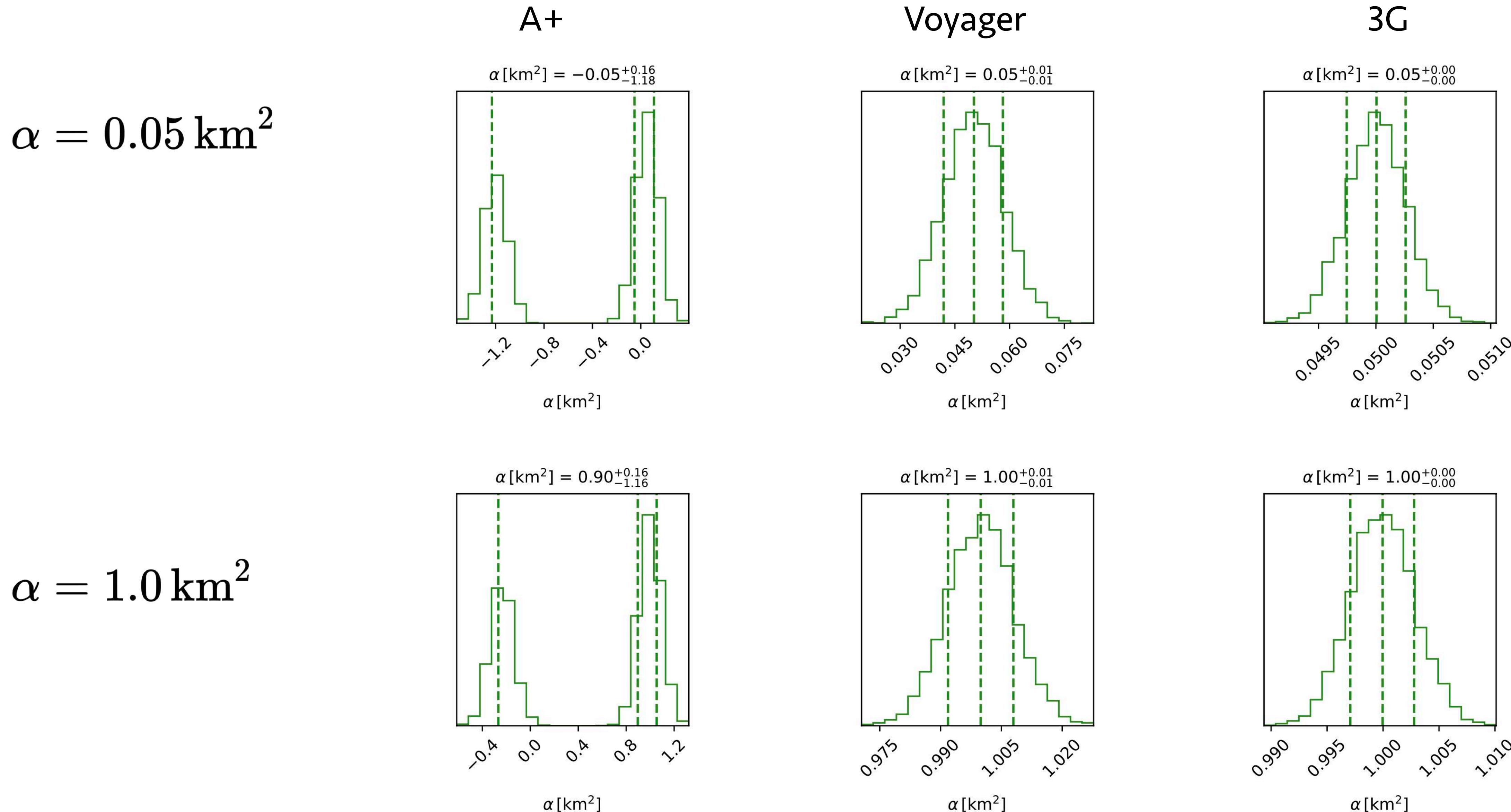
Numerical code run time:	(Mean)	(Min)	(Max)
	1003.5 ms	147.96 ms	18122.4 ms
Output method	Speed Up (Mean)	Speed Up (Minimum)	Speed Up (Maximum)
model.predict( $X$ )	25.12	0.97	464.56
model( $X$ )	921.9	95.6	18102.1
model.predict( $\mathbf{X}$ )	31295.5	4614.5	565157.2

The achieved speed-up allows for millions of MCMC calls in a Bayesian inference computation with minimal overhead.

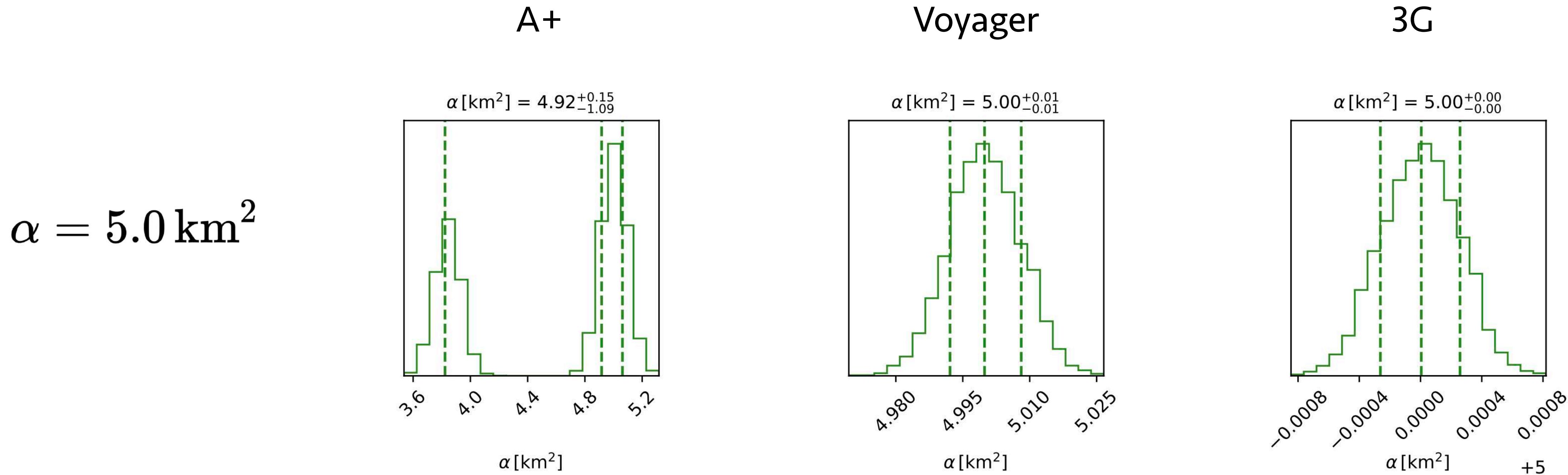


# RECOVERY OF INJECTED $\alpha$ VALUES

Hierarchical Bayesian Inference using astrophysical constraints for a set of 20 EOS:



# RECOVERY OF INJECTED $\alpha$ VALUES



A+ : for an injection of  $\alpha = 5 \text{ km}^2$ , the GR value of  $\alpha = 0$  is excluded at the  $3\sigma$  level.

Voyager/3G : even departures from GR at the  $\alpha = 0.05 \text{ km}^2$  level are accurately recovered.

**THANK YOU FOR YOUR ATTENTION**