

Assignment 5A

1. Random sample generation from Exponential Distributions:

(a) $f(x) = (1/\sigma) \exp(-x/\sigma)$, $x > 0, \sigma > 0$.

(b) $f(x) = (1/\sigma) \exp(-(x - \mu)/\sigma)$, $x > 0, \sigma > 0, \mu \in \mathbb{R}$.

Apply Probability Integral Transform to generate 2000 sample from the above two distributions. You can take specific choices of parameters.

2. Random sample generation from Cauchy Distributions:

(a) $f(x) = \frac{\sigma}{\pi(\sigma^2 + x^2)}$, $x \in \mathbb{R}, \sigma > 0$.

(b) $f(x) = \frac{\sigma}{\pi(\sigma^2 + (x - \mu)^2)}$, $x, \mu \in \mathbb{R}, \sigma > 0$.

Apply Probability Integral Transform to generate 2000 sample from the above two distributions. You can take specific choices of parameters.

3. $f(x) = \begin{cases} a + 2(1 - a)x, & 0 \leq x \leq 1 \\ 0, & \text{elsewhere.} \end{cases}$ Generate 5000 sample from the above

distribution using Probability Integral Transform method, if possible (taking specific value of the parameter). If not, use the following method:

Generate $U_1, U_2, U_3 \sim U(0, 1)$

If $U_1 \leq a$, $\{X = U_2\}$

Else, $\{X = \max(U_2, U_3)\}$