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1 #include "geometry.hpp"
2 #include "line.hpp"
3
4 class Circle
5 {
6 public:
7     Point p;
8     ld r;
9     Circle() : p(Point(0, 0)), r(0) {}
10    Circle(Point p, ld r) : p(p), r(r) {}
11 };
12
13 // c1, c2 の交点
14 std::vector<Point> is_cc(Circle c1, Circle c2)
15 {
16     std::vector<Point> res;
17     ld d = abs(c1.p - c2.p);
18     ld rc = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d);
19     ld dfr = c1.r * c1.r - rc * rc;
20     if (abs(dfr) < eps)
21         dfr = 0.0;
22     else if (dfr < 0.0)
23         return res; // no intersection
24     ld rs = sqrt(dfr);
25     Point diff = (c2.p - c1.p) / d;
26     res.emplace_back(c1.p + diff * Point(rc, rs));
27     if (dfr != 0.0)
28         res.emplace_back(c1.p + diff * Point(rc, -rs));
29     return res;
30 }
31
32 std::vector<Point> is_lc(Circle c, Line l)
33 {
34     std::vector<Point> res;
35     ld d = dist_lp(l, c.p);
36     if (d < c.r + eps)
37     {
38         ld len = (d > c.r) ? 0.0 : sqrt(c.r * c.r - d * d); //safety;
39         Point nor = (l.a - l.b) / abs(l.a - l.b);
40         res.emplace_back(proj(l, c.p) + len * nor);
41         res.emplace_back(proj(l, c.p) - len * nor);
42     }
43     return res;
44 }
45
46 std::vector<Point> is_sc(Circle c, Line l)
47 {
48     std::vector<Point> v = is_lc(c, l), res;
49     for (Point p : v)
50         if (isis_sp(l, p))
51             res.emplace_back(p);
52     return res;
53 }
54
55 // p から c への接線
56 std::vector<Line> tangent_cp(Circle c, Point p)
57 {
58     std::vector<Line> ret;
59     Point v = c.p - p;
60     ld d = abs(v);
61     ld l = sqrt(norm(v) - c.r * c.r);
62     if (isnan(l))
63     {
64         return ret;
65     }
66     Point v1 = v * Point(l / d, c.r / d);
67     Point v2 = v * Point(l / d, -c.r / d);
68     ret.emplace_back(Line(p, p + v1));
69     if (l < eps)
70         return ret;
71     ret.emplace_back(Line(p, p + v2));
72     return ret;
73 }
74
75 // c1, c2 の共通接線
76 std::vector<Line> tangent_cc(Circle c1, Circle c2)
77 {
78     std::vector<Line> ret;
79     if (abs(c1.p - c2.p) - (c1.r + c2.r) > -eps)
80     {
81         Point center = (c1.p * c2.r + c2.p * c1.r) / (c1.r + c2.r);
82         ret = tangent_cp(c1, center);
83     }
84     if (abs(c1.r - c2.r) > eps)
85     {
86         Point out = (-c1.p * c2.r + c2.p * c1.r) / (c1.r - c2.r);
87         std::vector<Line> nret = tangent_cp(c1, out);
88         ret.emplace(ret.end(), nret.begin(), nret.end());
89     }
90     else
91     {
92         Point v = c2.p - c1.p;
93         v /= abs(v);
94         Point q1 = c1.p + v * Point(0, 1) * c1.r;
95         Point q2 = c1.p + v * Point(0, -1) * c1.r;

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96     ret.emplace_back(Line(q1, q1 + v));  
97     ret.emplace_back(Line(q2, q2 + v));  
98 }  
99 return ret;  
100 }  
101
```