

# Computer Vision Assignment 5

April 14, 2019

```
In [37]: import cv2
import numpy as np
import matplotlib.pyplot as plt
import glob

plt.rcParams['figure.figsize'] = [14, 12]
```

## 0.1 Lucas Kanade Algorithm

The Lucas-Kanade optical flow algorithm is a simple technique which can provide an estimate of the movement of interesting features in successive images of a scene. We would like to associate a movement vector  $(u, v)$  to every such "interesting" pixel in the scene, obtained by comparing the two consecutive images.

The Lucas-Kanade algorithm makes some implicit assumptions:

- The two images are separated by a small time increment  $\Delta t$ , in such a way that objects have not displaced significantly (that is, the algorithm works best with slow moving objects).
- The images depict a natural scene containing textured objects exhibiting shades of gray (different intensity levels) which change smoothly.

The Lucas-Kanade method assumes that the displacement of the image contents between two nearby instants (frames) is small and approximately constant within a neighborhood of the point  $p$  under consideration. Thus the optical flow equation can be assumed to hold for all pixels within a window centered at  $p$ . Namely, the local image flow (velocity) vector  $(V_x, V_y)$  must satisfy

$$I_x(q_1)V_x + I_y(q_1)V_y = -I_t(q_1)$$

$$I_x(q_2)V_x + I_y(q_2)V_y = -I_t(q_2)$$

$$\vdots$$

$$I_x(q_n)V_x + I_y(q_n)V_y = -I_t(q_n)$$

where  $q_1, q_2, \dots, q_n$  are the pixels inside the window, and  $I_x(q_i), I_y(q_i), I_t(q_i)$  are the partial derivatives of the image  $I$  with respect to position  $x, y$  and time  $t$ , evaluated at the point  $q_i$  and at the current time.

These equations can be written in matrix form  $Av = b$ , where

$$A = \begin{bmatrix} I_x(q_1) & I_y(q_1) \\ I_x(q_2) & I_y(q_2) \\ \vdots & \vdots \\ I_x(q_n) & I_y(q_n) \end{bmatrix} \quad v = \begin{bmatrix} V_x \\ V_y \end{bmatrix} \quad b = \begin{bmatrix} -I_t(q_1) \\ -I_t(q_2) \\ \vdots \\ -I_t(q_n) \end{bmatrix}$$

This system has more equations than unknowns and thus it is usually over-determined. The Lucas–Kanade method obtains a compromise solution by the least squares principle. Namely, it solves the  $2 \times 2$  system

$$A^T A v = A^T b$$

$$v = (A^T A)^{-1} A^T b$$

That is, it computes

$$\begin{bmatrix} V_x \\ V_y \end{bmatrix} = \begin{bmatrix} \sum_i I_x(q_i)^2 & \sum_i I_x(q_i) I_y(q_i) \\ \sum_i I_y(q_i) I_x(q_i) & \sum_i I_y(q_i)^2 \end{bmatrix}^{-1} \begin{bmatrix} -\sum_i I_x(q_i) I_t(q_i) \\ -\sum_i I_y(q_i) I_t(q_i) \end{bmatrix}$$

```
In [2]: def lucas_kadane(frame1, frame2, win = 2):
    Ix = np.zeros(frame1.shape, dtype=np.float32)
    Iy = np.zeros(frame1.shape, dtype=np.float32)
    It = np.zeros(frame1.shape, dtype=np.float32)
    Ix[1:-1, 1:-1] = cv2.subtract(frame1[1:-1, 2:], frame1[1:-1, :-2]) / 2
    Iy[1:-1, 1:-1] = cv2.subtract(frame1[2:, 1:-1], frame1[:-2, 1:-1]) / 2
    It[1:-1, 1:-1] = cv2.subtract(frame1[1:-1, 1:-1], frame2[1:-1, 1:-1])

    params = np.zeros(frame1.shape + (5,))
    params[...] , 0] = Ix ** 2
    params[...] , 1] = Iy ** 2
    params[...] , 2] = Ix * Iy
    params[...] , 3] = Ix * It
    params[...] , 4] = Iy * It
    del It, Ix, Iy
    cum_params = np.cumsum(np.cumsum(params, axis=0), axis=1)
    del params
    win_params = (cum_params[2 * win + 1:, 2 * win + 1:] -
                  cum_params[2 * win + 1:, :-1 - 2 * win] -
                  cum_params[:-1 - 2 * win, 2 * win + 1:] +
                  cum_params[:-1 - 2 * win, :-1 - 2 * win])
    del cum_params
    op_flow = np.zeros(frame1.shape + (2,))
    det = win_params[...] , 0] * win_params[...] , 1] - win_params[...] , 2] ** 2

    op_flow_x = np.where(det != 0,
                          (win_params[...] , 1] * win_params[...] , 3] -
                           win_params[...] , 2] * win_params[...] , 4]) / det,
                          0)
    op_flow_y = np.where(det != 0,
                          (win_params[...] , 0] * win_params[...] , 4] -
                           win_params[...] , 2] * win_params[...] , 3]) / det,
                          0)
    op_flow[win + 1: -1 - win, win + 1: -1 - win, 0] = op_flow_x[:-1, :-1]
```

```

op_flow[win + 1: -1 - win, win + 1: -1 - win, 1] = op_flow_y[:-1, :-1]
op_flow = op_flow.astype(np.float32)
return op_flow

```

### 0.1.1 Draw Flow

```

In [3]: def draw_flow(img, flow, show=True):
        x = np.arange(0, img.shape[1], 1)
        y = np.arange(0, img.shape[0], 1)
        x, y = np.meshgrid(x, y)
        plt.figure()
        fig = plt.imshow(img, cmap='gray', interpolation='bicubic')
        plt.axis('off')
        fig.axes.get_xaxis().set_visible(False)
        fig.axes.get_yaxis().set_visible(False)
        step = img.shape[0] // 20
        plt.quiver(x[::step, ::step], y[::step, ::step],
                  flow[::step, ::step, 0], flow[::step, ::step, 1],
                  color='r', pivot='middle', headwidth=2, headlength=3)
        if show:
            plt.show()

```

### Illustration of optical flow on first set of image

```

In [10]: img11 = cv2.imread('eval-gray-twoframes/eval-data-gray/Army/frame10.png', 0)
        img12 = cv2.imread('eval-gray-twoframes/eval-data-gray/Army/frame11.png', 0)

```

```

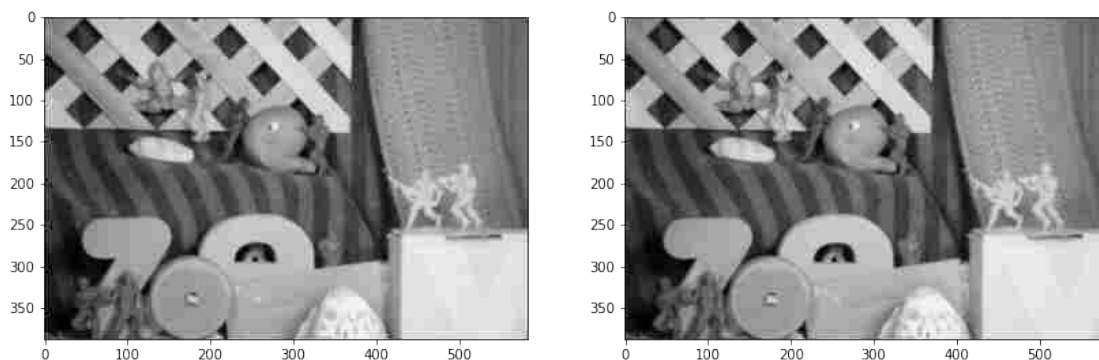
In [11]: fig, ax = plt.subplots(1,2)
        ax[0].imshow(img11, cmap='gray', interpolation='bicubic')
        ax[1].imshow(img12, cmap='gray', interpolation='bicubic')

```

```

Out[11]: <matplotlib.image.AxesImage at 0x7f4c7c5aa8d0>

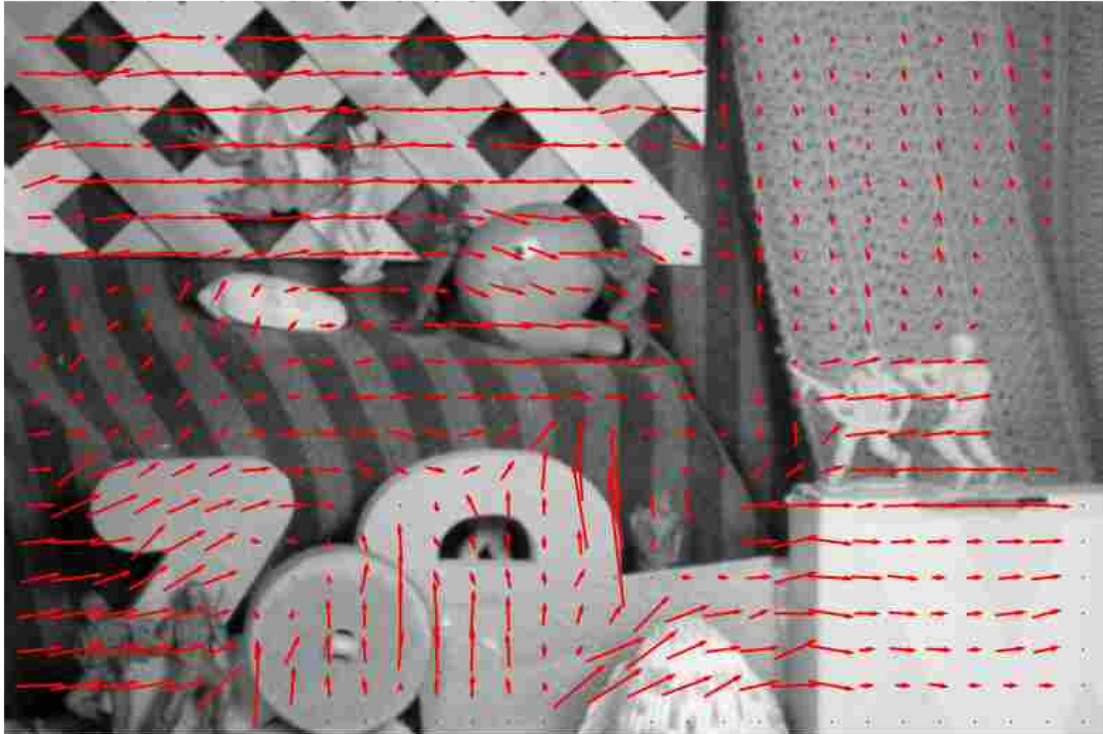
```



```

In [12]: flow1 = lucas_kadane(img11, img12, win=15)
        draw_flow(img11, flow1)

```

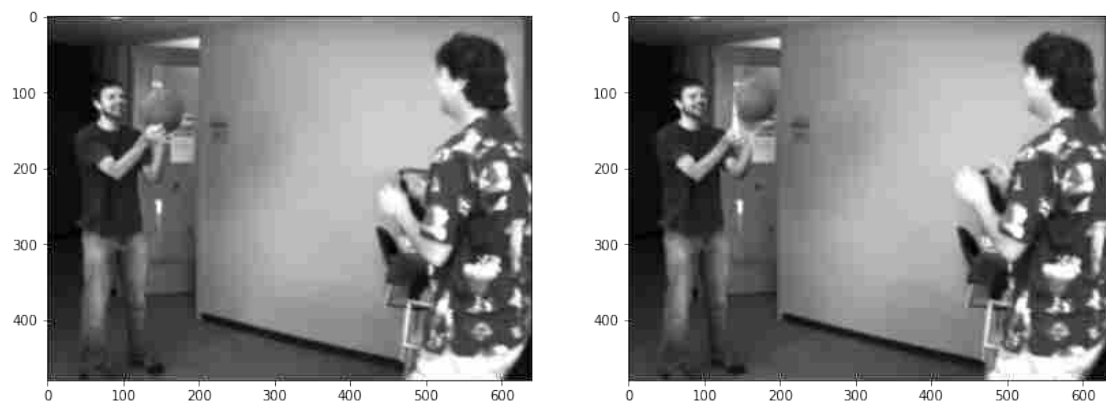


### Illustration of optical flow on second set of image

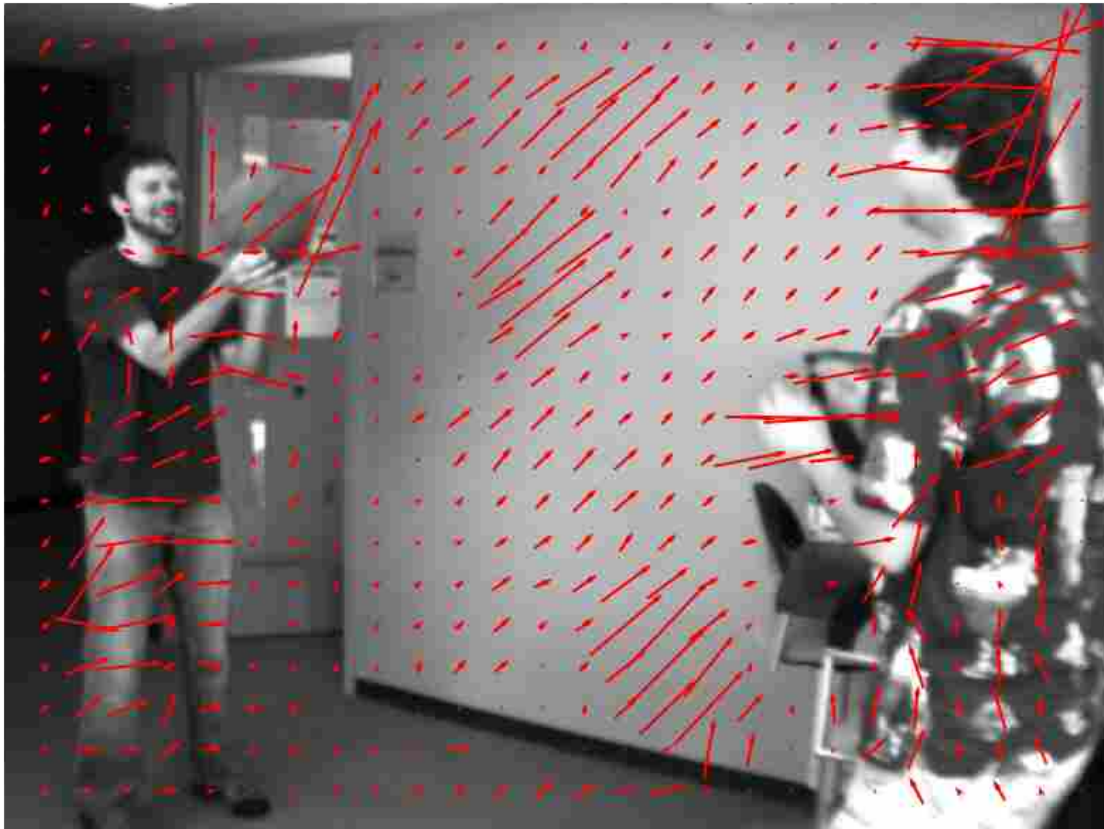
```
In [50]: img21 = cv2.imread('eval-gray-twoframes/eval-data-gray/Basketball//frame10.png', 0)
         img22 = cv2.imread('eval-gray-twoframes/eval-data-gray/Basketball//frame11.png', 0)
```

```
In [51]: fig, ax = plt.subplots(1,2)
         ax[0].imshow(img21, cmap='gray', interpolation='bicubic')
         ax[1].imshow(img22, cmap='gray', interpolation='bicubic')
```

```
Out[51]: <matplotlib.image.AxesImage at 0x7f6dc38736a0>
```



```
In [57]: flow2 = lucas_kadane(img21, img22, win=15)
         draw_flow(img21, flow2)
```



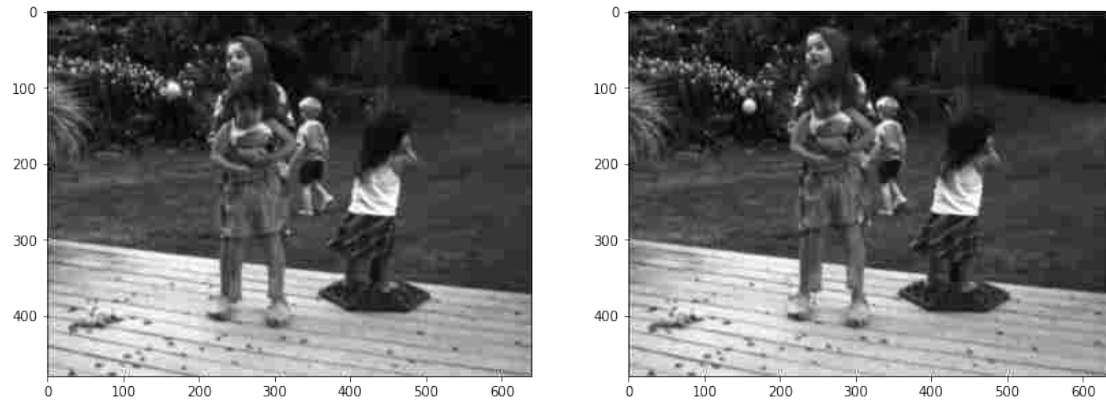
### Illustration of optical flow on third set of image

```
In [55]: img31 = cv2.imread('eval-gray-twoframes/eval-data-gray/Backyard//frame10.png', 0)
         img32 = cv2.imread('eval-gray-twoframes/eval-data-gray/Backyard//frame11.png', 0)
```

```
In [56]: fig, ax = plt.subplots(1,2)
         ax[0].imshow(img31, cmap='gray', interpolation='bicubic')
         ax[1].imshow(img32, cmap='gray', interpolation='bicubic')
```

```
Out[56]: <matplotlib.image.AxesImage at 0x7f6dc3659780>
```





```
In [59]: flow3 = lucas_kadane(img31,img32, win=15)
         draw_flow(img31, flow3)
```

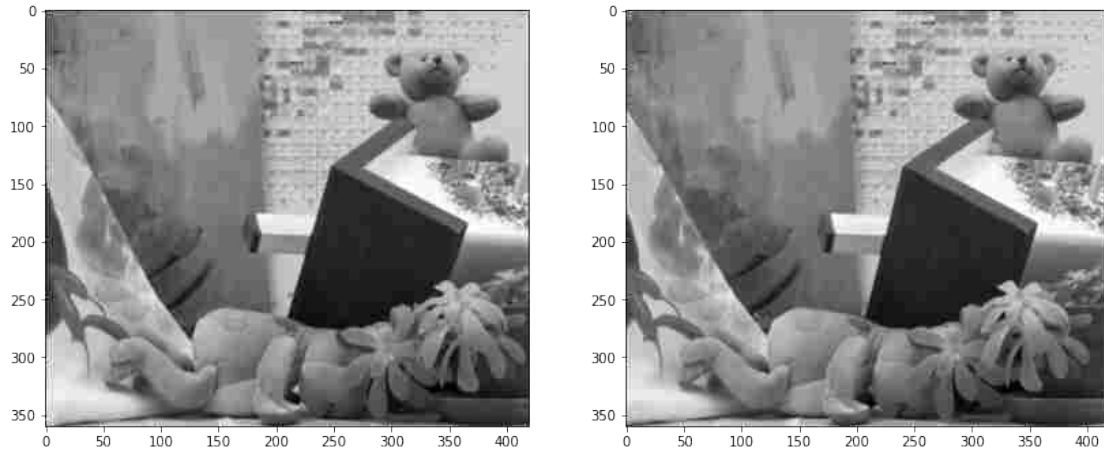


**Illustration of optical flow on first set of image**

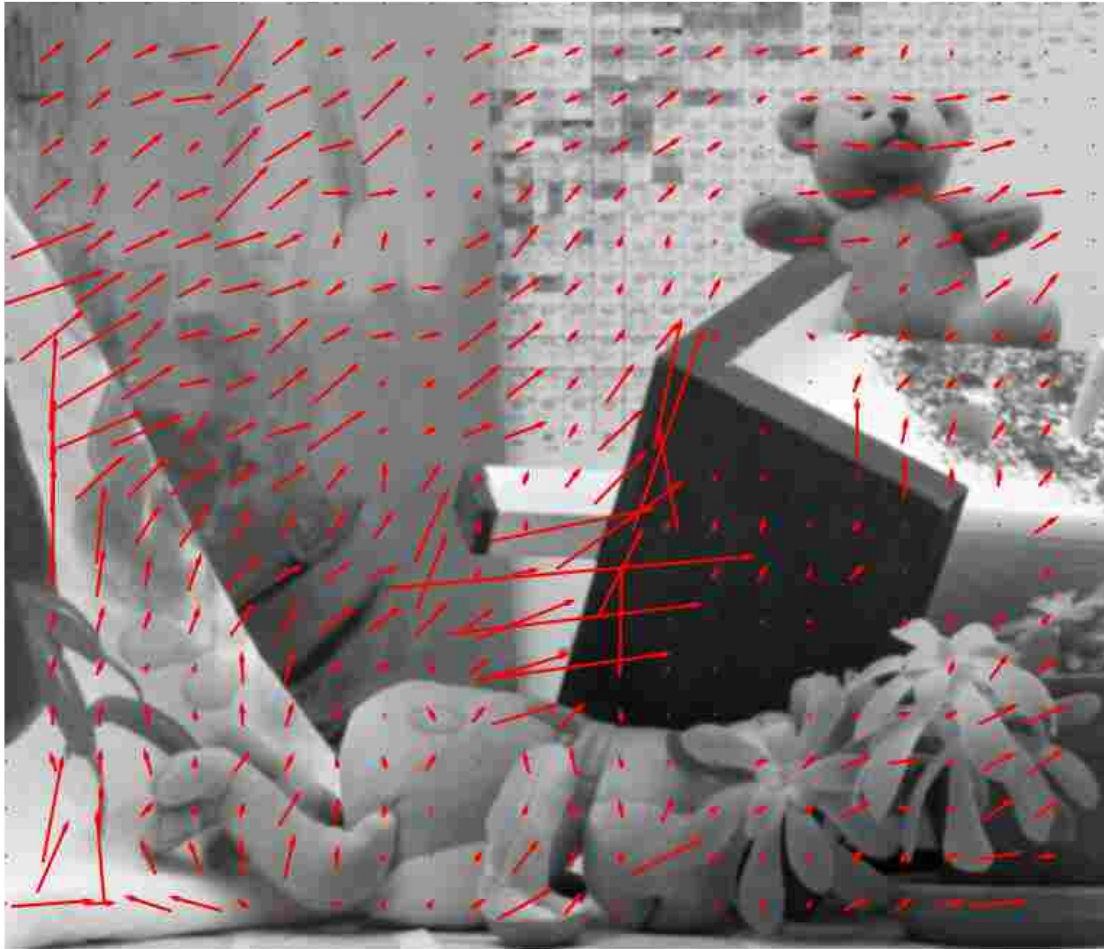
```
In [60]: img41 = cv2.imread('eval-gray-twoframes/eval-data-gray/Teddy/frame10.png', 0)
         img42 = cv2.imread('eval-gray-twoframes/eval-data-gray/Teddy/frame11.png', 0)
```

```
In [61]: fig, ax = plt.subplots(1,2)
         ax[0].imshow(img41, cmap='gray', interpolation='bicubic')
         ax[1].imshow(img42, cmap='gray', interpolation='bicubic')
```

```
Out[61]: <matplotlib.image.AxesImage at 0x7f6dc329a518>
```



```
In [62]: flow4 = lucas_kadane(img41, img42, win=15)
         draw_flow(img41, flow4)
```



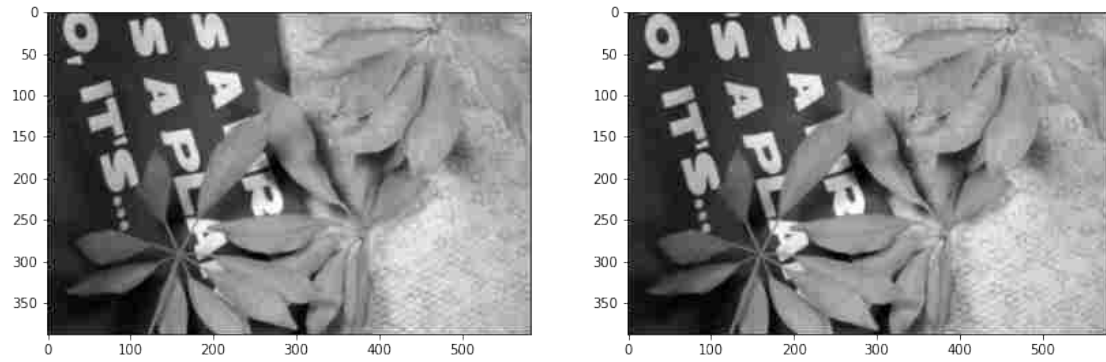
### Illustration of optical flow on first set of image

```
In [63]: img51 = cv2.imread('eval-gray-twoframes/eval-data-gray/Schefflera/frame10.png', 0)
         img52 = cv2.imread('eval-gray-twoframes/eval-data-gray/Schefflera/frame11.png', 0)
```

```
In [64]: fig, ax = plt.subplots(1,2)
         ax[0].imshow(img51, cmap='gray', interpolation='bicubic')
         ax[1].imshow(img52, cmap='gray', interpolation='bicubic')
```

```
Out[64]: <matplotlib.image.AxesImage at 0x7f6dc3199780>
```





```
In [65]: flow5 = lucas_kadane(img51,img52, win=15)
         draw_flow(img51, flow5)
```



## 0.2 Optical Flow to detect and segment moving objects in a video frame

To detect and segment moving objects in a frame, algorithm is: - Find magnitude and angle of flow - Convert  $\text{hsv}[\dots, 0]$  to  $\text{ang} \cdot 180 / \text{np.pi} / 2$ , where  $\text{hsv}$  is array with shape of input frame and  $\text{ang}$  is angle for flow - Convert  $\text{hsv}[\dots, 1]$  to 255 - Convert  $\text{hsv}[\dots, 2]$  to normalized magnitude - Convert this hsv to BGR form and return the image

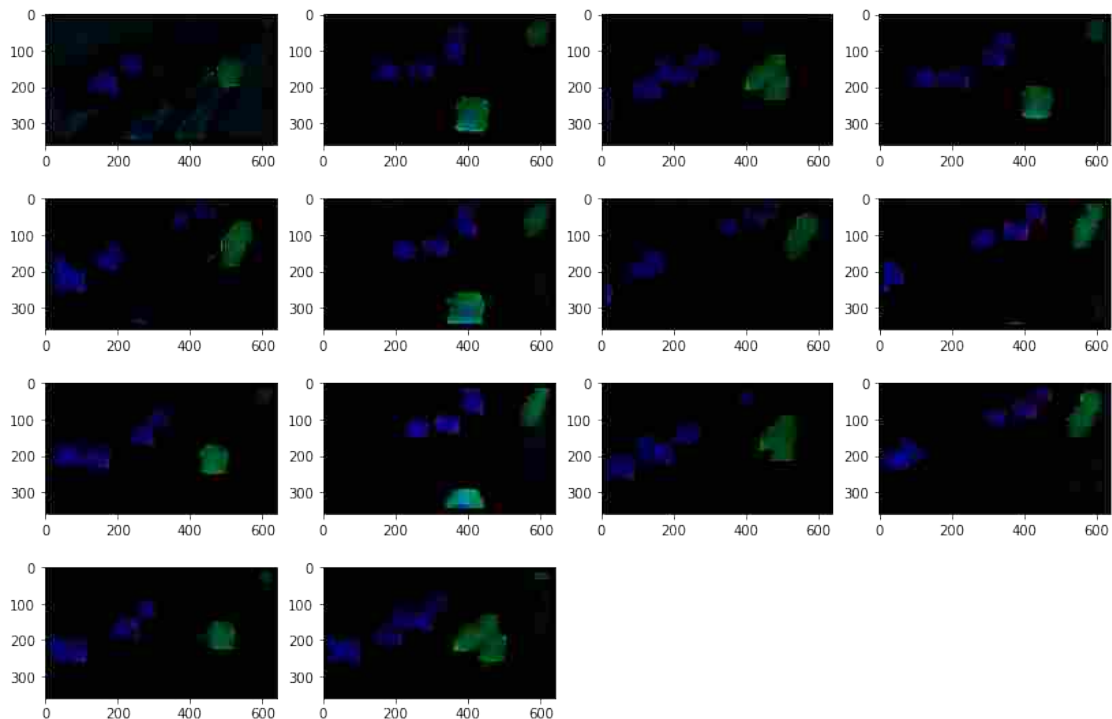
## 0.2.1 Detect and segment moving objects

```
In [3]: def draw_hsv(flow, img):
        hsv = np.zeros_like(img)
        mag, ang = cv2.cartToPolar(flow[...,0], flow[...,1])
        hsv[...,0] = ang*180/np.pi/2
        hsv[...,1] = 255
        hsv[...,2] = cv2.normalize(mag, None, 0, 255, cv2.NORM_MINMAX)
        bgr = cv2.cvtColor(hsv, cv2.COLOR_HSV2BGR)
        #cv2.imshow('hsv', bgr)
        return bgr
```

## 0.2.2 Results

```
In [76]: imageshsv = [cv2.imread(file) for file in glob.glob('output/imageshsv/*.png')]
```

```
In [77]: w=10
        h=10
        fig=plt.figure(figsize=(14, 12))
        columns = 4
        rows = 5
        for i in range(0, len(imageshsv)):
            img = np.random.randint(10, size=(h,w))
            fig.add_subplot(rows, columns, i+1)
            plt.imshow(imageshsv[i])
        plt.show()
```



### 0.3 Optical Flow to track moving objects in a video frame

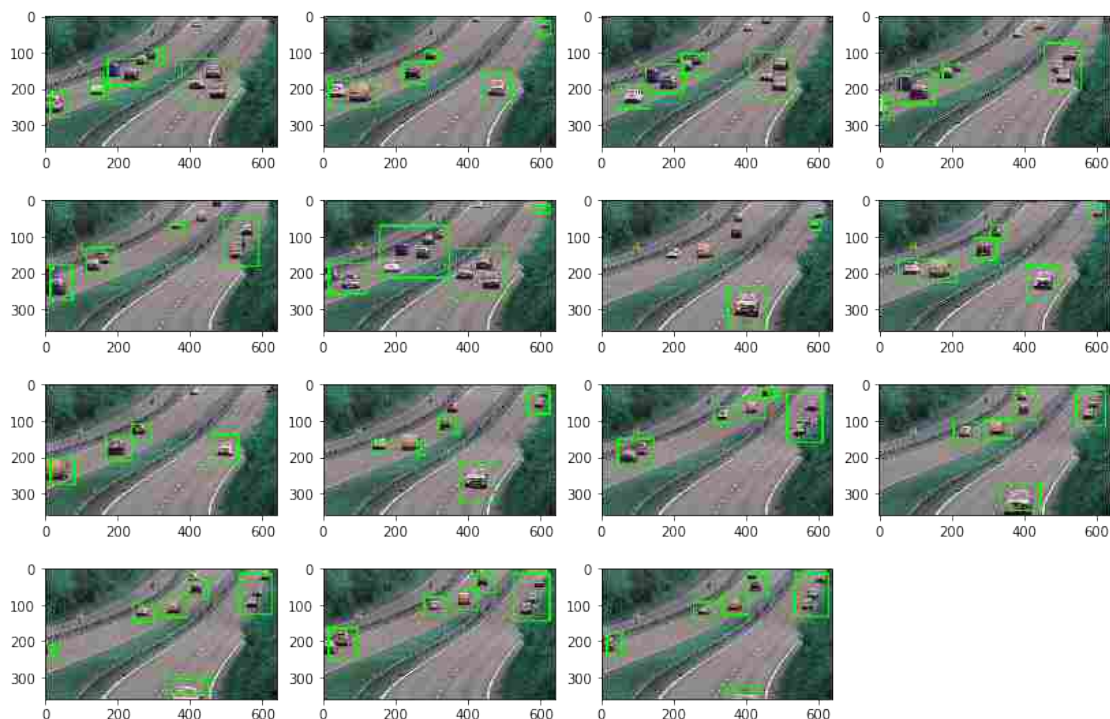
To track moving objects, the algorithm used is: - Segment the moving object first - Use `cv2.threshold` to check pixels that has value above `cv2.THRESH_BINARY` - Dilate this thresh image - Find contour in this threshold image - For each contour if the bounding box has width and height than 15 we draw the bounding box around the moving object

```
In [75]: def track_moving_objects(frame, flow):
        hsv1 = draw_hsv(flow, prev)
        gray1 = cv2.cvtColor(hsv1, cv2.COLOR_BGR2GRAY)
        thresh = cv2.threshold(gray1, 25, 0xFF,
                               cv2.THRESH_BINARY)[1]
        thresh = cv2.dilate(thresh, None, iterations=2)
        gray2, cnts, hierarchy = cv2.findContours(thresh.copy(), cv2.RETR_EXTERNAL, cv2.CHAIN_APPROX_SIMPLE)

        # loop over the contours
        for c in cnts:
            # if the contour is too small, ignore it
            (x, y, w, h) = cv2.boundingRect(c)
            if w > 15 and h > 15 and w < 900 and h < 680:
                cv2.rectangle(vis, (x, y), (x + w, y + h), (0, 0xFF, 0), 4)

In [78]: imagestack = [cv2.imread(file) for file in glob.glob('output/imagetrack/*.png')]

In [79]: w=10
        h=10
        fig=plt.figure(figsize=(14, 12))
        columns = 4
        rows = 5
        for i in range(0, len(imagestack)):
            img = np.random.randint(10, size=(h,w))
            fig.add_subplot(rows, columns, i+1)
            plt.imshow(imagestack[i])
        plt.show()
```



## 0.4 Analyze how does your algorithm work when camera is moving.

Observation when camera is moving: - The camera movement leads to movement of whole frame captured by the camera - This leads to optical flow being observed in whole frame - Image segmentation isn't that good, because even the background is moving - Tracking foreground moving objects is difficult because even the background is seen moving

### 0.4.1 Results

#### Optical flow

```
In [45]: imagesflow = [cv2.imread(file) for file in glob.glob('output/imageflow/*.png')]
```

```
In [51]: w=25
         h=25
         fig=plt.figure(figsize=(28, 24))
         columns = 4
         rows = (len(imagesflow)//4 + 1)
         for i in range(0, len(imagesflow)):
             fig.add_subplot(rows, columns, i+1)
             plt.imshow(imagesflow[i])
         plt.show()
```

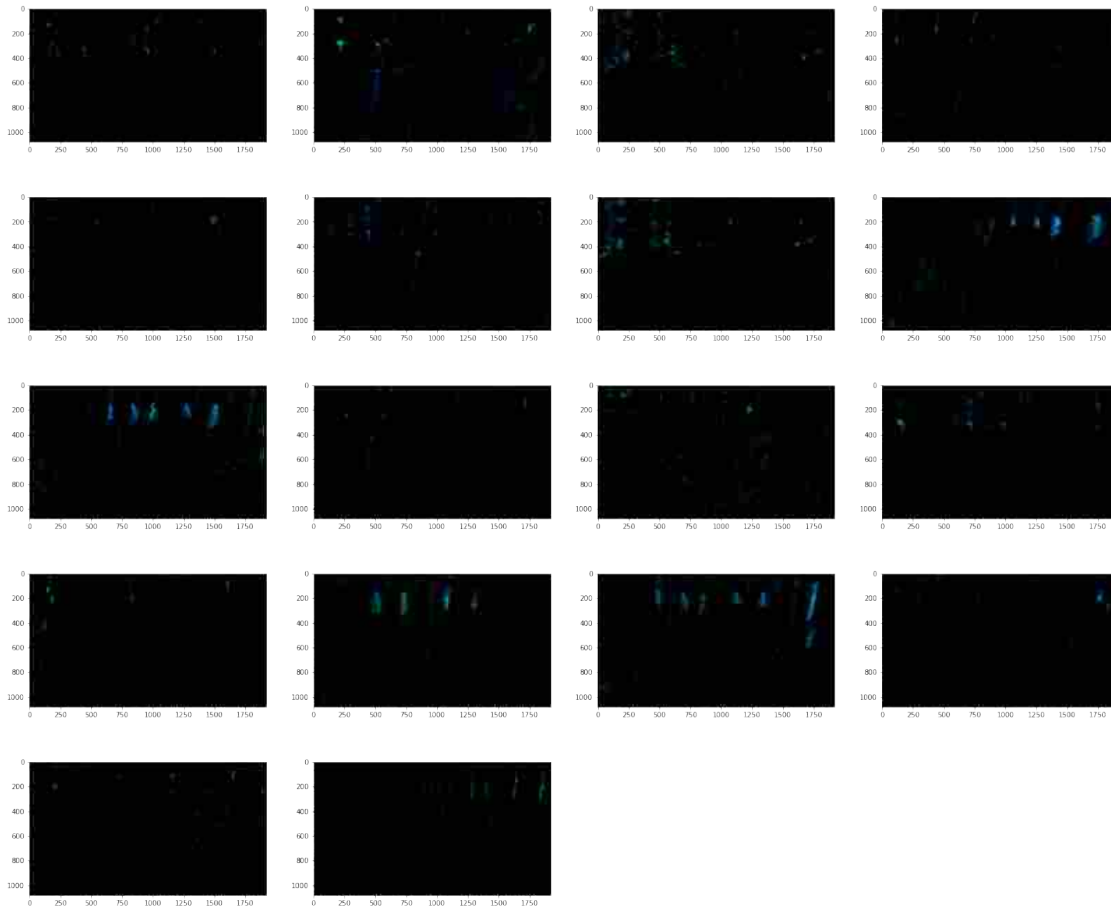


## Image segmentation

```
In [52]: imageshsv = [cv2.imread(file) for file in glob.glob('output/imageshv/*.png')]
```

```
In [53]: w=25
          h=25
          fig=plt.figure(figsize=(28, 24))
          columns = 4
          rows = (len(imageshsv)//4 +1)
          for i in range(0, len(imageshsv)):
              img = np.random.randint(10, size=(h,w))
              fig.add_subplot(rows, columns, i+1)
              plt.imshow(imageshsv[i])
          plt.show()
```





## Tracking moving objects

In [62]: `imagetrack = [cv2.imread(file) for file in glob.glob('output/imagetrack/*.png')]`

```
In [63]: w=25
          h=25
          fig=plt.figure(figsize=(28, 24))
          columns = 4
          rows = (len(imagetrack)//4 + 1)
          for i in range(0, len(imagetrack)):
              img = np.random.randint(10, size=(h,w))
              fig.add_subplot(rows, columns, i+1)
              plt.imshow(imagetrack[i])
          plt.show()
```



In [ ]: