

## Scheduling Algorithms

This document provides pseudo codes representing the implemented algorithms, that we consider in our simulation study. In Table 1, we explain the notations used in the description of these algorithms.

Notation	Description
$l(m_i)$	Remaining load on core $m_i$
$L$	Maximum load caused by the new job
$d_{lim}$	Deadline threshold
$t_{i,j}$	Total idle time caused by allocating multi-core job $j$ to core $m_i$

Table 1: Definition of notations used in the description of algorithms

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### Algorithm 1 Greedy Balanced

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```

1: initialize  $l(m_h) = 0$  for all cores
2: for the next job  $j$  do
3:   update  $l(m_h)$  for all cores
4:    $L = l(m_{c_j}) + p_j$ 
5:   if  $L \leq d_j - r_j$  then
6:     accept  $j$ 
7:     allocate  $j$  to cores  $m_1$  to  $m_{c_j}$ 
8:     update  $l(m_h)$  to  $L$  for  $1 \leq h \leq c_j$ 
9:     sort all cores in increasing order of  $l(m_h)$ 
10:  else
11:    reject  $j$ 

```

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### Algorithm 2 Greedy BestFit

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```

1: initialize  $l(m_h) = 0$  for all cores
2: for the next job  $j$  do
3:   update  $l(m_h)$  for all cores
4:   if  $l(m_{c_j}) + p_j + r_j \leq d_j$  then
5:     accept  $j$ 
6:      $m_i$ : last core with  $d_j - r_j \geq l(m_i) + p_j$ 
7:      $L = l(m_i) + p_j$ 
8:     allocate  $j$  to cores  $m_{i-c_j+1}$  to  $m_i$ 
9:     update  $l(m_h)$  to  $L$  for  $i - c_j + 1 \leq h \leq i$ 
10:    sort all cores in increasing order of  $l(m_h)$ 
11:  else
12:    reject  $j$ 

```

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**Algorithm 3** Threshold

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```
1: initialize  $l(m_h) = 0$  for all cores and  $d_{lim} = 0$ 
2: for the next job  $j$  do
3:   update  $l(m_h)$  for all cores
4:   determine  $d_{lim}$ 
5:   if  $d_j < d_{lim}$  then
6:     reject  $j$ 
7:   else
8:     accept  $j$ 
9:     use the allocation part of Algorithm 2
```

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**Algorithm 4** Greedy MinIdle

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```
1: initialize  $l(m_h) = 0$  for all cores
2: for the next job  $j$  do
3:   update  $l(m_h)$  for all cores
4:    $L = l(m_{c_j}) + p_j$ 
5:   if  $L \leq d_j - r_j$  then
6:     accept  $j$ 
7:     for all  $m_i$  in  $c_j \leq i \leq m$  do
8:       determine  $L = l(m_i) + p_j$ 
9:       if  $L \leq d_j - r_j$  then
10:        initialize  $t_{i,j} = 0$ 
11:        for all  $m_a$  in  $i - c_j + 1 \leq a \leq i$  do
12:           $t_{i,j} = t_{i,j} + l(m_i) - l(m_a)$ 
13:        determine  $m_i$  with  $\min_i \{t_{i,j}\}$ 
14:        allocate  $j$  to cores  $m_{i-c_j+1}$  to  $m_i$ 
15:        update  $l(m_a)$  to  $L$  for  $i - c_j + 1 \leq a \leq i$ 
16:        sort all cores in increasing order of  $l(m_h)$ 
17:   else
18:     reject  $j$ 
```

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**Algorithm 5** Greedy Balanced BackFill

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```
1: initialize  $l(m_h) = 0$  for all cores
2: for the next job  $j$  do
3:   if backfilling is possible then
4:     allocate  $j$  via backfilling
5:   else
6:     apply Algorithm 1
```

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**Algorithm 6** Greedy BestFit BackFill

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```
1: initialize  $l(m_h) = 0$  for all cores
2: for the next job  $j$  do
3:   if backfilling is possible then
4:     allocate  $j$  via backfilling
5:   else
6:     apply Algorithm 2
```

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