

GARCH_USD/EUR_RATE

Load data & Unit Root Test

```
library(vars)
```

```
## Loading required package: MASS
## Loading required package: strucchange
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##   as.Date, as.Date.numeric
## Loading required package: sandwich
## Loading required package: urca
## Loading required package: lmtest
```

```
library(quantmod)
```

```
## Loading required package: xts
## Loading required package: TTR
## Registered S3 method overwritten by 'quantmod':
##   method             from
##   as.zoo.data.frame zoo
## Version 0.4-0 included new data defaults. See ?getSymbols.
```

```
library(parallel)
```

```
library(rugarch)
```

```
##
## Attaching package: 'rugarch'
## The following object is masked from 'package:stats':
##
##   sigma
```

```
library(rmgarch)
```

```
##
## Attaching package: 'rmgarch'
```

```

## The following objects are masked from 'package:xts':
##
##     first, last
library(tseries)
library(zoo)
library(forecast)

## Registered S3 methods overwritten by 'forecast':
##   method          from
##   fitted.fracdiff  fracdiff
##   residuals.fracdiff fracdiff
library(fGarch)

## Loading required package: timeDate
## Loading required package: timeSeries
##
## Attaching package: 'timeSeries'
## The following object is masked from 'package:zoo':
##
##     time<-
## Loading required package: fBasics
##
## Attaching package: 'fBasics'
## The following object is masked from 'package:TTR':
##
##     volatility
library(FinTS)

##
## Attaching package: 'FinTS'
## The following object is masked from 'package:forecast':
##
##     Acf
library(lmtest)
library(urca)
library(xts)
library(Metrics)

##
## Attaching package: 'Metrics'
## The following object is masked from 'package:forecast':
##
##     accuracy
library(DistributionUtils)

##
## Attaching package: 'DistributionUtils'
## The following object is masked from 'package:fBasics':

```

```

##
##      tsHessian

## The following objects are masked from 'package:timeDate':
##
##      kurtosis, skewness

library(readxl)
library(fUnitRoots)

##
## Attaching package: 'fUnitRoots'

## The following objects are masked from 'package:urca':
##
##      punitroot, qunitroot, unitrootTable

ratedata = read.csv("D:/2019-2020/Time Series/hw/group/rate.csv")
rate = xts(ratedata$currency.rate, as.Date(ratedata$i..DATE, format='%m/%d/%y', tz = "US"))
rate_train = rate[1:1080]
rate_test = rate[1081:1343]
#head(rate_train)
#tail(rate_train)
#head(rate_test)
#tail(rate_test)

df = read.csv("D:/2019-2020/Time Series/hw/group/data.csv")
data = ts(df[2:10], start = c(2015, 1), end = c(2020, 2), frequency=12)
head(data)

##           M1_US   M1_EU   GDP_US   GDP_EU   CPI_US   CPI_EU   XAU_USD   WTI_USD   RATE
## Jan 2015 2941.1 6031.11 17984.18 99.6455 99.0423 98.24 1251.57 47.2480 0.8603
## Feb 2015 2979.6 6061.48 17984.18 99.6860 99.2933 98.85 1227.08 50.7400 0.8808
## Mar 2015 3023.9 6119.64 17984.18 99.7202 99.5608 100.00 1179.55 48.0423 0.9237
## Apr 2015 3035.4 6203.81 18219.40 99.7481 99.6646 100.43 1200.30 54.6200 0.9245
## May 2015 2975.9 6302.87 18219.40 99.7713 99.9932 100.71 1199.07 59.4310 0.8964
## Jun 2015 3020.7 6361.57 18219.40 99.7918 100.2700 100.72 1182.39 59.7718 0.8901

M1_US_rt = dailyReturn(data[, 1])
M1_EU_rt = dailyReturn(data[, 2])
GDP_US_rt = dailyReturn(data[, 3])
GDP_EU_rt = dailyReturn(data[, 4])
CPI_US_rt = dailyReturn(data[, 5])
CPI_EU_rt = dailyReturn(data[, 6])
XAU_USD_rt = dailyReturn(data[, 7])
WTI_USD_rt = dailyReturn(data[, 8])
RATE_rt = dailyReturn(data[, 9])

df_US = read_excel("D:/2019-2020/Time Series/hw/group/US_part.xlsx", sheet=1, na="NA")
data_US = ts(df_US[2:4], start = c(2011, 1), end = c(2020, 2), frequency = 12)
#head(data_US)
M1_US1_rt = dailyReturn(data_US[, 1])
CPI_US1_rt = dailyReturn(data_US[, 2])
RATE1_rt = dailyReturn(data_US[, 3])

df_D = read_excel("D:/2019-2020/Time Series/hw/group/DAILY_part.xlsx", sheet=1, na="NA")
data_D = xts(df_D[, 2:4], as.Date(df_D$DATE, format='%m/%d/%y', tz = "US"))

```

```
#head(data_D)
XAU_USD1_rt = dailyReturn(data_D$XAU_USD, type = "log")
WTI_USD1_rt = dailyReturn(data_D$WTI_USD, type = "log")
RATE2_rt = dailyReturn(data_D`currency rate`, type = "log")
```

```
adfTest(M1_US_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -6.4703
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(M1_EU_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -2.8249
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(GDP_US_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -5.0516
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(GDP_EU_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -1.0457
## P VALUE:
## 0.2793
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(CPI_US_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -2.7051
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(CPI_EU_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -5.4888
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(XAU_USD_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
```

```
##
## Test Results:
##   PARAMETER:
##     Lag Order: 1
##   STATISTIC:
##     Dickey-Fuller: -4.7869
##   P VALUE:
##     0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(WTI_USD_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
##   PARAMETER:
##     Lag Order: 1
##   STATISTIC:
##     Dickey-Fuller: -5.2505
##   P VALUE:
##     0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(RATE_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
##   PARAMETER:
##     Lag Order: 1
##   STATISTIC:
##     Dickey-Fuller: -5.3706
##   P VALUE:
##     0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

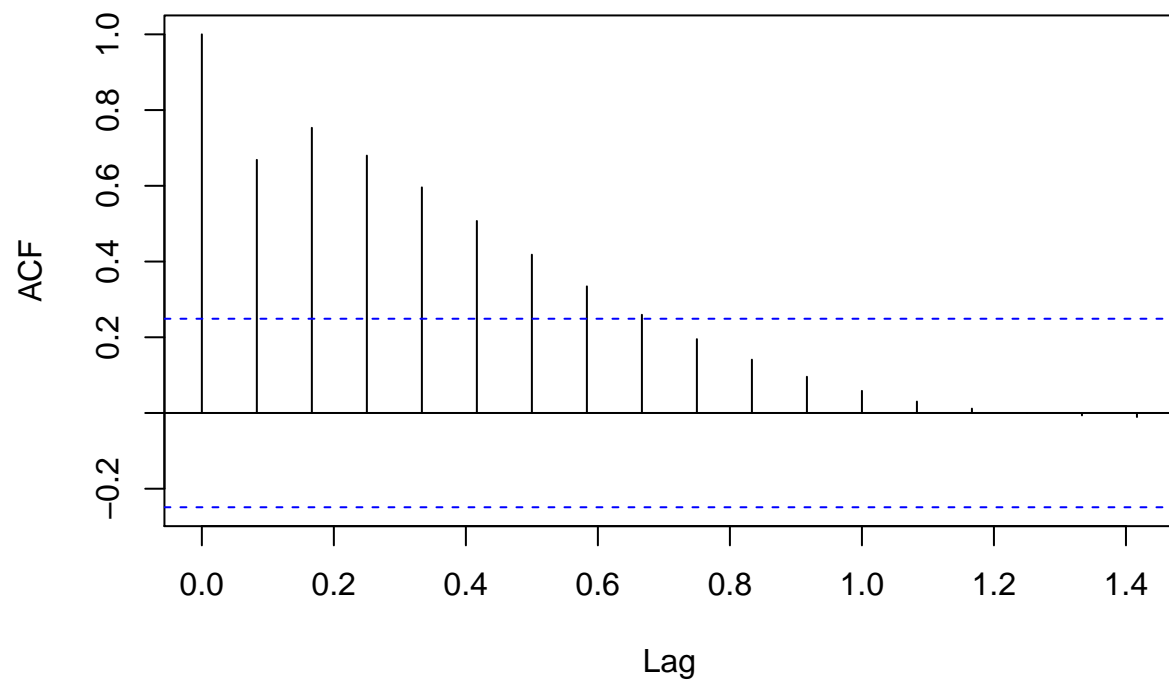
```
GDP_EU_sta = ur.df(GDP_EU_rt, type='none', selectlags='AIC')
summary(GDP_EU_sta)
```

```
##
## #####
## # Augmented Dickey-Fuller Test Unit Root Test #
## #####
##
## Test regression none
##
```

```
##
## Call:
## lm(formula = z.diff ~ z.lag.1 - 1 + z.diff.lag)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -8.207e-04 -1.803e-04 -3.924e-05  6.816e-05  1.858e-03
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## z.lag.1      -0.08348    0.07983  -1.046    0.3
## z.diff.lag  -1.04775    0.17428  -6.012  1.3e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.00035 on 58 degrees of freedom
## Multiple R-squared:  0.4326, Adjusted R-squared:  0.413
## F-statistic: 22.11 on 2 and 58 DF,  p-value: 7.307e-08
##
##
## Value of test-statistic is: -1.0457
##
## Critical values for test statistics:
##      1pct  5pct 10pct
## tau1 -2.6 -1.95 -1.61
```

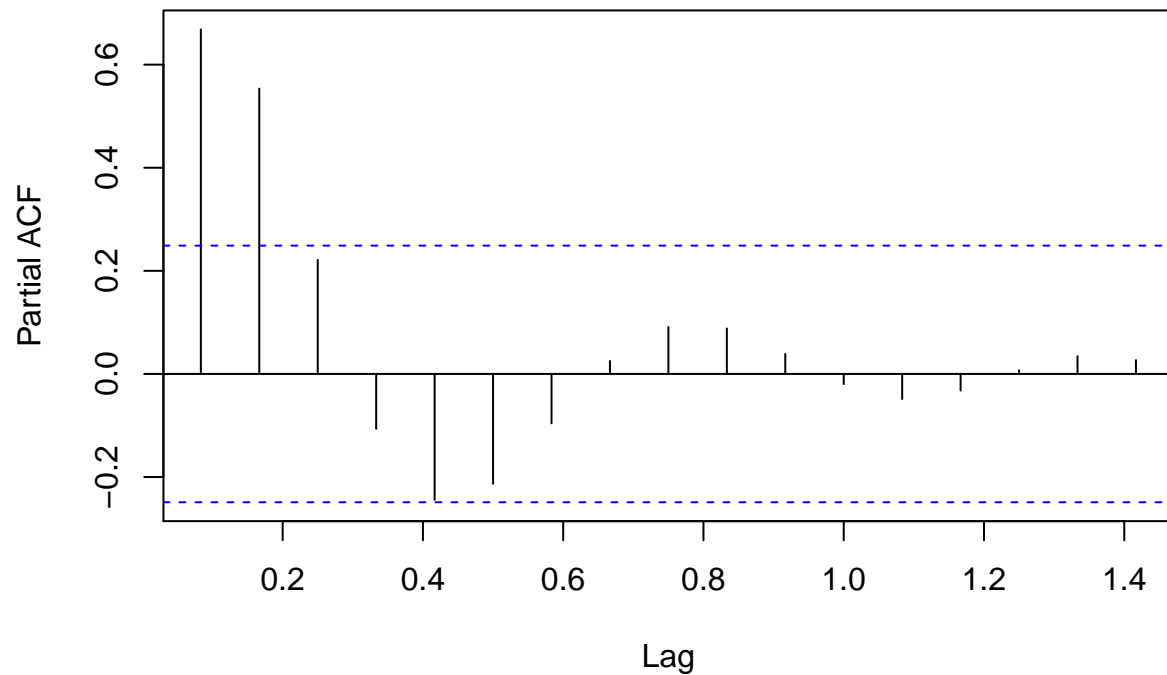
`acf(GDP_EU_rt)`

Series GDP_EU_rt



```
pacf(GDP_EU_rt)
```

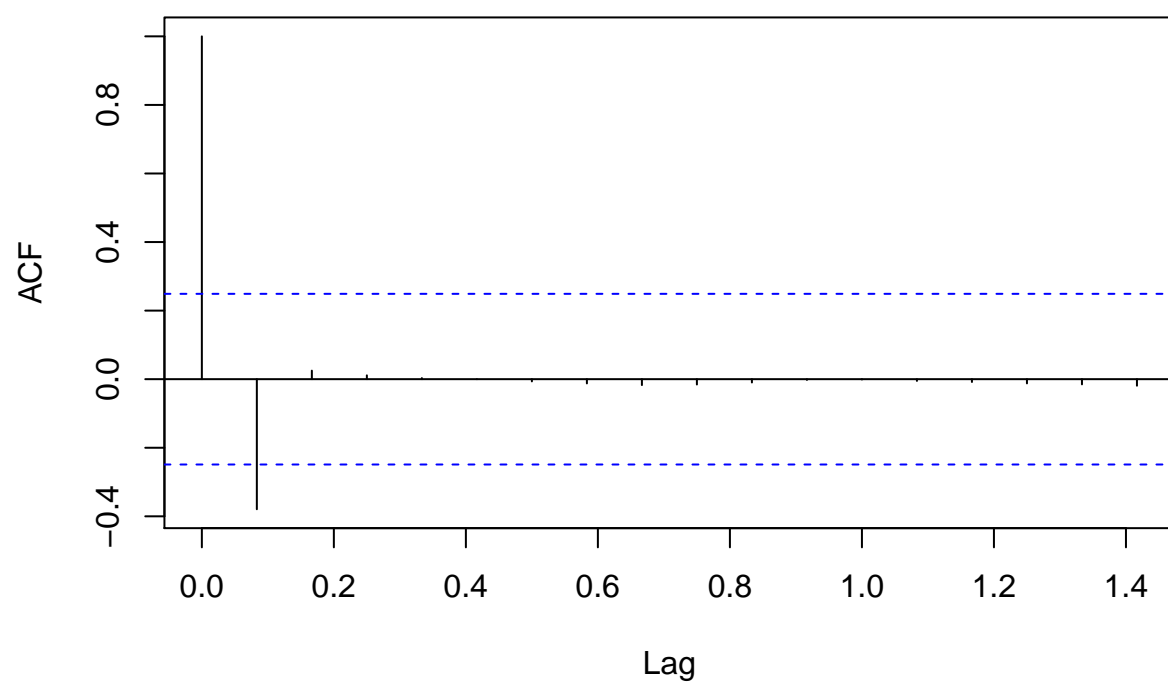

Series GDP_EU_rt



```
GDP_EU_rt_dif = diff(GDP_EU_rt, 1)
adfTest(GDP_EU_rt_dif)
```

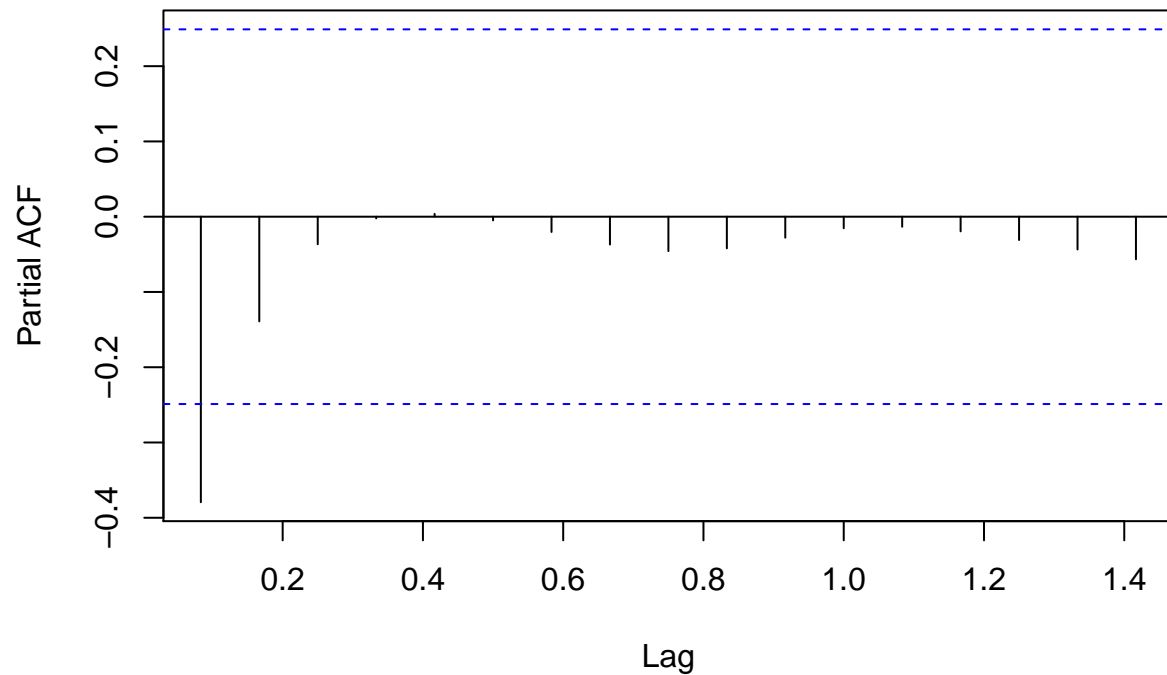
```
##
## Title:
##   Augmented Dickey-Fuller Test
##
## Test Results:
##   PARAMETER:
##     Lag Order: 1
##   STATISTIC:
##     Dickey-Fuller: -2.4217
##   P VALUE:
##     0.01791
##
## Description:
##   Thu Apr 30 20:18:13 2020 by user: yangm
acf(GDP_EU_rt_dif, na.action = na.pass)
```

Series GDP_EU_rt_dif



```
pacf(GDP_EU_rt_dif, na.action = na.pass)
```

Series GDP_EU_rt_dif



```
GDP_EU_rt_dif[1] = 0
data_rt = cbind(M1_US_rt, M1_EU_rt, GDP_US_rt, GDP_EU_rt_dif, CPI_US_rt, CPI_EU_rt, XAU_USD_rt, WTI_USD_rt, RATE_rt)
names(data_rt) = c("M1_US", "M1_EU", "GDP_US", "GDP_EU", "CPI_US", "CPI_EU", "XAU_USD", "WTI_USD", "RATE")
head(data_rt)
```

```
##           M1_US      M1_EU      GDP_US      GDP_EU      CPI_US
## Jan 2015  0.000000000 0.000000000 0.00000000  0.000000e+00 0.000000000
## Feb 2015  0.013090340 0.005035557 0.00000000  4.064408e-04 0.002534271
## Mar 2015  0.014867767 0.009595016 0.00000000 -6.336357e-05 0.002694039
## Apr 2015  0.003803036 0.013754077 0.01307966 -6.329443e-05 0.001042579
## May 2015 -0.019602029 0.015967607 0.00000000 -4.719695e-05 0.003297058
## Jun 2015  0.015054269 0.009313218 0.00000000 -2.711597e-05 0.002768188
##           CPI_EU      XAU_USD      WTI_USD      RATE
## Jan 2015  0.000000e+00 0.000000000 0.000000000  0.000000000
## Feb 2015  6.209283e-03 -0.019567423 0.073907890  0.0238288969
## Mar 2015  1.163379e-02 -0.038734231 -0.053167127  0.0487057221
## Apr 2015  4.300000e-03 0.017591454 0.136914761  0.0008660821
## May 2015  2.788012e-03 -0.001024744 0.088081289 -0.0303948080
## Jun 2015  9.929501e-05 -0.013910781 0.005734381 -0.0070281124
```

```
data_rt_train = data_rt[1:50]
data_rt_test = data_rt[51:62]
head(data_rt_train)
```

```
##           M1_US      M1_EU      GDP_US      GDP_EU      CPI_US
## Jan 2015  0.000000000 0.000000000 0.00000000  0.000000e+00 0.000000000
## Feb 2015  0.013090340 0.005035557 0.00000000  4.064408e-04 0.002534271
```

```
## Mar 2015 0.014867767 0.009595016 0.00000000 -6.336357e-05 0.002694039
## Apr 2015 0.003803036 0.013754077 0.01307966 -6.329443e-05 0.001042579
## May 2015 -0.019602029 0.015967607 0.00000000 -4.719695e-05 0.003297058
## Jun 2015 0.015054269 0.009313218 0.00000000 -2.711597e-05 0.002768188
##          CPI_EU      XAU_USD      WTI_USD      RATE
## Jan 2015 0.000000e+00 0.000000000 0.000000000 0.000000000
## Feb 2015 6.209283e-03 -0.019567423 0.073907890 0.0238288969
## Mar 2015 1.163379e-02 -0.038734231 -0.053167127 0.0487057221
## Apr 2015 4.300000e-03 0.017591454 0.136914761 0.0008660821
## May 2015 2.788012e-03 -0.001024744 0.088081289 -0.0303948080
## Jun 2015 9.929501e-05 -0.013910781 0.005734381 -0.0070281124
```

```
tail(data_rt_train)
```

```
##          M1_US      M1_EU      GDP_US      GDP_EU      CPI_US
## Sep 2018 -0.003960826 0.0087118555 0.000000000 1.171062e-04 1.413229e-03
## Oct 2018 0.012774071 0.0009322294 0.007135121 1.033482e-04 2.045445e-03
## Nov 2018 -0.011241394 0.0118258355 0.000000000 6.661096e-05 -4.547615e-04
## Dec 2018 0.032693249 0.0056064240 0.000000000 1.185759e-05 -3.564701e-05
## Jan 2019 -0.013537716 -0.0046682541 0.009619336 -4.496457e-05 -4.080790e-04
## Feb 2019 -0.011560848 0.0049636199 0.000000000 -1.008665e-04 2.499214e-03
##          CPI_EU      XAU_USD      WTI_USD      RATE
## Sep 2018 0.0039419287 -0.001924455 0.031029314 -0.0094710095
## Oct 2018 0.0024899445 0.014440373 0.005364252 0.0145755597
## Nov 2018 -0.0055406955 0.004525520 -0.199687884 0.0114929318
## Dec 2018 -0.0004803074 0.025408943 -0.135881640 -0.0001136235
## Jan 2019 -0.0103796252 0.032352119 0.052681773 -0.0048863636
## Feb 2019 0.0032048169 0.020675514 0.066100455 0.0054813292
```

```
head(data_rt_test)
```

```
##          M1_US      M1_EU      GDP_US      GDP_EU      CPI_US
## Mar 2019 0.013992059 0.016589706 0.000000000 -1.259414e-04 0.0036098177
## Apr 2019 0.017555076 0.005449530 0.011443290 -1.081730e-04 0.0033375184
## May 2019 -0.008377402 0.010288682 0.000000000 -7.441387e-05 0.0008785533
## Jun 2019 0.010639421 0.010970957 0.000000000 -4.658100e-05 0.0009205101
## Jul 2019 0.008542097 0.003311277 0.009478466 -4.368961e-05 0.0026819653
## Aug 2019 -0.003522586 0.010211425 0.000000000 -4.880721e-05 0.0008089162
##          CPI_EU      XAU_USD      WTI_USD      RATE
## Mar 2019 0.010164569 -0.013835505 0.05454139 0.003747871
## Apr 2019 0.007187350 -0.011208315 0.09938069 0.006675718
## May 2019 0.001332065 -0.001671539 -0.04662916 0.004495897
## Jun 2019 0.001615355 0.060424114 -0.09752982 -0.006489874
## Jul 2019 -0.004743383 0.039686270 0.04817172 0.001576754
## Aug 2019 0.001429797 0.061982595 -0.04623632 0.010007871
```

```
tail(data_rt_test)
```

```
##          M1_US      M1_EU      GDP_US      GDP_EU      CPI_US
## Sep 2019 0.0071220628 0.0001729649 0.000000000 -4.793411e-05 0.0011661543
## Oct 2019 0.0122077118 0.0065624278 0.008661189 -1.696112e-05 0.0024792327
## Nov 2019 0.0001274892 0.0142193326 0.000000000 2.115868e-05 0.0023127736
## Dec 2019 0.0303130736 0.0003387976 0.000000000 4.132768e-05 0.0024048826
## Jan 2020 -0.0146734962 -0.0052919190 -0.024350913 1.889987e-03 0.0014545081
## Feb 2020 -0.0089904571 0.0089903623 0.000000000 -2.883148e-03 0.0008892031
##          CPI_EU      XAU_USD      WTI_USD      RATE
```

```
## Sep 2019 0.002189225 0.003166009 0.04060189 0.0099087063
## Oct 2019 0.001424637 -0.008771872 -0.05294307 -0.0003307243
## Nov 2019 -0.003224583 -0.016561873 0.05672116 -0.0034186149
## Dec 2019 0.003139867 0.008522418 0.04619973 -0.0019918114
## Jan 2020 -0.010054064 0.051815184 -0.03106880 -0.0032154341
## Feb 2020 0.001820446 0.023057194 -0.12308128 0.0190211346
```

```
adfTest(M1_US1_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -5.8253
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(CPI_US1_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -4.7782
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(RATE1_rt)
```

```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -5.5966
## P VALUE:
## 0.01
##
## Description:
```

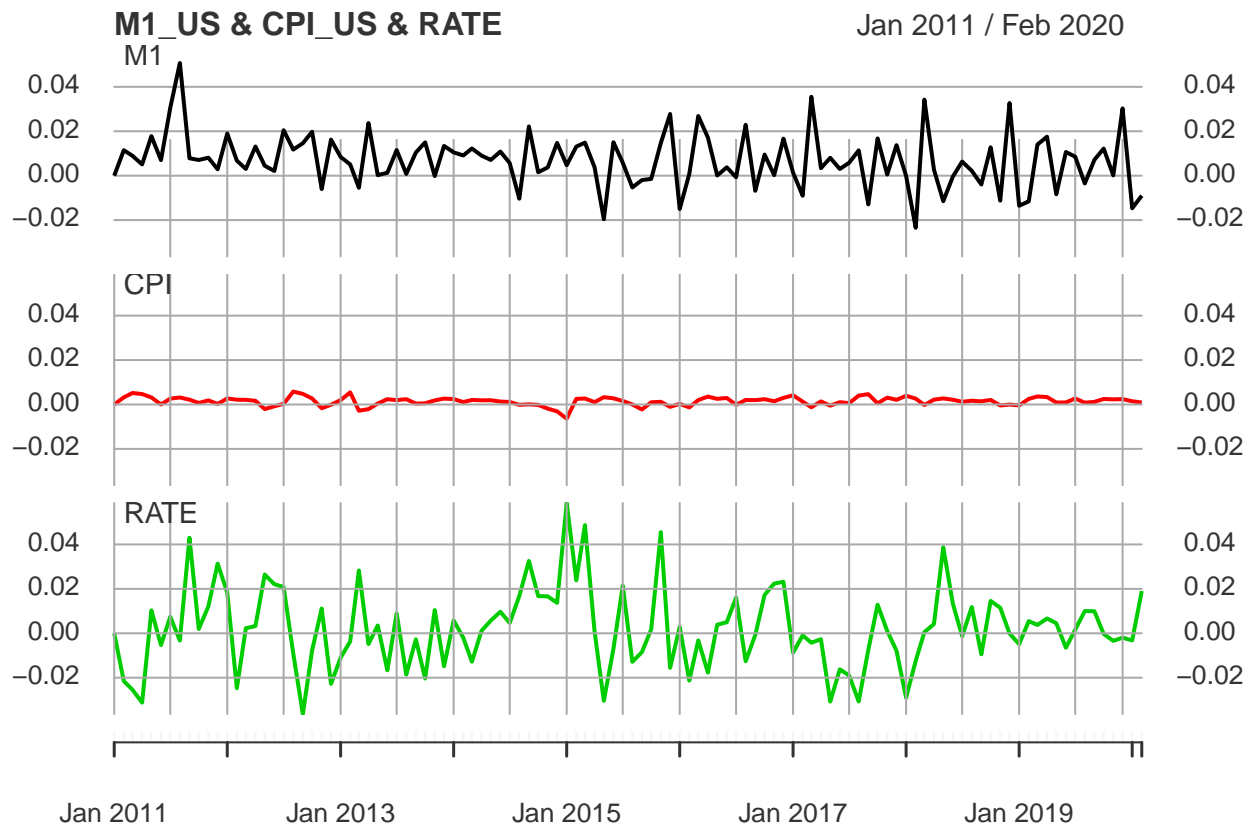
```
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
data_US_rt = cbind(M1_US1_rt, CPI_US1_rt, RATE1_rt)
```

```
names(data_US_rt) = c("M1", "CPI", "RATE")
```

```
#head(data_US_rt)
```

```
plot(as.xts(data_US_rt), type="l", multi.panel=TRUE, theme="white", main="M1_US & CPI_US & RATE", major
```



```
adfTest(XAU_USD1_rt)
```

```
##
```

```
## Title:
```

```
## Augmented Dickey-Fuller Test
```

```
##
```

```
## Test Results:
```

```
## PARAMETER:
```

```
## Lag Order: 1
```

```
## STATISTIC:
```

```
## Dickey-Fuller: -25.9239
```

```
## P VALUE:
```

```
## 0.01
```

```
##
```

```
## Description:
```

```
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(WTI_USD1_rt)
```

```
##
```

```
## Title:
```

```
## Augmented Dickey-Fuller Test
##
## Test Results:
##   PARAMETER:
##     Lag Order: 1
##   STATISTIC:
##     Dickey-Fuller: -27.2385
##   P VALUE:
##     0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
adfTest(RATE2_rt)
```

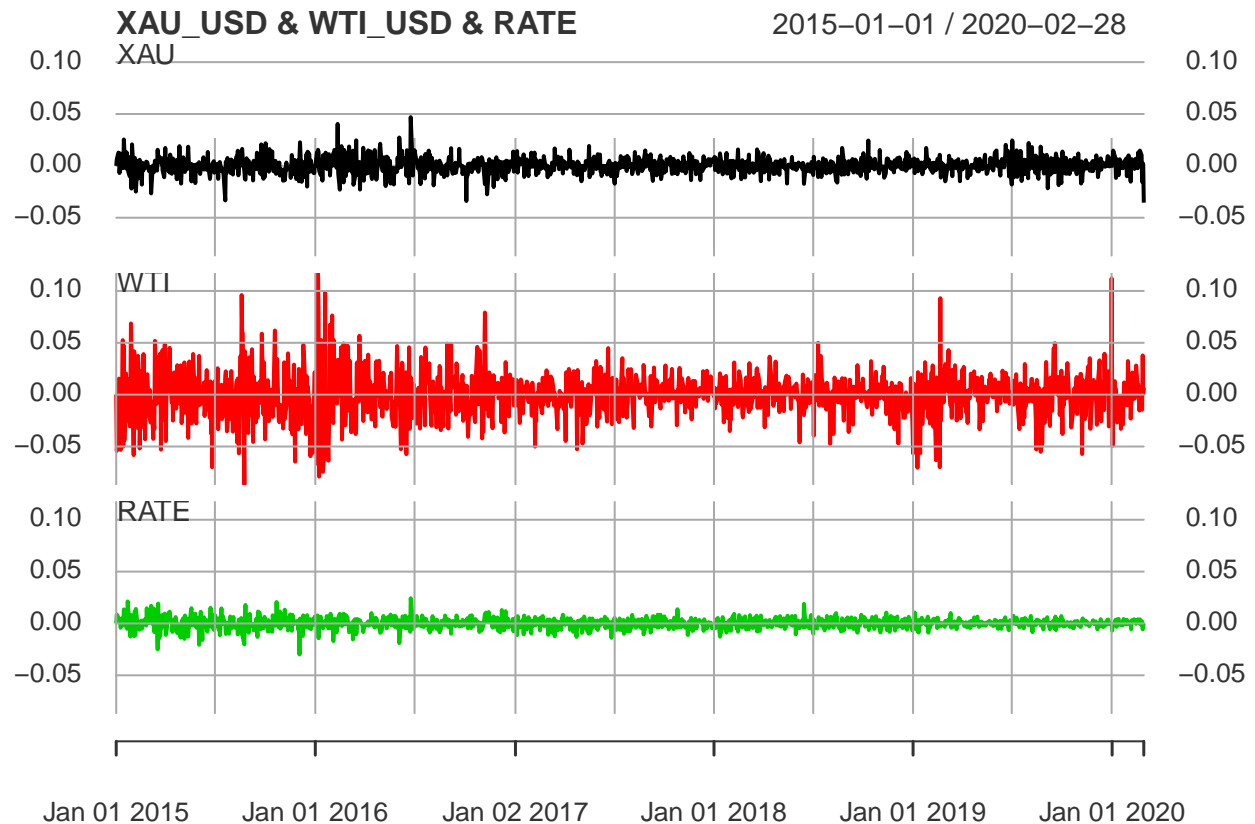
```
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
##   PARAMETER:
##     Lag Order: 1
##   STATISTIC:
##     Dickey-Fuller: -26.3354
##   P VALUE:
##     0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
data_D_rt = data.frame(XAU_USD1_rt, WTI_USD1_rt, RATE2_rt)
```

```
names(data_D_rt) = c("XAU", "WTI", "RATE")
```

```
#head(data_D_rt)
```

```
plot(as.xts(data_D_rt), type="l", multi.panel=TRUE, theme="white", main="XAU_USD & WTI_USD & RATE", maj
```



```
data_D_rt_train = data_D_rt[1:1330,]
data_D_rt_test = data_D_rt[1331:1344,]
```

ARIMA & GARCH

Use “auto.arima” to fit a model for daily return of currency rate.
Then check out ARCH effect to build GARCH model.

```
md_arima_1 = auto.arima(rate_train)
md_arima_1

## Series: rate_train
## ARIMA(1,1,1)
##
## Coefficients:
##      ar1      ma1
##    0.8903 -0.9086
## s.e. 0.0926 0.0844
##
## sigma^2 estimated as 2.45e-05: log likelihood=4197.75
## AIC=-8389.5   AICc=-8389.48   BIC=-8374.55

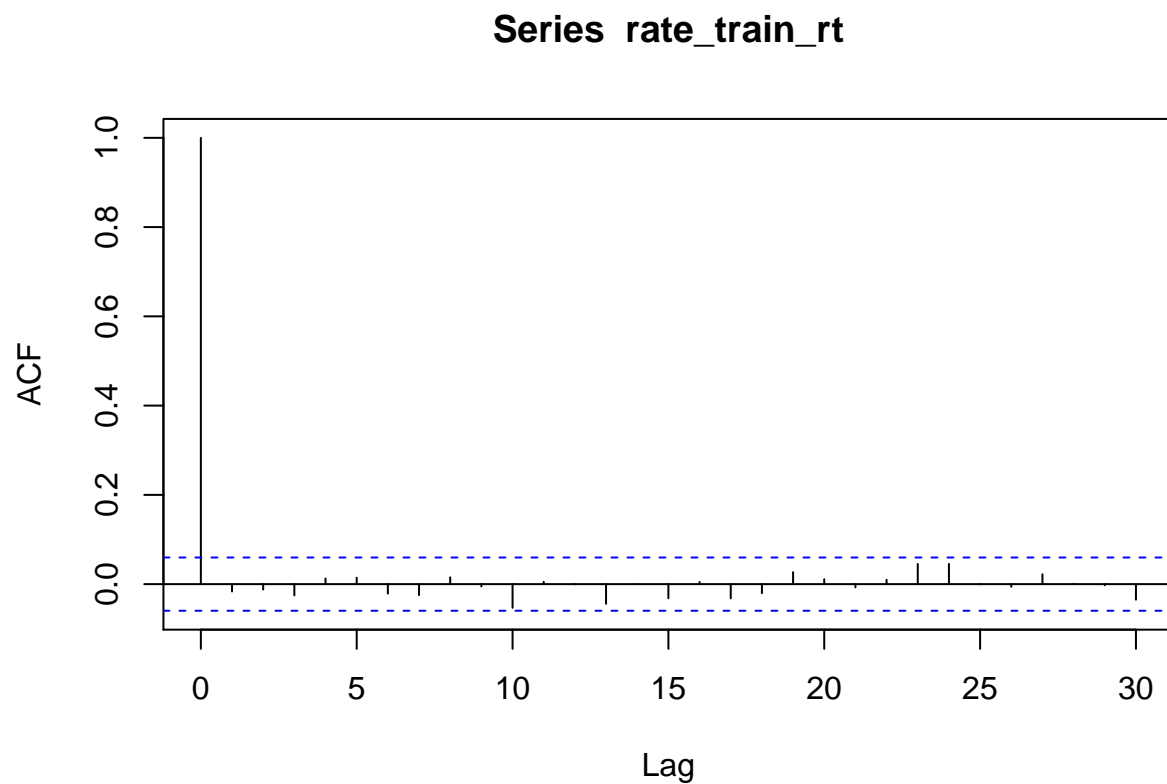
rate_train_rt = dailyReturn(rate_train, type = "log")
rate_test_rt = dailyReturn(rate_test, type = "log")
adfTest(rate_train_rt)

##
```



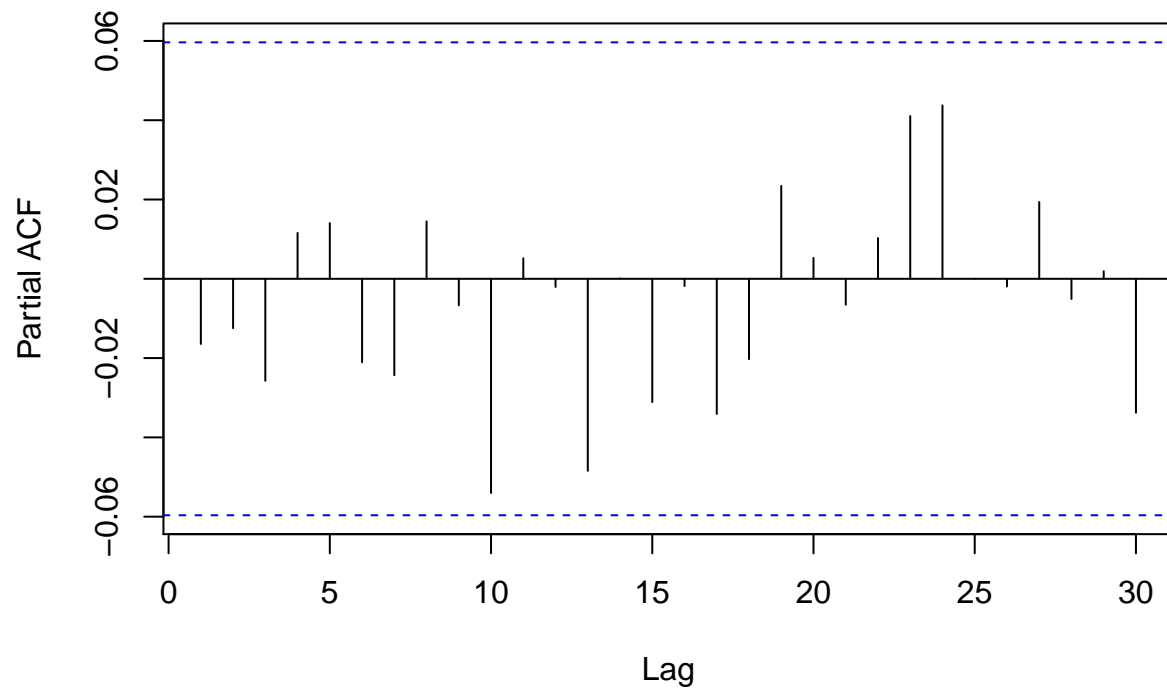
```
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 1
## STATISTIC:
## Dickey-Fuller: -23.699
## P VALUE:
## 0.01
##
## Description:
## Thu Apr 30 20:18:13 2020 by user: yangm
```

```
acf(rate_train_rt)
```



```
pacf(rate_train_rt)
```

Series rate_train_rt



```
md_arima_2 = auto.arima(rate_train_rt)
md_arima_2

## Series: rate_train_rt
## ARIMA(2,0,1) with zero mean
##
## Coefficients:
##      ar1      ar2      ma1
##      0.8742 -0.0013 -0.8919
## s.e.  0.1063  0.0314  0.1021
##
## sigma^2 estimated as 3.077e-05: log likelihood=4079.17
## AIC=-8150.34   AICc=-8150.3   BIC=-8130.4

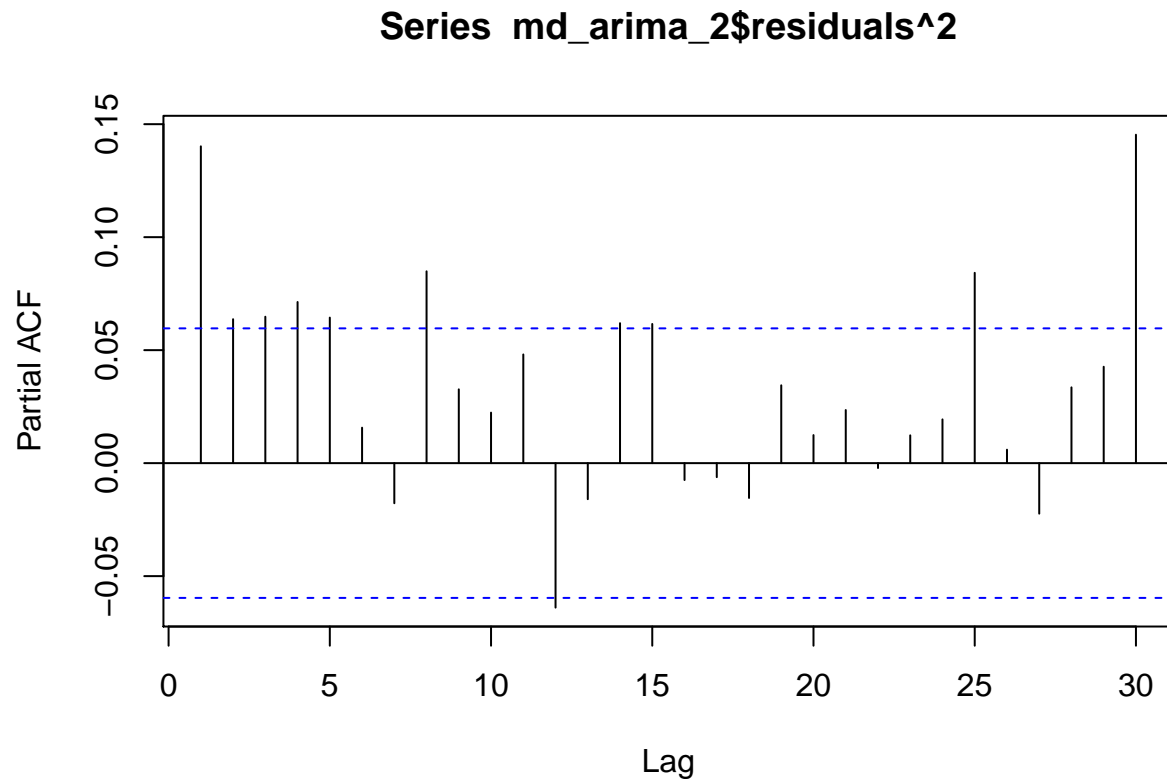
pred_arima = predict(md_arima_2, 263)
rmse(predicted = as.numeric(unlist(pred_arima[1])), actual = as.numeric(unlist(rate_test_rt)))

## [1] 0.002864903

Box.test(md_arima_2$residuals^2, 10, type = "Ljung")

##
## Box-Ljung test
##
## data: md_arima_2$residuals^2
## X-squared = 76.58, df = 10, p-value = 2.341e-12
```

```
pacf(md_arma_2$residuals^2)
```



```
md_arch_G = garchFit(~garch(1, 0), data = rate_train_rt, trace = F)
summary(md_arch_G)
```

```
##
## Title:
##  GARCH Modelling
##
## Call:
##  garchFit(formula = ~garch(1, 0), data = rate_train_rt, trace = F)
##
## Mean and Variance Equation:
##  data ~ garch(1, 0)
## <environment: 0x000000001e313410>
## [data = rate_train_rt]
##
## Conditional Distribution:
##  norm
##
## Coefficient(s):
##      mu      omega    alpha1
## 7.4600e-05 2.7171e-05 1.1065e-01
##
## Std. Errors:
## based on Hessian
```

```
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      7.460e-05  1.643e-04   0.454 0.649719
## omega   2.717e-05  1.400e-06  19.410 < 2e-16 ***
## alpha1  1.106e-01  3.316e-02   3.337 0.000848 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 4089.615      normalized:  3.786681
##
## Description:
## Thu Apr 30 20:18:14 2020 by user: yangm
##
##
## Standardised Residuals Tests:
##
##              Statistic p-Value
## Jarque-Bera Test    R      Chi^2 226.2105 0
## Shapiro-Wilk Test   R      W      0.9811974 1.327954e-10
## Ljung-Box Test      R      Q(10) 5.749473 0.8358539
## Ljung-Box Test      R      Q(15) 9.499013 0.8500155
## Ljung-Box Test      R      Q(20) 12.16536 0.9102667
## Ljung-Box Test      R^2 Q(10) 27.13427 0.002479927
## Ljung-Box Test      R^2 Q(15) 41.87955 0.0002345467
## Ljung-Box Test      R^2 Q(20) 47.57534 0.0004877931
## LM Arch Test        R      TR^2  28.51072 0.004654617
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -7.567806 -7.553960 -7.567822 -7.562563
```

```
pred_arch_G = predict(md_arch_G, 263)
pred_arch_G
```

```
##      meanForecast meanError standardDeviation
## 1  7.460029e-05 0.005213301      0.005213301
## 2  7.460029e-05 0.005493445      0.005493445
## 3  7.460029e-05 0.005523569      0.005523569
## 4  7.460029e-05 0.005526892      0.005526892
## 5  7.460029e-05 0.005527260      0.005527260
## 6  7.460029e-05 0.005527300      0.005527300
## 7  7.460029e-05 0.005527305      0.005527305
## 8  7.460029e-05 0.005527305      0.005527305
## 9  7.460029e-05 0.005527305      0.005527305
## 10 7.460029e-05 0.005527305      0.005527305
## 11 7.460029e-05 0.005527305      0.005527305
## 12 7.460029e-05 0.005527305      0.005527305
## 13 7.460029e-05 0.005527305      0.005527305
## 14 7.460029e-05 0.005527305      0.005527305
## 15 7.460029e-05 0.005527305      0.005527305
## 16 7.460029e-05 0.005527305      0.005527305
## 17 7.460029e-05 0.005527305      0.005527305
## 18 7.460029e-05 0.005527305      0.005527305
## 19 7.460029e-05 0.005527305      0.005527305
```

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23

[illegible]


```

## 236 7.460029e-05 0.005527305 0.005527305
## 237 7.460029e-05 0.005527305 0.005527305
## 238 7.460029e-05 0.005527305 0.005527305
## 239 7.460029e-05 0.005527305 0.005527305
## 240 7.460029e-05 0.005527305 0.005527305
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## 261 7.460029e-05 0.005527305 0.005527305
## 262 7.460029e-05 0.005527305 0.005527305
## 263 7.460029e-05 0.005527305 0.005527305

rmse(predicted = as.numeric(unlist(pred_arch_G[1])), actual = as.numeric(unlist(rate_test_rt)))

## [1] 0.002861563

md_arch_t = garchFit(~garch(1, 0), data = rate_train_rt, cond.dist = c("std"), trace = F)
summary(md_arch_t)

##
## Title:
##  GARCH Modelling
##
## Call:
##  garchFit(formula = ~garch(1, 0), data = rate_train_rt, cond.dist = c("std"),
##    trace = F)
##
## Mean and Variance Equation:
##  data ~ garch(1, 0)
##  <environment: 0x00000000212b82e0>
##  [data = rate_train_rt]
##
## Conditional Distribution:
##  std
##
## Coefficient(s):
##      mu      omega    alpha1    shape
## 8.7910e-05 2.6882e-05 1.2063e-01 6.3475e+00

```

```
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      8.791e-05  1.532e-04   0.574  0.56598
## omega  2.688e-05  1.913e-06  14.054 < 2e-16 ***
## alpha1 1.206e-01  4.043e-02   2.983  0.00285 **
## shape  6.347e+00  1.142e+00   5.558  2.72e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 4118.921    normalized:  3.813816
##
## Description:
## Thu Apr 30 20:18:14 2020 by user: yangm
##
##
## Standardised Residuals Tests:
##
##      Statistic p-Value
## Jarque-Bera Test  R    Chi^2 229.3519 0
## Shapiro-Wilk Test  R    W    0.9810736 1.194785e-10
## Ljung-Box Test    R    Q(10) 5.724152 0.8378819
## Ljung-Box Test    R    Q(15) 9.467828 0.8518147
## Ljung-Box Test    R    Q(20) 12.14253 0.9110828
## Ljung-Box Test    R^2 Q(10) 26.04315 0.003682578
## Ljung-Box Test    R^2 Q(15) 40.35298 0.0004010477
## Ljung-Box Test    R^2 Q(20) 46.04301 0.0007951392
## LM Arch Test      R    TR^2  27.84604 0.005826142
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -7.620225 -7.601763 -7.620252 -7.613234
pred_arch_t = predict(md_arch_t, 263)
pred_arch_t[1]
```

```
##      meanForecast
## 1  8.791044e-05
## 2  8.791044e-05
## 3  8.791044e-05
## 4  8.791044e-05
## 5  8.791044e-05
## 6  8.791044e-05
## 7  8.791044e-05
## 8  8.791044e-05
## 9  8.791044e-05
## 10 8.791044e-05
## 11 8.791044e-05
## 12 8.791044e-05
## 13 8.791044e-05
## 14 8.791044e-05
## 15 8.791044e-05
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16 8.791044e-05
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```

## 232 8.791044e-05
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## 259 8.791044e-05
## 260 8.791044e-05
## 261 8.791044e-05
## 262 8.791044e-05
## 263 8.791044e-05

rmse(predicted = as.numeric(unlist(pred_arch_t[1])), actual = as.numeric(unlist(rate_test_rt)))

## [1] 0.002861171

md_garch_G = garchFit(~garch(1, 1), data = rate_train_rt, trace = F)
summary(md_garch_G)

##
## Title:
##  GARCH Modelling
##
## Call:
##  garchFit(formula = ~garch(1, 1), data = rate_train_rt, trace = F)
##
## Mean and Variance Equation:
##  data ~ garch(1, 1)
##  <environment: 0x0000000020d83688>
##  [data = rate_train_rt]
##
## Conditional Distribution:
##  norm
##

```

```
## Coefficient(s):
##      mu      omega      alpha1      beta1
## 1.6178e-05 5.1841e-08 1.3089e-02 9.8430e-01
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      1.618e-05 1.558e-04  0.104  0.917
## omega  5.184e-08 4.734e-08  1.095  0.273
## alpha1 1.309e-02 3.037e-03  4.310 1.64e-05 ***
## beta1  9.843e-01 3.089e-03 318.694 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 4121.965      normalized: 3.816634
##
## Description:
## Thu Apr 30 20:18:14 2020 by user: yangm
##
## Standardised Residuals Tests:
##
##      Statistic p-Value
## Jarque-Bera Test  R      Chi^2 77.34754 0
## Shapiro-Wilk Test  R      W      0.9903362 1.549384e-06
## Ljung-Box Test     R      Q(10) 3.616231 0.9630037
## Ljung-Box Test     R      Q(15) 7.300761 0.9487601
## Ljung-Box Test     R      Q(20) 8.588938 0.9871979
## Ljung-Box Test     R^2 Q(10) 8.738132 0.5571231
## Ljung-Box Test     R^2 Q(15) 20.51427 0.1530793
## Ljung-Box Test     R^2 Q(20) 23.81096 0.2507476
## LM Arch Test       R      TR^2 16.09945 0.1867234
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -7.625860 -7.607398 -7.625888 -7.618870
pred_garch_G = predict(md_garch_G, 263)
rmse(predicted = as.numeric(unlist(pred_garch_G[1])), actual = as.numeric(unlist(rate_test_rt)))

## [1] 0.00286401

md_garch_t = garchFit(~garch(1, 1), data = rate_train_rt, cond.dist = c("std"), trace = F)
summary(md_garch_t)

##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~garch(1, 1), data = rate_train_rt, cond.dist = c("std"),
## trace = F)
##
```



```

## Mean and Variance Equation:
## data ~ garch(1, 1)
## <environment: 0x000000002521dbf0>
## [data = rate_train_rt]
##
## Conditional Distribution:
## std
##
## Coefficient(s):
##      mu      omega      alpha1      beta1      shape
## 4.6927e-05 1.5507e-07 1.7696e-02 9.7603e-01 8.4884e+00
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      4.693e-05 1.502e-04 0.312 0.75472
## omega 1.551e-07 1.010e-07 1.536 0.12453
## alpha1 1.770e-02 5.692e-03 3.109 0.00188 **
## beta1 9.760e-01 7.186e-03 135.816 < 2e-16 ***
## shape 8.488e+00 1.897e+00 4.475 7.66e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 4137.931 normalized: 3.831418
##
## Description:
## Thu Apr 30 20:18:14 2020 by user: yangm
##
## Standardised Residuals Tests:
##
##      Statistic p-Value
## Jarque-Bera Test R Chi^2 95.93217 0
## Shapiro-Wilk Test R W 0.9890606 3.310632e-07
## Ljung-Box Test R Q(10) 3.529829 0.9660758
## Ljung-Box Test R Q(15) 7.177869 0.9525247
## Ljung-Box Test R Q(20) 8.399585 0.9888765
## Ljung-Box Test R^2 Q(10) 7.80879 0.6475078
## Ljung-Box Test R^2 Q(15) 18.94319 0.2163198
## Ljung-Box Test R^2 Q(20) 22.23991 0.3276358
## LM Arch Test R TR^2 13.59259 0.3274774
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -7.653577 -7.630499 -7.653619 -7.644838
pred_garch_t = predict(md_garch_t, 263)
rmse(predicted = as.numeric(unlist(pred_garch_t[1])), actual = as.numeric(unlist(rate_test_rt)))

## [1] 0.002862574

md_tgarch = garchFit(~aparch(1,1), rate_train_rt, delta = 2, include.delta = F, trace = F)
summary(md_tgarch)

```

```

##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~aparch(1, 1), data = rate_train_rt, delta = 2,
## include.delta = F, trace = F)
##
## Mean and Variance Equation:
## data ~ aparch(1, 1)
## <environment: 0x0000000020ca1720>
## [data = rate_train_rt]
##
## Conditional Distribution:
## norm
##
## Coefficient(s):
##      mu      omega      alpha1      gamma1      beta1
## 4.1302e-05  5.7739e-08  9.1342e-03 -3.6299e-01  9.8701e-01
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      4.130e-05  1.564e-04   0.264 0.791692
## omega   5.774e-08  3.882e-08   1.487 0.136937
## alpha1  9.134e-03  2.397e-03   3.811 0.000138 ***
## gamma1 -3.630e-01  1.984e-01  -1.829 0.067343 .
## beta1   9.870e-01  2.136e-03 462.073 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 4124.41      normalized:  3.818898
##
## Description:
## Thu Apr 30 20:18:14 2020 by user: yangm
##
## Standardised Residuals Tests:
##
##      Statistic p-Value
## Jarque-Bera Test  R      Chi^2 67.8008 1.887379e-15
## Shapiro-Wilk Test R      W      0.9911581 4.428322e-06
## Ljung-Box Test    R      Q(10) 3.45741 0.9685247
## Ljung-Box Test    R      Q(15) 7.230621 0.9509312
## Ljung-Box Test    R      Q(20) 8.564348 0.987426
## Ljung-Box Test    R^2 Q(10) 7.695832 0.6585199
## Ljung-Box Test    R^2 Q(15) 20.1506 0.1662314
## Ljung-Box Test    R^2 Q(20) 23.00657 0.2884719
## LM Arch Test      R      TR^2 15.07848 0.2371728
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC

```

```
## -7.628536 -7.605459 -7.628579 -7.619798
pred_tgarch = predict(md_tgarch, 263)
rmse(predicted = as.numeric(unlist(pred_tgarch[1])), actual = as.numeric(unlist(rate_test_rt)))

## [1] 0.002862812
```

VAR & VEC

#Apply granger test for determining whether one time series is useful in forecasting currency rate.

```
grangertest(M1_US_rt, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(M1_US_rt, 1:1)
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 0.5625 0.4563
```

```
grangertest(M1_EU_rt, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(M1_EU_rt, 1:1)
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 0.6713 0.416
```

```
grangertest(GDP_US_rt, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(GDP_US_rt, 1:1)
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 1.0581 0.3079
```

```
grangertest(GDP_EU_rt_dif, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(GDP_EU_rt_dif, 1:1)
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 4.9294 0.03033 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
grangertest(CPI_US_rt, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(CPI_US_rt, 1:1)
```

```
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 1.0585 0.3078
```

```
grangertest(CPI_EU_rt, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(CPI_EU_rt, 1:1)
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 0.4625 0.4992
```

```
grangertest(XAU_USD_rt, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(XAU_USD_rt, 1:1)
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 0.4613 0.4997
```

```
grangertest(WTI_USD_rt, RATE_rt, order = 1, na.action = na.omit)
```

```
## Granger causality test
##
## Model 1: RATE_rt ~ Lags(RATE_rt, 1:1) + Lags(WTI_USD_rt, 1:1)
## Model 2: RATE_rt ~ Lags(RATE_rt, 1:1)
##   Res.Df Df       F Pr(>F)
## 1      58
## 2      59 -1 0.957  0.332
```

From the result, only GDP_EU_rt is significant, while it is a first order differential. So we tried cointegration test.

```
currency.rate = as.numeric(RATE_rt)
#M1_US = as.numeric(M1_US_rt)
#M1_EU = as.numeric(M1_EU_rt)
#GDP_US = as.numeric(GDP_US_rt)
GDP_EU = as.numeric(GDP_EU_rt_dif)
#CPI_US = as.numeric(CPI_US_rt)
#CPI_EU = as.numeric(CPI_EU_rt)
#XAU_USD = as.numeric(XAU_USD_rt)
#WTI_USD = as.numeric(WTI_USD_rt)

#md_lm = lm(currency.rate ~ M1_US + M1_EU + GDP_US + GDP_EU + CPI_US + CPI_EU + XAU_USD + WTI_USD)
md_lm = lm(currency.rate ~ GDP_EU_rt, data_rt_train)
summary(md_lm)
```

```
##
## Call:
## lm(formula = currency.rate ~ GDP_EU_rt, data = data_rt_train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```

```
## -0.031104 -0.008666 -0.000061 0.004642 0.049526
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.0008595 0.0020683 0.416 0.679
## GDP_EU_rt   -4.8953780 3.2925461 -1.487 0.142
##
## Residual standard error: 0.01622 on 60 degrees of freedom
## Multiple R-squared: 0.03553, Adjusted R-squared: 0.01946
## F-statistic: 2.211 on 1 and 60 DF, p-value: 0.1423
```

```
dwtest(md_lm)
```

```
##
## Durbin-Watson test
##
## data: md_lm
## DW = 1.5607, p-value = 0.03119
## alternative hypothesis: true autocorrelation is greater than 0
```

```
res = residuals(md_lm)
ur.df(res, type = "none", selectlags = "AIC")
```

```
##
## #####
## # Augmented Dickey-Fuller Test Unit Root / Cointegration Test #
## #####
##
## The value of the test statistic is: -5.6952
```

```
x = cbind(GDP_EU_rt, RATE_rt)[1:50]
names(x) = c("GDP_EU", "RATE")
head(x)
```

```
##             GDP_EU      RATE
## Jan 2015 0.0000000000 0.0000000000
## Feb 2015 0.0004064408 0.0238288969
## Mar 2015 0.0003430773 0.0487057221
## Apr 2015 0.0002797828 0.0008660821
## May 2015 0.0002325859 -0.0303948080
## Jun 2015 0.0002054699 -0.0070281124
```

```
vecm = ca.jo(x, K = 2, ecdet = "const")
summary(vecm)
```

```
##
## #####
## # Johansen-Procedure #
## #####
##
## Test type: maximal eigenvalue statistic (lambda max) , without linear trend and constant in cointegration
##
## Eigenvalues (lambda):
## [1] 5.430146e-01 1.116981e-01 5.204170e-17
##
## Values of teststatistic and critical values of test:
##
```

```
##          test 10pct  5pct  1pct
## r <= 1 |   5.69   7.52   9.24 12.97
## r = 0  |  37.59 13.75 15.67 20.20
##
## Eigenvectors, normalised to first column:
## (These are the cointegration relations)
##
##          GDP_EU.12      RATE.12      constant
## GDP_EU.12  1.0000000000  1.0000000000  1.0000000000
## RATE.12    0.0720521911 -0.0135857305 -0.0044551604
## constant -0.0001026826  0.0002173345 -0.0009482182
##
## Weights W:
## (This is the loading matrix)
##
##          GDP_EU.12      RATE.12      constant
## GDP_EU.d  -0.01118603 -0.03512347  3.263710e-17
## RATE.d    -14.86184372  3.24985614 -1.146792e-14
```

To construct the VAR model for the selected endogenous variables, the co-integration test is needed. Apply durbin-watson test to linear model. As the value of p-value is small enough, indicating that the residual sequence is not independent at the significance level of 5% and has autocorrelation. According to the stationariness test results of the residual series, the null hypothesis that the residual series has unit root is rejected at the significance level of 5%, that is, the residual series is stable, indicating that there is a co-integration relationship between currency rate and GDP of EU.

From the result of Johansen procedure, we know the rank of the co-integration vector is 1.

Then used cajorls() to estimate the coefficient matrix of the VEC model. Then VEC model is converted to horizontal VAR model to predict currency rate.

```
md_vec = cajorls(vecm, r=1)
md_vec

## $rlm
##
## Call:
## lm(formula = substitute(form1), data = data.mat)
##
## Coefficients:
##          GDP_EU.d      RATE.d
## ect1          -1.119e-02  -1.486e+01
## GDP_EU.dl1       7.195e-01   5.522e+01
## RATE.dl1        -6.986e-04  -8.953e-01
##
##
## $beta
##          ect1
## GDP_EU.12  1.0000000000
## RATE.12    0.0720521911
## constant -0.0001026826
md_var = vec2var(vecm, r = 1)
md_var
```

```
##
## Coefficient matrix of lagged endogenous variables:
##
```

```
## A1:
##      GDP_EU.11      RATE.11
## GDP_EU  1.719549 -0.0006985824
## RATE   55.223957  0.1046873174
##
##
## A2:
##      GDP_EU.12      RATE.12
## GDP_EU -0.7307353 -0.0001073955
## RATE  -70.0858006 -0.1755157216
##
##
## Coefficient matrix of deterministic regressor(s).
##
##      constant
## GDP_EU 1.148610e-06
## RATE   1.526052e-03

pred_var = predict(md_var, 12)
rmse(predicted = pred_var$fcst$RATE[1], actual = as.numeric(unlist(data_rt_test$RATE)))

## [1] 0.006963041
#irf(md_var)
```

DCC-GARCH

```
#Calculate the maximum, minimum, median, skewness, kurtosis and extremum
data_outline = function(x){
  m = mean(x)
  d=max(x)
  xd=min(x)
  me = median(x)
  s = sd(x)
  kur=kurtosis(x)
  ske=skewness(x)
  R = max(x)-min(x)
  data.frame(Mean=m, Median=me, max=d,min=xd,std_dev=s, Skewness=ske, Kurtosis=kur, R=R)
}
for (i in 1:3){print(data_outline(data_D_rt[,i]))}
```

```
##      Mean      Median      max      min      std_dev      Skewness
## 1 0.000218366 0.0002179542 0.04692827 -0.03546172 0.007752035 0.09691199
##      Kurtosis      R
## 1 2.613654 0.08238999
##      Mean      Median      max      min      std_dev      Skewness      Kurtosis
## 1 5.168222e-05 0.0003836707 0.1171551 -0.08648298 0.02193947 0.1926181 2.554549
##      R
## 1 0.2036381
##      Mean      Median      max      min      std_dev      Skewness      Kurtosis
## 1 7.937433e-05      0 0.02430363 -0.02995268 0.005129614 -0.1159179 2.713915
##      R
## 1 0.05425631
```

```
ArchTest(M1_US1_rt)
```

```
##  
## ARCH LM-test; Null hypothesis: no ARCH effects  
##  
## data: M1_US1_rt  
## Chi-squared = 18.056, df = 12, p-value = 0.114
```

```
ArchTest(CPI_US1_rt)
```

```
##  
## ARCH LM-test; Null hypothesis: no ARCH effects  
##  
## data: CPI_US1_rt  
## Chi-squared = 12.432, df = 12, p-value = 0.4117
```

```
ArchTest(RATE1_rt)
```

```
##  
## ARCH LM-test; Null hypothesis: no ARCH effects  
##  
## data: RATE1_rt  
## Chi-squared = 13.725, df = 12, p-value = 0.3186
```

```
ArchTest(XAU_USD1_rt)
```

```
##  
## ARCH LM-test; Null hypothesis: no ARCH effects  
##  
## data: XAU_USD1_rt  
## Chi-squared = 32.052, df = 12, p-value = 0.001358
```

```
ArchTest(WTI_USD1_rt)
```

```
##  
## ARCH LM-test; Null hypothesis: no ARCH effects  
##  
## data: WTI_USD1_rt  
## Chi-squared = 207.04, df = 12, p-value < 2.2e-16
```

```
ArchTest(RATE2_rt)
```

```
##  
## ARCH LM-test; Null hypothesis: no ARCH effects  
##  
## data: RATE2_rt  
## Chi-squared = 91.377, df = 12, p-value = 2.671e-14
```

There is no ARCH effect of the monthly time series data, we decided to use the daily data, because ARCH effect shows in all three time series.

```
#Calculate the correlation coefficient matrix
```

```
corre = cor(data_D_rt)
```

```
corre
```

```
##           XAU           WTI           RATE  
## XAU    1.00000000  0.01908568 -0.2776450  
## WTI    0.01908568  1.00000000 -0.0317455  
## RATE -0.27764499 -0.03174550  1.00000000
```



```

#1: Conditional Mean (vs Realized Returns)
#2: Conditional Sigma (vs Realized Absolute Returns)
#3: Conditional Covariance
#4: Conditional Correlation
#5: EW Portfolio Plot with conditional density VaR limits
myuspec = multispec(replicate(3, ugarchspec(mean.model = list(armaOrder = c(1,1)))))
mydcc = dccspec(myuspec, VAR = TRUE, lag = 1, lag.max = 12, dccOrder = c(1, 1), distribution = 'mvnorm')
md_dcc = dccfit(mydcc, data = data_D_rt_train, fit.control = list(eval.se=TRUE))

myuspec1 = multispec(replicate(2, ugarchspec(mean.model = list(armaOrder = c(1,1)))))
mydcc1 = dccspec(myuspec1, VAR = TRUE, lag = 1, lag.max = 12, dccOrder = c(1, 1), distribution = 'mvnorm')
md_dcc_xau = dccfit(mydcc1, data = data_D_rt_train[, c(1, 3)], fit.control = list(eval.se=TRUE))
#plot(md_dcc_xau)

md_dcc_wti = dccfit(mydcc1, data = data_D_rt_train[, c(2, 3)], fit.control = list(eval.se=TRUE))
#plot(md_dcc_wti)

#Predict with DCC-GARCH
pred_dcc = dccforecast(md_dcc, n.ahead = 14)
#pred_dcc
#fitted(pred_dcc)
rmse(predicted = as.numeric(unlist(fitted(pred_dcc)[3])), actual = as.numeric(unlist(data_D_rt_test[3])))

## [1] 0.002723984

```