Exploration and Exploitation (Bandits)

Last Time

- What is Reinforcement Learning?
- What are the main challenges in Reinforcement Learning?
- How do we categorize RL approaches?

Last Time

First RL Algorithm:

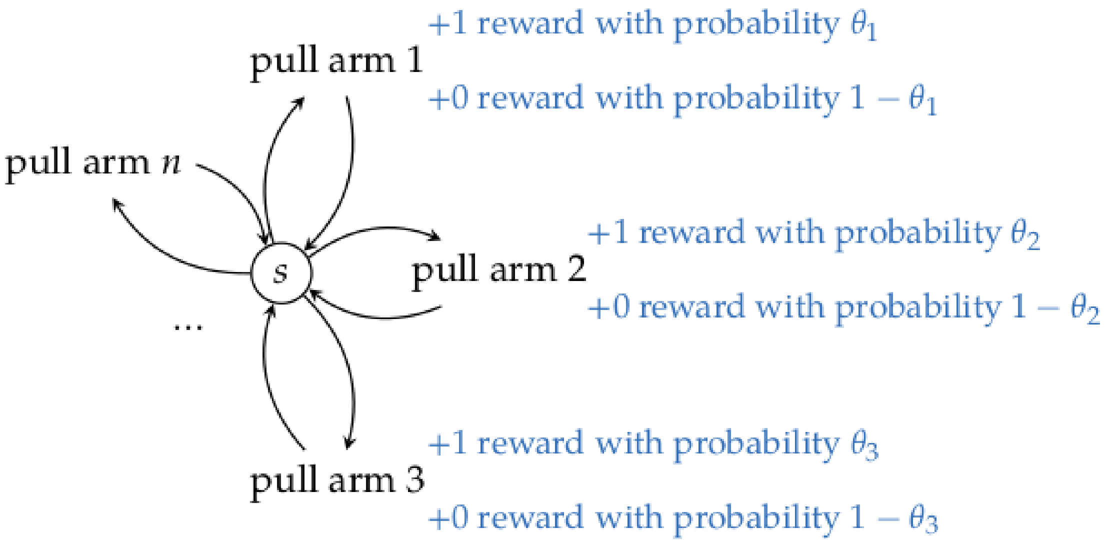
Tabular Maximum Likelihood Model-Based Reinforcement Learning

loop
    choose action a
    gain experience
    estimate T, R
    solve MDP with T, R

Guiding Questions

- What are the best ways to trade off Exploration and Exploitation?

Bandits



- Bernoulli Bandit with parameters θ
- $\theta^* \equiv \max \theta$

"According to Peter Whittle, "efforts to solve [bandit problems] so sapped the energies and minds of Allied analysts that the suggestion was made that the problem be dropped over Germany as the ultimate instrument of intellectual sabotage."

Greedy Strategy

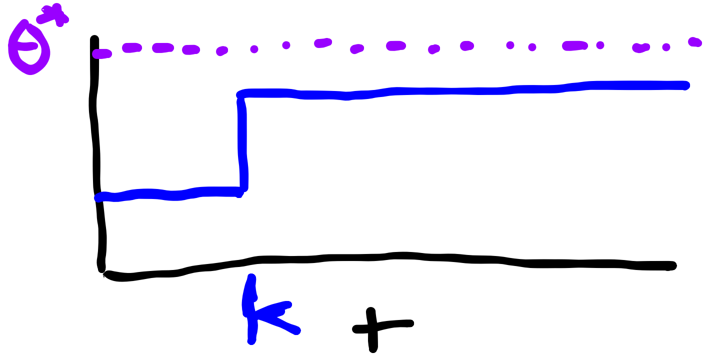
$$\rho_a = \frac{\text{number of wins}}{\text{number of tries}}$$

Definition in book uses Laplace Smoothing

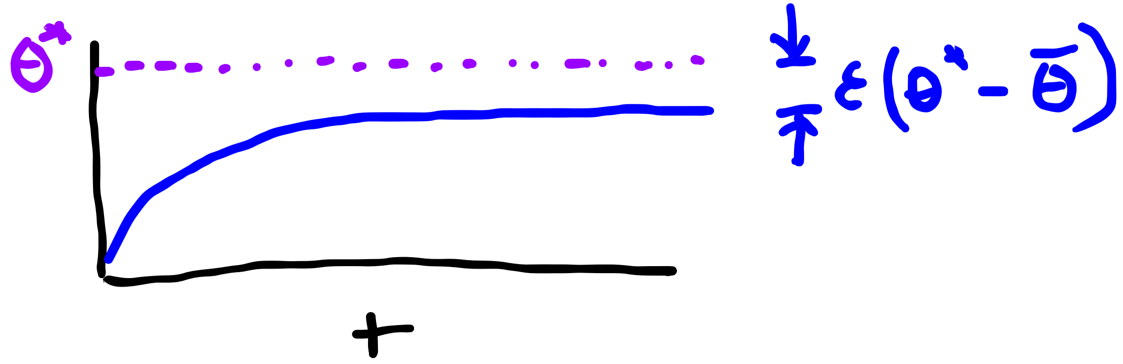
Choose $\underset{a}{\operatorname{argmax}}\, \rho_a$

Undirected Strategies

- Explore then Commit
  Choose a randomly for k steps
  Then choose $\underset{a}{\operatorname{argmax}}\, \rho_a$



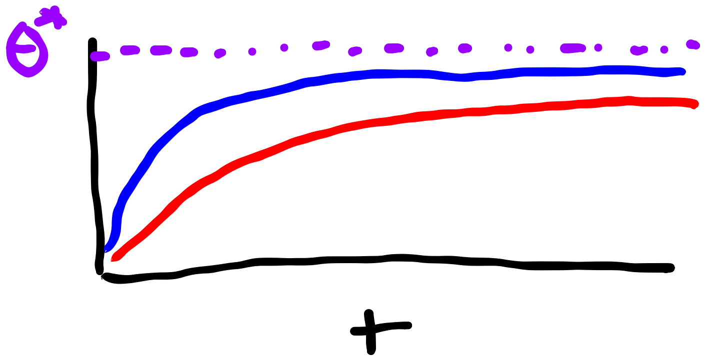
- ϵ - greedy
  With probability ϵ, choose randomly
  Otherwise choose $\underset{a}{\operatorname{argmax}}\, \rho_a$



Directed Strategies

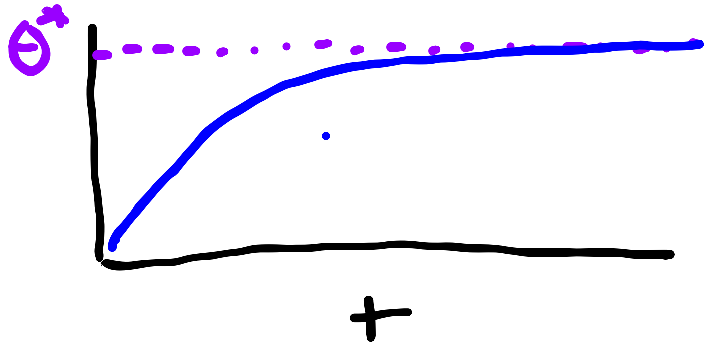
- Softmax
  Choose a with probability proportional to $e^{\lambda \rho_a}$

(remove gap with $\lambda \to \infty$)



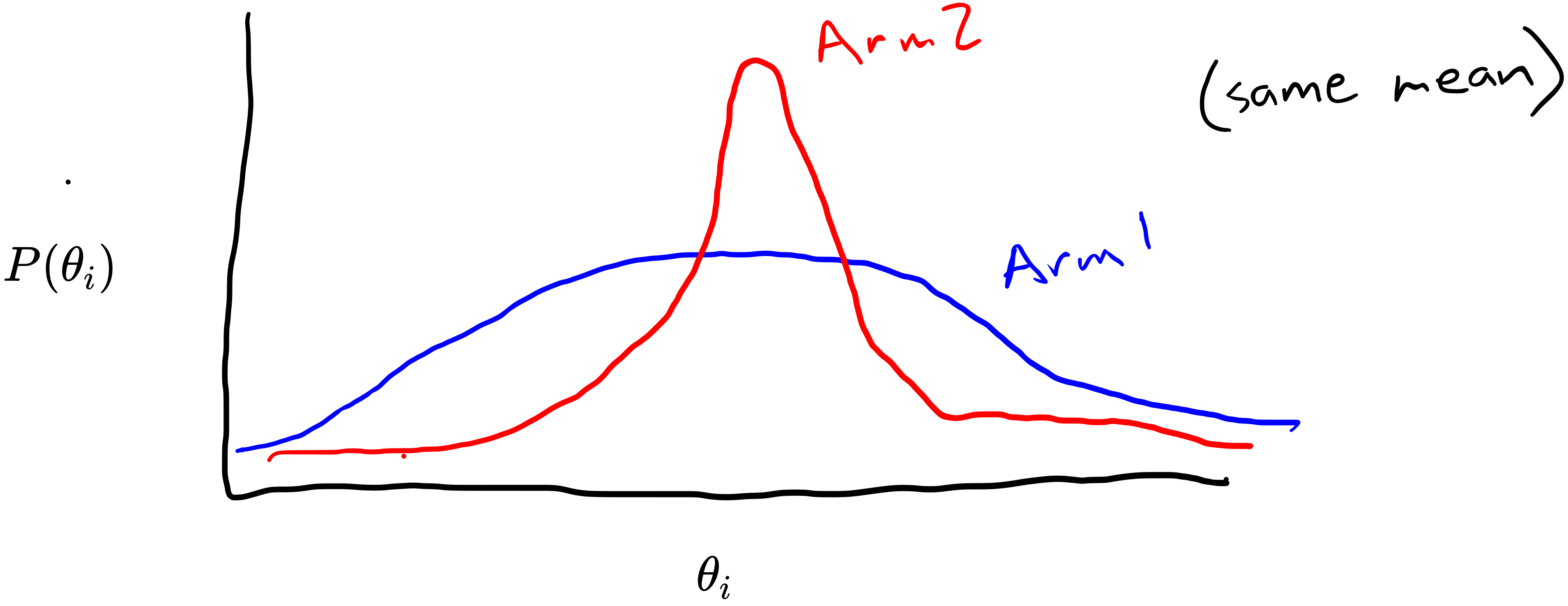
ε-greedy

- Upper Confidence Bound (UCB)
  Choose $\underset{a}{\operatorname{argmax}}\, \rho_a + c\sqrt{\frac{\log N}{N(a)}}$



Break

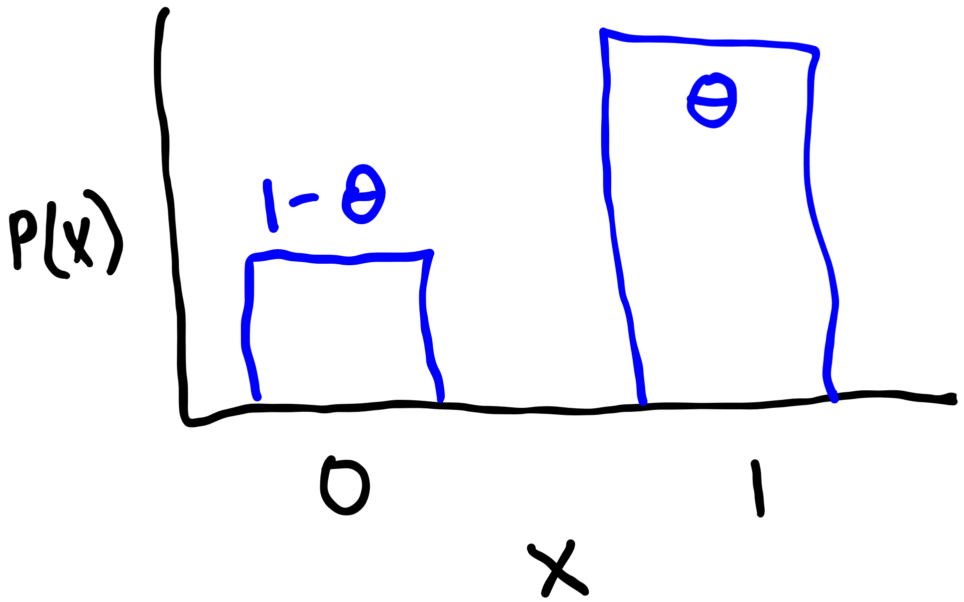
Discuss with your neighbor: Suppose you have the following *belief* about the parameters θ. Which arm should you choose to pull next?



Bayesian Estimation

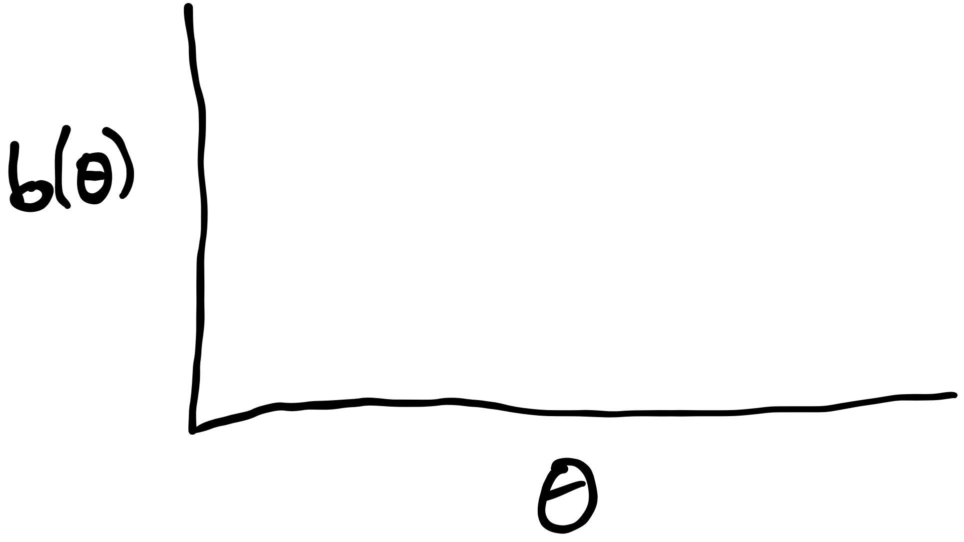
Bernoulli Distribution

$$\text{Bernoulli}(\theta)$$



Discussion: Given that I have received w wins and l losses, what should my belief (probability distribution) about θ look like?

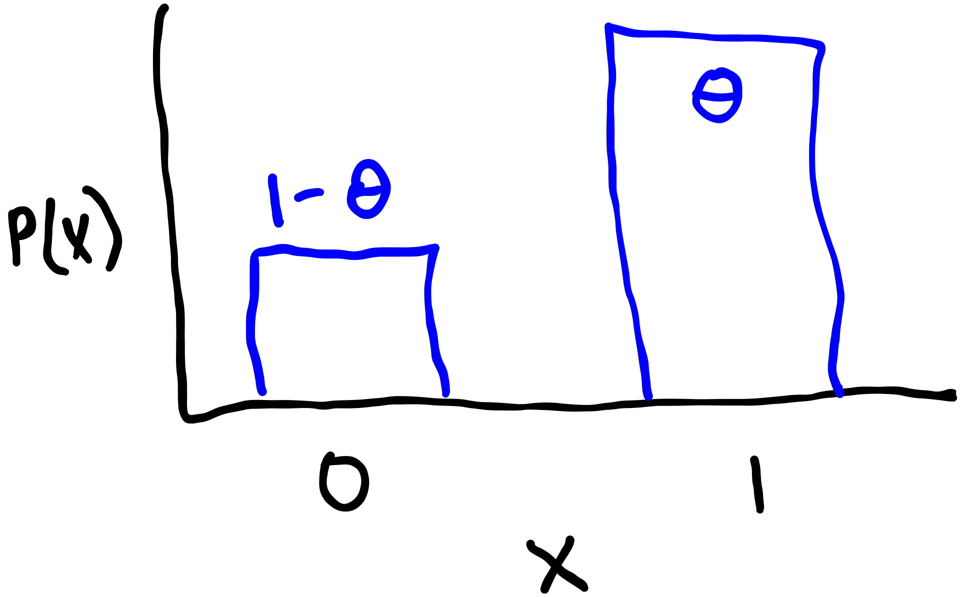
$w=4,\ l=1$



Bayesian Estimation

Bernoulli Distribution

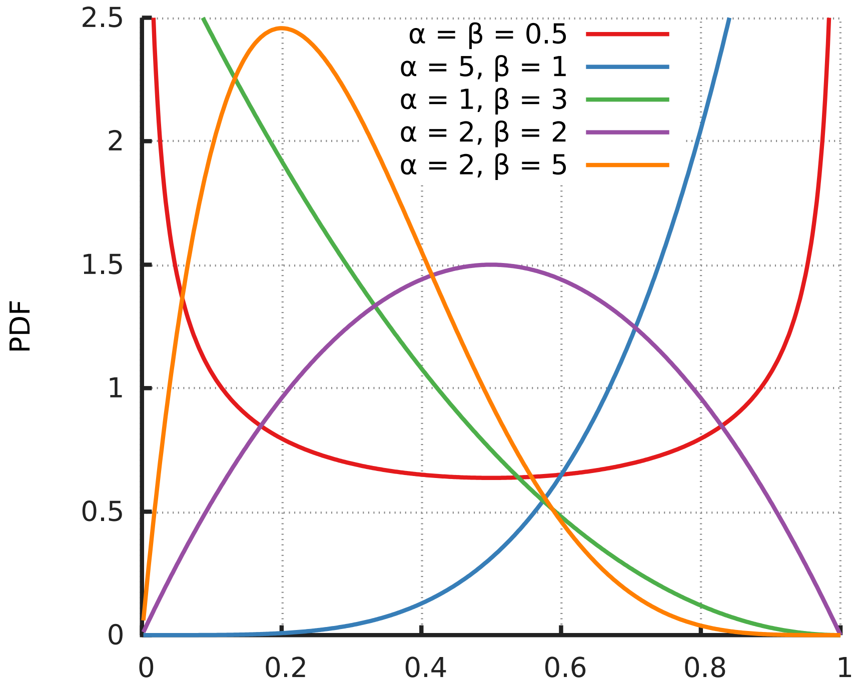
$$\text{Bernoulli}(\theta)$$



Beta Distribution

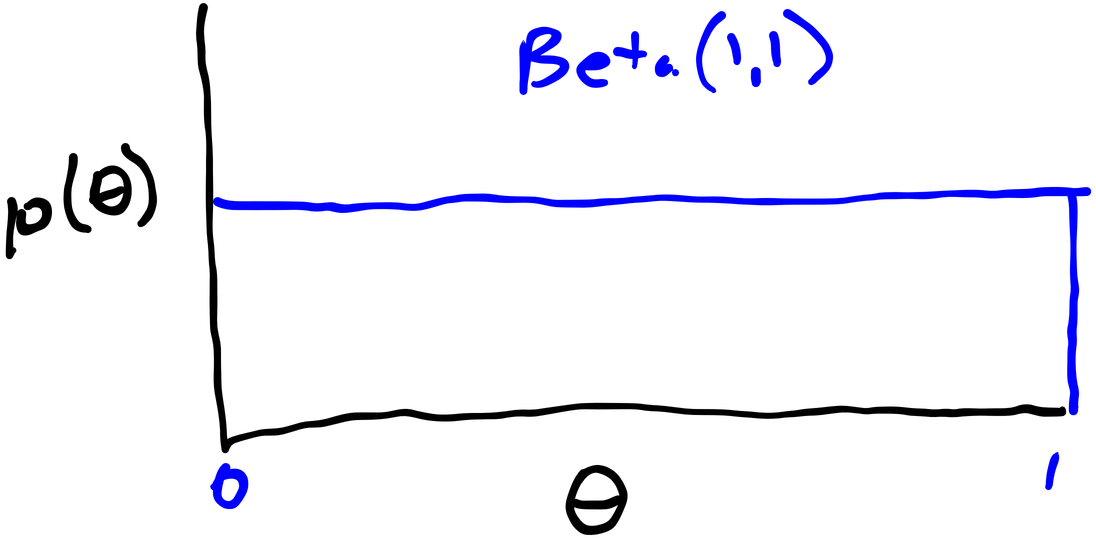
(distribution over Bernoulli distributions)

$$\text{Beta}(\alpha, \beta)$$



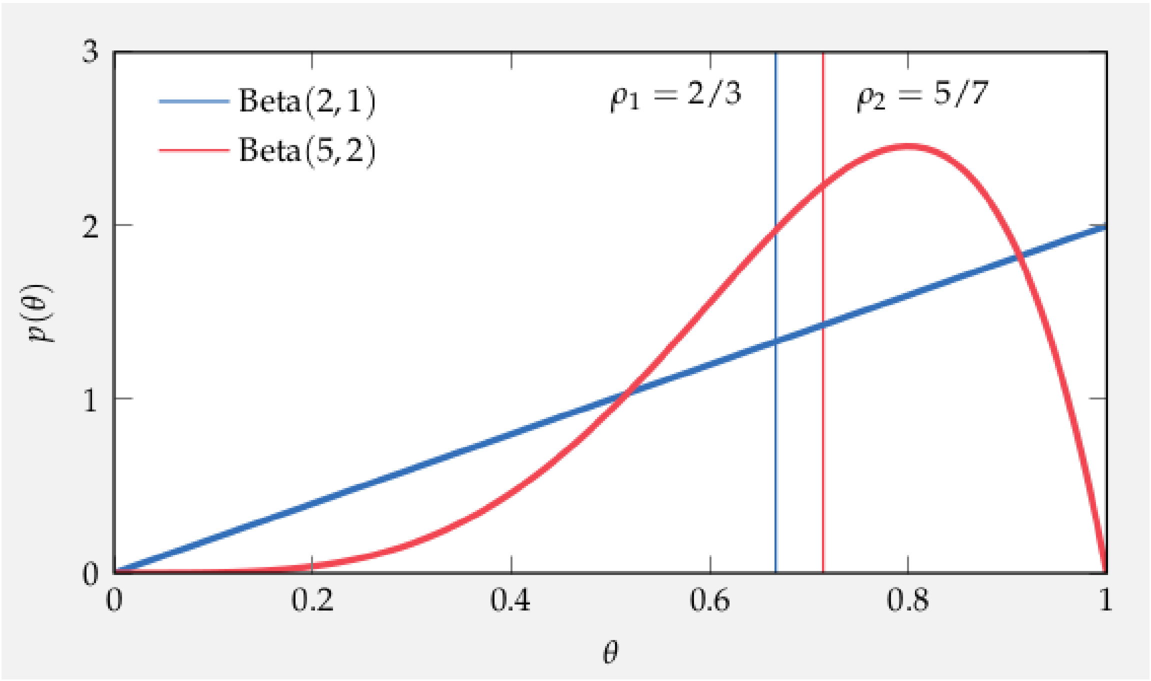
Bayesian Estimation

Given a $\mathrm{Beta}(1,1)$ prior distribution

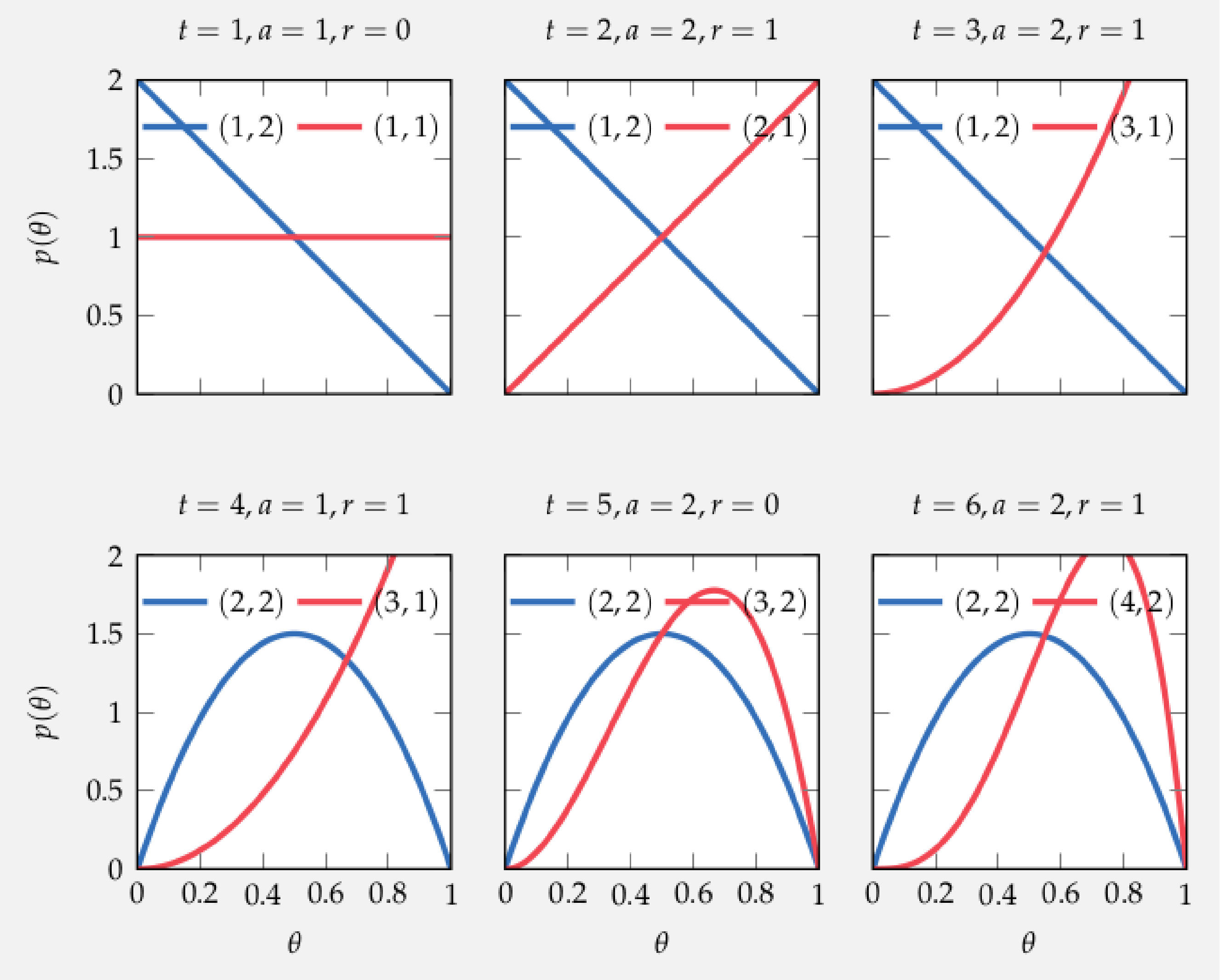


The posterior distribution of θ is

$$\mathrm{Beta}(w+1, l+1)$$



Bayesian Estimation



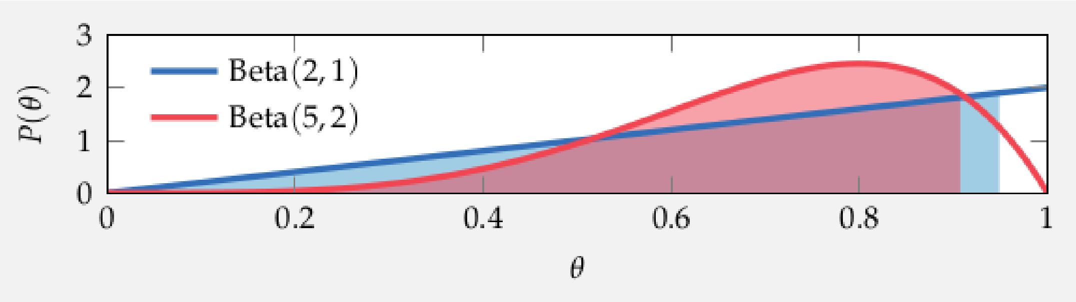
t = time

a = arm pulled

r = reward

Bayesian Bandit Algorithms

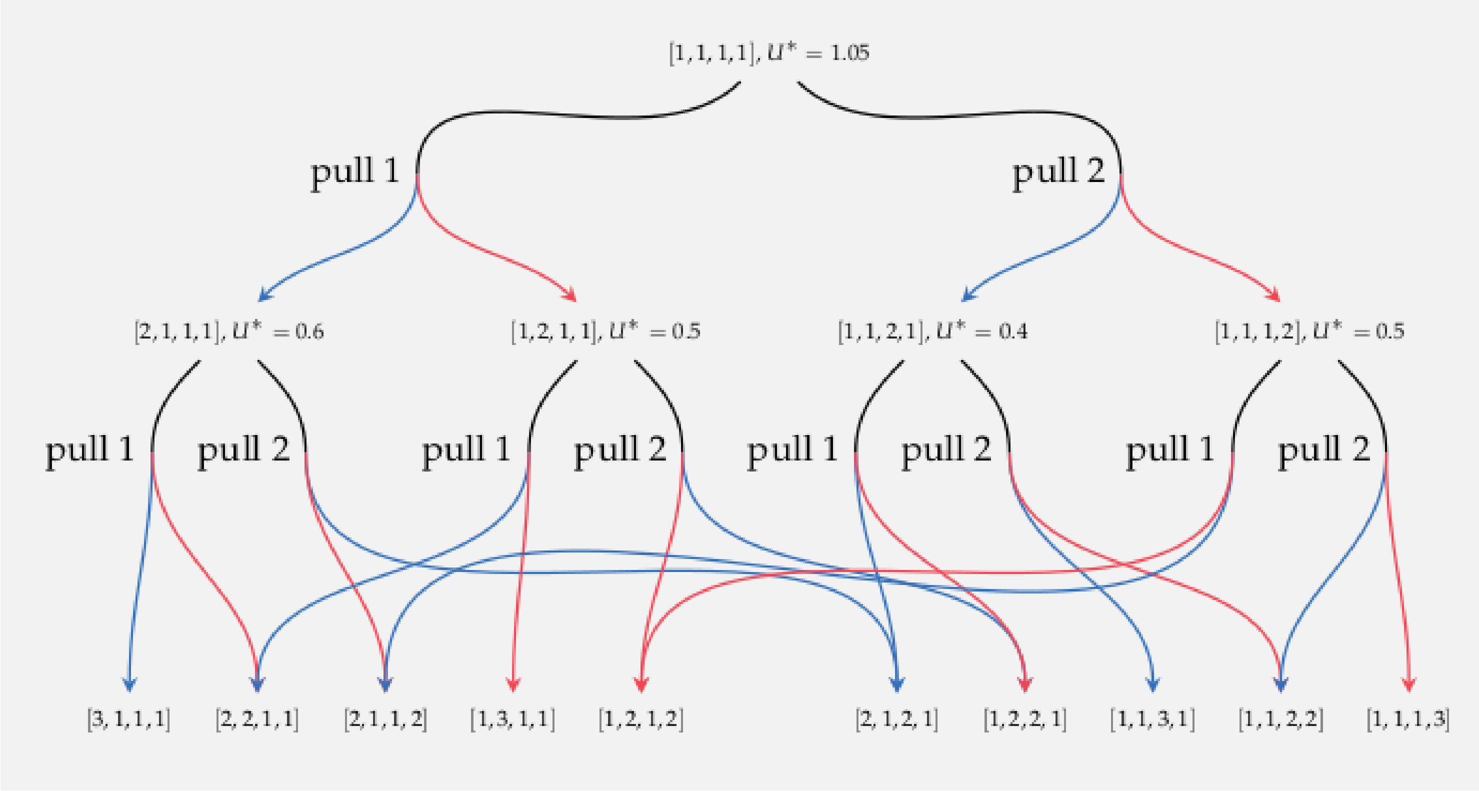
$\alpha = 0.9$



- Quantile Selection
  Choose a for which the α quantile of $b(\theta)$ is highest

- Thompson Sampling
  Sample $\hat{\theta}$
  Choose $\operatorname*{argmax}_a \hat{\theta}_a$

Optimal Algorithm - Dynamic Programming



Review

Guiding Questions

- What are the best ways to trade off Exploration and Exploitation