Because many outstanding problems in number theory, such as [Goldbach's conjecture](http://en.wikipedia.org/wiki/Goldbach%27s_conjecture) are equivalent to solving the halting problem for special programs (which would basically search for counter-examples and halt if one is found),