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This is SBCL 1.3.4.15614.texmacs.1-0729f5c41-WIP, an implementation of ANSI
  Common Lisp.
  More information about SBCL is available at <a href="http://www.sbcl.org/">http://www.sbcl.org/>.
  SBCL is free software, provided as is, with absolutely no warranty.
  It is mostly in the public domain; some portions are provided under
  BSD-style licenses. See the CREDITS and COPYING files in the
  distribution for more information.
SBCL> (ql::quickload :weyl)
  To load "weyl":
    Load 1 ASDF system:
       weyl
   ; Loading "weyl"
   (:WEYL)
SBCL> (declaim (sb-ext:muffle-conditions cl:warning))
   ((#<SB-KERNEL::CONDITION-CLASSOID WARNING> . MUFFLE-WARNING))
SBCL> (in-package :weyl)
  #<PACKAGE "WEYL">
SBCL> (reset-domains)
  NIL
SBCL> (ge-variable? 'x)
  NIL
SBCL> (setf ZZ (get-rational-integers))
SBCL> (setf R (get-polynomial-ring ZZ '(x1 x2 x3)))
  Z[x1, x2, x3]
SBCL> (setf x (coerce 'x1 R))
      (setf y (coerce 'x2 R))
      (setf z (coerce 'x3 R))
  x1
  x2
  xЗ
SBCL> (setf r1 (* (expt (-x) 3) (+ y (* 2 z))))
   (-x2 + -2x3)x1^3
SBCL> (partial-deriv r1 x)
  (-3 x2 + -6 x3) x1^2
SBCL>
SBCL> (setf QQ (get-rational-numbers))
  Q
SBCL> (setf RR (get-real-numbers))
SBCL> (setf CC (get-complex-numbers))
  С
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SBCL> (setf Q4 (get-quaternion-domain QQ))
  Quat(Q)
SBCL> (setf a (coerce 1234567890 ZZ))
  1234567890
SBCL> (setf b (coerce 127654 ZZ))
  127654
SBCL> (setf c (/ a b))
  \#<SIMPLE-ERROR "No applicable contagion method for ^{\sim}S and ^{\sim}S" {1003193BF3}>
SBCL> (setf q (coerce (/ 23 789) QQ))
  23/789
SBCL> (* a q)
  9465020490/263
SBCL> (prime? 77)
  NIL
SBCL> (factor 1234567890)
  ((2 . 1) (3 . 2) (5 . 1) (3607 . 1) (3803 . 1))
SBCL> (setq c 12345)
  12345
SBCL> (factor c)
  ((3 . 1) (5 . 1) (823 . 1))
SBCL> (factorial 32)
  263130836933693530167218012160000000
SBCL> (prime? 5678691)
  NIL
SBCL> (totient 123)
SBCL> (pochhammer 123 6)
  3905000064000
SBCL> (combinations 23 12)
  1352078
SBCL> (newprime 2332)
  #<UNDEFINED-FUNCTION NEWPRIME {1003510CB3}>
SBCL> q
  23/789
SBCL> (floor q)
  0
  23
SBCL> (ceiling q)
  1
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-766
SBCL> (truncate q)
              0
              23
SBCL> (round q)
              0
              23
SBCL> (+ b (* a q))
              9498593492/263
SBCL> (setf q (coerce 'q *general*))
              q
SBCL> q
SBCL> (setf p (coerce 'p *general*))
SBCL> (cl-user::type-of q)
              WEYLI::GE-VARIABLE
SBCL> (ge-variable? q)
SBCL> (setf ge1 (/ (* (+ 23 (* p q)) p) (- p q)))
               (-1 q + p)^-1 (23 + q p) p
SBCL> (setf ge2 (* (+ p q) (-p q)))
              (-1 q + p) (q + p)
SBCL> (simplify ge2)
              (-1 q + p) (q + p)
SBCL> (deriv ge1 'p 'q 'p)
              2 (-1 q + p)^-1 - (2 (-1 q + p)^-2 q) - (4 (-1 q + p)^-2 p) + 4 (-1 q + p)^-3
              (23 + q p) + 4 (-1 q + p)^{-3} q p + 2 (-1 q + p)^{-3} p^{2} - (6 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p
              + q p) p)
SBCL> (expand ge2)
              -1 q^2 + p^2
SBCL> (setf ge3 (/ ge1 ge2))
               (-1 q + p)^{-1} (23 + q p) p ((-1 q + p) (q + p))^{-1}
SBCL> (simplify ge3)
               (-1 q + p)^{-1} (23 + q p) p ((-1 q + p) (q + p))^{-1}
SBCL> (expand ge3)
SBCL> (simplify (deriv ge1 'p 'q 'p))
              2 (-1 q + p)^{-1} - (2 (-1 q + p)^{-2} q) - (4 (-1 q + p)^{-2} p) + 4 (-1 q + p)^{-3}
              (23 + q p) + 4 (-1 q + p)^{-3} q p + 2 (-1 q + p)^{-3} p^{2} - (6 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p) + 4 (-1 q + p)^{-4} (23 + q p
              + q p) p)
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SBCL> (expand (deriv ge1 'p 'q 'p))
SBCL> (simplify (/ p p))
SBCL> (simplify (/ ge2 ge2))
   (-1 q + p) (q + p) ((-1 q + p) (q + p))^-1
SBCL> (expand (/ ge2 ge2))
  0
SBCL> (reset-domains)
      (setf R *general*)
  NIL
  #<Domain: GENERAL-EXPRESSIONS>
SBCL> (setf u (coerce 'u R))
      (setf v (coerce 'v R))
      (setf w (coerce 'w R))
SBCL> (ge-variable? v)
SBCL> (add-subscripts u '(1 2 'a))
  u((1 2 'A))
SBCL> (get-variable-property R u 'key)
SBCL> (declare-dependencies u v w)
  (w v)
SBCL> (depends-on? u v)
SBCL> (setf x (+ 2 (* u v)))
  2 + v u
SBCL> (different-kernels x '(v))
   (u v V)
SBCL> (different-kernels x (list v))
  (u v)
SBCL> (setf xx (simplify (- x x)))
  2 - (2 + v u) + v u
SBCL> (simplify xx)
  2 - (2 + v u) + v u
SBCL> (expand xx)
  0
SBCL> (deriv x 'v)
  u
```

```
SBCL> (deriv (* x x) 'v)
   2 (2 + v u) u
SBCL> (expand (deriv (* x x) 'v))
   2 v u^2 + 4 u
SBCL> (expand xx)
SBCL> (let ((count 0)) (permute '(a b c d) (p) (print p) (incf count))
          (format t "~%~D permutations total. ~%" count))
   (D C B A)
   (C D B A)
   (D B C A)
   (B D C A)
   (C B D A)
   (B C D A)
   (D C A B)
   (C D A B)
   (D A C B)
   (A D C B)
   (C A D B)
   (A C D B)
   (D B A C)
   (B D A C)
   (D A B C)
   (A D B C)
   (B A D C)
   (A B D C)
   (C B A D)
   (B C A D)
   (C A B D)
   (A C B D)
   (B A C D)
   (A B C D)
   24 permutations total.
   NIL
SBCL> (weyli:partition (1 10) (print 1))
   (1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1)
   (2 1 1 1 1 1 1 1 1)
   (3 1 1 1 1 1 1 1)
   (2 2 1 1 1 1 1 1)
   (4 1 1 1 1 1 1)
   (3 2 1 1 1 1 1)
   (5 1 1 1 1 1)
   (2 2 2 1 1 1 1)
   (4 2 1 1 1 1)
   (3 3 1 1 1 1)
   (6 1 1 1 1)
   (3 2 2 1 1 1)
   (5 2 1 1 1)
   (4 3 1 1 1)
   (7 1 1 1)
   (2 2 2 2 1 1)
```

```
(4 2 2 1 1)
   (3 \ 3 \ 2 \ 1 \ 1)
   (6 2 1 1)
   (5 3 1 1)
   (4 \ 4 \ 1 \ 1)
   (8 1 1)
   (3 2 2 2 1)
   (5 2 2 1)
   (4 \ 3 \ 2 \ 1)
   (7 2 1)
   (3 \ 3 \ 3 \ 1)
   (6\ 3\ 1)
   (5 \ 4 \ 1)
   (9 1)
   (2 2 2 2 2)
   (4 2 2 2)
   (3 3 2 2)
   (622)
   (5\ 3\ 2)
   (4 \ 4 \ 2)
   (8\ 2)
   (4 \ 3 \ 3)
   (7\ 3)
   (6 \ 4)
   (55)
   (10)
SBCL> (require :sb-introspect)
   ("SB-INTROSPECT")
SBCL> (sb-introspect::who-calls 'weyli:ge-variable? )
   ((WEYLI::STANDARD-DERIVATION
                . #S(SB-INTROSPECT:DEFINITION-SOURCE
                     :PATHNAME #P"/home/kfp/quicklisp/local-projects/weyl/
   differential-domains.lisp"
                     :FORM-PATH (12)
                     :FORM-NUMBER 20
                     :CHARACTER-OFFSET 5097
                     :FILE-WRITE-DATE 3938251414
                     :PLIST NIL
                     :DESCRIPTION NIL))
               (WEYLI::STANDARD-DERIVATION
                . #S(SB-INTROSPECT:DEFINITION-SOURCE
                     :PATHNAME #P"/home/kfp/quicklisp/local-projects/weyl/
   differential-domains.lisp"
                     :FORM-PATH (12)
                     :FORM-NUMBER 33
                     :CHARACTER-OFFSET 5097
                     :FILE-WRITE-DATE 3938251414
                     :PLIST NIL
                     :DESCRIPTION NIL))
               (WEYLI::SAFE-DISPLAY
                . #S(SB-INTROSPECT:DEFINITION-SOURCE
                     :PATHNAME #P"/home/kfp/quicklisp/local-projects/weyl/
   general.lisp"
                     :FORM-PATH (100)
```

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:FORM-NUMBER 14
                    :CHARACTER-OFFSET 20112
                   :FILE-WRITE-DATE 3938251414
                   :PLIST NIL
                   :DESCRIPTION NIL)))
SBCL> (sb-introspect::function-lambda-list 'weyli:deriv)
  (WEYLI::EXPRESSION &REST WEYLI::VARIABLES)
SBCL> (sb-introspect::function-type 'weyli:deriv)
  (FUNCTION (T &REST T) COMMON-LISP:*)
SBCL> (sb-introspect::function-type 'weyli:expand)
  (FUNCTION (T) COMMON-LISP:*)
SBCL> (sb-introspect::find-function-callers 'weyli:expand)
  (#<FUNCTION MAKE-APP-FUNCTION>
             #<FUNCTION (SB-PCL::FAST-METHOD EXPAND (WEYLI::GE-EXPT))>
             #<FUNCTION (SB-PCL::FAST-METHOD EXPAND (WEYLI::GE-PLUS))>
             #<FUNCTION WEYLI::EXPAND-PRODUCT1>)
SBCL> (cl-user::quit)
  Busy...
SBCL>
```