

Model-Based RL as Stackelberg Games: Don't Be Fooled by Your Own Model

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1 Background

Model-based RL enables efficient learning and can be framed as a Stackelberg game [1]. In [2] they propose an algorithm to learn Stackelberg equilibria (in simple iterated matrix games).

Model Based RL as Stackelberg Game [1]

Environment M , Model \hat{M} , Policy π

Policy as Leader: $\max_{\pi} \left\{ J(\pi, \hat{M}^{\pi}) \mid \hat{M}^{\pi} \in \arg \min_{\hat{M}} \ell(\hat{M}, \mu_M^{\pi}) \right\}$
(PAL)

Model as Leader: $\min_{\hat{M}} \left\{ \ell(\hat{M}, \mu_M^{\pi}) \mid \pi \in \arg \max_{\pi} J(\pi, \hat{M}) \right\}$
(MAL)

where
 $\mu_M^{\pi} = \frac{1}{T} \sum_{t=0}^T P(s_t = s, a_t = a)$ and $\ell(\hat{M}, \mu) = \mathbb{E}_{(s,a) \sim \mu} [D_{KL}(P(\cdot|s,a), \hat{P}(\cdot|s,a))]$

Theorem 1: Given policy π and model \hat{M} such that

$$\ell(\hat{M}, \mu_M^{\pi}) \leq \epsilon_M \text{ and } J(\pi, \hat{M}) \geq J(\pi', \hat{M}) - \epsilon_{\pi} \forall \pi'$$

then for any optimal policy π^*

$$J(\pi^*, M) - J(\pi, M) \leq O(\epsilon_{\pi} + \frac{\sqrt{\epsilon_M}}{(1-\gamma)^2}) + \frac{1}{1-\gamma} D_{TV}(\mu_M^{\pi^*}, \mu_M^{\pi})$$

Learning a Stackelberg Equilibrium [2]

Contextualized Follower

for each pre-training iteration do // Follower Pretraining

sample random leader

query leader -> leader description ω

train follower given leader description ω (e.g. PPO)

for each training iteration do // Leader Training

query leader -> leader description ω

get best-response follower using ω

train leader

Inner-Outer Loop

for each leader iteration do // Outer Loop

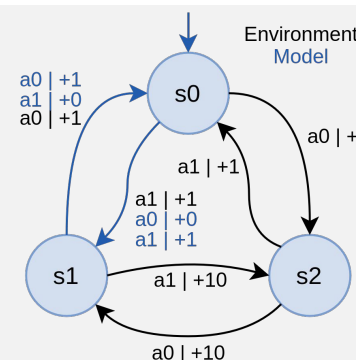
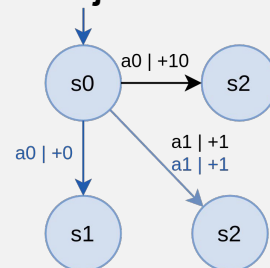
for each follower iteration do // Inner Loop

train follower

train leader

2 Theory

MAL Objective Flawed



MDP can be designed such that the final policy performs arbitrarily bad. We can prove that PAL does not suffer from this.

Theorem (ours): Given an approximate solution π to **PAL** with approximate best-responding models $\hat{M}(\pi)$, such that

$$\ell(\hat{M}(\pi), \mu_M^{\pi}) \leq \epsilon_M, \forall \pi \text{ and } J(\pi, \hat{M}(\pi)) \geq \sup_{\pi'} J(\pi', \hat{M}(\pi')) - \epsilon_{\pi}$$

$$\text{then } J(\pi^*, M) - J(\pi, M) \leq \epsilon_{\pi} + \frac{4\gamma\sqrt{\epsilon_M}R_{max}}{(1-\gamma)^2}$$

where π^* is an optimal policy and R_{max} is a bound on the absolute values of all rewards.

Fixing MAL

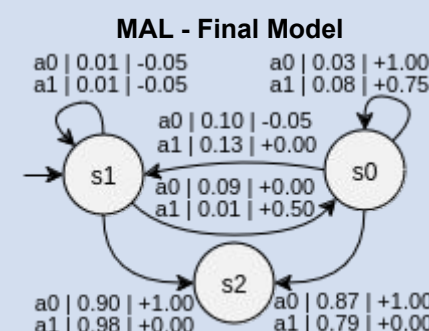
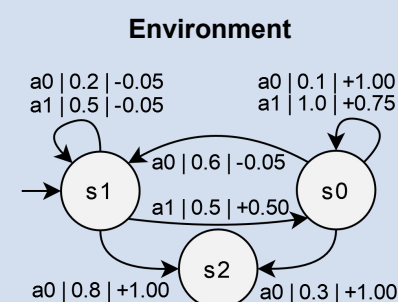
(MAL + Agent Reward)

$$\min_{\hat{M}} \left\{ \alpha \cdot \ell(\hat{M}, \mu_M^{\pi}) - (1-\alpha) \cdot J(\pi, \hat{M}) \mid \pi \in \arg \max_{\pi} J(\pi, \hat{M}) \right\}$$

(MAL + Random Noise)

$$\min_{\hat{M}} \left\{ \ell(\hat{M}, \alpha \mu_M^{\pi} + (1-\alpha) \mathbb{E}_{\pi' \in \Pi} [\mu_M^{\pi'}]) \mid \pi \in \arg \max_{\pi} J(\pi, \hat{M}) \right\}$$

3 Experiments



4 Results

Problem Formulation	Avg. Ep. Reward
MAL	00.97 ± 00.05
MAL + Agent Reward	36.93 ± 00.57
MAL + Random Noise	36.74 ± 00.67
PAL	36.77 ± 00.64

The average reward is the mean of 5 experiments.

5 Discussion

Model as Leader

- Can fail because the model is not incentivized to maximize the reward, thus it can hide parts of the environment
- Ergodicity and determinism are not strong enough
- Good mixing $D_{TV}(\mu_M^{\pi^*}, \mu_M^{\pi}) \rightarrow 0$ can solve the issue [1]
- MAL with changed leader objective can work
- Learns model only for best responding policies

Policy as Leader

- Provably aligned with the actual goal
- Reduces to normal model based RL in MDPs

6 Future Work

- Sample efficiency of PAL (e.g. on POMDPs)
- Theoretical guarantees for our MAL formulations
- Complex MDPs
- Thoroughly investigate why [1] worked
- Continuous environments

References

[1] Aravind Rajeswaran, Igor Mordatch, and Vikash Kumar. A game theoretic framework for model based reinforcement learning. CoRR, abs/2004.07804, 2020. URL <https://arxiv.org/abs/2004.07804>.

[2] Matthias Gerstgrasser and David C. Parkes. Oracles followers: Stackelberg equilibria in deep multi-agent reinforcement learning, 2023. URL <https://proceedings.mlr.press/v202/gerstgrasser23a/gerstgrasser23a.pdf>