Heidelberg University
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Project report for the lecture Fundamentals of Machine Learning

Reinforcement Learning for Bomberman

`https://github.com/nilskre/bomberman_rl`

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Abstract

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Contents

List of Abbreviations

CUDA	Compute Unified Device Architecture
DQN	Deep-Q-Networks
ELU	Exponential Linear Unit
MDP	Markov Decision Process
ReLU	Rectifier Linear Unit
PER	Prioritized Experience Replay

1 Introduction

Reinforcement Learning is a part of Machine Learning, where an agent is trained to interact in a desired way with its environment. Based on the current state, the agent decides for an action and can receive a reward for the chosen action. [13]

The potential of Reinforcement Learning is proven many times in varying contexts. E.g. attention was generated by the success of DeepMind's AlphaGo, the first artificial agent defeating a human in the game Go. For training this agent they used Reinforcement Learning. [15]

Salvador, Oliveira and Breternitz have summarized the evolution of Reinforcement in a literature review [13]. They start in 1989 with the publication introducing Q-learning. In the recent past many publications deal with the combination of Deep Learning with Reinforcement Learning. This area is known as Deep-Q-learning.

As part of this project we use Reinforcement Learning for learning how to play Bomberman. Bomberman is a strategic board game, which is played on a field containing walls, crates, bombs, coins and other players. For winning the game one must kill all other players. Typically in a game round first the walls around the player are removed by placing bombs. Next the agent can navigates to his opponents kill them by placing bombs. [11]

After introducing the fundamentals and related work in chapter 2, our approach is described in chapter 3. Therefore our selected Reinforcement Learning method and the training process are presented. In chapter 4 the results of our experiments are described. A conclusion is drawn in chapter 5.

2 Fundamentals and Related Work

Q-Learning is a known off-policy and model-free approach to train an agent based on temporal difference in an environment that can be modeled as a Markov Decision Process (MDP). An agent therefore does not necessarily use the policy it is trained for and does not know the transition probabilities and rewards in the MDP beforehand. Equation 1 shows the iterative update formula for the Q-values that an online model uses to choose the right action [7].

$$Q_{k+1}(s,a) = (1-\alpha)Q_k(s,a) + \alpha(r + \gamma \max_{a'} Q_k(s',a')) \tag{1}$$

The problem with conventional Q-Learning is that in most of the cases the state dimension is far too high to explore and model the MDP entirely

in foreseeable future. To deal with this problem the Q-values need to be approximated using a regression model. Deep neural networks have proven to be highly applicable for this task, which leads to the term of *Deep-Q-Learning* and respectively *Deep-Q-Networks* (DQN) for such network architectures. DQNs use the vectorized numerical state as its input and outputs the predicted Q-values. It learns through backpropagating the temporal difference error over each step for a single neuron. Note that for the Q-Learning algorithm a backpropagation is done after every step of the simulation. To avoid temporal correlation between succeeding experiences an experience replay buffer is used to randomly sample a training batch in each step. Also rare experiences will be used more frequently to update the model parameters using this approach. In the following papers regarding DQN architectures shall be introduced as well as papers dealing with the bomberman environment for reinforcement learning.

Paper [16] tackles the problem that the *max* operator in 1 often leads to overoptimistic value estimates as the DQN uses the same Q-values to both select and evaluate an action. It therefore changes the iterative update formula to 2.

$$Q_{k+1}(s,a) = (1-\alpha)Q_k(s,a) + \alpha(r + \gamma Q'_k(s', arg\max_{a'} Q_k(s',a'))) \tag{2}$$

Now a target DQN is used to separate the determination of the greedy policy, which is still done by the online network, from the Q-value estimation. Using this double DQN approach results in less overestimated Q-values and therefore better policies by more accurate Q-value estimates. It also makes the learning process more stable and reliable. The weights are copied from the online network to the target network after a fixed amount of episodes.

Another optimization was introduced in paper [17]. It changes the architecture of the DQN by splitting it into two separate value streams. One stream estimates the state value function and the other one the state-dependent action advantage function. Both streams are then combined again using a special aggregating layer to produce an estimate of the Q-values (see Figure 1).

The state-dependent action advantage function is defined as

$$A^\pi(s,a) = A^\pi(s,a) - V^\pi(s) \tag{3}$$

and measures the importance of each action. The special aggregating layer uses Equation 4 to estimate the Q-values while also tackling the issue

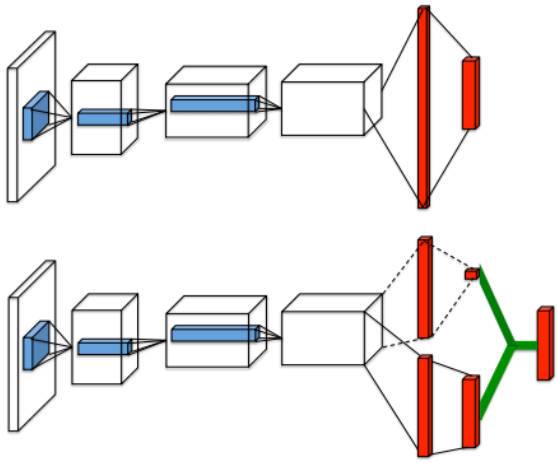


Figure 1: Architecture of a normal DQN (top) compared to a dueling DQN (bottom)

of identifiability.

$$Q(s,a;\theta,\alpha,\beta) = V(s;\theta,\beta) + (A(s,a;\theta,\alpha) - \frac{1}{|A|}\sum_{a'} A(s,a';\theta,\alpha)) \tag{4}$$

Using the dueling architecture approach an agent can learn which states are valuable independently of each action, which is esspecially useful in case actions do not influence the environment in any useful way. This leads to a better and more robust policy evaluation in the presence of many similar-valued actions. Also when looking at the last layer of a conventional DQN (see Figure 1) it usually becomes much more sparse and biased. As the state value is modeled as a single neuron in the dueling architecture, learning the state value function becomes much more efficient.

Obviously, approaches exist that combine double Deep-Q-Learning with dueling architectures like [10].

Besides optimizing the learning process itself and the model architecture, [14] now proposes a way to sample more efficiently from the experience replay buffer. Each experience is assigned a learning priority score p_i with

$$p_i = \frac{1}{rank(i)} \tag{5}$$

where $rank(i)$ is the rank of experience i in the priority queue built upon the magnitude of the temporal difference error δ of each experience.

The stochastic sampling probability of each experience is then calculated according to

$$P(i) = \frac{p_i^\alpha}{\sum_k p_k^\alpha} \quad with\ 0 \leq \alpha \leq 1. \tag{6}$$

The hyperparameter α determines the degree of using prioritization over random sampling. Using this stochastic sampling approach tackles the problem of a diversity loss and subsequent over-fitting when just greedyly sampling according to the magnitude of δ. One could also choose

$$p_i = |\delta_i| + \epsilon \tag{7}$$

instead of 5 but the latter is more prone to outliers. Furthermore, each gradient descent step during backpropagation needs to be weighted with

$$w_i = (\frac{1}{N}\frac{1}{P(i)})^\beta \tag{8}$$

to counter a bias towards high prioritized experiences introduced using the prioritized experience replay buffer. The weights should also be normalized with $\frac{1}{max_i w_i}$. As an unbiased nature of weight updates is esspecially important during the last training updates near convergence, β increases slowly from a start value β_0 to 1 over time.

There are several other improvements mentioned in the rainbow paper [9] like multi-step learning, distributional reinforcement learning and noisy nets, but these are out of the scope for this small research project.

Other papers were found that explicitly use DQNs within the Bomberman environment. One of them being [11] which introduces two novel exploration strategies, Error-Driven-ϵ and Interval-Q, and compares them to conventional exploration strategies like Diminishing ϵ-Greedy and Max-Boltzmann, whereas Max-Boltzmann with decreasing temperature parameter still performs best in the long run by empirical evaluation. Nevertheless Error-Driven-ϵ, despite being less stable, learns faster than all other exploration techniques. The paper also gives an approach to encode the state. Therefore, for each cell four values are computed:

- Free, breakable and obstructed cells are encoded as either 1, 0 or -1,
- The position of the player and opponent players are encoded as 1, free cells as 0 and
- The danger score for each cell is calculated as $\frac{timepassed}{timeneededtoexplode}$, which gets an additional negative sign in case a bomb was planted by the player itself.

The paper also gives valuable insights into the configuration of hyperparameters, rewards and the amount of training needed until convergence, which is about 100 generations à 10.000 episodes.

[6] uses an imitation-based learner that trains its model with the actor-critic proximal-policy optimization method in the Bomberman environment. Here insights about how rewards need to be chosen and which state representation to choose can also be derived.

Bomberman seems to provide a perfect environment to try out different reinforcement learning methods, which is why [5] provided an artificial intelligence platform around Bomberman including several associated intelligent agents and empirical experiments.

3 Approach

3.1 Reinforcement Learning Method and Regression Model

3.1.1 Features

This chapter describes how the game state is transformed into input features for the model. Our initially tried encoding is based on [11]. The dictionary containing the game state is transformed into one vector, containing the input features. Our input feature vector consists of the following five independent matrices:

- Field state: free (0), breakable (1), obstructed cell (0.5)
- Player position: player (1), otherwise(0)
- Opponent positions: opponent (1), otherwise(0)
- Danger level of position: danger (1), no danger (0)
  Danger is caused by bombs on all fields an explosion can reach. Two aspects influence the value how dangerous a field is. The time until the bomb explodes and the distance from the bomb. We derived following equation for calculating the danger of a field for the field containing the bomb and the surrounding fields. The resulting danger score is normalized through the equation in the range between 0 and 1.

  $$danger = \frac{\frac{time\_Passed}{time\_needed\_to\_explode}}{\sqrt{distance}}$$

  Example 1: the bomb explodes after 4 time steps. Currently 2 time steps are over and the distance to the bomb is 3:

  $$danger = \frac{\frac{2}{4}}{\sqrt{3}} = 0.28$$

Example 2: the bomb explodes after 4 time steps. Currently 3 time steps are over and the distance to the bomb is 1:

$danger = \frac{\frac{3}{4}}{\sqrt{2}} = 0.75$

- Desirability of position: coin (1), no coin (0)

These matrices are flattened and concatenated. This results in a feature vector containing 1445 elements (5*17*17).

Among other factors due to the high dimensionality the training process could be very slow. That is why the input state is further minimized. Franca, Paes and Clua [6] evaluated five different strategies for state representation (Binary Flag, Normalized Binary Flag, Hybrid, ICAART, ZeroOrOne). The performance of the different encodings is measured by the cumulative rewards during training in relation to the number of episodes. Their results were that Hybrid, ICAART and ZeroOrOne perform better than Binary Flag and Normalized Binary Flag. The best encoding regarding to [6] is ICAART. That is why our finally implemented encoding is based on ICAART.

The following paragraphs describe our finally chosen encoding: The matrices above encode three different types of information: general information (field state, player position, opponent positions), desired positions (Desirability of position) and dangerous positions (Danger level of position). We minimize the input state by concatenating general information and desired positions in one matrix and dangerous fields in another one. This keeps the balance between clearly separated information and maximal state minimization.

- General information and desired positions: free (0), breakable (1.5), obstructed cell (-1.5), own position (2), opponent positions (-2), coin (1)
- Danger level of position: danger (-1), no danger (0)

These matrices are flattened and concatenated. This results in a feature vector containing 578 elements (2*17*17).

3.1.2 Double Dueling DQN

3.2 Training process

3.2.1 Exploration-Exploitation

When choosing the right method for the exploration-exploitation tradeoff, [11] gives an insight in how different exploration methods perform in the Bomberman environment (see Figure 2).

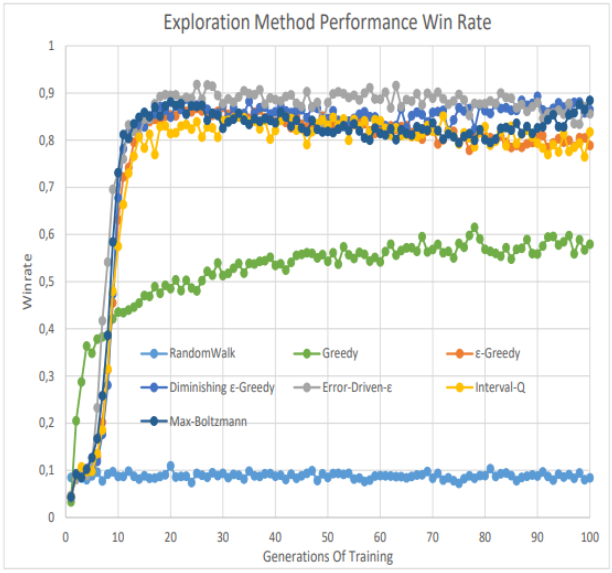


Figure 2: Comparison of different exploration methods

In the long run, Max Boltzmann performs best with

$$\Pi(s,a) = \frac{e^{Q(s,a)/T}}{\sum_i^{|A|} e^{Q(s,a^i)/T}} \tag{9}$$

and T being the temperature parameter. But as the result is based on 100 generations of training with each generation comprising 10.000 episodes, Diminishing ϵ-Greedy as the second best exploration method was chosen as this exploration method converges faster in the early stages of training.

Two improvements where considered to optimize the exploration phase, but were discarded in the end. The first one is to replace the uniform sampling method by a multinomial sampling method in case an exploration step should be done, i.e. when a randomly generated number is smaller than ϵ. This means the second best action would be chosen more often compared to other actions during the exploration phase. This could be beneficial especially in later phases of training in case the Q-values are close to each other. But esspecially in the beginning of the training phase this could lead towards an unintended bias towards specific actions as the exploration of others will be suppressed probabilistically.

The second improvement was to include an exploration function as [7] proposes. A simple exploration function could be

$$f(q,n) = q + \frac{K}{1+n} \tag{10}$$

with q being the Q-value and n being the count how often a specific action a was chosen in state s. K is a hyperparameter that determines the amount of curiosity during training. To implement this one would need to store n for every state and action. But as the state is far too high dimensional in the Bomberman environment this would require a lot of training just as using the Max Boltzmann exploration method to be beneficial in the end.

3.2.2 Prioritized Experience Replay Buffer and SumTree

Furthermore, a prioritized experience replay buffer was utilized to speed up the training process. To efficiently sample from it, a SumTree data structure was implemented inspired by [14], which is a binary tree whose parent nodes store the sum of its children. All leaf nodes of the SumTree store the priority of each temporal difference error which is the L1-norm between two succeeding Q-values. The SumTree inherently offers a stratified sampling method to sample experiences with a high temporal difference error and therefore high priority more often. Therefore the leaf nodes are grouped into sum segments with a sum value greater or equal a threshold value. Each segment can therefore contain a different amount of leaf nodes as priorities often differ in their magnitude. The amount of segments is determined by the demanded batch size and the threshold value by dividing the total sum of the tree (stored in the root node) by the batch size. From each segment one priority is sampled uniformly. As high priorities have less competitors in their segment, they will be sampled more frequently until they get overwritten.

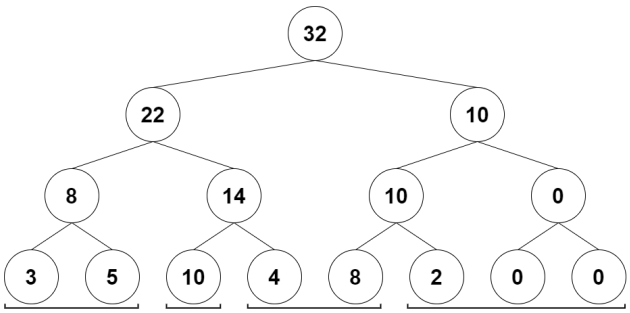


Figure 3: Stratified sampling of priorities from a SumTree

Figure 3 illustrates the process of sampling priorities with a batch size of four. One can see that the priority with magnitude ten will be sampled every time as it is the only priority within the sum segment. One can also see that in case the prioritized experience replay buffer is not filled, zeros might be sampled. To counteract this, the amount of sum segments to divide the SumTree into is the batch size plus one. Adding values to the SumTree

has the complexity O(n) whereas updating the SumTree has the complexity O(log n).

The prioritized experience replay buffer only stores the priorities in the SumTree. The tuple (s, a, r, s') is stored in a separate list. To access the according experience tuple for a priority, one can easily calculate the acording index by $index_{list} = index_{tree} - size_{per} + 1$. Note that Equation 7 is used to calculate the priority value for each temporal difference error instead of Equation 5 as one would need to also sort the priorities in a different data structure which would add additional complexity and computing time. When sampling a batch from the prioritized experience replay buffer the tupel (s, a, r, s'), the according priorities, normalized weighting factors and update indices are returned.

Drawbacks of using a prioritized experience replay buffer over a normal experience replay buffer is the continuous maintenance of the SumTree data structure, which is currently updated every training step, i.e. every step in an episode. Updated value changes need to be propagated to the root node. This adds additional computing time but the time gained in training progress by using prioritization should make up the time lost by maintaining the SumTree. Besides updating existing experiences every step also a new experience is added to the prioritized experience replay buffer every step which on the other hand executes fast.

3.2.3 Imitation Learning

For addressing the challenge of long training times Imitation learning can be used. With the rule based agent already a strong agent is present in the project. The idea of Imitation learning is to speed up training by learning from existing behavior (e.g. from the rule based agent).

Paper X Y and Z have done IL and received XYZ results. can outperform their teachers

How it is realized This optimization is realized Training process is split into a pretraining phase and a training phase. In the pretraining phase two tasks train network fill experience buffer

Second step: Start training (standard RL) with the already filled experience buffer.

3.2.4 Reward shaping

Rewards are given when different kind of actions are taken or different kind of events occur. An overview of all rewards is given in Table 1.

Table 1: Reward function

Reward	**Amount**
Movement in/out of danger zone	-0.3/+0.3
Movement towards/away from nearest coin	+0.1/-0.1
Movement towards/away from nearest opponent	+0.05/-0.05
WAITED	-0.2
INVALID_ACTION	-1
BOMB_DROPPED	0.4
CRATE_DESTROYED	0.7
COIN_COLLECTED	0.2
KILLED_OPPONENT	1
KILLED_SELF	-1
GOT_KILLED	-1

Setting the rewards properly is a very difficult task and hard to evaluate without empirical study. Specifically for the Bomberman environment only for literatue was found that covers a reward function [11, 6]. All rewards are normalized to be in between -1 and 1 for more efficient training. Also focus was set on giving reward feedback as soon as possible to guide the training process better towards the desired behavior.

In the first step the agent should be encouraged to gather coins, which is why the movement towards the nearest coin is rewarded. Nevertheless especially in the beginning of a game and also in late game phases setting bombs to find coins, to explore the arena and to kill opponents is even more crucial than finding coins. This is why the reward for dropping bombs is even higher than moving towards coins and gathering coins. To place bombs near creates the reward for destroying crates is set above the reward to simply dropping a bomb.

Having this setup of arranging rewards leads to a lot of suicide of the agent in the very beginning of the training phase even if the the own agents death is punished. Therefore rewards for moving out of danger zones and punishments for moving in danger zones are given to encourage the agent to walk away from bombs dropped. Note that this reward is even higher than the movement reward towards the nearest coin to keep an agent out of a danger zone in case a coin is located in the bomb radius.

Also an agent doing nothing or a invalid action should be punished by a negative reward. Therefore also no reward is given for rounds survived. Committing suicide or idleing was a big problem especially in the early stages

of the training phase that should be countered using the introduced reward function.

Killing opponents gives the highest reward, which is exactly five times higher than collecting a coin just like the points given inside the game. Finally to encourage an agent to also move towards an opponent agent an additional movement reward is given for moving towards the nearest opponents and a punishment in case the agent runs away from the nearest agent. Nevertheless such a reward is scaled quite low and only becomes more important in the late game steps. In the early stages of a game the agent should rather learn how to collect coins, how to destroy crates and how to survive.

One could also think of introducing a reward schedule that increases certain rewards during a game and lowers others. This could be applied when all coins are collected and an agents score can only be increased by killing opponents. This still has to be evaluated.

3.2.5 Hyperparameters

Table 2 shows the choice of hyperparameters during training. As the computing resources are limited the hyperparameters were chosen to reach a fast convergence towards a first proper behavior which does not need to be optimal in the first place. [11] states to train an agent over 100 generations à 10.000 episodes whereas the win rate in Figure 2 is already quite high just after 10 generations. Having 400 steps per episode 1.800 episodes can be trained locally within 24 hours which is really low inspite of using CUDA on a graphics card with a computing power score of 6.1 of 10.

The amount neurons per dense layer inside the dueling double DQN should not be higher than the input dimension itself as such a high degree of freedom is not needed to model the bomberman environment. For simplicity of the training process 128 was prefered over 256.

The Exponential Linear Unit (ELU) activation function was chosen to fight the dead ReLU problem and to speed up training by pushing the mean activation towards zero and therefore decreasing the bias shift from ReLU. To be more robust towards outliers a Huber loss function was prefered over a conventional Squared Error loss function. The learning rate was set quite high with 0.01 to reach a fast convergence towards a first playable behavior on limited computing resources.

The choice of the prioritized experience replay buffer hyperparameters was inspired by [14]. α was chosen slightly higher to once again speed up training through more prioritization. The β increment summand was chosen just as high to converge β to 1 at approximately the same time as ϵ converges to its lower limit after around 60.000 steps.

Table 2: Hyperparameters

Hyperparameter	**Value**
Dense layer dimension	128
Activation function	ELU
Loss function	Huber
Learning rate	0.01
α	0.65
β	0.4
β increment	0.00001
temporal difference ϵ bias	0.01
PER buffer min size	8.192
PER buffer max size	65.536
Batch size	64
γ	0.95
ϵ start	0.3
ϵ end	0.16
ϵ decay factor	0.99999

The size of the prioritized experience replay buffer needs to be a power of two to result in a balanced SumTree. The batch size should be lower than one percent of the total prioritized experience replay buffer size, which is why the minimum size of the prioritized experience replay buffer was chosen to be 8192. This leads to a start of the training process after around 148 episodes.

Choosing the right γ in approximative Q-learningis not too important as future rewards are approximated. Using a decaying factor of $\gamma = 0.95$ means rewards after 13 steps are only half that important as current rewards. ϵ is often decayed to around 0.05-0.2 and starts at either 1 or 0.3 [9, 11, 6]. To not have too much random behavior but setting more focus on fast behavior learning, 0.3 was chosen as the start value for ϵ.

Furthermore, the model and the prioritized experience replay buffer are stored every 100 epsiodes in case the training process crashes because of unforeseen events.

3.2.6 Local Training Setup

3.2.7 Training Visualization

3.2.8 Cloud Training

To further accelerate the training process and enable fast iterations for improving the approach, the possibility of training in the Cloud was evaluated.

The prospects of success were shown by Lawrence et al. [12]. They evaluated the TensorFlow Deep Learning performance between CPUs, GPUs, local computers and the cloud. Their findings were that the usage of GPUs leads to a significant performance increase. Furthermore the cloud is not better by default. That is why it is recommended to compare the GPU performance metrics (compute capability score) of the local and the cloud configuration.

Based on these findings for our purposes two requirements exist:

1. The Cloud GPUs should be much more performant than the local GPUs. To notice visible improvements we at least expect a compute capability score of seven.

2. The GPUs could be used for free.

Hale [8] compares the following Cloud providers: Google Colab, Google Cloud Platform, AWS, Paperspace and vast.ai. In general either the first or the second requirement are not fulfilled by the different cloud providers.

This is exemplary illustrated by means of Google Colab and Google Cloud Platform. On the one hand Google Colab can be used after converting the project into one jupyter notebook. GPUs can be used for a limited time frame for free. The available GPUs are Nvidia K80s, T4s, P4s and P100s, which are assigned automatically [1]. The compute capability score lies depending on the GPU between 3.7 and 7.5 [4]. So Google Colab matches the second requirement, but not the first one. On the other hand the Google Cloud Platform, especially the AI Platform offers many performant GPUs to choose from, but it can quickly become very expensive, as the following example calculation shows [3].

The calculation was done with the Google Cloud Pricing Calculator [2] and following parameters:

- Region: United States
- Selected tier: BASIC_GPU
- Job run time in minutes: 4320min (3 days)

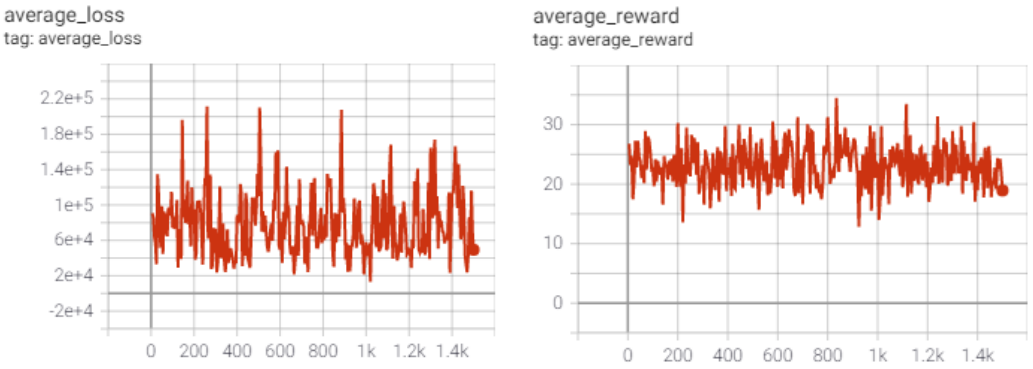
- => estimated costs: 71.93€

That is why the Google Cloud Platform matches the first requirement, but not the second one.

Based on the above findings the possibility of cloud training is not realized.

4 Experimental results

When starting the initial training process first a pre-training is executed which serves to fill the prioritized experience replay buffer with experiences from an expert rule-based agent and to pre-train the model itself to build up on some agent behavior already for the later training process. To not introduce a heavy bias the pre-training is stopped after 1.5k training games. Figure 4a shows the aggregated step loss per episode averaged after five episodes and Figure 4b the reward per episode averaged after five episodes.



(a) Pre-training loss

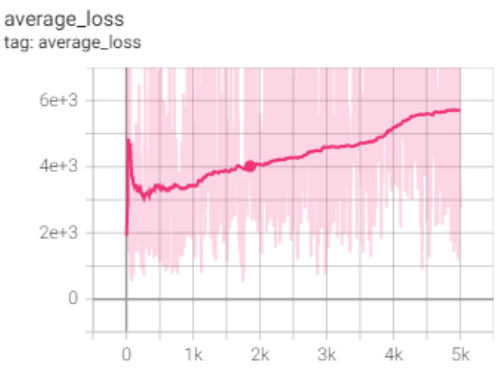
(b) Pre-training average reward

When initiating the main training process with experiences gained from the dueling double DQN itself the following training curves can be experienced:

The complete opposite of what was expected was observed, the loss increased whereas the average reward decreased. One possible explanation was a possible training bias introduced through the prioritized experience replay buffer towards transition with a high temporal difference error. Even if the gradient weighting factors were calculated and used to anneal the bias as proposed in the original paper, still this unintended behavior could be experienced. Therefore the training process was aborted after 5k episodes.

The next generation of the model was trained on a normal experience replay buffer with the following results:

[image here]



(a) Main-training loss

(b) Main-training average reward

We also increased the initial exploration factor ϵ to one to counter a possible pre-training bias and decreased the maximum size of the experience replay buffer to 32.768 instead of 65.536 to train on more recent experiences.

5 Conclusion

A Appendix

A.1 Appendix A

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