# Automatic Retinal Vessel Segmentation via Deeply Supervised and Smoothly Regularized Network

Yi Lin, Honggong Zhang, and Guang Hu

Abstract—In recent years, retinal vessel segmentation technology has become an important component for disease screening and diagnosing in clinical medicine. However, retinal vessel segmentation is a challenging task due to complex distribution of blood vessels, relatively low contrast between target and background, and potential presence of illumination and pathologies. In this paper, we propose an automatic retinal vessel segmentation network using deep supervision and smoothness regularization, which integrates holistically-nested edge detector (HED) and global smoothness regularization from conditional random fields (CRFs). It is an end-to-end and pixel-to-pixel deep convolutional network, can perform better results than HED-based methods and the methods where CRF inference is applied as a post-processing method. With co-constraints between pixels, the proposed DSSRN obtains better results. Finally, we show that our proposed method obtains a sate-of-the-art vessel segmentation performance on all three benchmarks, DRIVE, STARE and CHASE DB1.

Index Terms—Vessel segmentation, deep learning, medical image analysis, deep supervision, conditional random field.

#### I. Introduction

The delineation of morphological attributes of retinal blood vessels has a certain connection with cardiovascular diseases, such as diabetes and hypertension [1], [2]. Retinal vessel segmentation technology is becoming a fundamental and important component for disease screening and diagnosing in clinical medicine. On the one hand, it helps speed up automatic retinal disease screening [3], releasing the labor of doctors and specialists; on the other hand, retinal vessel segmentation will help to early detect and control related diseases, has good effect of diabetic retinopathy [4], hypertensive retinopathy [5], cardiovascular diseases [6] and arterial narrowing [7].

At present, the existing retinal vessel segmentation algorithms can automatically classify blood vessels from background, but there are still two main challenges: First, the contrast between retinal blood vessels and background in different retinal image databases is different; it is easier to good segmentation results where the region has a striking contrast; otherwise. it is harder. Second, illumination and pathologies have a great influence, as is known, the vessels are dark and background is bright in retinal images, which is the most important factor to make a distinction, but the brightness

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can be affected by illumination reflection and pathologies in the form of cotton wool spots, bright and dark lesions.

Due to the importance of the retinal vessel segmentation problem, there are many methods have been proposed to address this challenging task [8], [9], [10], [11], [12] by utilizing different image features, such as textual features and wavelet features, and different machine learning methods, such as supervised classifiers and unsupervised matching methods. However, their performance of vessel segmentation is not satisfactory enough.

It is natural to apply deep learning for this vessel segmentation problem. Inspired by other semantic segmentation tasks, most research of using Fully Convolutional Networks (FCNs) have successfully achieve remarkable result. Long et al. [13] showed that a FCN trained end-to-end, pixel-topixel map on semantic segmentation, and exceeded the most existing methods. Later, Xie et al. [14] further proposed the Holistically-Nested Edge Detector (HED) model, which is to automatically learn the rich hierarchical representations with deep supervision, and resolved the challenging ambiguity in edge and object boundary detection. Besides, most researchers have given attention to pixel-level labelling in image understanding. The HED model obtains very impressive on the problem of edge detection in natural images, which is getting close human's performance. Since the retinal vessel segmentation problem is similar to the edge detection problem, applying holistically-nested edge detection network for vessel segmentation seems to be a very good solution.

However, thought the vessel segmentation problem and the edge detection problem is similar, there are clear differences. Notices that not all edge pixels in retina images are vessels and not all vessel pixels appear on boundaries. Besides, different from edges which have a width of one pixel, vessel have variant width. Thus, we need to develop new techniques to address these differences. Our observation is that nonmaximum suppression is applied for removing duplicated edge pixels and only the skeleton of edge is preserved. But the vessel widths are different, we should have a model to reasoning the contextual information to obtain the true region of vessels. In addition, contextual information is also important to avoid false positives and recall false negatives. To accomplish this task, we recall a classical statistical model which is good modeling contextual information, which the conditional random field (CRF) method [15]. CRF acts as a smoothness regularizer and can use the spatial contextual information in image to obtain better segmentation results.

In the recent research of deep learning based semantic segmentation works, Zheng et al. [16] proposed the CRFasRNN,

integrated CRF modelling with CNN, trained the whole deep end-to-end network, which is efficient in semantic segmentation task. By taking the advantages in the previous literatures, in this paper, we propose a deep retinal vessel segmentation network based on the holistic-nested edge detection model which provides deep supervision, and combine CRF to provide the global smoothness correlation. The deep network is termed as deeply supervised and smoothly regularized network (DSSRN).

Compared to widely used HED network structure, the proposed DSSRN has the following advantages: 1) shallower side outputs capture rich detailed information; 2) deeper side outputs have better global high level knowledge but fuzzy. So, we combined CRF with HED, built an end-to-end network, put the smooth correlation into the deeply supervised net. With co-constraints between pixels, results from DSSRN method perform better: 1) shallower side contains more detailed information; 2) segmentation result retains more tiny vessels. Our method produces state-of-the-art results on three widely used retinal vessel segmentation datasets.

The details of the proposed DSSRN will be given section III. In the experiments, we have tested three public available datesets, the DRIVE dataset [8], the STARE dataset [17] and the CHASE\_DB1 dataset [18]. The retinal images in the three datasets are captured under different conditions. The proposed DSSRN retinal vessel segmentation method can obtain the state-of-the-art performance on all three datasets, which confirms the effectiveness and superiorities of the proposed method. Besides of the advanced the results, the main contribution of the paper is a deeply supervised and smoothly regularized network for retinal vessel segmentation and beyond, as other vessel segmentation tasks will also be beneficial from the proposed network design.

In the rest of the paper, Section II will briefly introduce related works; Section III will give the details of the proposed deeply supervised and smoothly regularized network for retina vessel segmentation; Section IV will gives the details of the experiments, compare the proposed method to other methods and carry out ablation studies; Finally, Section V will concludes the paper.

#### II. RELATED WORKS

Since the last century, many algorithms have been published relating to segment the retinal vessels. For example, Chaudhuri et al. [19] utilized matched filtering for the detection of retinal vessels, and proposed a two-dimensional linear kernel with a Gaussian profile. Staal et al. [8] proposed a ridge based vessel segmentation, the ridge line is regarded as the structure of blood vessels; the image is partitioned into convex set regions by assigning each pixel to the closest line element, then each pixel is classified by a k-NN classifier. Marin et al. [20] proposed a neural network based supervised algorithm, which used a 7-D feature vector composed of gray-level and moment invariant-based features for representation, and classified each pixel by a multi-layer network. Most of the existing algorithms for retinal vessel segmentation are based on manual designed features, which are not efficient to describe or discriminate

the target(vessels) and the background. Moreover, manual designed features are not robust to noise and lack of spatial constraint information, cut and burr appears easily in the segmentation results.

Compared with manual designed features [19], [8], [21], [22], [23], CNN-based methods have an impressive record of applications in image analysis and interpretation, including medical imaging. Liskowski et al. [24] proposed a deep learning based method for the problem of detecting blood vessels in fundus imagery, in which they regarded retinal vessel segmentation as a image detection task, assumed that the decision on pixel's class can be made based on its neighborhood, defined as a square window (patch) centered on the pixel to be classified. The supervised segmentation technique used a deep neural network (two stack of convolutional layers and three fully-connected layers) trained on a large sample of examples pre-processed with global contrast normalization, zero-phase whitening, and augmented using geometric transformations and gamma corrections. The CNNs based method significantly outperform the previous algorithms on the accuracy of classification, but it has some disadvantages as follows: first, the method selects size-fixed patch centered on each image pixel, which brings about large storage; second, each neighbouring image patch will be calculated in the network, which spends plenty of training time; third, the method lack of global smoothness correlation, that is, each training patch is individual, there is less global spatial relationship between pixels.

Then, fully convolutional networks (FCN) become more and more popular. The first work was proposed by Long et al. in [13] which reveals the relation between image classification and semantic segmentation and obtains pixel to pixel prediction. Different from the previous deep learning based semantic segmentation methods which rely on a sliding window strategy to classify every region in a highly inefficient way, FCN works very fast and runs in real-time on GPU. The reason is that all pixels in a testing image sharing features only the last simple linear classifier requires individual calculations. Our DSSRN method is based FCN and enjoys the fast testing speed.

Deep supervision does not add much extra computation in training and testing the network. In directviewing, it only adds some shortcut connections between the intermediate feature maps in the deep network and the final ground-truth [14]. However, theoretically, it is very important, since it helps to alleviate the problem of gradient vanishing. Thus, it helps to learn better deep features and produce better semantic segmentation performance. Our work adopt this deep supervision network structure and confirms the effectiveness of deep supervision in the task of retinal vessel segmentation. Besides, we add smoothness term in the work to further boost the performance.

CRF [25] is one of the most applied machine learning models. Xu et. al applied it for semantic segmentation in [15]. In deep convolutional neural networks, it is still useful since FCN predicts the label of pixels individually and pay less attention on modeling the pairwise/contextual information in images. CRF helps and be integrated into FCN as a module. The proposed DSSRN enjoys the contextual modeling power

of CRF. One related work proposed by Fu et. al [26] which also use CRF and FCN for retinal vessel segmentation. However, the proposed method uses CRF to regularize intermediate feature map in the work and optimize them in a end-to-end manner, and our superior results confirms the effectiveness of this design.

In all, we propose the deeply supervised and smoothed regularized network (DSSRN) for retinal vessel segmentation. DSSRN is constructed on fully convolutional network (FCN), which is deeply supervised, the label information is used in all intermediate layers; then we add global smoothness correlation into the net via conditional random field (CRF) to build an end-to-end and pixel-to-pixel segmentation network.

#### III. APPROACH

To overcome the aforementioned problem, we propose a deep learning based vessel segmentation method, named as deeply supervised and smoothly regularized network (DSSRN), which is efficiently discriminative and has global spatial constraint information to the whole network. Specifically, DSSRN is an end-to-end network for pixel-to-pixel image segmentation network, which combines the strengths of both fully convolutional network (FCN) and conditional random field (CRF). The FCN is deeply supervised as the label information is used in all intermediate layers, and the CRF introduces global smoothness regularization into the network.

**DSSRN:** The proposed method is built on holistically-nested edge detection (HED), which is based on fully CNNs and deeply-supervised net; then combined with conditional random field (CRF) to construct an end-to-end segmentation system, the idea of CRF layer is based on CRF-RNN, which formulates mean-field approximate inference for the dense CRF with Gaussian pairwise potentials as a recurrent neural network (RNN). DSSRN is an end-to-end net, when properly trained, the network should outperform a system where CRF inference is applied as a post-processing method [26], such as the method proposed by Fu et al. Fig. III gives the illustration of our architecture (DSSRN) for retinal vessel segmentation. The following subsections are dedicated to a detailed description of the proposed approach.

## A. Deeply Supervised Network

We first start out with the HED architecture, which has five blocks, and each block includes multiple convolutional and ReLU layers. Most importantly, the side-output from each intermediate layer will be connected to the last convolutional layer, thus the network is deeply supervised. HED is designed for resolving the challenging ambiguity in edge and object boundary detection, the trained images are mostly natural and scene images, usually are multi-scale and multi-object. Unlike retinal images, the composition is simpler, one pixel is either vessel target or background. The blood vessel is a line-shape object, which has fine structure. Thus, we adjust the convolution\_param of the first convolutional stage to retain more details. More implementation details can be found in the next section.

Let  $T=\{(X_n,Z_n,n=1,...,N)\}$  denote the training data set, where  $X_n=\{x_j^n,j=1,...,|X_n|\}$  is the input image and  $Z_n=\{z_j^n,j=1,...,|X_n|\}$ ,  $z_j^n\in[0,1]$  denotes the corresponding ground truth binary vessel segmentation map (label information) for image  $X_n$ . We omit the subscript n for notational convenience since we assume the inputs are all independent of one another. We denote the collection of all standard network layer parameters as  $\mathbf{W}$ . Suppose in the network we have totally M side-output layers. Each side-output layer is associated with a classifier, in which the corresponding weights can be represented as  $\mathbf{w}=(\mathbf{w}^1,\mathbf{w}^2,...,\mathbf{w}^M)$ . Thus, the side objective function of HED can be given by

$$L_{side}\left(\mathbf{W}, \mathbf{w}\right) = \sum_{m=1}^{M} \alpha_{m} l_{side}^{(m)}\left(\mathbf{W}, \mathbf{w}^{(m)}\right)$$
(1)

where  $\alpha_m$  is the weight of the mth side loss and  $l_{side}^{(m)}$  denotes the image-level class-balanced cross-entropy loss function for the mth side output. Besides, a weighted-fusion layer is added to better capture the advantage of each side output. The fusion loss at the fusion layer can be expressed as

$$L_{fuse}(\mathbf{W}, \mathbf{w}, \mathbf{f}) = \sigma(Z, h(\sum_{m=1}^{M} f^m A_{side}^{(m)}))$$
(2)

where  $\mathbf{f}=(f_1,...,f_M)$  is the fusion weight,  $A_{side}^{(m)}$  are activations of the mth side output,  $h(\cdot)$  denotes the sigmoid function, and  $\sigma(\cdot,\cdot)$  denotes the distance between the ground truth map and the fused predictions, which is set to be imagelevel class-balanced cross-entropy lass here. Therefore, the final loss function can be give by

$$L_{fical}(\mathbf{W}, \mathbf{w}, \mathbf{f}) = L_{fuse}(\mathbf{W}, \mathbf{w}, \mathbf{f}) + L_{side}(\mathbf{W}, \mathbf{w})$$
 (3)

HED connects each side output to the last convolutional layer (fuse layer) in each stage of the VGGNet. Each intermediate layer and the last fuse layer can predict a learned segmentation result from the trained net model.

## B. Smoothly Regularized Network

Conditional Random Field (CRF) usually is used in the context of pixel-wise label prediction, which models pixel labels as random variables that form a Markov Random Field (MRF) when conditioned upon a global observation (the image). Note that, different from the previous methods which use CRF as a post-processing tool, the proposed DSSRN integrates CRF as a module of the deep network and optimize the parameters in an end-to-end manner.

Let  $X_i$  be the random variable associated to pixel i, which represents the label assigned to the pixel i and can take any value from a predefined set of labels  $\mathcal{L} = \{1_1, 1_2, ..., l_L\}$ . Let  $\mathbf{X}$  be the vector formed by the random variables  $X_1, X_2, ..., X_N$ , where N is the number of pixels in the image. Given a graph G = (V, E), where  $V = \{X_1, X_2, ..., X_N\}$ , and a global observation (the image)  $\mathbf{I}$ , the pair  $(\mathbf{I}, \mathbf{X})$  can be modeled as a CRF characterized by a Gibbs distribution of the form  $P(\mathbf{X} = \mathbf{x} | \mathbf{I}) = \frac{1}{Z(\mathbf{I})} \exp{(-E(\mathbf{x} | \mathbf{I}))}$ . Here  $E(\mathbf{x})$  is called the energy of the configuration  $\mathbf{x} \in \mathcal{L}^N$  and  $Z(\mathbf{I})$  is

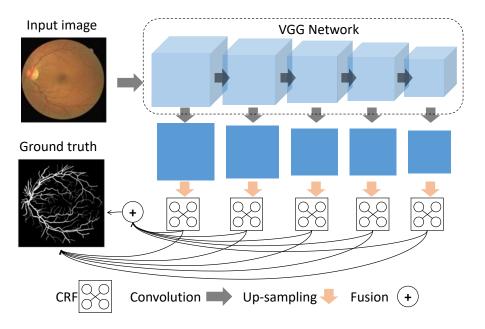


Fig. 1. The architecture of the proposed DSSRN. The network combines deep supervision of VGG network and smoothness regularization of CRF, is an end-to-end and pixel-to-pixel network for retinal vessel segmentation.

the partition function (We drop the conditioning on I in the notation for convenience).

Krähenbühl et al. [27] proposed the fully connected pairwise CRF model, the energy of a label assignment x is given by

$$E(\mathbf{x}) = \sum_{i} \varphi_{u}(x_{i}) + \sum_{i < j} \varphi_{p}(x_{i}, x_{j}) \tag{4}$$

where the unary energy components  $\varphi_u(x_i)$  measure the inverse likelihood of the pixel i taking the label  $x_i$ , and pairwise energy components  $\varphi_p(x_i,x_j)$  measure the cost of assigning labels  $x_i,x_j$  to pixels i,j simultaneously. In our model, unary energies are obtained from HED, which, roughly speaking, predicts labels for pixels without considering the smoothness and the consistency of the label assignments. The pairwise energies provide an image data-dependent smoothing term that encourages assigning similar labels to pixels with similar properties. We model pairwise potentials as a weighted Gaussian

$$\varphi_p(x_i, x_j) = \mu(x_i, x_j) \sum_{m=1}^M w^m k_G^{(m)}(\mathbf{f}_i, \mathbf{f}_j)$$
 (5)

where each  $k_G^{(m)}$  for m=1,...,M, is a Gaussian kernel applied on feature vectors. The feature vector of pixel i, denoted by  $\mathbf{f}_i$ , is derived from image features such as spatial location and RGB values. The function  $\mu(\cdot,\cdot)$ , called the label compatibility function, captures the compatibility between different pairs of labels as the name implies.

Minimizing the above CRF energy  $E(\mathbf{x})$  yields the most probable label assignment  $\mathbf{x}$  for the given image. Since this exact minimization is intractable, a mean-field approximation to the CRF distribution is used for approximate maximum posterior marginal inference. The mean-field CRF is based on CRFasRNN, which referred that filter-based approximate

mean-field inference approach for dense CRFs relies on applying Gaussian spatial and bilateral filters on the mean-field approximates in each iteration. Unlike the standard convolutional layer in a net, in which filters are fixed after the training stage, the method uses edge-preserving Gaussian filters, coefficients of which depend on the original spatial and appearance information of the image.

Combined mean-field CRF into HED, we construct an end-to-end deep network for retinal vessel segmentation. On the one hand, the method inherits the deeply supervised information from fully convolutional network; on the other hand, it contains the global smoothness correlation via conditional random field. In the experiments, we will show the effectiveness of end-to-end training by comparing the methods which use CRF as a post-processing tool.

#### IV. EXPERIMENTS

We evaluate our method on three publicly available DRIVE [8], STARE [17] and CHASE\_DB1 [18] datasets. These three datasets all provide two manual segmentation results generated by two different experts for each image, we select the first observer's as the ground truth. Here, we perform the evaluation in terms of Accuracy (Acc) and Sensitivity (Sen), their definitions are shown as follows, and the evaluation is computed in the field of view (FOV, the circular active area) of retinal images.

$$Acc = \frac{TP + TN}{TP + TN + FP + FN} \tag{6}$$

$$Sen = \frac{TP}{TP + FN} \tag{7}$$

where TP, TN, FP, FN are respectively the numbers of true positive, true negative, false positive and false negative decisions. To put it simply, we consider P as the predicted

pixel is vessel, and N means the predicted pixel is background, exactly corresponding to the two objects in retinal images. Acc is measured by the ratio of the total number of correctly classified pixels to the number of all pixels in the image field of view. Sen represents the ability of detecting the vessel pixels correctly.

Examples and detailed messages of the three datasets are illustrated in Fig IV and Table I respectively. We choose one half of the datasets as training images, the other half as test images, which is the standard setting has been applied in previous works [26], [24], [20], [22], [21], [8].

Dataset	Image size	Training images	Testing images
DRIVE	564×584	20	20
STARE	$700 \times 605$	10	10
CHASE_DB1	$999 \times 960$	14	14

#### A. Implementation details

In our architecture, DSSRN is based on HED and CRF. HED is a five-stage deeply supervised network, the segmentation results form each layer as well as the last fuse layer then connects mean-field CRF, which provides the global smoothness information for the whole net.

The hyper-parameters used in this work contain: the learning rate is initially set to  $10^{-8}$ , and then decreased by a factor of 10 every 10000 iterations. The momentum is 0.9, weight\_decay is 0.0002. Our target, the blood vessel is a line-shape and fine-structure object, as the vessel width can range from one pixel to twenty pixels. To get accurate segmentation result, we adjust the convolution\_param of HED, make the receptive field be close to the original input. The convolution\_param(pad) of the first convolutional stage is changed from 35 to 1. The fusion layer weights are initialized with 0.2, 0.28, 0.28, 0.2, 0.04. We set the number of mean-field iterations in the CRF layer to 5 during training, to avoid exploding gradient problems and to reduce the training time; and increase the iteration count to 10 during testing.

## B. Running time

The implementation is based on the Caffe framework [28], and conducted on NVIDIA GTX Titan X GPU. We first prepare one half, 44 images from three datasets (DRIVE, STARE and CHASE\_DB1) as the training images, and then raise the data using flip transform. We use the random crop data augmentation by randomly cropping  $500 \times 500$  subimages during training. Finally, we obtain the trained model after 10000 iterations. Training of a model can take up to 12 hours on a single GPU, and the testing of one retinal image only needs 0.3 seconds in average.

## C. Results and Comparison with the State-of-the-arts

We compare our method with several state-of-the-art vessel segmentation methods, and also report the ground truth labeling of the second observer as the human performance. The details of the three tested datasets are given separately as follows.

TABLE II
RESULTS ON THE THE DRIVE DATASET. THE RESULTS ARE EVALUATED USING THE ACCURACY (ACC) AND SENSITIVITY (SEN) CRITERIA.

Methods	Acc	Sen		
Human observer	0.9473	0.7482		
Unsupervised methods				
Zana et al [29]	0.9377	0.6971		
Jiang et al [30]	0.9212	-		
Mendonca et al [31]	0.9452	0.7344		
Miri et al [32]	0.9458	0.7352		
Fraz et al [33]	0.9430	0.7152		
You et al [34]	0.9434	0.7410		
Supervised methods				
Niemeijer et al [35]	0.9416	-		
Cheng et al [36]	0.9474	0.7252		
Staal et al [8]	0.9442	-		
Fraz et al [21]	0.9480	0.7406		
Marin et al [20]	0.9452	0.7067		
Liskowski et al [24]	0.9495	0.7763		
Fu et al [26]	0.9470	0.7294		
Ours (DSSRN)	0.9536	0.7632		

The results of proposed DSSRN are shown and compared to the previous state-of-the-art methods in Table II, Table III and Table IV on the DRIVE dataset, the STAR dataset and the CHASE\_DB1 dataset, respectively. In each table, there are three sections: the first section shows the performance of human observer; the second section shows the results of some unsupervised methods; the third section shows the results of some supervised methods. The symbol "-" means the corresponding result is not available in the original paper.

TABLE III
RESULTS ON THE THE STARE DATASET. THE RESULTS ARE EVALUATED USING THE ACCURACY (ACC) AND SENSITIVITY (SEN) CRITERIA.

Methods	Acc	Sen		
Human observer	0.9323	0.8517		
Unsupervised methods				
Zana et al [29]	0.9009	-		
Mendonca et al [31]	0.9440	0.6996		
Fraz et al [21]	0.9442	0.7311		
You et al [34]	0.9497	0.7260		
Supervised methods				
Staal et al [8]	0.9516	-		
Fraz et al [21]	0.9534	0.7548		
Marin et al [20]	0.9526	0.6944		
Liskowski et al [24]	0.9566	0.7867		
Fu et al [26]	0.9545	0.7140		
Ours (DSSRN)	0.9603	0.7423		

From the results, we can observe that the supervised learning methods are generally work better than the unsupervised methods. Due to the difficulties of problem, the progress on this problem is not fast. However, it is exciting that

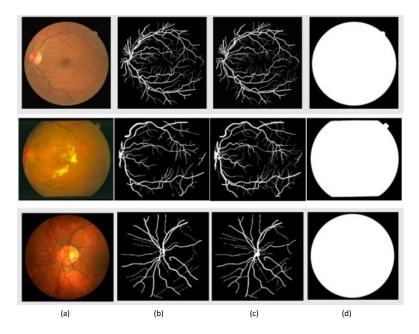


Fig. 2. Example images in the three tested datasets. Each row shows an example from a dataset. (a) shows the original retinal image; (b) and (c) show two annotated ground truth images; (c) shows the mask of the retinal region.

many methods have outperform the human observer, which is calculated on the second observer (GT\_2nd).

Among the compare methods, our method can obtain better *Acc* performance than others on the three datasets, and get the best results on the STARE and CHASE\_DB1 datasets. Note that these two datasets contains more pathological retinal images, which shows that our method is efficient and robust. Also, our method outperforms than the human observer.

TABLE IV
RESULTS ON THE THE CHASE\_DB1 DATASET. THE RESULTS ARE EVALUATED USING THE ACCURACY (ACC) AND SENSITIVITY (SEN)
CRITERIA.

Methods	Acc	Sen		
Human observer	0.9520	0.7038		
Unsupervised methods				
Azzopardi et al [37]	0.9387	0.7585		
Supervised methods				
Fraz et al [21] Roychowdhury et al [22]	0.9469 0.9530	0.7224 0.7259		
Ours (DSSRN)	0.9587	0.7815		

Compared with the DeepVessel work proposed by Fu et al [26], where CRF inference is applied as a post-processing method, according to Table II and Table III, the proposed DSSRN consistently obtains better results; especially, the end-to-end training strategy obtains a significant better performance when considering sensitivity. Overall, the proposed DSSRN method obtains the state-of-the-art performance on the three tested datasets.

## D. Ablation studies

The effectiveness of data augmentation: Data augmentation is widely used in deep learning for natural image object recognition/segmentation. In this retinal vessel segmentation task, data augmentation should be also applied since the number of training image is relatively small considering there are usually tens of thousands of natural images for training. As mentioned above, we perform random crop data augmentation on training images. For each training, we randomly crop a  $500 \times 500$  sub-image in each iteration during training. In testing, image is resized to  $500 \times 500$  before it is fed into the network. To verify the effectiveness of the data augmentation, we carry out experiments on the DRIVE dataset without using data augmentation, we obtain 0.9342 accuracy and 0.7028 sensitivity. The results show that the data augmentation is essential to obtain an excellent performance on this task.

The effectiveness of the smoothness regularization: By comparing the proposed DSSRN with the DeepVessel method, we can observe that the end-to-end learning of CRF with deep CNN is helpful. Furthermore, we conduct experiments on the STARE using CRF; thus, we use test the HED network on the retinal vessel segmentation task. The results are 0.9415 accuracy and 0.7142 sensitivity. The results confirms the effectiveness of the CRF smoothness regularization. To qualitative show the contribution of the smoothness regularization, Fig IV-D shows some vessel segmentation results using and without using the regularization term. From the images, we can observe that the output the proposed DSSRN is adaptively smoothed compared to the HED results.

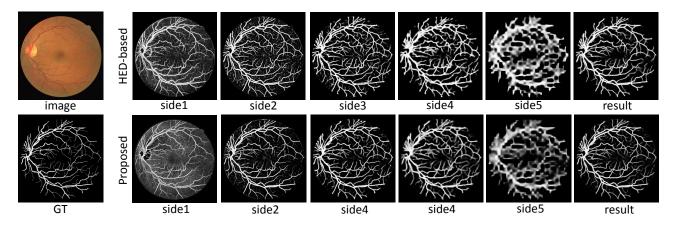


Fig. 3. Visualization of the retinal vessel segmentation result by comparing with HED. The first column is the original image and corresponding ground truth, the rest columns are the side-output and final segmentation result of network. (The original image is from the DRIVE dataset: 01\_test.jpg.)

#### V. CONCLUSION

In this paper, we developed a new deep learning based method for retinal vessel segmentation. The method combines deep supervision of HED architecture and global smoothness regularization of CRF, is an end-to-end and pixel-to-pixel segmentation network. It outperforms HED-based method, and outperforms a system where CRF inference is applied as a post-processing method. Our experiments show that our proposed method achieves the state-of-the-art results on DRIVE, STARE and CHASE\_DB1 datasets, is efficient to retain more vessels in retinal images.

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