

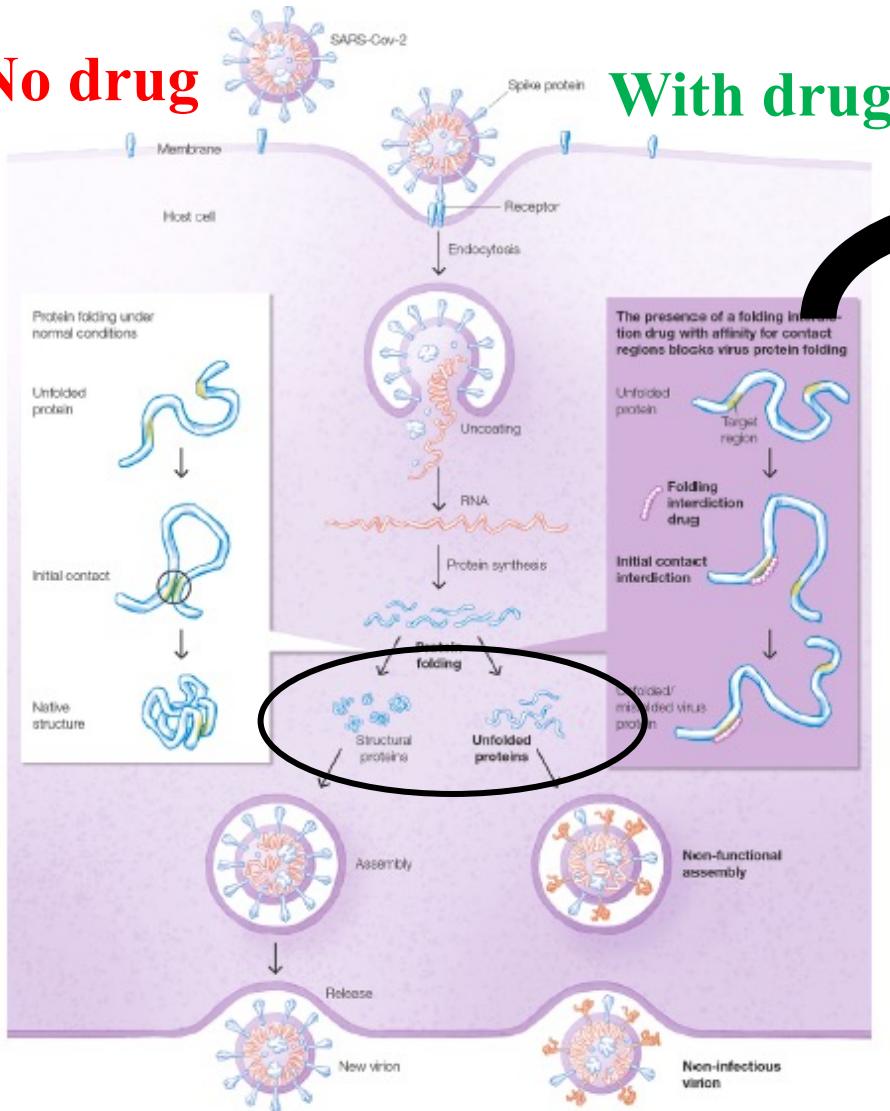
# Engineering high-fidelity gates in silicon quantum processors

Nima Leclerc ([nleclerc@seas.upenn.edu](mailto:nleclerc@seas.upenn.edu)), PhD Student  
Sigillito Lab

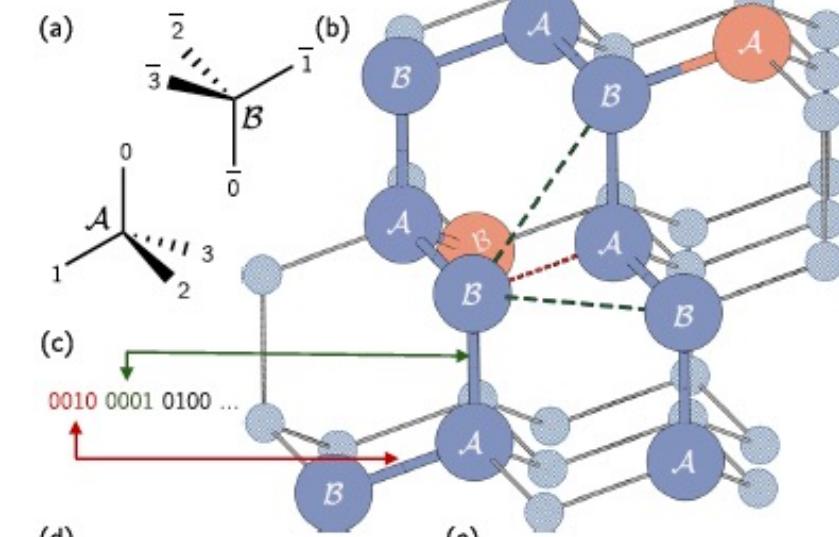
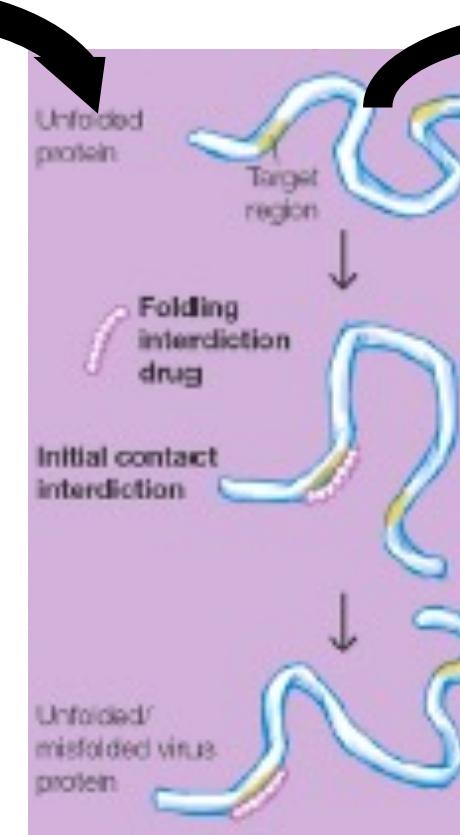
Electrical and Systems Engineering Colloquium, University of Pennsylvania  
October 22, 2021

# Therapeutic drug design for COVID-19

No drug



With drug

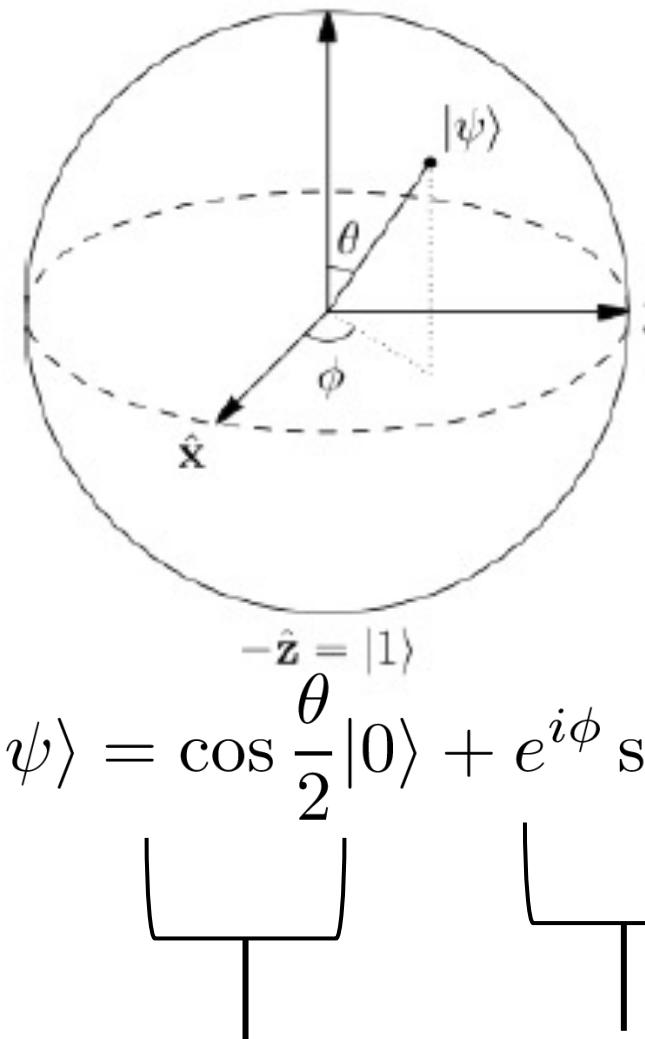


# Increase computational space with different encodings

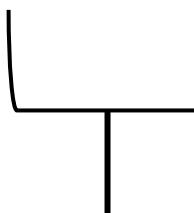
**Bits = deterministic**



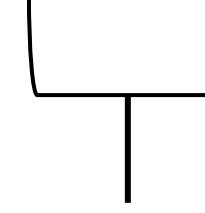
**Qubits = probabilistic**  $\hat{z} = |0\rangle$



$$|\psi\rangle = \cos \frac{\theta}{2} |0\rangle + e^{i\phi} \sin \frac{\theta}{2} |1\rangle$$



$c_1$



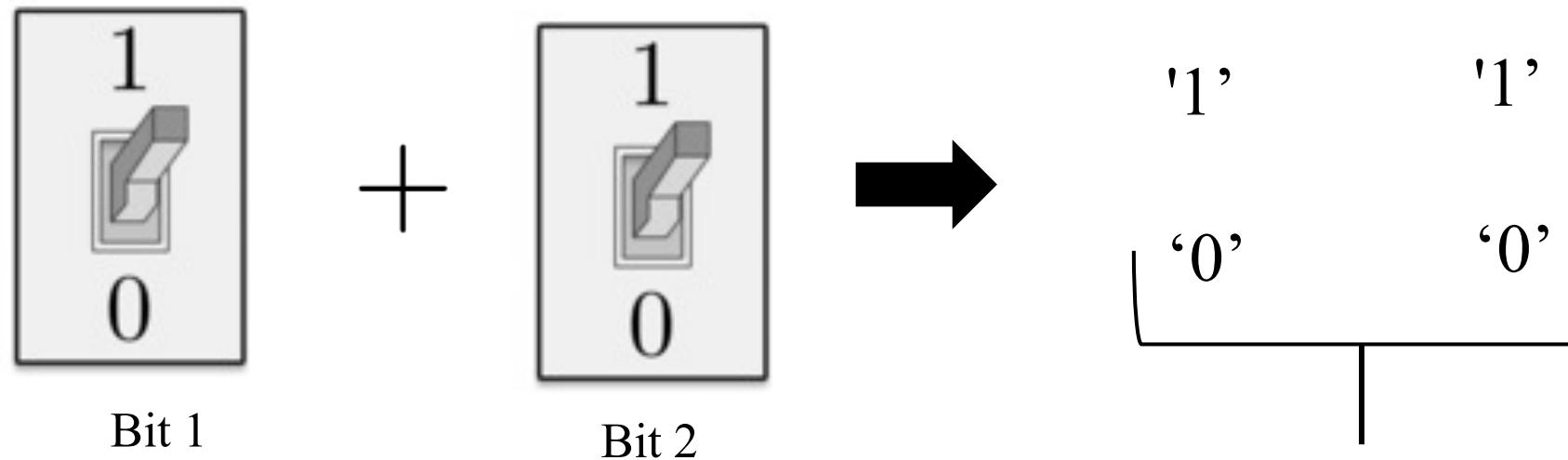
$c_2$

$c_1 \quad c_2$

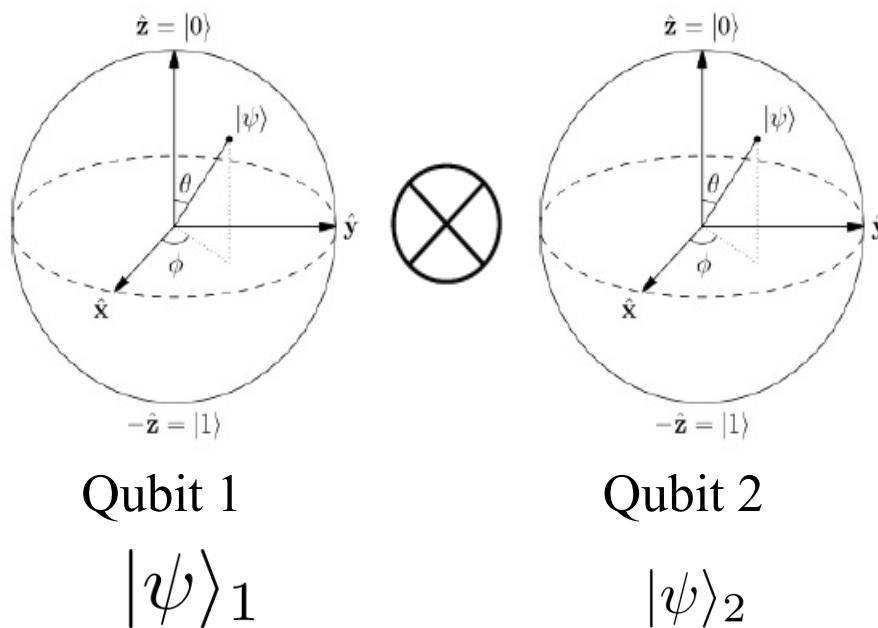
→ probabilities  
of being in  
 $|0\rangle$  and  $|1\rangle$   
states.

# Increase computational space combining multiple qubits

Classical



Quantum

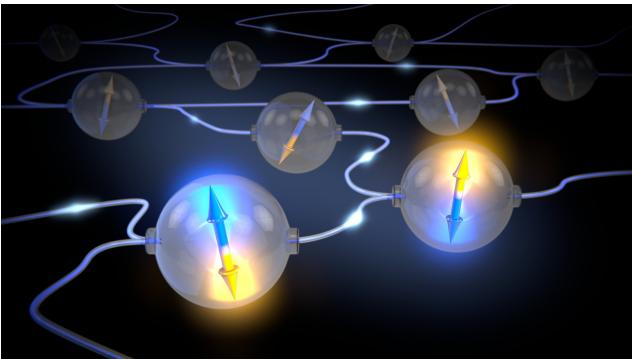


**2 computational states from 2 bits**

$$|\psi\rangle_1 \otimes |\psi\rangle_2 = (c_1^1|0\rangle_1 + c_2^1|1\rangle_1) \otimes (c_1^2|0\rangle_2 + c_2^2|1\rangle_2)$$
$$= c_1^1 c_1^2 |0\rangle_1 |0\rangle_2 + c_1^1 c_2^2 |0\rangle_1 |1\rangle_2 + c_2^1 c_1^2 |1\rangle_1 |0\rangle_2 + c_2^1 c_2^2 |1\rangle_1 |1\rangle_2$$

**4 computational states from 2 qubit  $\Rightarrow$  4 states for each qubit pair**

# Encoding information in correlations



‘spooky action at a distance’  $\Rightarrow$  *entanglement*

$$|\psi\rangle_1 \otimes |\psi\rangle_2 = (c_1^1|0\rangle_1 + c_2^1|1\rangle_1) \otimes (c_1^2|0\rangle_2 + c_2^2|1\rangle_2)$$

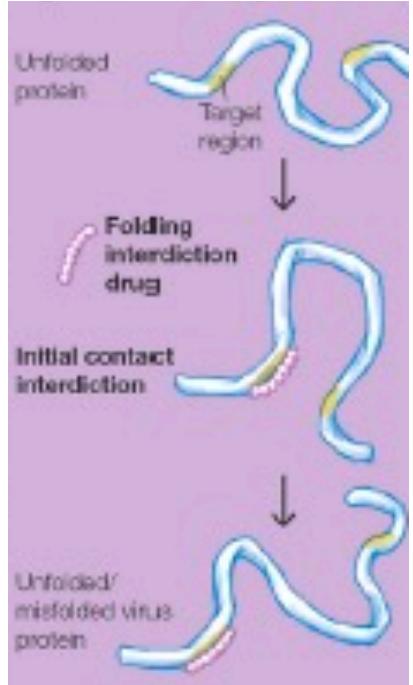
Information is stored in the correlation between states  $\Rightarrow$  exponentially increased computational space

$$|\psi\rangle = (|0\rangle + |1\rangle)^{\otimes N}$$

$N \rightarrow$  number of physical qubits

- $N = 30$  (IonQ machine)  $\Rightarrow \sim 1$  GB classical transistors
- $N = 50$  (Google machine)  $\Rightarrow \sim 8,000$  TB classical transistors
- $N = 800 \Rightarrow >$  number of atoms in the universe to encode information !!

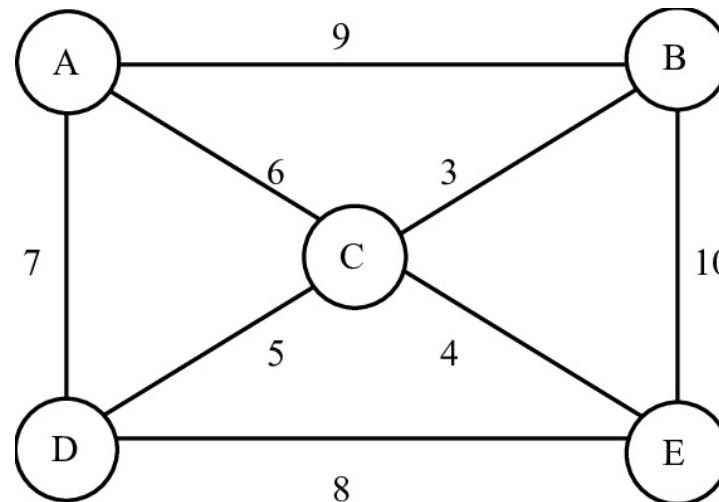
# Entanglement encoding for drug design and other applications



**Protein folding**  
*Quantum simulation*

Classical algorithm (HF):  $\mathcal{O}(2^N)$

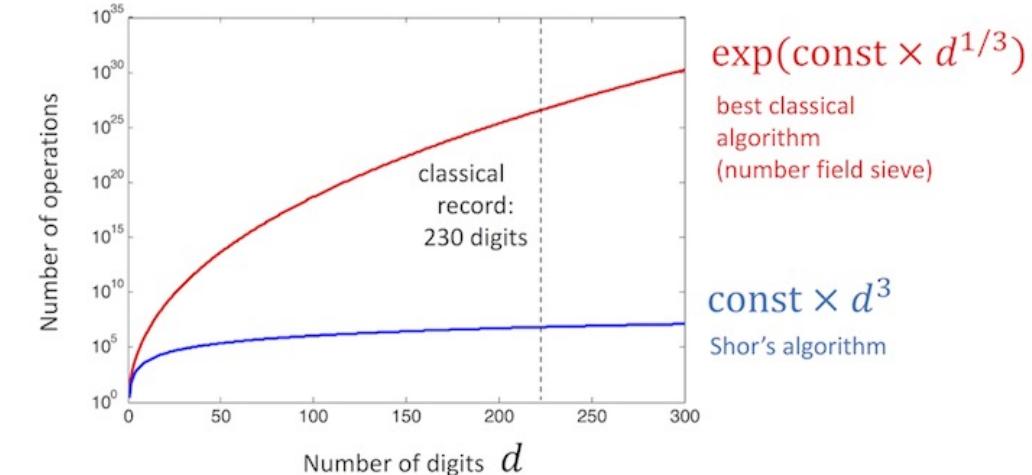
Quantum algorithm (VQE):  $\mathcal{O}(N^3)$



**Optimization**  
*Search algorithms*

Classical algorithm (MTZ):  $\mathcal{O}(2^N)$

Quantum algorithm (Grover):  $\mathcal{O}(\sqrt{N})$

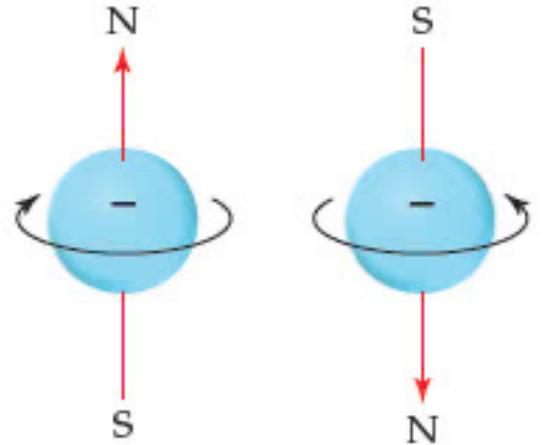


**Factoring**  
*Quantum Fourier transform*

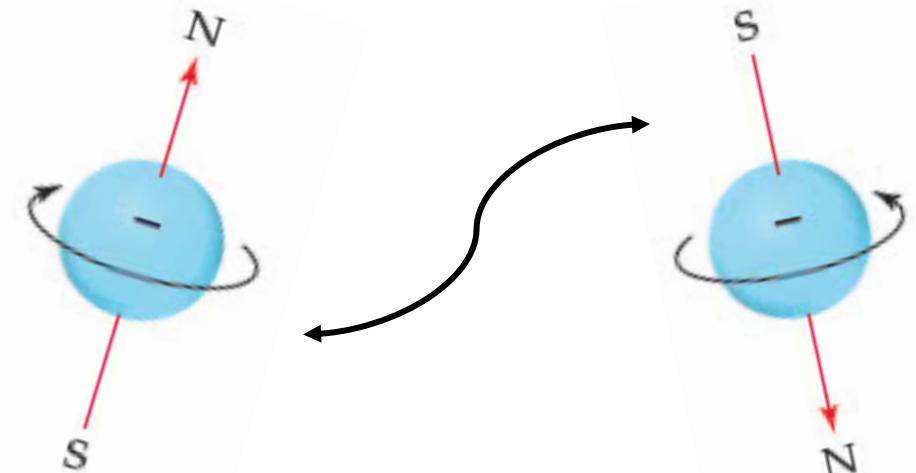
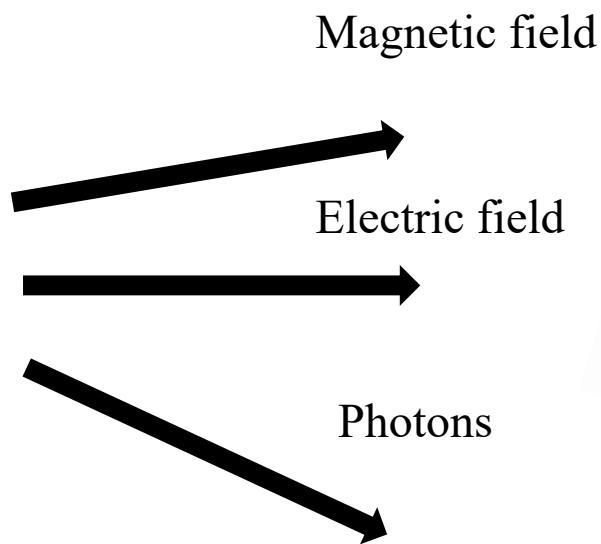
Classical algorithm (NFS):  $\mathcal{O}(2^N)$

Quantum algorithm (Shor's):  
 $\mathcal{O}(\log N)$  or  $\mathcal{O}(N^3)$

# Encoding quantum information in a physical system: small magnets

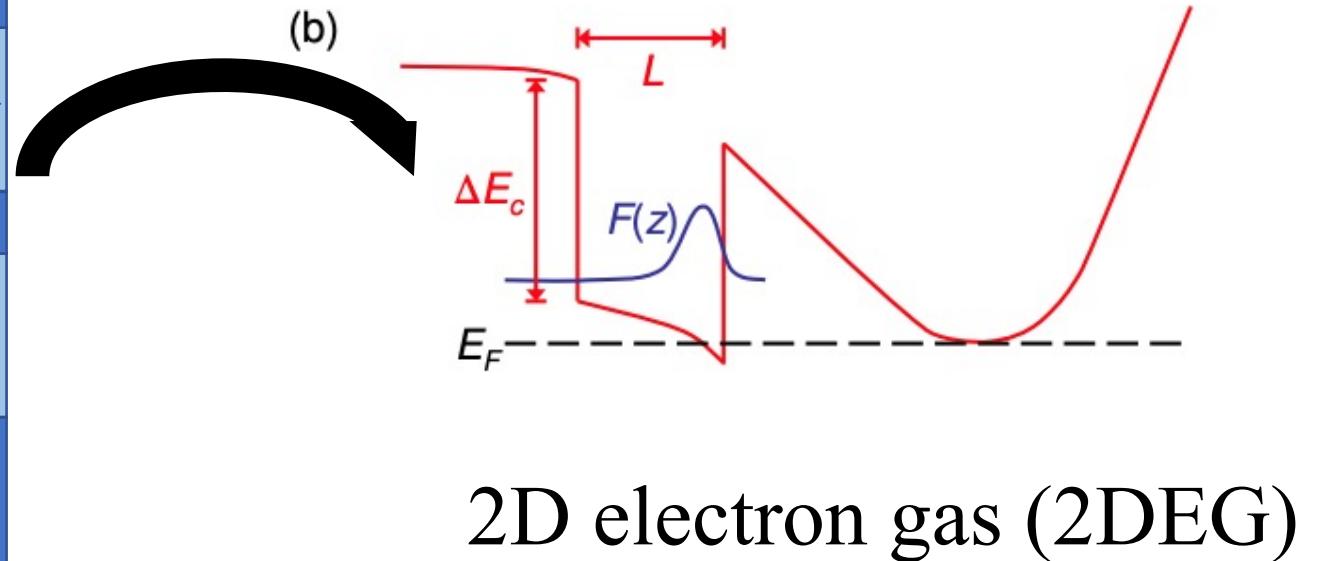
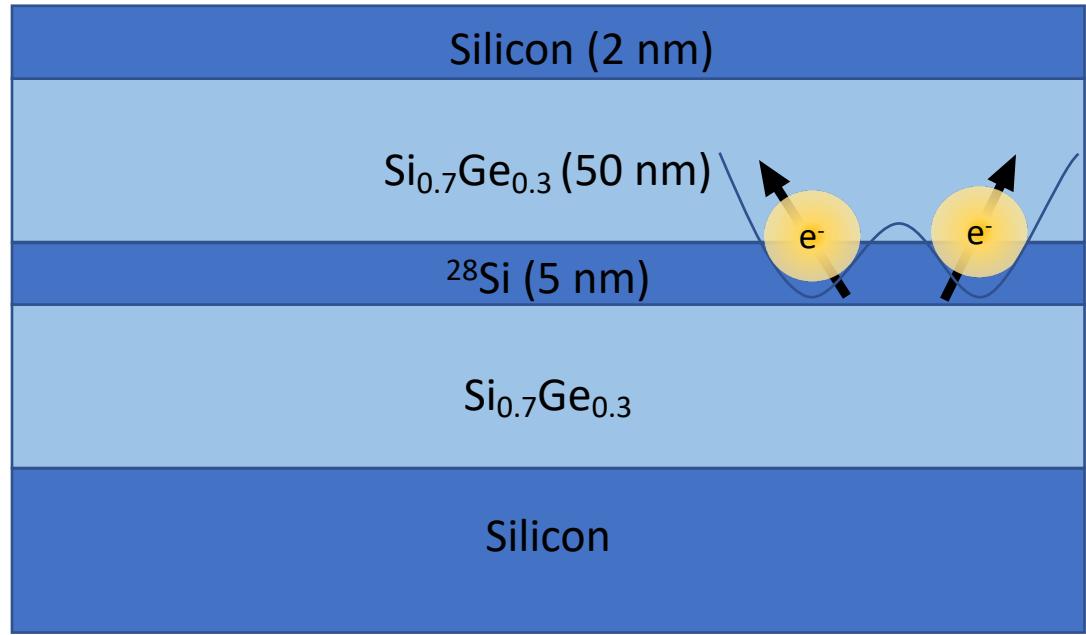


$$|\psi\rangle_1 = |\uparrow\rangle \quad |\psi\rangle_2 = |\downarrow\rangle$$

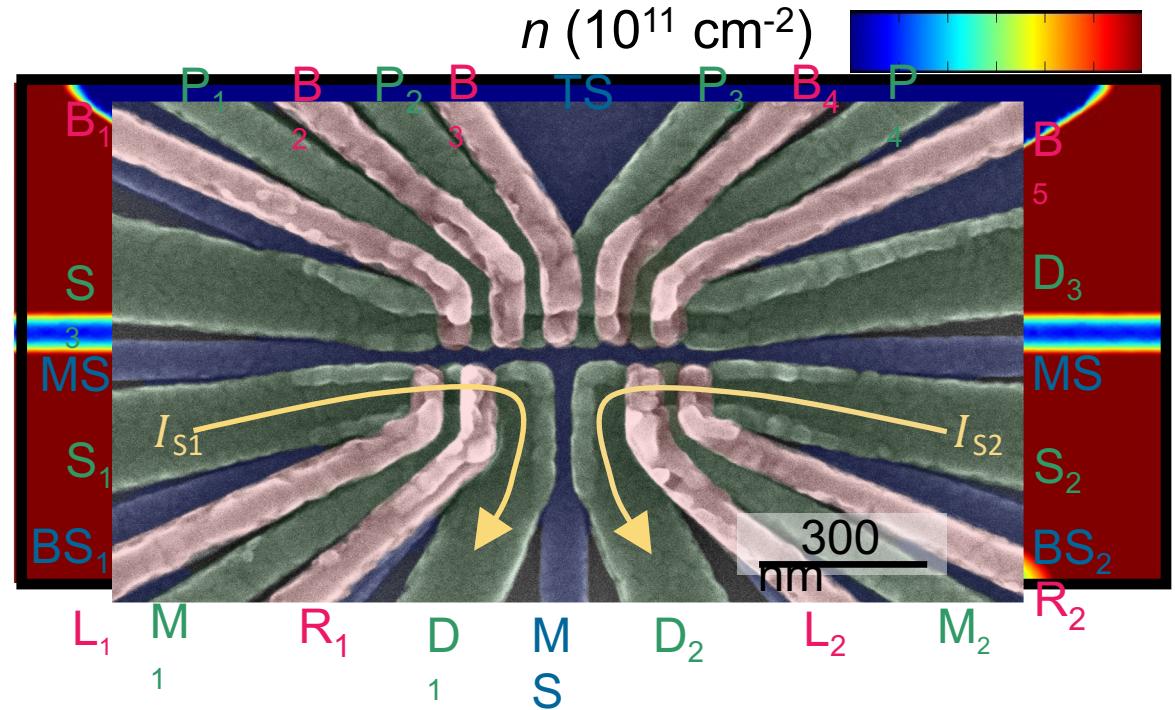
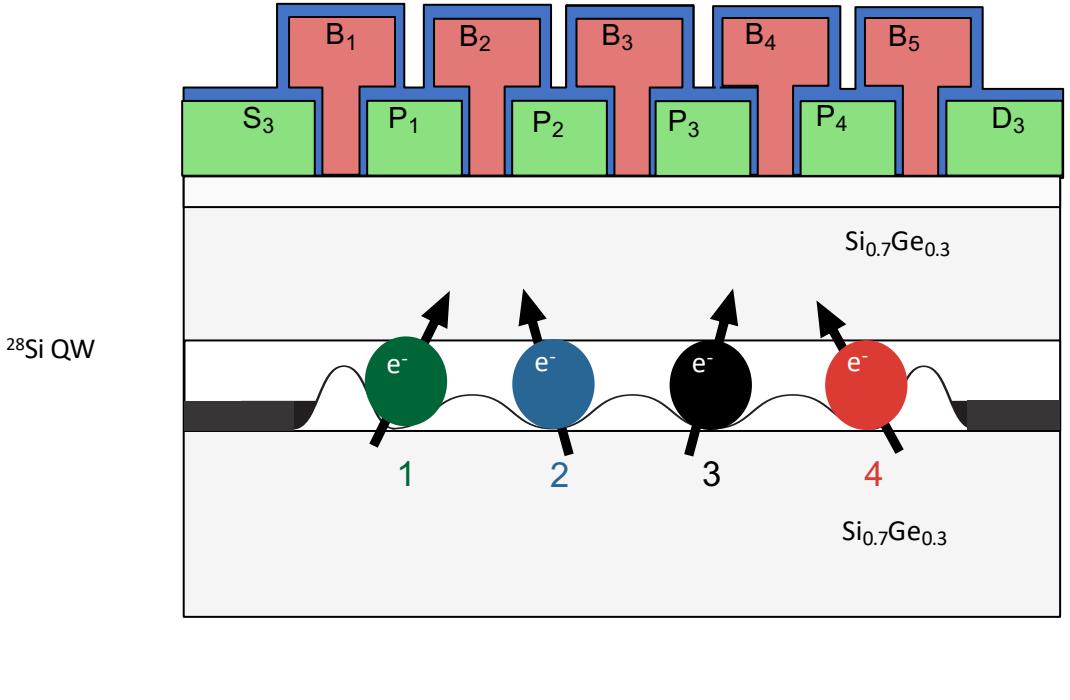


$$|\psi\rangle_1 \otimes |\psi\rangle_2$$

# Trapping single spins in semiconductors

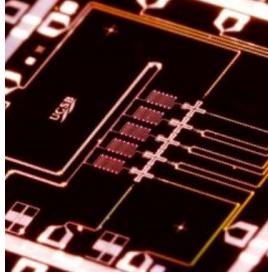
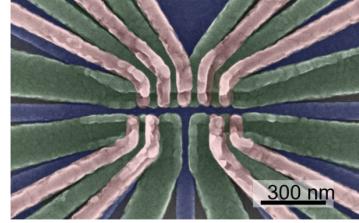
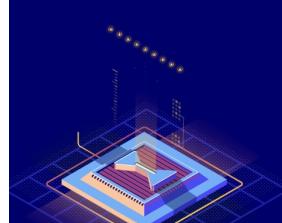
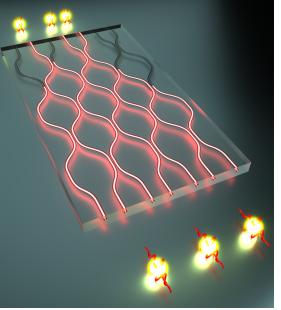


# Trapping single spins in semiconductors



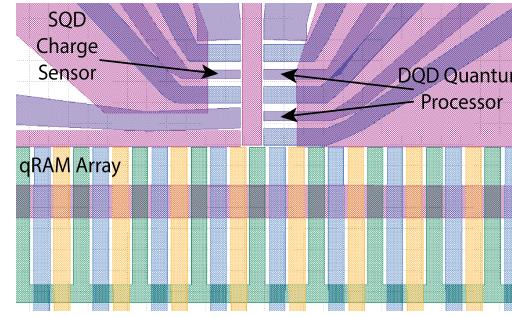
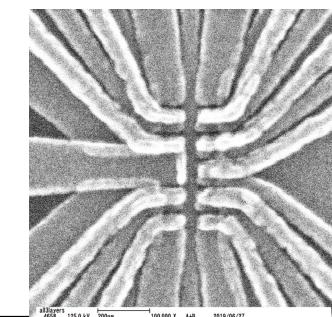
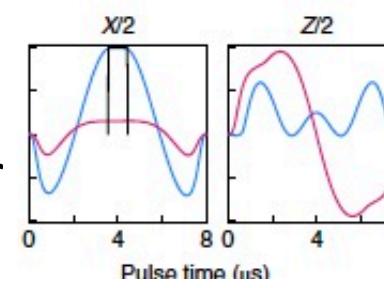
Voltage gates modify 2DEG potential → trap electrons with high precision

# A zoo of quantum computing architectures

Qubit	Superconducting	Silicon Spin Qubits	Ions/Atoms	Photons
		 300 nm		
Number Qubits Demonstrated	72 (Bristlecone) 53 (Sycamore) 50 IBM	4	32	~70
Gate Fidelities (2 QB)	99.9%	>99.5%	>99.9%	>99.5
One qubit gate fidelity	99.95%	>99.95%	>99.99%	>99.5
Challenges in qubit scalability	Qubit crosstalk dominates, decoherence, too big	Low 2-qubit fidelities, too many wires , too cold	Bulky vacuum systems, soft potential ( weak interaction)	Cannot reliably produce photons, difficult to mediate interaction

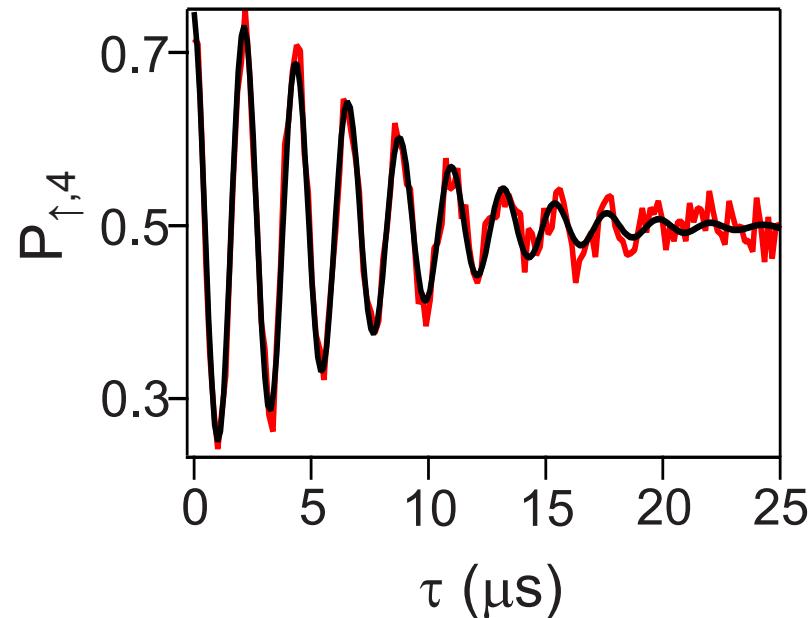
Images from: Martinis Group/Google, IonQ, PsiQuantum

# Towards an intermediate scale silicon quantum computer

Challenges	Proposed solution
<b>Low-connectivity</b> <ul style="list-style-type: none"><li>- Spins limited to nearest-neighbor interactions</li><li>- Difficult to form large cluster states</li></ul>	Quantum random access memory 
<b>Complexity</b> <ul style="list-style-type: none"><li>- Each qubit requires multiple wires connected to bond pads</li><li>- Simultaneous voltage + MW control</li></ul>	Overlapping gate architecture → all qubits share same barrier voltage 
<b>Qubit infidelity</b> <ul style="list-style-type: none"><li>- Decoherence induced → spin-spin interactions lead to information loss</li><li>- Noise induced → charge noise leading to fluctuations in exchange interactions</li></ul>	Pulse engineering for noise induced infidelity. Res-Sqrt(SWAP) gates for decoherence induced. 

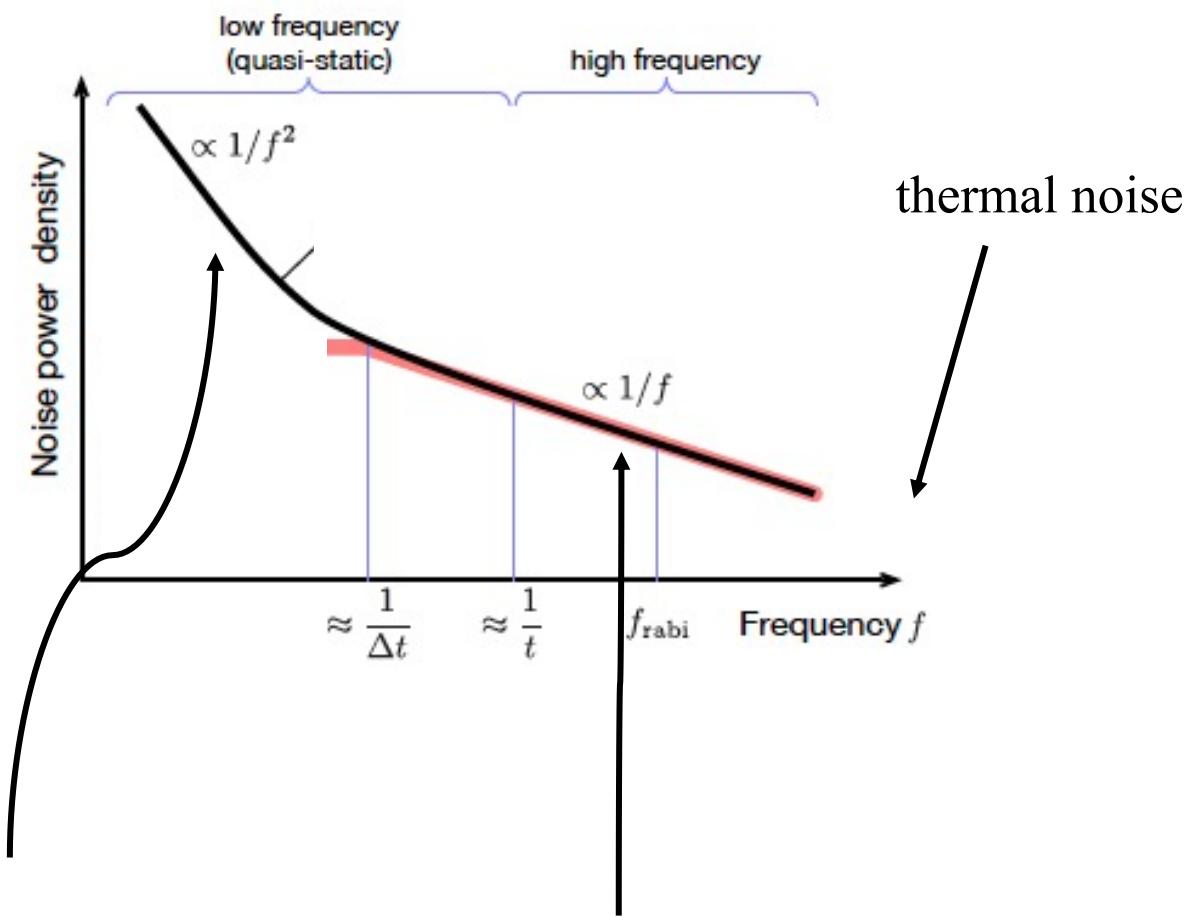
# Infidelity in silicon spin-qubit systems: decoherence + noise

## Decoherence



Sigillito et al., Phys. Rev. Appl. 6, 061006 (2019)

## Noise



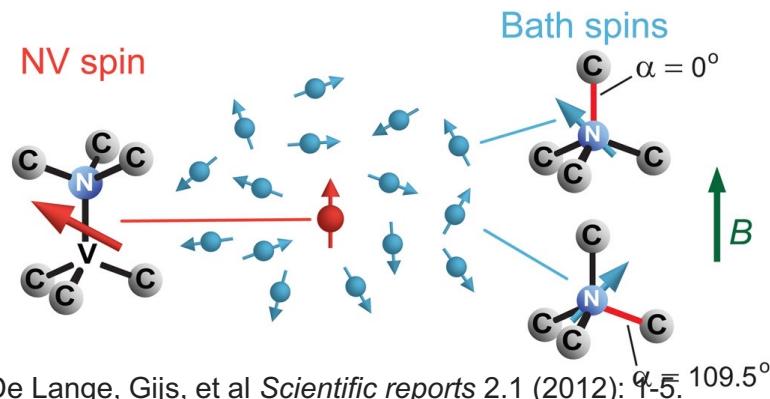
fluctuating charges ( $\delta Q$ ) →

fluctuating exchange ( $\delta J$ )

→ fluctuating magnetic fields

$\delta B$

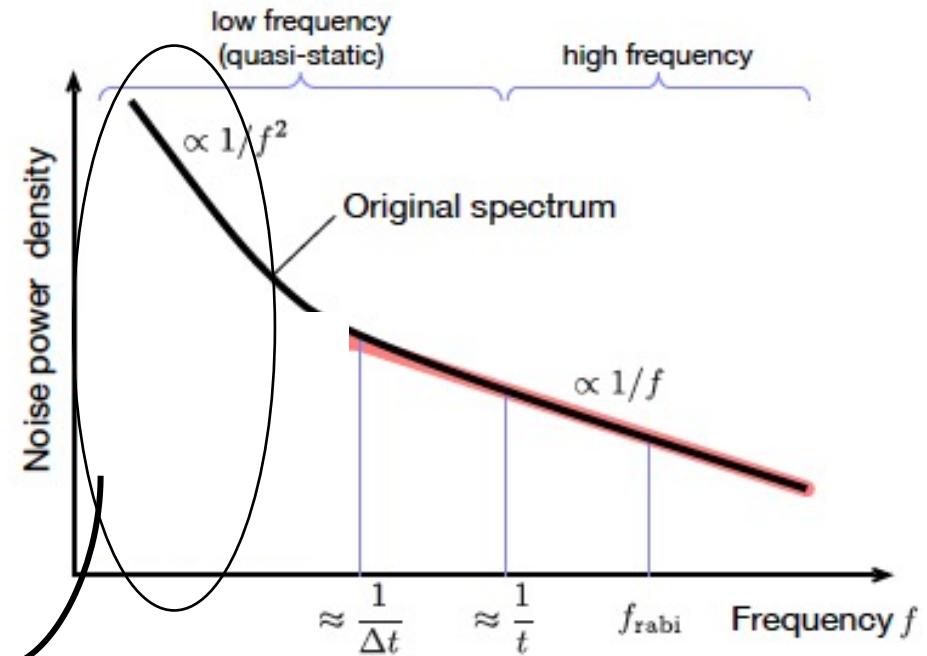
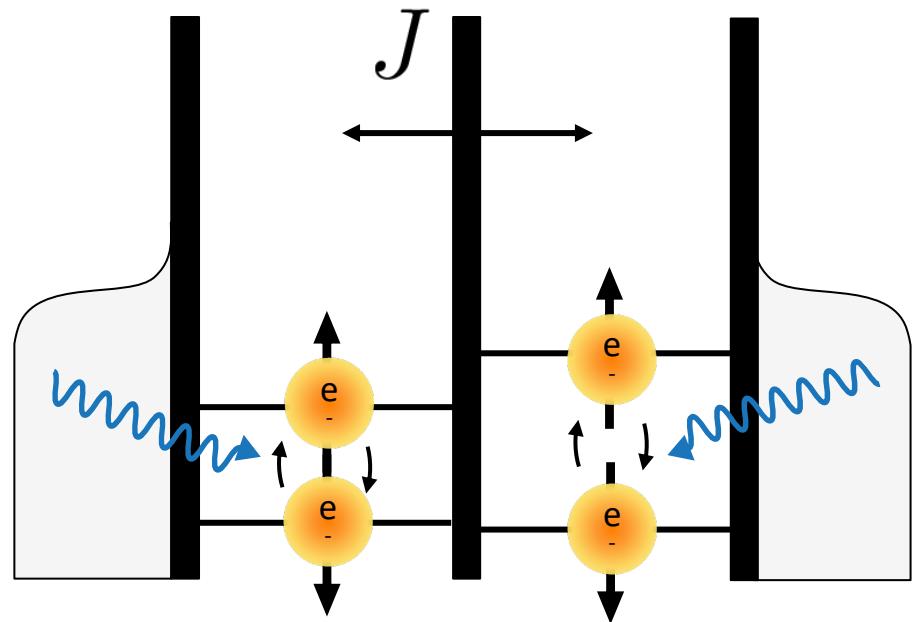
fluctuating surface magnetic fields  
 $\delta B$



Spins interacting with other spins! (hyperfine coupling)

Nakajima, Takashi, et al. Physical Review X 10.1 (2020): 011060.

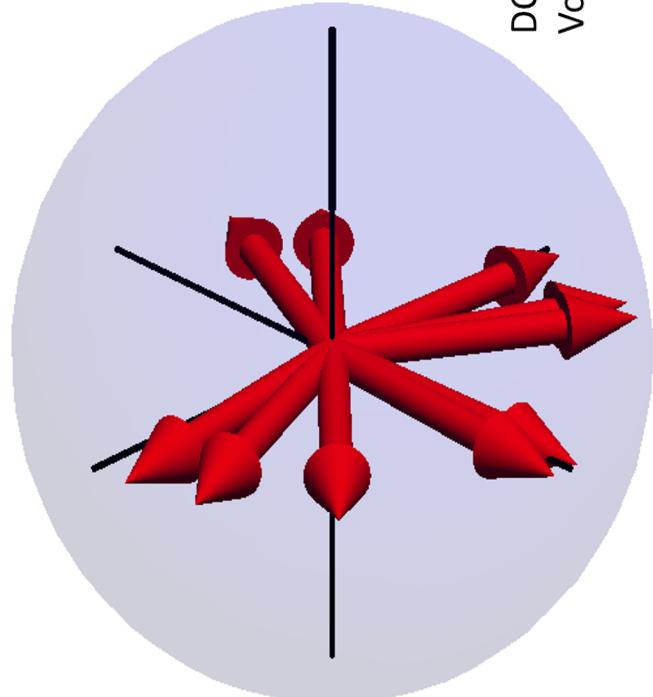
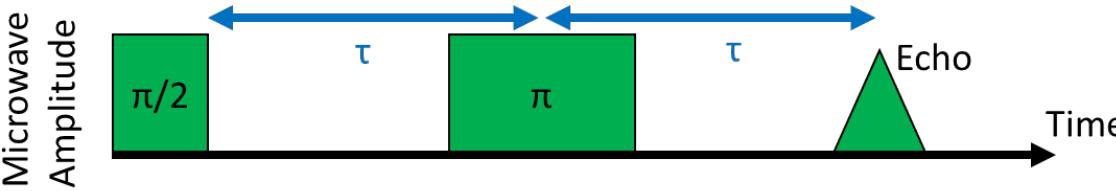
# Charge noise induced infidelity



$$H = \begin{pmatrix} E_z & 0 & 0 & 0 \\ 0 & -(\delta E_z + J)/2 & J/2 & 0 \\ 0 & J/2 & (\delta E_z - J)/2 & 0 \\ 0 & 0 & 0 & -E_z \end{pmatrix}$$

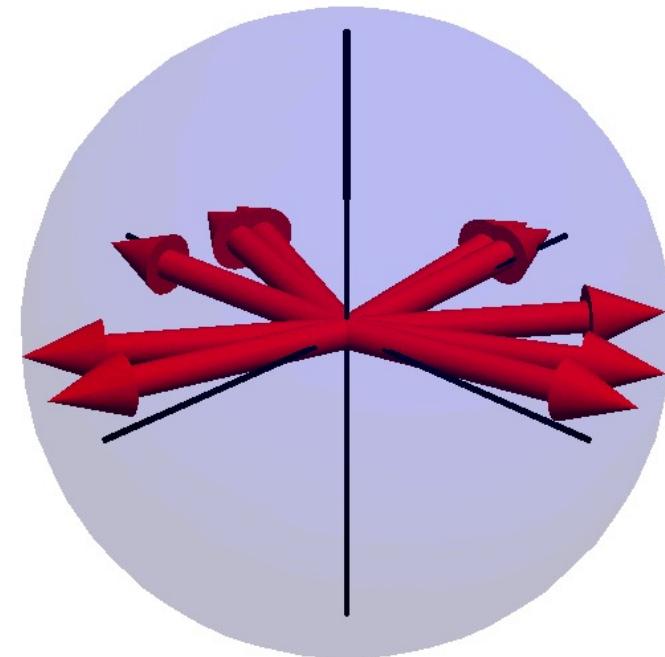
$$J = J_0 + \delta J$$

# Charge noise induced infidelity (cont'd))



Unperturbed system

$$\delta B = 0$$

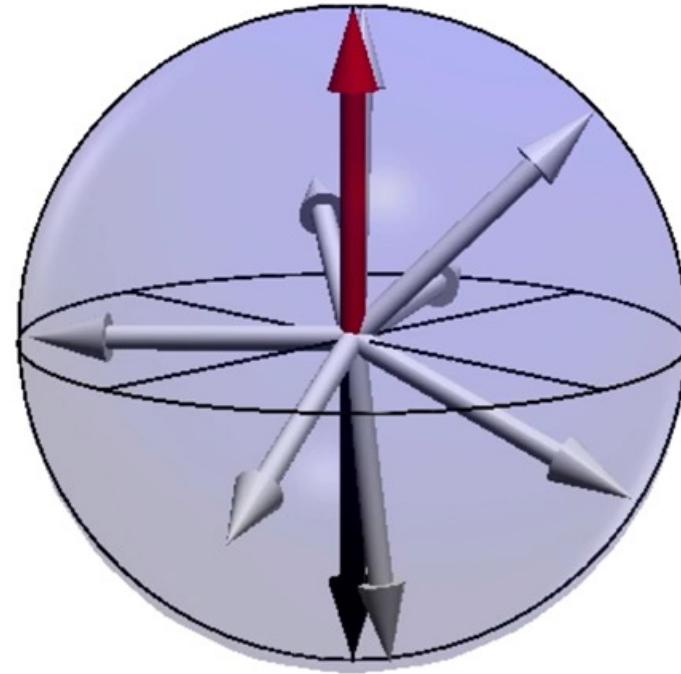


Charge noise present

$$\delta B \neq 0$$

# Controlling spins with microwaves

- Apply magnetic field orthogonal to  $B$
- Needs to be resonant with spins rotating frame
- Microwave frequencies
- Axis of rotation = phase

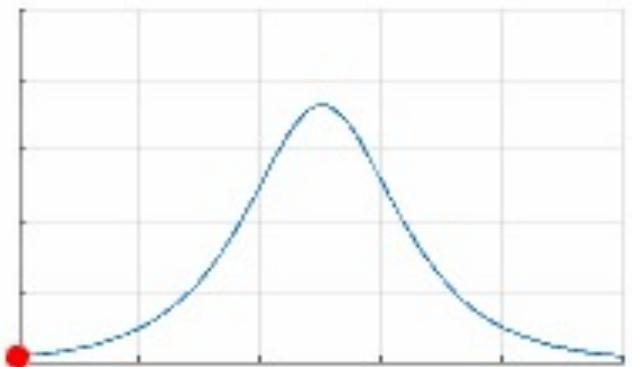


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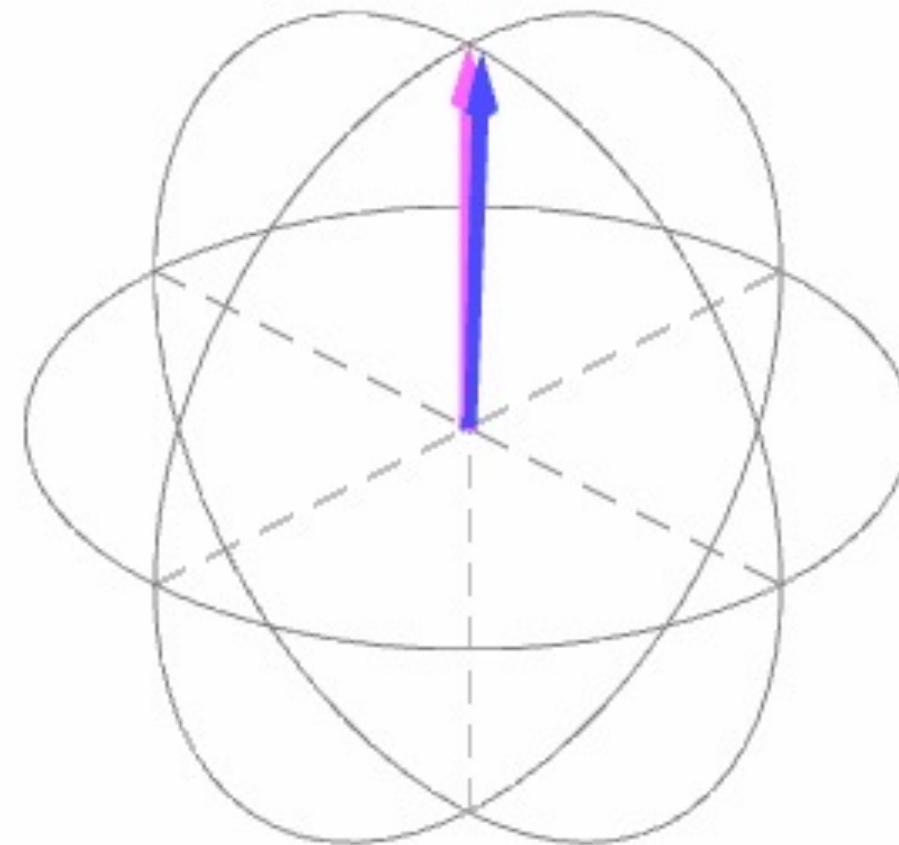
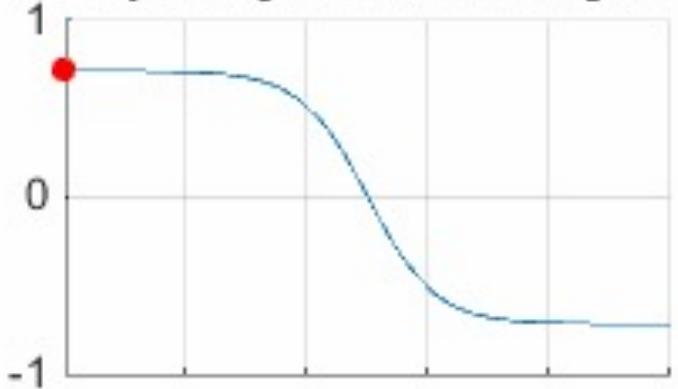
$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

# Shaping pulses for noise robustness

Pulse Amplitude

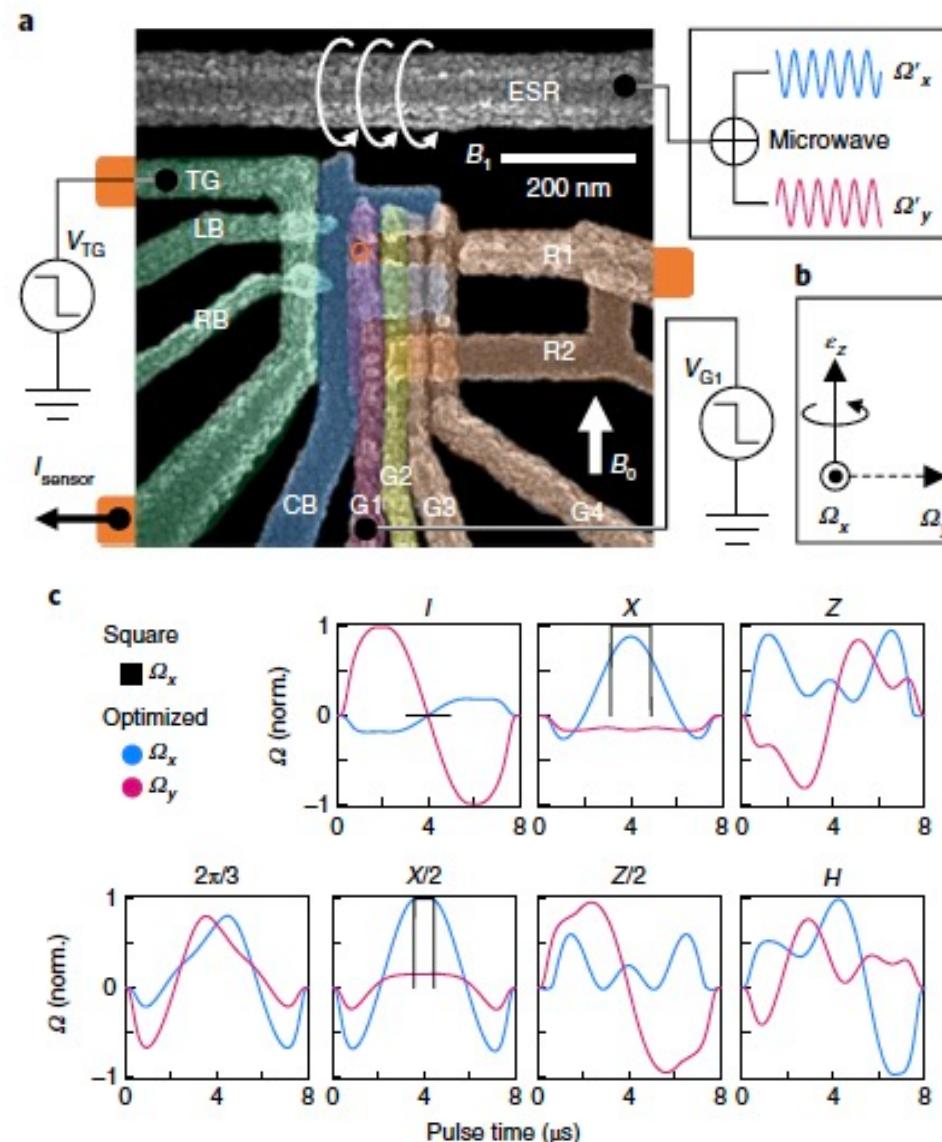


Frequency Modulation [kHz]



# Systematic pulse engineering for single qubit gates

Operator	Gate(s)	Matrix
Pauli-X (X)		$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
Pauli-Y (Y)		$\begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$
Pauli-Z (Z)		$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$
Hadamard (H)		$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
Phase (S, P)		$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$
$\pi/8$ (T)		$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$
Controlled Not (CNOT, CX)		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$
Controlled Z (CZ)		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$
SWAP		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$
Toffoli (CCNOT, CCX, TOFF)		$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$

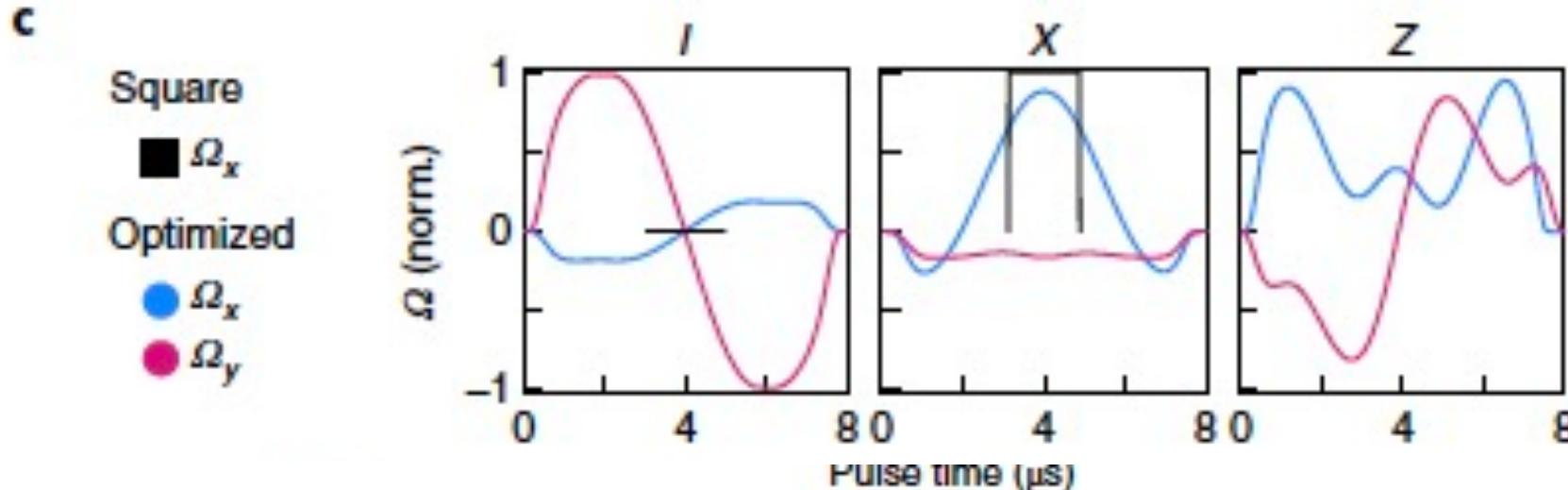
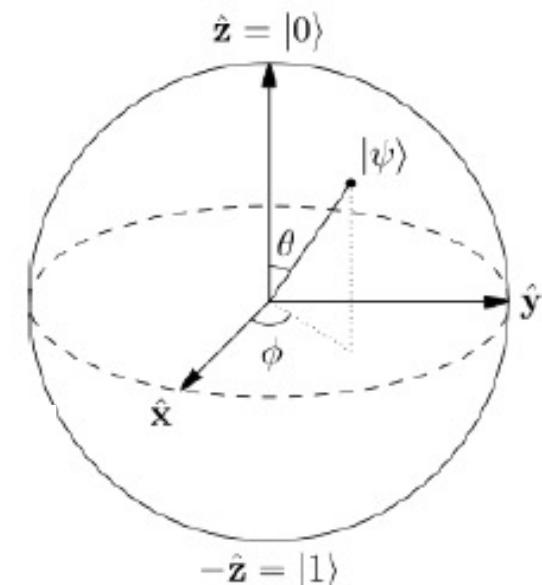


# Pulse engineering protocol: gradient based optimization

$$\mathcal{H} = \Omega_{drift}\Omega_{ESR}(\Omega_x\sigma_x + \Omega_y\sigma_y) + (f_{ESR} + \epsilon_z)\sigma_z$$

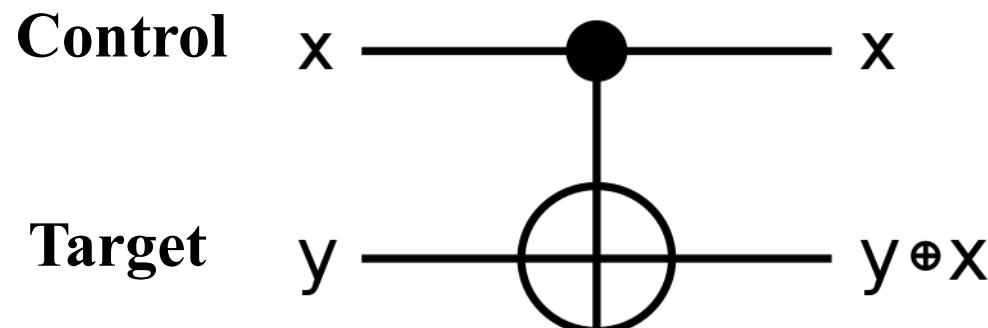
$\epsilon_z$   noise from phase flips

- (1) Randomize  $\epsilon_z$
- (2) Calculate  $\frac{\delta\Psi}{\delta\Omega}$  for all  $\Omega$  pointwise, with the current Hamiltonian  $H$
- (3) Update  $\Omega \rightarrow \Omega + \eta \frac{\delta\Psi}{\delta\Omega}$
- (4) Filter  $\Omega$  for smoothness and bound condition  $\Omega_{max}^2 \geq \Omega_x^2 + \Omega_y^2$



# Extension to 2-qubit gates: CNOT gate

Operator	Gate(s)	Matrix
Pauli-X (X)		$\oplus$ $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
Pauli-Y (Y)		$\begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$
Pauli-Z (Z)		$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$
Hadamard (H)		$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
Phase (S, P)		$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$
$\pi/8$ (T)		$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$
Controlled Not (CNOT, CX)		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$
Controlled Z (CZ)		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$
SWAP		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$
Toffoli (CCNOT, CCX, TOFF)		$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$

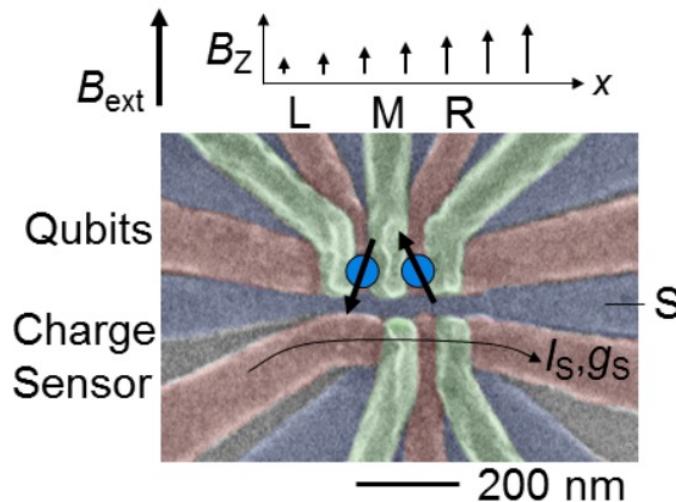
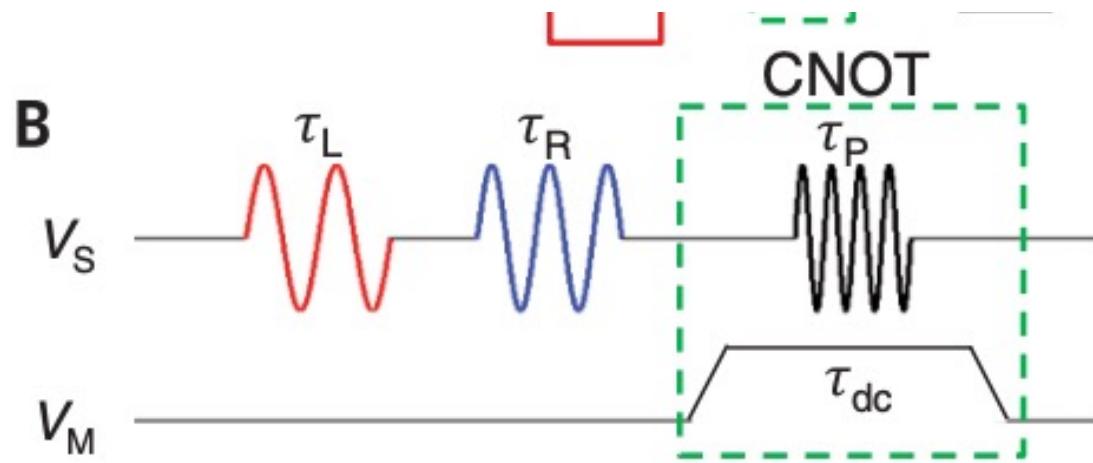


input		output	
x	y	x	$y+x$
$ 0\rangle$	$ 0\rangle$	$ 0\rangle$	$ 0\rangle$
$ 0\rangle$	$ 1\rangle$	$ 0\rangle$	$ 1\rangle$
$ 1\rangle$	$ 0\rangle$	$ 1\rangle$	$ 1\rangle$
$ 1\rangle$	$ 1\rangle$	$ 1\rangle$	$ 0\rangle$

If control = 1, flip target!

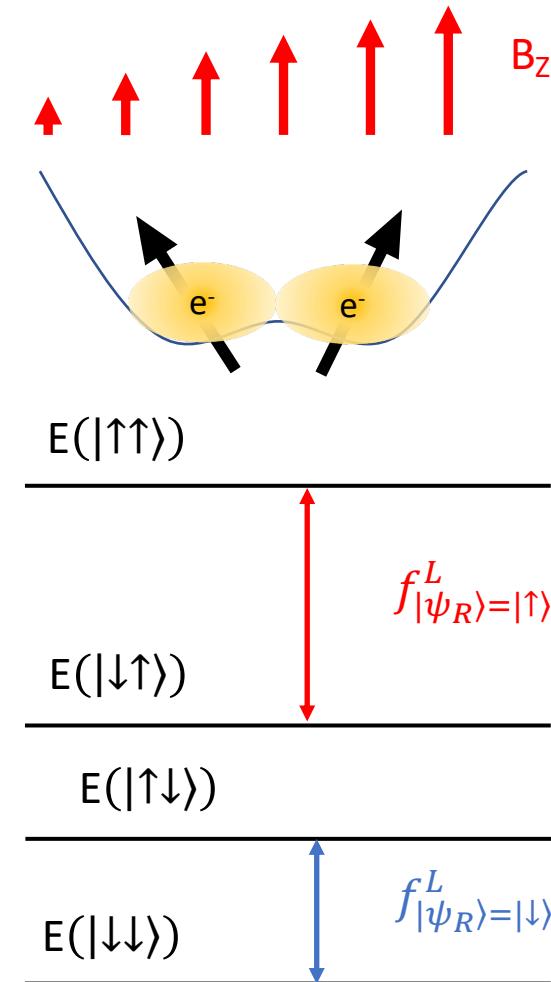
# Pulse shaping for CNOT gate

$$\delta E_z \gg J$$

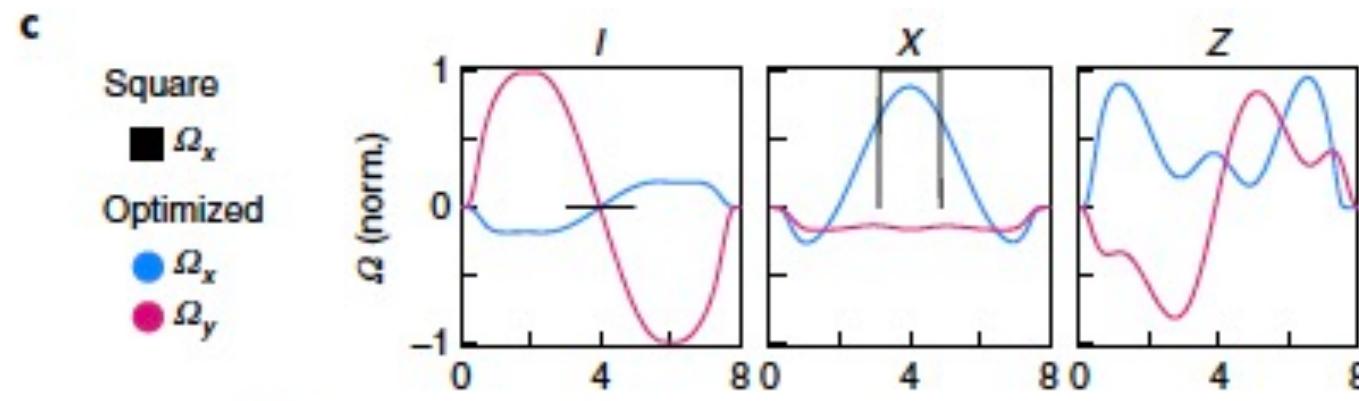
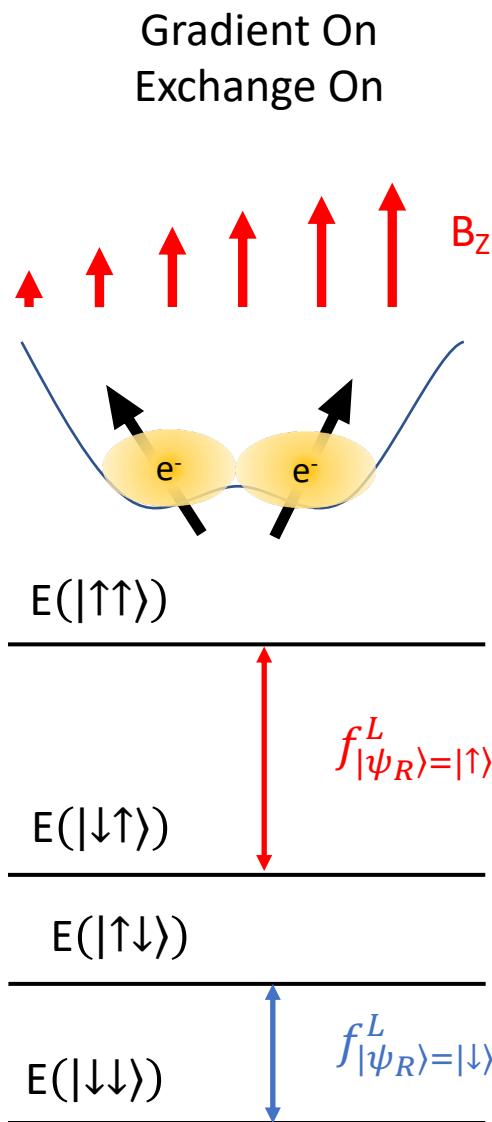


Zajac, AJS *et al.*, Science (2018)  
Russ, AJS *et al.*, PRB (2018)

Gradient On  
Exchange On



# Pulse shaping for CNOT gate (cont'd)

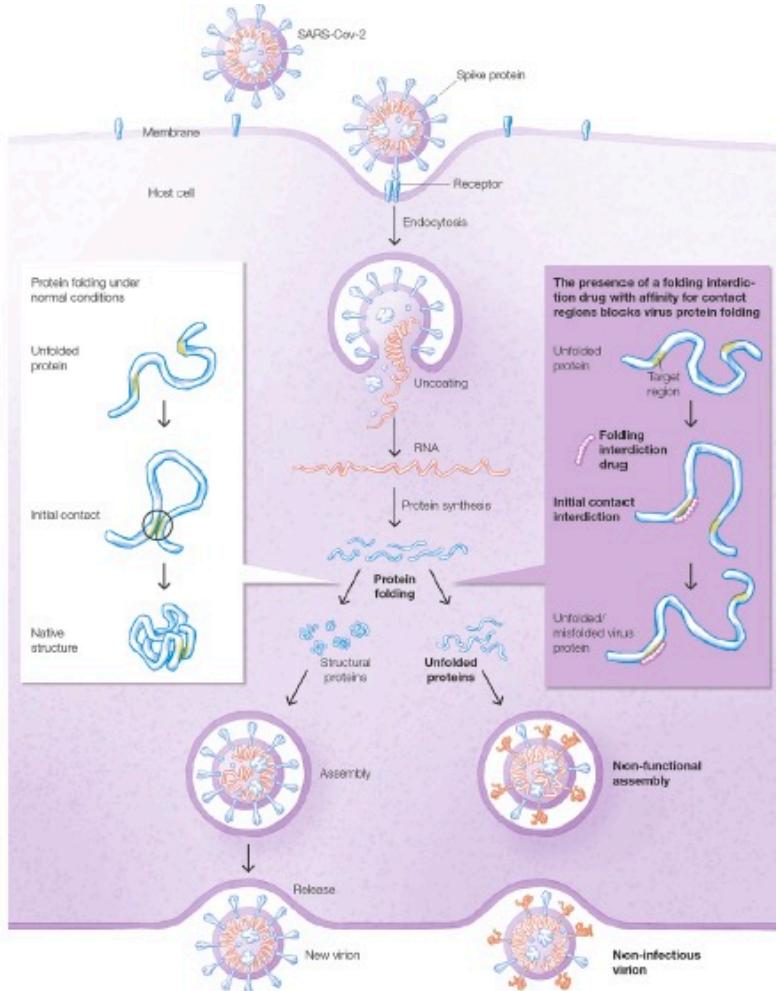


+

$$V_M \rightarrow J$$

Optimized res-CNOT gate as first 2-gate demonstration,  
many more to come!

# Outlook: towards therapeutic drug design using quantum



$$\mathcal{O}(2^N) \xrightarrow{\hspace{1cm}} \mathcal{O}(N^3) ??$$

Challenges	Proposed solution
<b>Low-connectivity</b> <ul style="list-style-type: none"><li>- Spins limited to nearest-neighbor interactions</li><li>- Difficult to form large cluster states</li></ul>	Quantum random access memory
<b>Complexity</b> <ul style="list-style-type: none"><li>- Each qubit requires multiple wires connected to bond pads</li><li>- Simultaneous voltage + MW control</li></ul>	Overlapping gate architecture → all qubits share same barrier voltage
<b>Qubit infidelity</b> <ul style="list-style-type: none"><li>- Decoherence induced → spin-spin interactions lead to information loss</li><li>- Noise induced → charge noise leading to fluctuations in exchange interactions</li></ul>	Pulse engineering for noise induced infidelity. Res-Sqrt(SWAP) gates for decoherence induced.

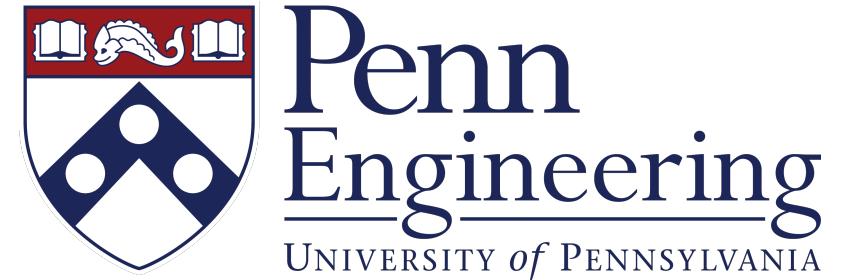
Will need hundreds of qubits!

# Acknowledgments



**Prof. Anthony Sigillito**

**Dr. Seong Oh**



**ESE PhD Association!**