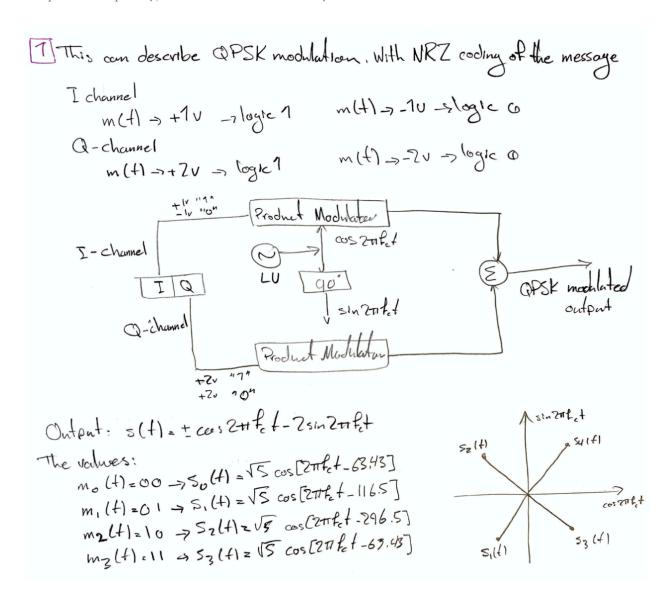
## Digital Communications

## Homework #4

1. Suppose that a transmitter modulates a sinusoid by using an in-phase component consisting of a square wave that takes on values of either +1 or -1 and a quadrature component consisting of a square wave that takes on values of either +2 or -2. How is the resulting sinusoid modulated (amplitude, phase or frequency)? How many values can the (amplitude/phase/frequency) assume and what are they?



2. An analog voice signal is to be sampled, quantized and transmitted using BPSK modulation. The original analog signal has a bandwidth of 4kHz. A quantization SNR of 50dB is desired. The quantization SNR can be written as

$$SNR(dB) = 6.02n + 4.77 - 20\log 10 \left( V_{\text{peak}} / V_{rms} \right)$$

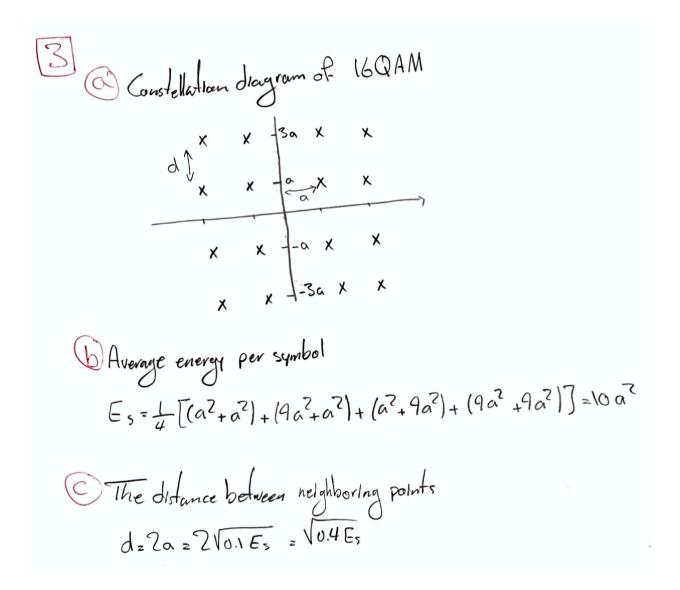
where n is the number of bits used in the quantization process and  $V_{\rm peak}/V_{\rm rms}$  is the peak-to-average voltage ratio of the signal (linear). If the peak to average power ratio of the analog signal of interest is 10dB, what is the bandwidth of the transmitted BPSK signal if a raised cosine pulse is used with roll-off factor 0.5 (assume infinitely long pulses)?

[2] 
$$SNR_{2}SOJB$$

10  $Joy(\frac{J_{peak}^{2}}{J_{rms}^{2}}) = 10 dB = 20 log(\frac{J_{peak}}{J_{rms}})$ 
 $SRR_{2}6.02N + 9.77 - 20 log(\frac{J_{peak}}{J_{rms}})$ 
 $\Rightarrow 50 - 9.77 + 10 = 6.02N \Rightarrow N = 9.74 \Rightarrow N = 10$ 
 $BW = (1+v) Nf_{5} \leftarrow Sumplying freq$ 
 $voll-off Radov$ 
 $\Rightarrow BW = (1+0.5) 80$ 
 $SW = 60 kHz$ 

## 3.

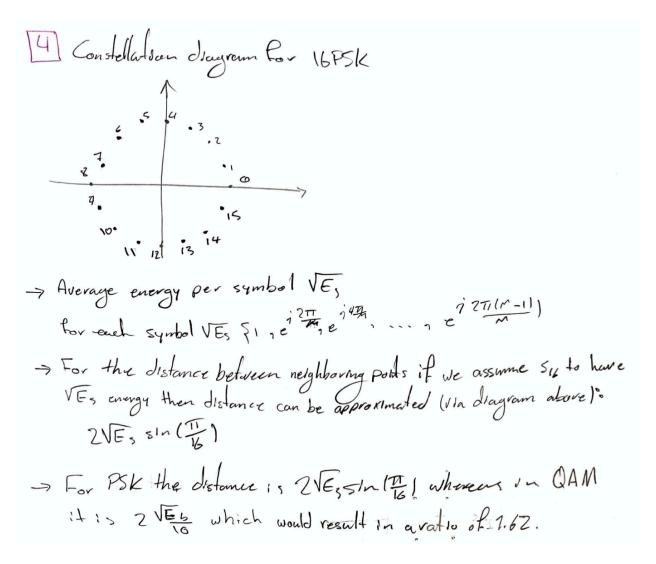
- 3.1. Draw the signal constellation diagram for a 16-QAM signal with maximum amplitude A
- 3.2. What is the average energy per symbol?
- **3.3.**What is the distance between neighboring signal points in terms of the averaged energy per symbol?



## 4.

- **4.1.** Draw the signal constellation diagram for a 16-PSK signal with maximum amplitude *A*
- **4.2.** What is the average energy per symbol?
- **4.3.** What is the distance between neighboring signal points in terms of the average energy per symbol?

**4.4.** Change the amplitude so that the average energy is the same as in 16-QAM presented in problem 3. How do the minimum distance between signal points compare?



5. Explain the difference between coherent reception, non-coherent reception and differentially coherent reception.

Coherent systems refer to the situation where the receiver needs the phase information of the transmitter (the carrier phase) to recover the transmitted data at the receiving side. The phase information comes from either a reference from the transmitter or could be from a local oscillator at the receiving side. The oscillators used at both the transmitter and receiver are not phase-locked; therefore there is a phase difference between the reference signal transmitted and the reference signal used in the demodulator. This phase difference must be estimated and corrected. The receiver is more complicated and expensive. But it has better bit error rate of detection.

On the other hand, in non-coherent systems the receiver do not need the phase information the the transmitter carrier to recover the signal. This type of systems do not require expensive and complex carrier recovery circuit. But it has worse bit error rate of detection in comparison with the coherent systems.

In differentially coherent receiver a very simple estimate of the fading distortion is used whereas the coherent receiver uses the optimal estimate.

6.

- 6.1. Explain the trade-off between energy efficiency and bandwidth efficiency for MPSK and MASK.
- 6.2. Does this trade-off differ for MFSK?

Energy efficiency comparison

MPSK:

-At Pixed Eb/No, increasing M degrades Pb (bit error vate)

-At Pixed Po, increasing M can provide an improvement.

MFSK:

-At Pixed Po, increasing M can provide an improvement on Po

-At Pixed Po, increasing M can provide a reduction in Egyng requirement

> Therefore, MFSK is more energy efficient than MPSK

Bondwidth efficiency comparison.

In general, the bandwidth required to pass MPSK IMAAM signal
is approximately given by 
$$B = \frac{1}{15}$$

and  $R_S = \frac{\log_2 M}{B} = \text{bit rate}$ 

Then bondwidth efficiency cam be expressed as

 $f = \frac{R_B}{B} = -\log_2 M$  (bits/sec/Hz)

MFSK

- Bondwidth required to transmit MFSK signal is

 $B = \frac{M}{2T}$  (adjacent frequencies need to be separated by  $\frac{1}{2T}$ 

to maintain orthogonality)

- Bendwidth efficiency of MFSK signal

 $f = \frac{R_B}{B} = \frac{2\log_2 M}{B}$  (bitisec/Hz)

Thousefore, as M increases, bandwidth efficiency of MPSK/MQAM increases, but bandwidth efficiency of MFSK decrease.

- 7. Assume that a QPSK signal is used to send data at a rate of 30Mbps over a satellite transponder. The transponder has a bandwidth of 24MHz.
  - 7.1. If the satellite signal is to use a raised pulse shape, what is the roll-off factor r that is required?
  - 7.2. Could a rolloff factor r be found so that a 50-Mbps data rate could be supported?

7 deta rate 
$$R_b = 30 \text{ Mbps}$$

Bandwith =  $24 \text{ MHz}$ 

a)  $BW = \frac{R_b(1+\alpha)}{\log_2 m}$ 
 $M_- 4 \text{ for QPSK} \Rightarrow 24 \text{ M} = \frac{30 \text{ M}}{2} (\alpha + 1)$ 
 $\Rightarrow \alpha + 1 = 1.6 \Rightarrow \text{ roll off } R_{actor} = \frac{30 \text{ M}}{2} (\alpha + 1)$ 

For  $R_b = 50 \text{ Mbps} \Rightarrow 24 \text{ M} = \frac{50 \text{ M}}{2} (\alpha + 1)$ 
 $\Rightarrow \alpha + 1 = 0.96 \Rightarrow \alpha = -0.04 \Rightarrow \text{but it can not be negative}_{1} = 50 \text{ the data rate is not achievable}_{2}$