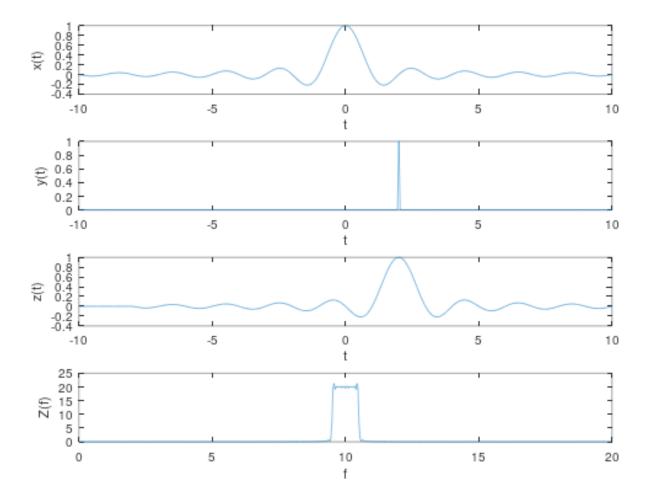
Digital Communications Nina Malammadi Homework #1 Convolution of a sinc function and an impulse [10] Defermine the convolution of sinc (+) with 5(+-2) We have that x(+) * S(+ ta) = x(+ ta) Then Sinc (t) *8(t-2) = Sinc (t-2) In Frequency Jonain X(+) * y(+) < = > X(+)Y(+) Some (+) ← +>TT(+) (S(+-2) = + e-j2w

⇒ 5/nc(f) *8(+-2) < +> T(+). e-j2w

MATLAB/Octave code

```
dt = 0.05;
t = -10:dt:10;
x = sinc(t);
y = zeros(1, length(t));
ind = find(t==2);
y(ind) = 1;
z = conv(x, y, 'same');
figure;
subplot(4,1,1);
plot(t, x)
xlabel('t')
ylabel('x(t)')
subplot(4,1,2);
plot(t, y)
xlabel('t')
ylabel('y(t)')
subplot(4,1,3);
plot(t, z)
xlabel('t')
ylabel('z(t)')
N = 512;
Zf = (fft(z,N));
fr=(0:N-1)/N/dt;
subplot(4,1,4);
plot(fr, fftshift(abs(Zf)));
xlabel('f')
ylabel('Z(f)')
```



Comble two square persons (in time domain) of width
$$T$$
, $\Pi(\frac{t}{T})$.

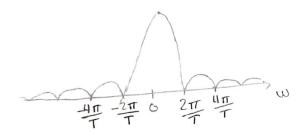
Plot the resulting time would from and its spectrum

 $\Pi(t) \rightarrow \frac{1}{2} \circ \frac{1}{2}$
 $X_1(t) = X_2(t) = \Pi(\frac{t}{T}) \rightarrow \frac{1}{2} \circ \frac{1}{2}$
 $X_1(t) = X_2(t) = \frac{1}{2} \circ \frac{1}{2}$
 $X_1(T) \circ \Pi(\frac{t}{T}) \rightarrow \frac{1}{2} \circ \frac{1}{2}$
 $X_2(t-T) \circ \Pi(\frac{t}{T}) \rightarrow \frac{1}{2} \circ \frac{1}{2} \circ \frac{1}{2}$
 $X_2(t-T) \circ \Pi(\frac{t}{T}) \rightarrow \frac{1}{2} \circ \frac{1$

Spectruma

$$Sinc(X) := \frac{Sin(\pi X)}{\tau \tau X}$$

$$\Rightarrow$$
 $x_1(t) * x_2(t) \xrightarrow{f} x_1(t) \cdot x_2(t)$



$$P_{z}\lim_{T\to\infty} \frac{1}{2T} \int_{-T}^{T} |w(t)|^{2} dt = \lim_{T\to\infty} \frac{1}{2T} \int_{-T}^{\frac{\tau_{0}}{2}} 1 dt$$

$$= \lim_{T\to\infty} \frac{1}{2T} \left[t \right]_{-\frac{\tau_{0}}{2}}^{\frac{\tau_{0}}{2}} = \lim_{T\to\infty} \frac{1}{2T} \left[\frac{\tau_{0}}{2} - \left[-\frac{\tau_{0}}{2} \right] \right]_{-\frac{\tau_{0}}{2}}^{\frac{\tau_{0}}{2}}$$

$$= \lim_{T\to\infty} \frac{1}{2T} \left[\tau_{0} \right] = 0 \quad \implies \text{OCE}(w) \text{ and } P_{z} = 0$$

$$|V(t)| = |T(\frac{t}{T_0}) \cos(2\pi r_0^2 t)| = \int_{-\infty}^{\infty} \cos(2\pi r_0^2 t) - \frac{T_0}{2} \cot(2\pi r_0^2 t)| = \int_{-\infty}^{\infty} (2\pi r_0^2 t) dt$$

$$= \int_{-\infty}^{\infty} \frac{1 + \cos(4\pi r_0^2 t)}{2} dt = \left[\frac{t}{2} + \frac{1}{4\pi r_0^2} \sin(4\pi r_0^2 t)\right] - \frac{T_0}{2}$$

$$= \left[\frac{T_0}{4} + \frac{1}{4\pi r_0^2} \sin(2\pi r_0^2 t_0)\right] - \left[\frac{T_0}{4} + \frac{1}{4\pi r_0^2} \sin(2\pi r_0^2 t_0)\right] - \left[\frac{T_0}{4} + \frac{1}{4\pi r_0^2} \sin(2\pi r_0^2 t_0)\right]$$

$$= \frac{T_0}{2} + \frac{1}{2\pi r_0^2} \sin(2\pi r_0^2 t_0) \implies 0 < E(\omega) \implies Energy Signal$$

$$\Rightarrow P_{\geq 0}(0)$$

$$E = \lim_{N \to \infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left(\frac{1}{2\pi f_0} + \frac{1}{2\pi f_0} \right) dt$$

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$$= \lim_{N \to \infty} \int_{-\infty}^{\infty} \left(\frac{1}{2\pi f_0} + \frac{1}{2\pi f_0}$$

(5) Using the convolution property, find the spectrum for $W(t) = \frac{\sin(2\pi f_1 t)}{x_1(t)} \frac{\cos(2\pi f_2 t)}{x_2(t)}$ $X_1(t) = \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} \right) \right) \right) = \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} \right) \right)$ $X_2(t) = \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} \right) + \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2}$

6) The signal x(t)=cos (10t) is input to a linear system that has an impuls response hitt Seto tro [6a] Wheat is the output time signal ? $\mathcal{F}\left[\cos(2\pi A + B)\right] = \int_{-\infty}^{\infty} \frac{e^{j(2\pi A + B)} + e^{-j(2\pi A + B)}}{7} e^{-j2\pi A + B} dt$ = 1 [(ejzT(A-f)+B d+ + (e-jzT(A+f)+B d+) = 1 e B [S(f-A) + 8(f+A)] $\Rightarrow \Im \left[X(t) \right] = \Im \left[\cos (10t) \right] = \Im \left[\cos (2\pi \frac{5}{5}t) \right]$ $= \frac{1}{2} \left[S(f - \frac{S}{T_0}) + S(f + \frac{S}{T_0}) \right]$ $\Rightarrow 5[e^{-\frac{1}{10}}] = \int_{0}^{\infty} e^{-\frac{1}{10}} e^{-\frac{1}{12\pi r^2}} dt = \frac{1}{\frac{1}{10} + (2\pi r^2)^2}$ >> X(P).71(P) = \frac{1}{\frac{1}{2\pi (2\pi P)^2}} \xeta\[\delta(P-\frac{\fra = \frac{1}{2[\frac{1}{2.000}]} \times \left[8(R-\frac{1}{2}) + 8(R+\frac{1}{2}) \right] $\frac{1}{2} \left[\frac{5(2-\frac{1}{100})}{\frac{1}{100}} + \frac{5}{100} \left(\frac{5(2+\frac{5}{100})}{\frac{1}{100}} \right) = \frac{\cos(10+1)}{\frac{1}{100}}$ [66] Interference signal ZL61= cos (15++ 1) $S[\cos(15t+\frac{\pi}{8})] = \frac{e^{\frac{\pi}{4}}}{7}[S(f-\frac{15}{2\pi})+S(f+\frac{5}{2\pi})]$ \Rightarrow $9+(f)=4\pi(\frac{1}{4}f)=4\pi(\frac{\omega}{8\pi})$

$$\Rightarrow 9H(f) = 4\pi (\frac{1}{4}f) = 4\pi (\frac{1}{8\pi})$$

$$\Rightarrow h(f) = 4 \sin (4\pi f)$$