# Digital Communications

Homework #6

## Question 1

$$\begin{array}{l}
\overline{F}_{S} = \frac{1}{8}(4a^{2} + 4(2a^{2})) = \frac{1}{2}a^{2} + a^{2} = a^{2}(\frac{3}{2}) \\
= \frac{3}{2}a^{2} \\
d_{1,1+1} = a \Rightarrow d = \sqrt{\frac{7E_{S}}{3}} \\
P_{E} = 2Q(\frac{1}{\sqrt{2N_{o}}}) = 2Q(\frac{\sqrt{\frac{3}{3}E_{S}}}{\sqrt{2N_{o}}}) = 2Q(\sqrt{\frac{E_{S}}{3}N_{o}}) \\
E_{o} \log(M) = E_{S} \Rightarrow E_{S} = 3E_{D}
\end{array}$$

$$= P_{e} = 2Q(\sqrt{\frac{E_{O}}{N_{o}}})$$

Comparing the plot with 8PSK, as follows, shows that the BER for the modulation scheme of the question is worse than 8PSK. This is not surprising as this the modulation with the constellation diagram shown in the question does not appear to be a popular one and if it had a better probability of error, people would probably use that instead of 8PSK.

To achieve the same probability of error, 8PSK requires a smaller SNR.

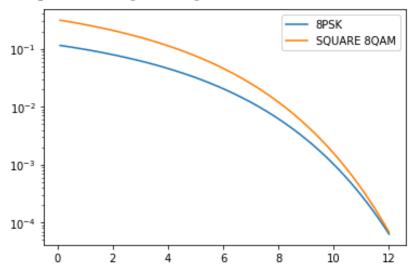
```
def calc8psk(ebn0dB):
    ebn0 = 10 ** (ebn0dB / 10)
    return (2/3) * qfunc(np.sqrt(6 * ebn0 * (np.sin(np.pi/8) ** 2)))

def calc8qam(ebn0dB):
    ebn0 = 10 ** (ebn0dB / 10)
    return 2.0 * qfunc(np.sqrt(ebn0))
```

```
ebn0dBs = np.linspace(0.1, 12, 100)

fig, ax1 = plt.subplots()
ax1.plot(ebn0dBs, calc8psk(ebn0dBs))
ax1.plot(ebn0dBs, calc8qam(ebn0dBs))
ax1.set_yscale('log')
ax1.legend(['8PSK', 'SQUARE 8QAM'])
```

### <matplotlib.legend.Legend at 0x7f02e6faeda0>



# Question 2

$$[Lp(dB)=20 \log_{10}(\frac{4\pi d}{9})=20 \log_{10}(\frac{4\pi (10,000)}{0.15})=118.4$$
  
 $A=0.15 \text{ for } f=2GHz$