

# Populating Occupancy Grids from LIDAR Scan Data

Course 4, Module 2, Lesson 2 – Part 2



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# Learning Objectives

- Create a simple Inverse Measurement Model
- Discuss an improvement using Bresenham line algorithm

# Inverse Measurement Module

$$l_{t,i} = \text{logit}\left(p(m^i|y_t)\right) + l_{t-1,i} - l_{0,i}$$

- State of the occupancy grid given a measurement
- So far we have only seen the following measurement model:

$$p(y_t|m^i)$$

- State of the occupancy grid given a measurement
- A inverse measurement model is needed!

# Inverse Measurement Module

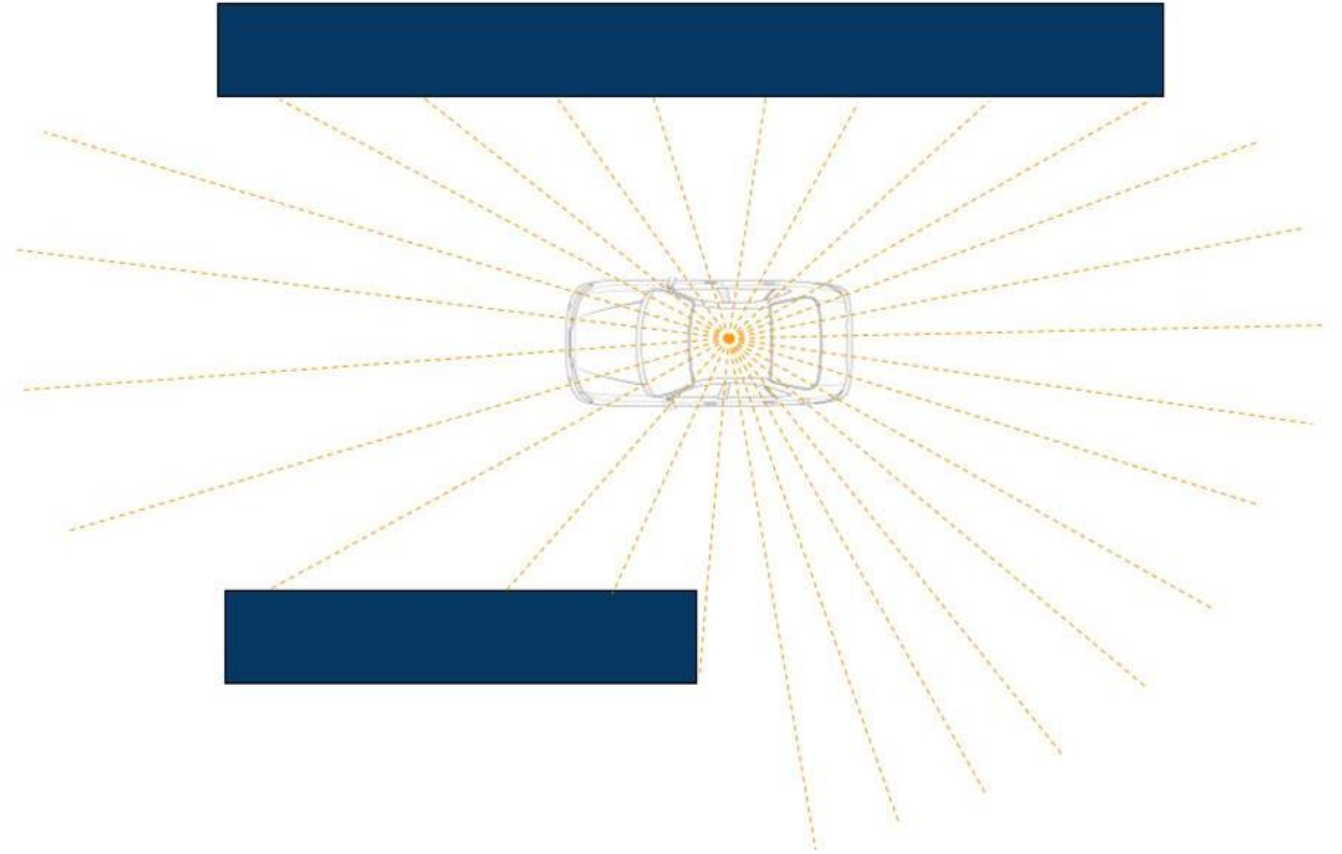


- Scanner bearing:

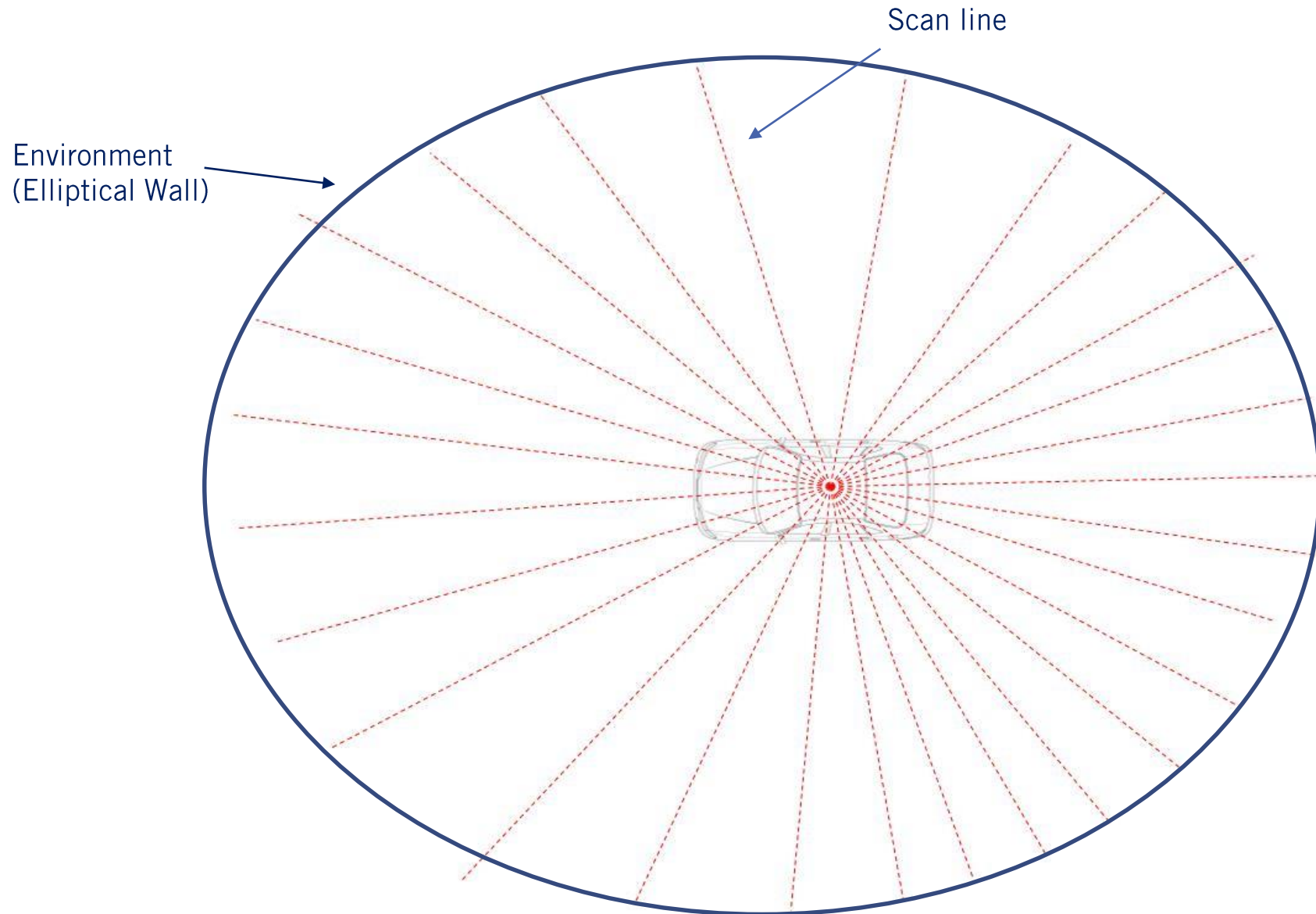
$$\phi^s = [-\phi_{max}^s \quad \dots \quad \phi_{max}^s] \quad \phi_j^s \in \phi^s$$

- Scanner ranges:

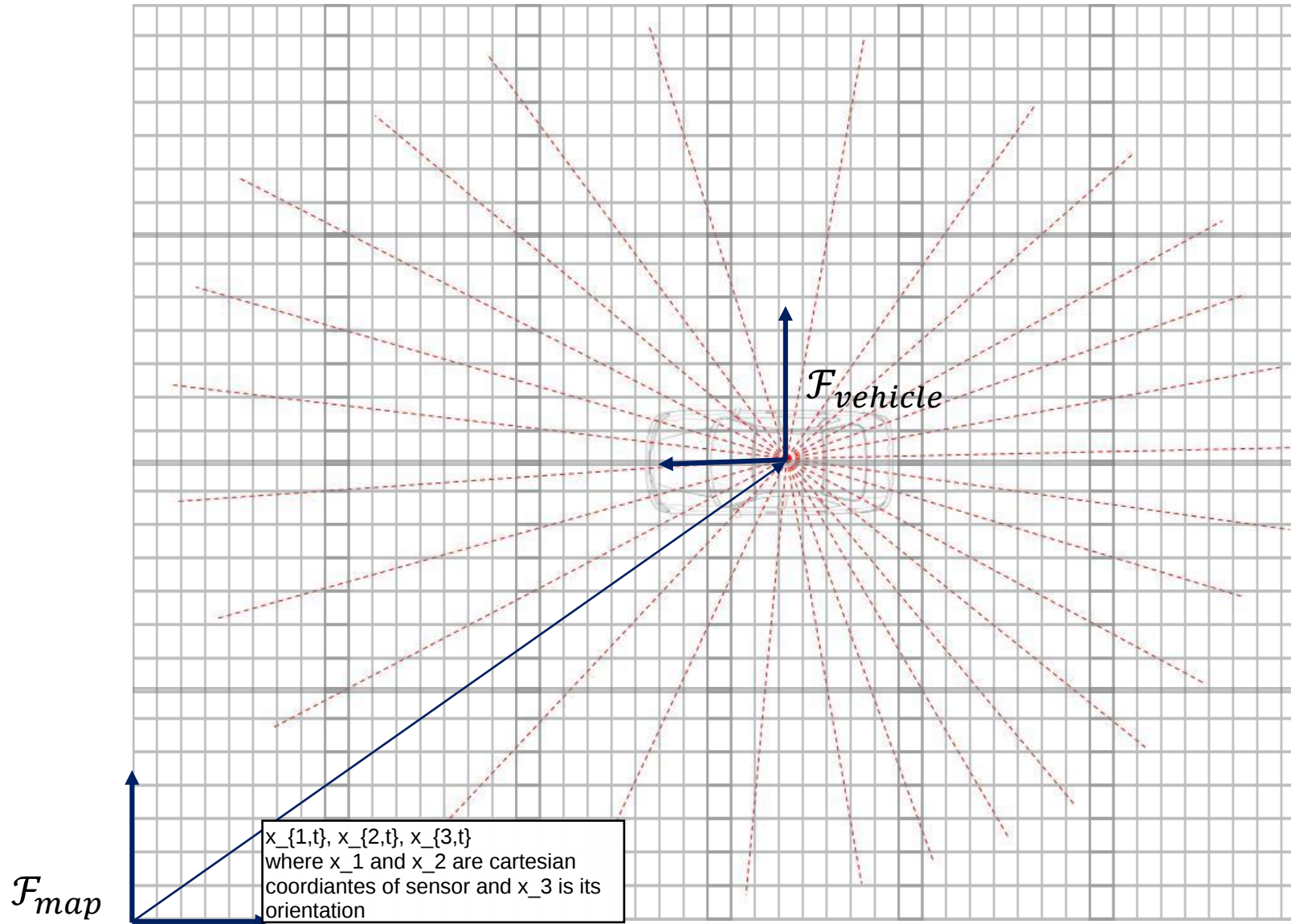
$$r^s = [r_1^s \quad \dots \quad r_j^s] \quad r_j^s \in [0, r_{max}^s]$$



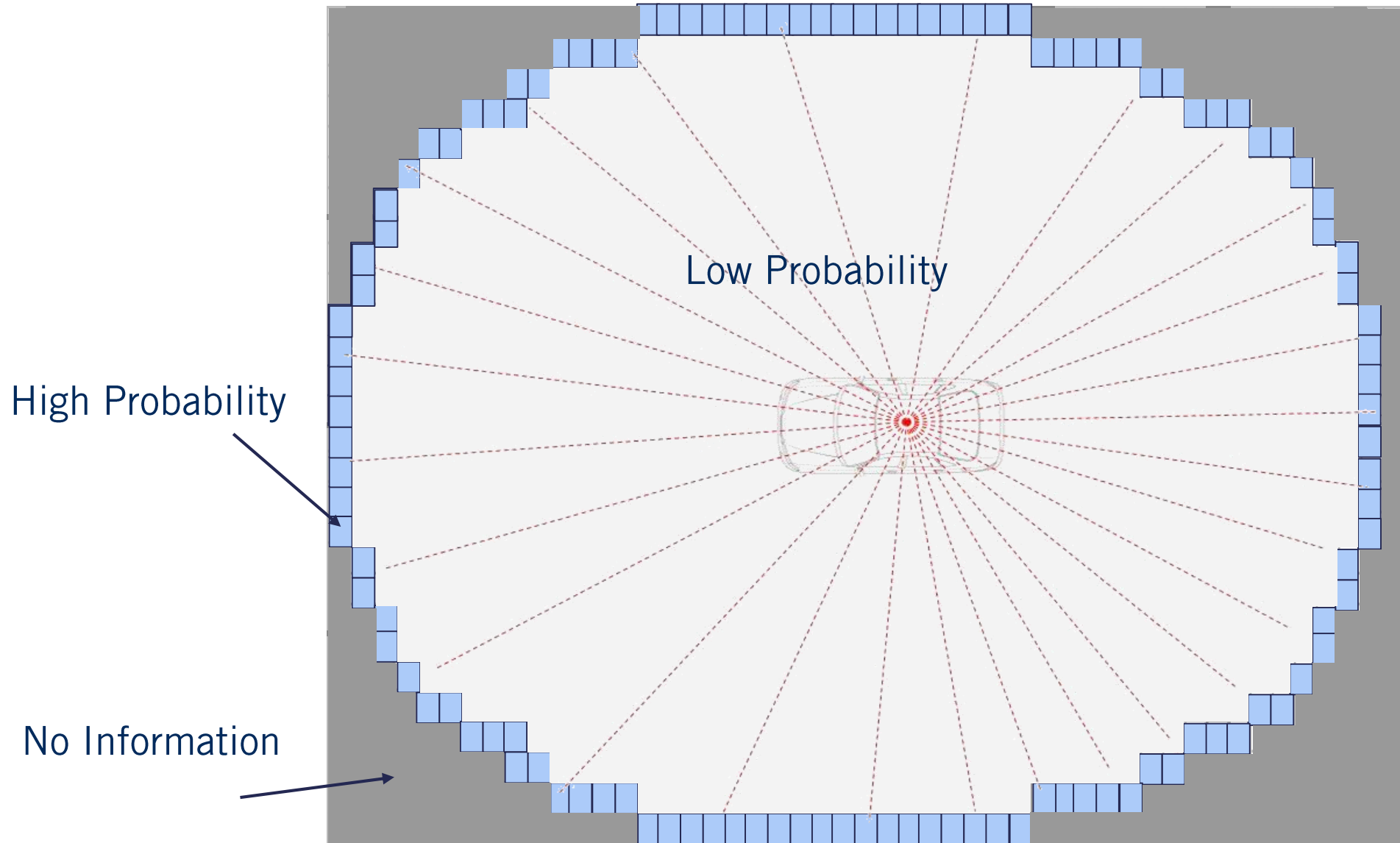
# Inverse Measurement Module



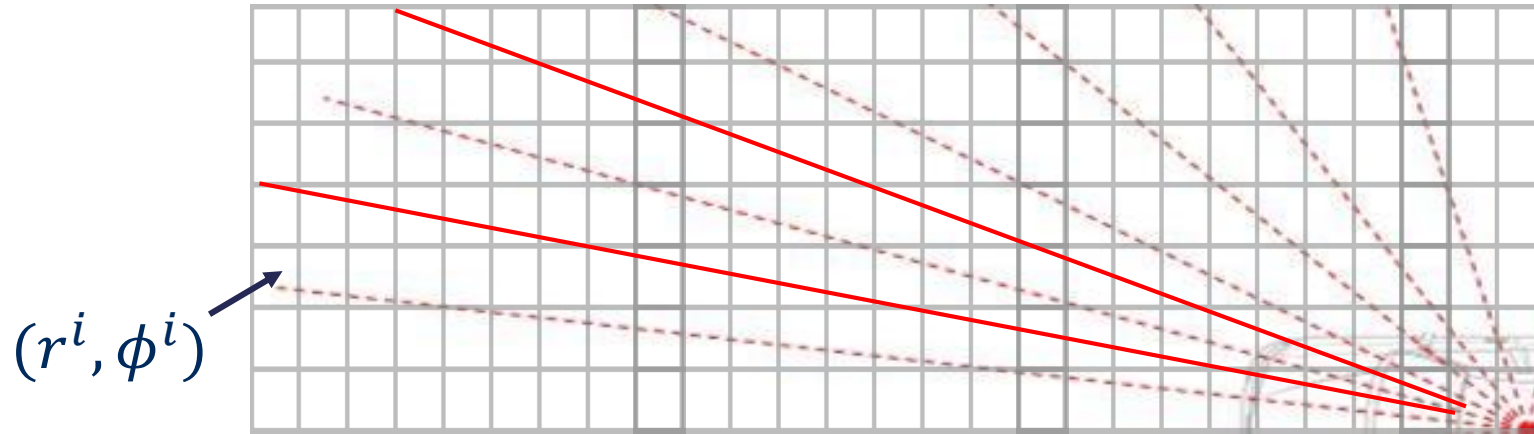
# Inverse Measurement Module



# Inverse Measurement Module



# Inverse Measurement Module – To be fixed



Closest relative bearing:



$$k = \operatorname{argmin}(|\phi^i - \phi_j^s|)$$

Relative range:

$$r^i = \sqrt{(m_x^i - x_{1,t})^2 + (m_y^i - x_{2,t})^2}$$

Relative bearing:

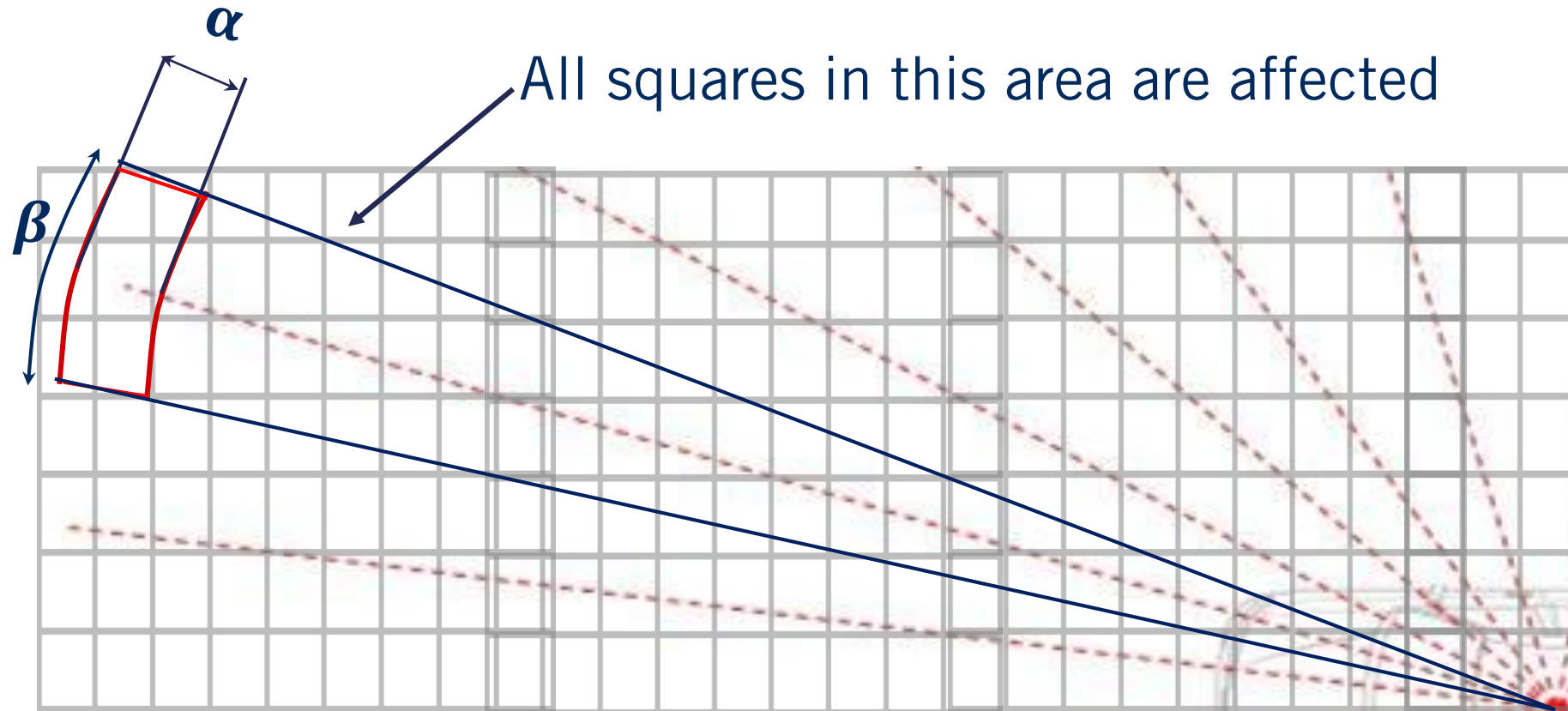
$$\phi^i = \tan^{-1} \left( \frac{m_y^i - x_{2,t}}{m_x^i - x_{1,t}} \right) - x_{3,t}$$



# Inverse Measurement Module



- $\alpha$  - defines the affected range for high probability
- $\beta$  - defines the affected angle for low and high probability



# Inverse Measurement Module - Algorithm

- No Information

if  $r^i > \min(r_{max}^s)$  or  $|\phi^i - \phi_k^s| > \beta/2$

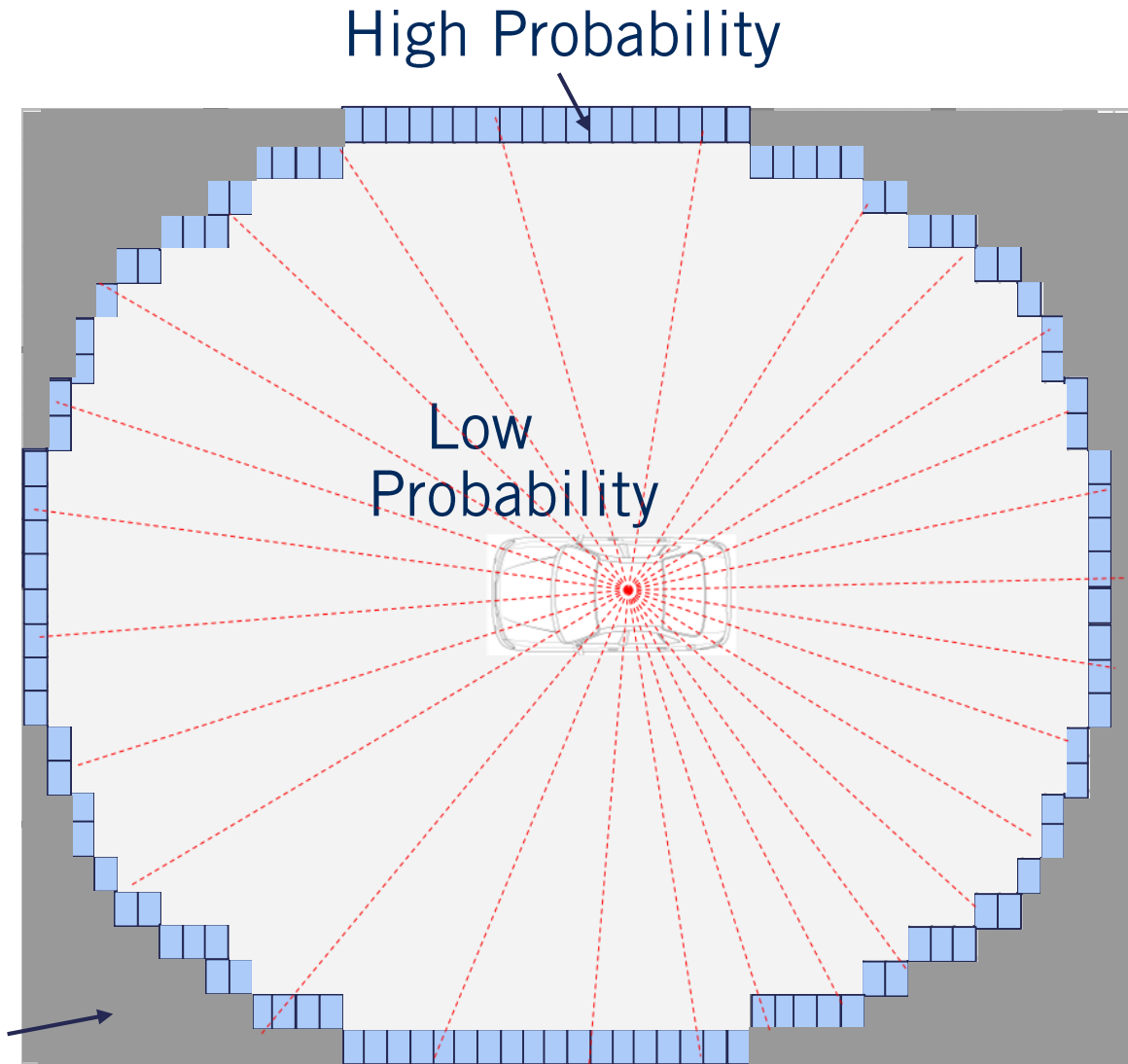
- High probability

if  $r_k^s < r_{max}^s$  and  $|r^i - r_k^s| > \alpha/2$

- Low probability

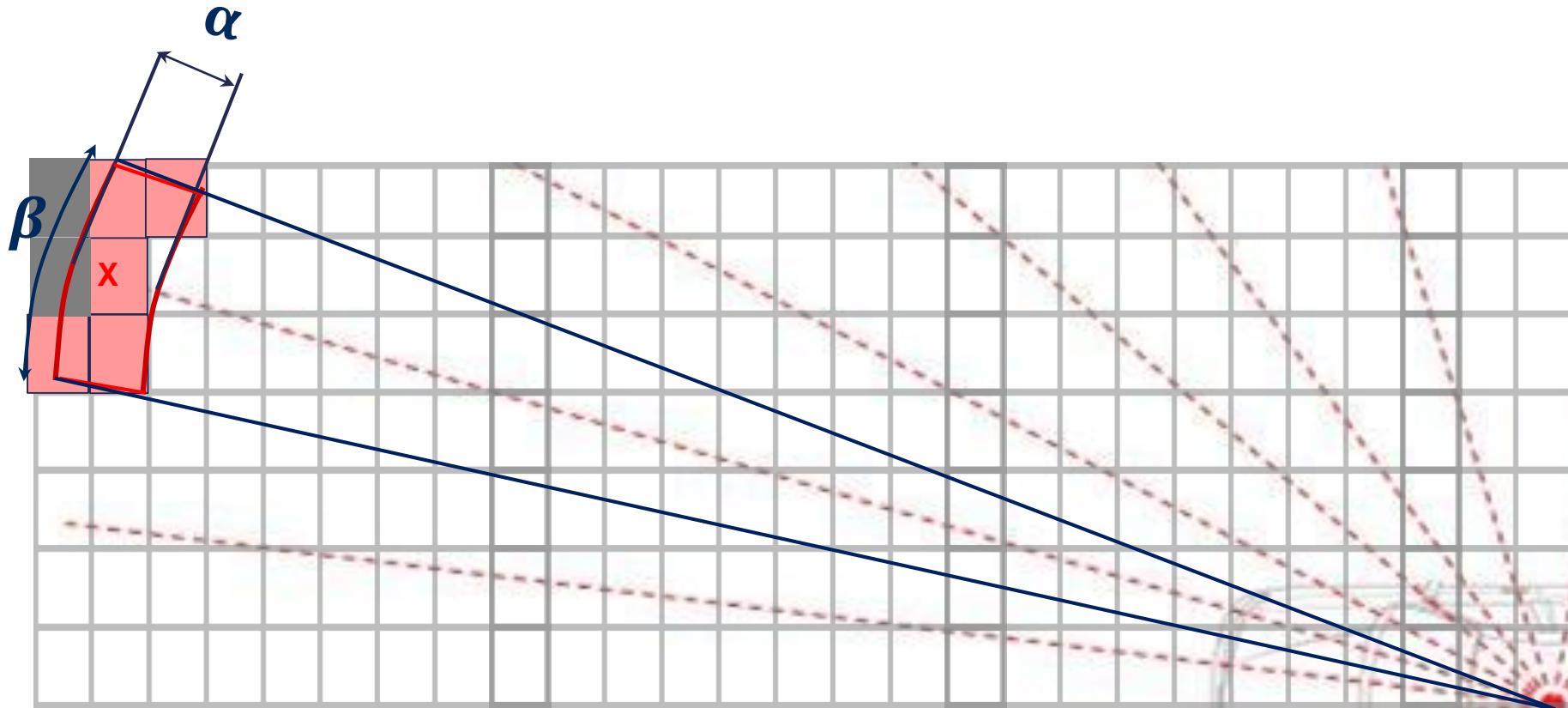
if  $r^i < r_k^s$

No Information



# Inverse Measurement Module

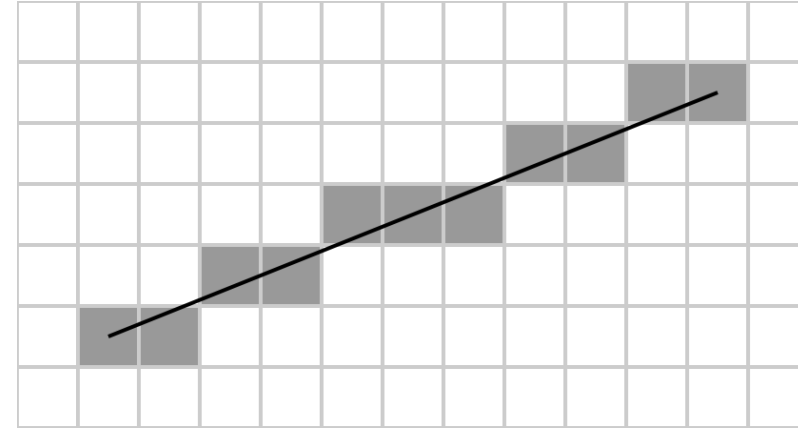
- Example – red cells denote high probability of occupied, given measurement denoted by red x.



# Inverse Measurement Module With Ray Tracing



- Ray tracing algorithm using Bresenham's line algorithm
  - Rasterized line algorithm
  - Uses very cheap fixed point operations for fast calculations
- Perform update on each beam from the LIDAR rather than each cell on the grid
  - Performs far fewer updates (ignores no information zone)
  - Much cheaper per operation



# Summary

- Create a simple Inverse Measurement Model
- Discuss an improvement using Bresenham line algorithm