

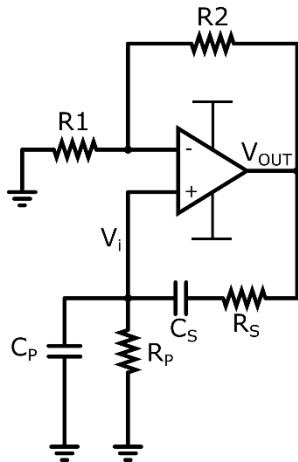
Assignment 5 solutions

EE204: Analog Circuits

Dept of Electrical Engineering, IITB

Autumn Semester 2023

Q1.Design a Wein-Bridge Oscillator as shown with the following requirements:



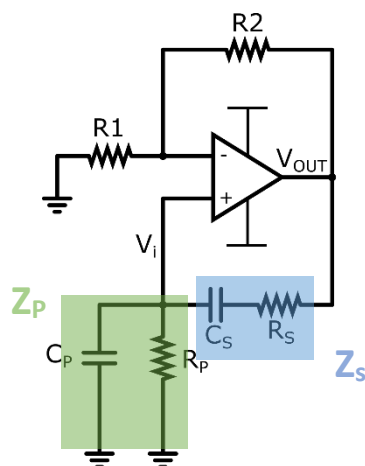
Frequency of Oscillation ω_0 should be $19/(1+x)$ kHz, where x is the last digit of your roll number.

Choose $R_s/R_p = 1+x$ and $C_p/C_s = 1+x$, where x is the last digit of your roll number.

$R_s, R_p, R_1, R_2 > 1 \text{ kohm}$, $C_p, C_s > 100 \text{ pF}$.

A. Determine the following to design the oscillator, assuming the opamp is ideal

A.1. $\beta(s)$ - Transfer function of the feedback path as a function of R_s , R_p , C_p and C_s (2m)



$$Z_p = \frac{R_p}{R_p s C_p + 1} \quad (0.5m)$$

$$Z_s = \frac{R_s C_s s + 1}{s C_s} \quad (0.5m)$$

$$\beta(s) = \frac{Z_P}{Z_P + Z_S} = \frac{1}{\frac{C_P}{C_S} + \frac{R_S}{R_P} + 1 + \left(\frac{1}{R_P C_S S} + R_S C_P S \right)} \quad (1m)$$

A.2. Values of circuit elements - Rs, Rp, Cp and Cs (2m)

From the barkhausen criterion, the loop gain should be 1, since the Opamp is ideal and in negative feedback its gain A_v is real so $\beta(s) * A_v = 1 \Rightarrow \angle \beta(s) = 0$

$$\beta(s) = \frac{1}{\frac{C_P}{C_S} + \frac{R_S}{R_P} + 1 + \left(\frac{1}{R_P C_S S} + R_S C_P S \right)}$$

$\frac{C_P}{C_S} + \frac{R_S}{R_P} + 1$ is real part and $\left(\frac{1}{R_P C_S S} + R_S C_P S \right)$ imaginary part, for $\angle \beta(s) = 0$ the imaginary part should become 0

So by evaluating the imaginary part to zero and substituting $S = j\omega_0$ we get

$$\begin{aligned} \frac{1}{R_P C_S S} + R_S C_P S &= 0 \\ \frac{1}{R_P C_S j\omega_0} &= -R_S C_P j\omega_0 \\ \frac{1}{R_P C_S R_S C_P} &= -j\omega_0 * j\omega_0 \\ \frac{1}{R_P C_S R_S C_P} &= \omega_0^2 \end{aligned}$$

Given $R_S/R_P = 1+x$ and $C_P/C_S = 1+x$

$$\begin{aligned} \text{so, } \frac{1}{R_P C_S (1+x)} &= \omega_0 = \frac{2\pi}{1+x} * 19 * 10^3 \quad (1m) \\ \frac{1}{R_P C_S} &= 2\pi * 19 * 10^3 \cong 120 * 10^3 \end{aligned}$$

Given $R_S, R_P, R_1, R_2 > 1\text{kohm}$, $C_P, C_S > 100\text{pF}$.

From the above constraints choose a value of R_P and C_S then $R_S = R_P (1+x)$, $C_P = C_S (1+x)$

(0.25m for each)

A.3. Using values from A.2, find $\beta(j\omega_0)$ - feedback Transfer Function at ω_0 (1m)

$$\beta(s) = \frac{1}{\frac{C_P}{C_S} + \frac{R_S}{R_P} + 1} = \frac{1}{1+x+1+x+1} = \frac{1}{3+2*x} \quad (1m)$$

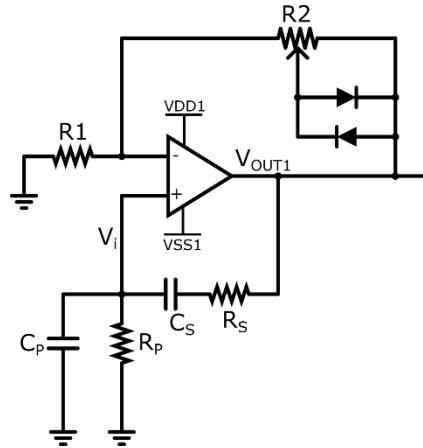
A.4. Using values from A.2, find the ratio R_2/R_1 for sustained oscillations (2m)

$$\begin{aligned} A_v &= 1 + \frac{R_2}{R_1} \quad (0.5m) \\ \beta(j\omega_0) * A_v &= 1 \quad (0.5m) \end{aligned}$$

$$\beta(j\omega_0) * \left(\frac{R2}{R1} + 1 \right) = 1$$

$$\frac{R2}{R1} = 2x + 2 \quad (1m)$$

B. The following amplitude control is implemented with all other circuit elements being the same as before, except R2 is now a potentiometer and two diodes are added across R2 as shown



B.1. Choose R2/R1 so that it is greater than the ratio obtained in A.4 . Determine the values of R2, R1. (1m)

Given $R_s, R_p, R_1, R_2 > 1\text{kohm}$

$$\frac{R2}{R1} > 2x + 2$$

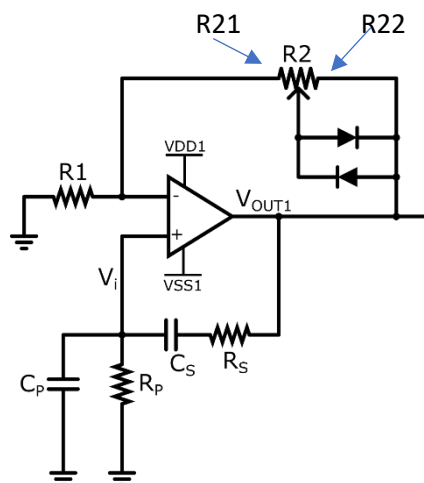
Then choose a value of R1 and evaluate the constraint on R2 [$R2 > R1(2+2x)$] and choose its value

(1m)

B.2. Find the setting on the R2 Potentiometer so that the output sine wave has an amplitude of 6V.

Given $V_{dd1} = -V_{ss1} = 15V$,

Diode current $I_D = I_s * (\exp(V/V_T))$ where $V_T = 25mV$, $I_s = 100nA$, and V is the drop across the diode. (2m)



Lets assume that potentiometer is in setting R21 , R22 as shown in the figure

From the positive feedback, $V_i = V_{out}/(3+2x)$

R1 also sees the voltage of V_i across it due to virtual short

Now a current of $V_i/R1$ flows through negative feedback loop

Let $3+2x=k$

$I_{feedback} = V_i/R1 = V_{out}/(3+2x)/R1 = V_{out}/(kR1)$

Then voltage drop across diode $V = V_{out} - (R21+R1)(I_{feedback})$

$$V = V_{out} - \frac{(R21 + R1)V_{out}}{k * R1}$$

$$V = V_{out} - \left(\frac{R21}{kR1} + \frac{1}{k} \right) V_{out}$$

$$V = V_{out} \left(1 - \frac{R21}{kR1} - \frac{1}{k} \right)$$

Let $R2/R1=q$, $q > 2x + 2$

Since the circuit is symmetrical we analyse it for maximum case at V_{outmax} We can now find the current through Forward biased diode and Current through R22 neglecting I through reverse biased diode.

So $I_{feedback} = I_{R22} + I_D$

Voltage across diode= voltage across R22= $V = V_{outmax} \left(1 - \frac{R21}{kR1} - \frac{1}{k} \right)$

$$I_{R22} = \frac{V}{R22}$$

$$I_D = I_s \exp\left(\frac{V}{V_t}\right)$$

$$I_{R22} + I_D = \frac{V_{outmax}}{k * R1}$$

$$\frac{V}{R22} + I_s \exp\left(\frac{V}{V_t}\right) = \frac{V_{outmax}}{k * R1}$$

$$\frac{V_{outmax} \left(1 - \frac{R21}{kR1} - \frac{1}{k} \right)}{R22} + I_s \exp\left(\frac{V_{outmax} \left(1 - \frac{R21}{kR1} - \frac{1}{k} \right)}{V_t}\right) = \frac{V_{outmax}}{k * R1}$$

$$\frac{V_{outmax} \left(1 - \frac{R21}{kR1} - \frac{1}{k} \right)}{qR1 - R21} + I_s \exp\left(\frac{V_{outmax} \left(1 - \frac{R21}{kR1} - \frac{1}{k} \right)}{V_t}\right) = \frac{V_{outmax}}{k * R1}$$

(1.5m)

The only parameter un known in the above non linear equation in R21 , substitute rest of the values.

RHS turns out to be a constant, then sweep the R21 parameter in the range to achieve the equality.

Also a good place to start the sweep is $r21=R1*(2x+2)$

Value of R22,R21 - (0.5m)

Here is a [desmos link](#) plotting these curves , substitute the values of your rollnumber , R1 , q that you have assumed to evaluate R21 and R22

<https://www.desmos.com/calculator/kwrbk42cdw>