

AP Physics 1

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Unit 1 - Kinematics

Kinematics is the study of motion without considering the forces that cause it. It focuses on describing motion using quantities like displacement, velocity, and acceleration.

1.1 Scalars and Vectors

- **Scalar:** A quantity with magnitude only (e.g., speed, distance, mass).
- **Vector:** A quantity with both magnitude and direction (e.g., velocity, displacement, acceleration, force).
- **Component Vectors:** If a vector is at an angle use trigonometric functions to get the x and y components. Remember to use the correct angle and appropriate Trig function. e.g.

$$\sin(\theta) = \frac{O}{H} \Rightarrow A_x = A \sin(\theta).$$

1.2 Distance, and Speed

- **Distance:** Distance is how far something moves and it includes the path travelled.
- **Speed:** $\frac{\text{distance}}{\text{time}}$

1.3 Displacement, Velocity, and Acceleration

| Quantity | Description | Equation |
|------------------------|--|--|
| Displacement | The straight-line distance from where the object started to where it ended. The change in position of an object. | $\Delta \vec{x} = \vec{x}_f - \vec{x}_i$ |
| Average Velocity | The rate of change of displacement over a time interval. | $\vec{v}_{\text{avg}} = \frac{\Delta \vec{x}}{\Delta t}$ |
| Instantaneous Velocity | The velocity of an object at a specific moment in time. | $\vec{v} = \frac{d\vec{x}}{dt}$ |
| Average Acceleration | The rate of change of velocity over a time interval. | $\vec{a}_{\text{avg}} = \frac{\Delta \vec{v}}{\Delta t}$ |

| Quantity | Description | Equation |
|----------------------------|---|---------------------------------|
| Instantaneous Acceleration | The acceleration of an object at a specific moment in time. | $\vec{a} = \frac{d\vec{v}}{dt}$ |

1.4 Equations of Motion (UAM - Uniformly Accelerated Motion)

These equations apply when acceleration is constant.

| *aa | Description | Equation |
|--|---|--------------------------------------|
| Velocity as a function of time | Relates final velocity to initial velocity, acceleration, and time. | $v_f = v_i + at$ |
| Displacement as a function of time | Relates displacement to initial velocity, acceleration, and time. | $\Delta x = v_i t + \frac{1}{2}at^2$ |
| Velocity as a function of displacement | Relates final velocity to initial velocity, acceleration, and displacement. | $v_f^2 = v_i^2 + 2a\Delta x$ |
| Displacement as a function of average velocity | Relates displacement to average velocity and time. | $\Delta x = \frac{1}{2}(v_i + v_f)t$ |

1.5 Graphical Analysis of Motion

| Graph | Slope Represents | Area Represents | Key Observations |
|-----------------------|------------------|--------------------|--|
| Position vs. Time | Velocity | - | Steeper slope = higher velocity, Zero slope = object at rest. |
| Velocity vs. Time | Acceleration | Displacement | Steeper slope = higher acceleration, Zero slope = constant velocity. |
| Acceleration vs. Time | - | Change in velocity | Area under the curve = Δv . |

1.6 Free Fall

- Acceleration due to gravity (g): $g = 9.81 \text{ m/s}^2$ (downward direction is negative).
- In free fall, the only force acting on the object is gravity (ignoring air resistance).
- Equations of motion apply with $a = -g$.

1.7 Projectile Motion

Projectile motion is the motion of an object launched into the air, subject only to gravity.

Key Points:

- The horizontal and vertical motions are independent.

- Horizontal motion: Constant velocity ($a_x = 0$).
- Vertical motion: Constant acceleration ($a_y = -g$).

Equations:

Horizontal displacement: $\Delta x = v_{x0}t$

| Quantity | Equation |
|-------------------------|---|
| Horizontal displacement | $\Delta x = v_{x0}t$ |
| Vertical displacement | $\Delta y = v_{y0}t - \frac{1}{2}gt^2$ |
| Time of flight | $t = \frac{2v_{y0}}{g}$ (for symmetric projectile motion) |

1.8 Relative Motion

- The motion of an object as observed from a different frame of reference
- Relative velocity: $\vec{v}_{A \text{ relative to } B} = \vec{v}_A - \vec{v}_B$

Unit 2 - Force and translational dynamics

Dynamics is the study of forces and how they affect the motion of objects. It builds on the concepts of kinematics by introducing the causes of motion.

2.1 Newton's Laws of Motion

| Law | Description | Equation/Key Points |
|------------------------------------|---|--|
| First Law (Inertia) | An object at rest stays at rest, and an object in motion stays in motion unless acted upon by a net external force. | $\sum \vec{F} = 0 \Rightarrow \vec{a} = 0$ |
| Second Law | The acceleration of an object is directly proportional to the net force and inversely proportional to its mass. | $\sum \vec{F} = m\vec{a}$ |
| Third Law (Action-Reaction) | For every action, there is an equal and opposite reaction. | $\vec{F}_{12} = -\vec{F}_{21}$ |

2.2 Types of Forces

| Force | Description | Equation/Key Points |
|----------------------------|--|--|
| Gravitational Force | The force exerted by Earth (or any massive object) on another object. | $\vec{F}_g = m\vec{g}$ |
| Normal Force | The force exerted by a surface to support an object. It acts perpendicular to the surface. | \vec{F}_N is perpendicular to the surface. |

| Force | Description | Equation/Key Points |
|-------------------------|---|---|
| Frictional Force | The force that opposes motion between two surfaces in contact. | - Static friction: $F_{f,\text{static}} \leq \mu_s F_N$ - Kinetic friction: $F_{f,\text{kinetic}} = \mu_k F_N$ |
| Tension | The force exerted by a string, rope, or cable. | \vec{T} acts along the direction of the string. |
| Applied Force | A force applied to an object by an external agent (e.g., pushing or pulling). | \vec{F}_{applied} |

2.3 Free Body Diagrams

- A diagram showing all the forces acting on an object.
- Steps to Draw:
 1. Identify the object of interest.
 2. Draw all forces acting on the object as vectors.
 3. Label each force (e.g., \vec{F}_g , \vec{F}_N , \vec{F}_f).
 4. Break forces into components if necessary (e.g., on an incline).

2.4 Inclined Planes

Forces on an object on an inclined plane can be broken into components parallel and perpendicular to the surface.

| Force Component | Description | Equation |
|---------------------------------|---|------------------------------------|
| Parallel to Incline | The component of gravity acting down the incline. | $F_{g,\parallel} = mg \sin \theta$ |
| Perpendicular to Incline | The component of gravity acting perpendicular to the incline. | $F_{g,\perp} = mg \cos \theta$ |

2.5 Friction

Friction opposes motion and depends on the normal force and the coefficient of friction.

| Type of Friction | Description | Equation |
|-------------------------|---|--------------------------------------|
| Static Friction | Prevents an object from moving when a force is applied. | $F_{f,\text{static}} \leq \mu_s F_N$ |
| Kinetic Friction | Acts on an object in motion. | $F_{f,\text{kinetic}} = \mu_k F_N$ |

2.6 Centripetal Force

The net force directed toward the center of a circular path that causes circular motion.

| Concept | Description | Equation |
|---------------------------------|--|-------------------------------------|
| Centripetal Force | Required for circular motion. | $F_c = \frac{mv^2}{r} = mr\omega^2$ |
| Centripetal Acceleration | The acceleration directed toward the center of the circle. | $a_c = \frac{v^2}{r} = r\omega^2$ |

2.7 Translational Equilibrium

- An object is in translational equilibrium when the net force acting on it is zero.
- **Condition:** $\sum \vec{F} = 0$
- **Implications:** The object is either at rest or moving with constant velocity.

2.8 Action-Reaction Pairs

- Forces always occur in pairs. For every action, there is an equal and opposite reaction.
- **Example:** When you push a wall, the wall pushes back on you with an equal force.

2.9 Applications of Newton's Laws

- **Atwood's Machine:** A system of two masses connected by a string over a pulley.
- **Pulleys:** Used to change the direction of a force.
- **Elevators:** Analyze forces when an elevator accelerates upward or downward.

Unit 3 - Work, energy, and, power

Work, energy, and power are fundamental concepts in physics that describe how forces transfer energy to objects and how that energy is used or transformed.

3.1 Work

Work is done when a force causes a displacement of an object.

| Concept | Description | Equation/Key Points |
|----------------------|--|--|
| Work | The product of force and displacement in the direction of the force. | $W = F \cdot d \cdot \cos \theta$ |
| Units | Work is measured in joules (J). | $1 \text{ J} = 1 \text{ N} \cdot \text{m}$ |
| Positive Work | Work is positive when force and displacement are in the same direction. | $\theta < 90^\circ$ |
| Negative Work | Work is negative when force and displacement are in opposite directions. | $\theta > 90^\circ$ |
| Zero Work | Work is zero when force and displacement are perpendicular. | $\theta = 90^\circ$ |

3.2 Kinetic Energy

Kinetic energy is the energy of motion.

| Concept | Description | Equation/Key Points |
|----------------------------|---|--|
| Kinetic Energy | The energy an object possesses due to its motion. | $KE = \frac{1}{2}mv^2$ |
| Work-Energy Theorem | The net work done on an object equals its change in kinetic energy. | $W_{\text{net}} = \Delta KE = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$ |

3.3 Potential Energy

Potential energy is the energy stored due to an object's position or configuration.

| Concept | Description | Equation/Key Points |
|---------------------------------------|---|---|
| Gravitational Potential Energy | Energy due to an object's height above a reference point. | $PE_g = mgh$ |
| Elastic Potential Energy | Energy stored in a compressed or stretched spring. | $PE_{\text{elastic}} = \frac{1}{2}kx^2$ |
| Conservation of Energy | Total mechanical energy (KE + PE) remains constant in the absence of non-conservative forces. | $KE_i + PE_i = KE_f + PE_f$ |

3.4 Power

Power is the rate at which work is done or energy is transferred.

| Concept | Description | Equation/Key Points |
|----------------------------|-------------------------------------|-------------------------------|
| Power | The rate of doing work. | $P = \frac{W}{t}$ |
| Units | Power is measured in watts (W). | $1 \text{ W} = 1 \text{ J/s}$ |
| Instantaneous Power | Power at a specific moment in time. | $P = F \cdot v$ |

3.5 Conservation of Energy

Energy cannot be created or destroyed, only transformed from one form to another.

| Concept | Description | Equation/Key Points |
|--------------------------------|--|--|
| Mechanical Energy | The sum of kinetic and potential energy. | $E_{\text{mech}} = KE + PE$ |
| Non-Conservative Forces | Forces like friction that cause energy to be lost as heat. | $W_{\text{non-conservative}} = \Delta E_{\text{mech}}$ |

3.6 Work Done by Variable Forces

When the force is not constant, work is calculated using integration.

| Concept | Description | Equation/Key Points |
|-------------------------------|--|--------------------------------|
| Work by Variable Force | Work is the area under the force vs. displacement graph. | $W = \int_{x_i}^{x_f} F(x) dx$ |
| Spring Force | The force exerted by a spring is proportional to its displacement. | $F = -kx$ |

3.7 Applications of Work, Energy, and Power

| Application | Description | Equation/Key Points |
|-----------------------------|---|---|
| Pulleys and Inclines | Systems involving pulleys or inclined planes can be analyzed using work and energy. | $W = F \cdot d$ |
| Efficiency | The ratio of useful work output to total work input. | $\text{Efficiency} = \frac{W_{\text{useful}}}{W_{\text{input}}} \times 100\%$ |

Unit 4 - Linear momentum

Linear momentum is a measure of an object's motion and is central to understanding collisions, explosions, and other interactions.

4.1 Momentum and Impulse

Momentum is a vector quantity that depends on an object's mass and velocity.

| Concept | Description | Equation/Key Points |
|---------------------------------|---|--|
| Momentum | The product of an object's mass and velocity. | $\vec{p} = m\vec{v}$ |
| Impulse | The change in momentum caused by a force acting over a time interval. | $\vec{J} = \Delta\vec{p} = \vec{F} \cdot \Delta t$ |
| Impulse-Momentum Theorem | The impulse equals the change in momentum. | $\vec{J} = \vec{p}_f - \vec{p}_i$ |

4.2 Conservation of Momentum

The total momentum of a system remains constant if no external forces act on it.

| Concept | Description | Equation/Key Points |
|---------------------------------|---|---|
| Conservation of Momentum | The total momentum before an interaction equals the total momentum after. | $\vec{p}_{\text{total, initial}} = \vec{p}_{\text{total, final}}$ |

| Concept | Description | Equation/Key Points |
|------------------------|--|--------------------------------------|
| Isolated System | A system with no external forces acting on it. | $\sum \vec{F}_{\text{external}} = 0$ |

4.3 Collisions

Collisions are interactions where objects exert forces on each other for a short time.

| Type of Collision | Description | Equation/Key Points |
|--------------------------------------|---|--|
| Elastic Collision | Kinetic energy and momentum are conserved. | $KE_{\text{initial}} = KE_{\text{final}}$ $\vec{p}_{\text{initial}} = \vec{p}_{\text{final}}$ |
| Inelastic Collision | Momentum is conserved, but kinetic energy is not. | $\vec{p}_{\text{initial}} = \vec{p}_{\text{final}}$ |
| Perfectly Inelastic Collision | Objects stick together after the collision. | $m_1 \vec{v}_1 + m_2 \vec{v}_2 = (m_1 + m_2) \vec{v}_f$ |

4.4 Center of Mass

The center of mass is the point where the mass of a system is concentrated.

| Concept | Description | Equation/Key Points |
|-----------------------------|---|--|
| Center of Mass (COM) | The average position of all the mass in a system. | $\vec{r}_{\text{COM}} = \frac{\sum m_i \vec{r}_i}{\sum m_i}$ |
| Motion of COM | The COM moves as if all the mass were concentrated at that point. | $\vec{v}_{\text{COM}} = \frac{\sum m_i \vec{v}_i}{\sum m_i}$ |

4.5 Recoil and Propulsion

Recoil and propulsion are applications of momentum conservation.

| Concept | Description | Equation/Key Points |
|--------------------------|---|---|
| Recoil | The backward motion of an object after ejecting part of its mass. | $m_1 \vec{v}_1 + m_2 \vec{v}_2 = 0$ |
| Rocket Propulsion | Rockets gain momentum by expelling exhaust gases. | $\Delta \vec{p}_{\text{rocket}} = -\Delta \vec{p}_{\text{exhaust}}$ |

4.6 Applications of Momentum

| Application | Description | Equation/Key Points |
|--------------------|--|---|
| Car Crashes | Seatbelts and airbags increase the time of impact, reducing the force on passengers. | $\vec{F} = \frac{\Delta \vec{p}}{\Delta t}$ |
| Sports | Momentum is key in analyzing collisions in sports like football or hockey. | $\vec{p} = m\vec{v}$ |

Unit 5 - Torque and rotational dynamics

Rotational dynamics deals with the motion of objects that rotate about an axis, introducing concepts like torque, angular momentum, and rotational inertia.

5.1 Torque

Torque is the rotational equivalent of force and causes objects to rotate.

| Concept | Description | Equation/Key Points |
|------------------|---|---|
| Torque | The product of force and the lever arm (distance from the pivot point). | $\tau = rF \sin \theta$ |
| Units | Torque is measured in newton-meters (N·m). | 1 N · m |
| Direction | Torque is a vector quantity with direction determined by the right-hand rule. | Clockwise: negative Counterclockwise: positive |
| Lever Arm | The perpendicular distance from the pivot point to the line of action of the force. | $r_{\perp} = r \sin \theta$ |

5.2 Rotational Inertia (Moment of Inertia)

Rotational inertia is the resistance of an object to changes in its rotational motion.

| Concept | Description | Equation/Key Points |
|--------------------------|--|----------------------|
| Moment of Inertia | Depends on the mass distribution relative to the axis of rotation. | $I = \sum m_i r_i^2$ |
| Common Shapes | <ul style="list-style-type: none"> - Point mass: $I = mr^2$ - Solid sphere: $I = \frac{2}{5}mr^2$ - Rod (center): $I = \frac{1}{12}mL^2$ | |

5.3 Rotational Kinematics

Rotational kinematics describes the motion of rotating objects without considering the forces involved.

| Concept | Description | Equation/Key Points |
|-----------------------------|---|--|
| Angular Displacement | The angle through which an object rotates. | $\Delta\theta = \theta_f - \theta_i$ |
| Angular Velocity | The rate of change of angular displacement. | $\omega = \frac{\Delta\theta}{\Delta t}$ |
| Angular Acceleration | The rate of change of angular velocity. | $\alpha = \frac{\Delta\omega}{\Delta t}$ |
| Equations of Motion | <ul style="list-style-type: none"> - $\omega_f = \omega_i + \alpha t$ - $\Delta\theta = \omega_i t + \frac{1}{2}\alpha t^2$ - $\omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta$ | |

5.4 Rotational Dynamics

Rotational dynamics relates torque to angular acceleration.

| Concept | Description | Equation/Key Points |
|---|---|--|
| Newton's Second Law for Rotation | The net torque equals the moment of inertia times angular acceleration. | $\sum \tau = I\alpha$ |
| Rotational Kinetic Energy | The energy due to rotational motion. | $KE_{\text{rot}} = \frac{1}{2}I\omega^2$ |

5.5 Angular Momentum

Angular momentum is the rotational equivalent of linear momentum.

| Concept | Description | Equation/Key Points |
|---|---|---|
| Angular Momentum | The product of moment of inertia and angular velocity. | $\vec{L} = I\vec{\omega}$ |
| Conservation of Angular Momentum | The total angular momentum of a system remains constant if no external torque acts on it. | $\vec{L}_{\text{initial}} = \vec{L}_{\text{final}}$ |

5.6 Rolling Motion

Rolling motion combines translational and rotational motion.

| Concept | Description | Equation/Key Points |
|---|---|--|
| Condition for Rolling Without Slipping | The point of contact with the ground has zero instantaneous velocity. | $v = r\omega$ |
| Total Kinetic Energy | The sum of translational and rotational kinetic energy. | $KE_{\text{total}} = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$ |

5.7 Applications of Rotational Dynamics

| Application | Description | Equation/Key Points |
|----------------------|--|---|
| Pulleys | Rotational motion is used to analyze systems with pulleys. | $\tau = rF$ |
| Gyroscopes | Devices that use angular momentum to maintain orientation. | $\vec{L} = I\vec{\omega}$ |
| Spinning Tops | Stability is due to conservation of angular momentum. | $\vec{L}_{\text{initial}} = \vec{L}_{\text{final}}$ |

Unit 6 - Energy and momentum of rotating systems

This unit explores the interplay between energy, momentum, and rotational motion, focusing on systems where rotation plays a key role.

6.1 Rotational Kinetic Energy

Rotational kinetic energy is the energy associated with an object's rotation.

| Concept | Description | Equation/Key Points |
|----------------------------------|---|--|
| Rotational Kinetic Energy | The energy due to rotational motion. | $KE_{\text{rot}} = \frac{1}{2}I\omega^2$ |
| Total Kinetic Energy | The sum of translational and rotational kinetic energy. | $KE_{\text{total}} = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$ |

6.2 Angular Momentum

Angular momentum is a conserved quantity in rotational systems.

| Concept | Description | Equation/Key Points |
|---|---|---|
| Angular Momentum | The product of moment of inertia and angular velocity. | $\vec{L} = I\vec{\omega}$ |
| Conservation of Angular Momentum | The total angular momentum of a system remains constant if no external torque acts on it. | $\vec{L}_{\text{initial}} = \vec{L}_{\text{final}}$ |

6.3 Rolling Motion and Energy

Rolling motion combines translational and rotational motion, and energy is shared between the two.

| Concept | Description | Equation/Key Points |
|---|---|---------------------|
| Condition for Rolling Without Slipping | The point of contact with the ground has zero instantaneous velocity. | $v = r\omega$ |

| Concept | Description | Equation/Key Points |
|----------------------------|--|--|
| Energy Distribution | Energy is divided between translational and rotational kinetic energy. | $KE_{\text{total}} = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$ |

6.4 Torque and Angular Acceleration

Torque causes angular acceleration in rotating systems.

| Concept | Description | Equation/Key Points |
|---|---|--|
| Newton's Second Law for Rotation | The net torque equals the moment of inertia times angular acceleration. | $\sum \tau = I\alpha$ |
| Work and Power in Rotation | Work done by torque and power in rotational systems. | $W = \tau\Delta\theta$ $P = \tau\omega$ |

6.5 Gyroscopic Motion

Gyroscopes exhibit unique behavior due to conservation of angular momentum.

| Concept | Description | Equation/Key Points |
|------------------------------|--|---------------------------|
| Gyroscopic Precession | The axis of rotation of a gyroscope moves in a circular path when a torque is applied. | $\Omega = \frac{\tau}{L}$ |
| Stability | Gyroscopes maintain orientation due to conservation of angular momentum. | $\vec{L} = I\vec{\omega}$ |

6.6 Applications of Rotational Energy and Momentum

| Application | Description | Equation/Key Points |
|-------------------------|--|--|
| Flywheels | Store rotational energy for use in mechanical systems. | $KE_{\text{rot}} = \frac{1}{2}I\omega^2$ |
| Figure Skaters | Skaters change their moment of inertia to control spin rate. | $I_1\omega_1 = I_2\omega_2$ |
| Planetary Orbits | Angular momentum plays a key role in the motion of planets and satellites. | $\vec{L} = m\vec{r} \times \vec{v}$ |

Unit 7 - Oscillations

Oscillations are repetitive motions around an equilibrium position. This unit covers simple harmonic motion, pendulums, and damped/driven oscillations.

7.1 Simple Harmonic Motion (SHM)

Simple harmonic motion is a type of periodic motion where the restoring force is directly proportional to the displacement.

| Concept | Description | Equation/Key Points |
|--------------------------|---|----------------------------------|
| Displacement | The position of the object relative to equilibrium. | $x(t) = A \cos(\omega t + \phi)$ |
| Amplitude | The maximum displacement from equilibrium. | A |
| Angular Frequency | The rate of oscillation in radians per second. | $\omega = \sqrt{\frac{k}{m}}$ |
| Period | The time for one complete oscillation. | $T = \frac{2\pi}{\omega}$ |
| Frequency | The number of oscillations per unit time. | $f = \frac{1}{T}$ |
| Phase Constant | Determines the initial position of the oscillator. | ϕ |

7.2 Energy in Simple Harmonic Motion

Energy in SHM is conserved and oscillates between kinetic and potential forms.

| Concept | Description | Equation/Key Points |
|--------------------------------|---|--------------------------------------|
| Potential Energy | Energy stored due to displacement from equilibrium. | $PE = \frac{1}{2}kx^2$ |
| Kinetic Energy | Energy due to motion. | $KE = \frac{1}{2}mv^2$ |
| Total Mechanical Energy | The sum of kinetic and potential energy. | $E_{\text{total}} = \frac{1}{2}kA^2$ |

7.3 Pendulums

Pendulums exhibit simple harmonic motion for small angles.

| Concept | Description | Equation/Key Points |
|---------------------------|---|-----------------------------------|
| Simple Pendulum | A mass swinging on a string. | $T = 2\pi\sqrt{\frac{L}{g}}$ |
| Physical Pendulum | A rigid body swinging about a pivot. | $T = 2\pi\sqrt{\frac{I}{mgh}}$ |
| Torsional Pendulum | A disk suspended by a wire that twists. | $T = 2\pi\sqrt{\frac{I}{\kappa}}$ |

7.4 Damped Oscillations

Damped oscillations occur when a resistive force (e.g., friction) reduces the amplitude over time.

| Concept | Description | Equation/Key Points |
|--------------------------|---|--|
| Damping Force | A force that opposes motion and reduces amplitude. | $F_d = -bv$ |
| Underdamped | Oscillations gradually decrease in amplitude. | $x(t) = Ae^{-\frac{b}{2m}t} \cos(\omega_d t + \phi)$ |
| Overdamped | The system returns to equilibrium without oscillating. | $x(t) = C_1 e^{-\gamma_1 t} + C_2 e^{-\gamma_2 t}$ |
| Critically Damped | The system returns to equilibrium as quickly as possible without oscillating. | $x(t) = (C_1 + C_2 t) e^{-\gamma t}$ |

7.5 Driven Oscillations and Resonance

Driven oscillations occur when an external force is applied to the system.

| Concept | Description | Equation/Key Points |
|-------------------------------|--|------------------------------------|
| Driving Force | An external force that sustains oscillations. | $F(t) = F_0 \cos(\omega_d t)$ |
| Resonance | Maximum amplitude occurs when the driving frequency matches the natural frequency. | $\omega_d = \omega_0$ |
| Amplitude at Resonance | The amplitude is maximized at resonance. | $A_{\max} = \frac{F_0}{b\omega_0}$ |

7.6 Applications of Oscillations

| Application | Description | Equation/Key Points |
|----------------------------|---|---|
| Clocks | Pendulums are used to regulate timekeeping. | $T = 2\pi \sqrt{\frac{L}{g}}$ |
| Musical Instruments | Strings and air columns oscillate to produce sound. | $f_n = \frac{n}{2L} \sqrt{\frac{T}{\mu}}$ |
| Seismometers | Measure ground motion during earthquakes. | $x(t) = A \cos(\omega t + \phi)$ |

Unit 8 - Fluids

Fluids are substances that flow, including liquids and gases. This unit covers fluid statics, dynamics, and the principles governing fluid behavior.

8.1 Fluid Statics

Fluid statics deals with fluids at rest and the forces exerted by them.

| Concept | Description | Equation/Key Points |
|----------------|--------------------------------------|----------------------|
| Density | Mass per unit volume of a substance. | $\rho = \frac{m}{V}$ |

| Concept | Description | Equation/Key Points |
|-----------------------------|--|--|
| Pressure | Force exerted per unit area. | $P = \frac{F}{A}$ |
| Hydrostatic Pressure | Pressure due to the weight of a fluid column. | $P = P_0 + \rho gh$ |
| Pascal's Principle | Pressure applied to a confined fluid is transmitted equally in all directions. | $\Delta P = \frac{F_1}{A_1} = \frac{F_2}{A_2}$ |
| Buoyant Force | The upward force exerted by a fluid on an immersed object. | $F_b = \rho_{\text{fluid}} V_{\text{displaced}} g$ |

8.2 Fluid Dynamics

Fluid dynamics deals with fluids in motion and the forces acting on them.

| Concept | Description | Equation/Key Points |
|-----------------------------|---|---|
| Continuity Equation | The product of cross-sectional area and flow speed is constant for an incompressible fluid. | $A_1 v_1 = A_2 v_2$ |
| Bernoulli's Equation | Relates pressure, speed, and height in a fluid. | $P_1 + \frac{1}{2} \rho v_1^2 + \rho gh_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho gh_2$ |
| Viscosity | A measure of a fluid's resistance to flow. | $\eta = \frac{F \cdot d}{A \cdot v}$ |
| Laminar Flow | Smooth, orderly flow of fluid layers. | - |
| Turbulent Flow | Chaotic, irregular flow of fluid. | - |

8.3 Applications of Fluid Principles

| Application | Description | Equation/Key Points |
|--------------------------|--|-------------------------------------|
| Hydraulic Systems | Use Pascal's Principle to amplify force. | $\frac{F_1}{A_1} = \frac{F_2}{A_2}$ |
| Aerodynamics | Study of air flow around objects, such as airplane wings. | Bernoulli's Equation |
| Blood Flow | Blood circulation in the human body follows fluid dynamics principles. | Continuity Equation |

8.4 Archimedes' Principle

Archimedes' Principle explains buoyancy and floating objects.

| Concept | Description | Equation/Key Points |
|----------------------|--|--|
| Buoyant Force | The upward force on an object immersed in a fluid. | $F_b = \rho_{\text{fluid}} V_{\text{displaced}} g$ |

| Concept | Description | Equation/Key Points |
|---------------------------|---|--|
| Floating Objects | An object floats when the buoyant force equals its weight. | $F_b = mg$ |
| Density Comparison | An object floats if its density is less than the fluid's density. | $\rho_{\text{object}} < \rho_{\text{fluid}}$ |

8.5 Surface Tension and Capillary Action

Surface tension and capillary action are phenomena caused by cohesive forces in liquids.

| Concept | Description | Equation/Key Points |
|-------------------------|---|--|
| Surface Tension | The energy required to increase the surface area of a liquid. | $\gamma = \frac{F}{L}$ |
| Capillary Action | The ability of a liquid to flow in narrow spaces without external forces. | $h = \frac{2\gamma \cos \theta}{\rho g r}$ |

8.6 Practice Problems

- Problem 1:** A block of wood with a volume of 0.01 m^3 is fully submerged in water. Calculate the buoyant force acting on the block. (Density of water = 1000 kg/m^3 , $g = 9.8 \text{ m/s}^2$)
 - Solution:** $F_b = \rho_{\text{fluid}} V_{\text{displaced}} g = 1000 \cdot 0.01 \cdot 9.8 = 98 \text{ N}$.
- Problem 2:** Water flows through a pipe with a cross-sectional area of 0.02 m^2 at a speed of 3 m/s . If the pipe narrows to 0.01 m^2 , what is the new speed of the water?
 - Solution:** $A_1 v_1 = A_2 v_2$
 $0.02 \cdot 3 = 0.01 \cdot v_2$
 $v_2 = 6 \text{ m/s}$.
- Problem 3:** A fluid with a density of 800 kg/m^3 flows through a horizontal pipe. At one point, the pressure is 120 kPa and the speed is 2 m/s . If the pipe narrows and the speed increases to 4 m/s , what is the new pressure? (Use Bernoulli's Equation)
 - Solution:** $P_1 + \frac{1}{2} \rho v_1^2 = P_2 + \frac{1}{2} \rho v_2^2$
 $120,000 + \frac{1}{2} \cdot 800 \cdot 2^2 = P_2 + \frac{1}{2} \cdot 800 \cdot 4^2$
 $120,000 + 1600 = P_2 + 6400$
 $P_2 = 115,200 \text{ Pa}$.

Appendix

Resources

- [College Board Course Guide](#)
- [Khan Academy](#)
- [Textbook](#)

- [Flipping Physics](#)