

LAB 4 - IMPLEMENTATION OF SET ADT USING BINARY SEARCH TREES

Due Date: Lab sessions March 13 – 24, 2023

Assessment: 5% of the total course mark.

DESCRIPTION:

In this lab you will implement the Set abstract data type using binary search trees. We will consider sets of integers where each integer will be stored in a tree node. Therefore, the number of nodes in the binary search tree must be equal to the size of the set.

You will have to write a C++ class `BSTSet` for this purpose. To implement the tree nodes you must use the C++ class `TNode` provided in this lab. Additionally, you will need to implement C++ class `MyStack` to perform non-recursive tree traversal of a `BSTSet`. You are *not permitted* to use `std::set` and `std::stack`. Please compute the asymptotic run time and space complexity of all methods and be ready to present them to the TA with explanations at your demo.

DEFINITIONS:

- A *set* is an unordered collection of elements with no repetition. Examples are the set of real numbers, the set of integer numbers or the set consisting of numbers 1, 2, 30.
- For this lab we will only be considering representing finite sets consisting of elements which are integers. Examples: $\{0, 34, 78, 1000\}$, $\{4, 5, 890, 65535\}$, $\{0, 1, 2, \dots, 65534, 65535\}$, $\{\}$ are all valid sets.
- The *union* of two sets, say A and B , is written as $A \cup B$ and is the set which contains all of the elements in either A or B or both. Example: If $A = \{3, 8, 14, 15\}$ and $B = \{2, 8, 9, 15, 100\}$, then $A \cup B = \{2, 3, 8, 9, 14, 15, 100\}$ (notice that there are no repeated elements in a set).
- The *intersection* of two sets A and B is written as $A \cap B$ and is the set which contains the elements that are common to A and B . Examples: If $A = \{3, 8, 14, 15\}$ and $B = \{2, 8, 9, 15, 100\}$, then $A \cap B = \{8, 15\}$. If $A = \{17, 20, 38\}$ and $B = \{200\}$, then $A \cap B = \{\}$, which is termed the *empty set*.
- The *difference* of two sets A and B is written as $A - B$ and is the set which contains the elements that are in A but not in B . Examples: If $A = \{3, 8, 12, 9\}$ and $B = \{9, 12, 15, 100\}$, then $A - B = \{3, 8\}$ and $B - A = \{15, 100\}$.

SPECIFICATIONS:

- You must use the C++ class `TNode` given below, to implement the tree nodes.

```
class TNode{
public:
    int element;
    TNode* left;
```

```
TNode* right;

TNode(int i, TNode* l, TNode* r)
{ element = i; left = l; right = r; }
};
```

- Class `BSTSet` must contain **only** one **private** field named `root`, of type `TNode*`, which is a pointer to the root of the tree. No other fields are allowed. When the set is empty you should have `root==NULL`.
- Class `BSTSet` must contain at least the following **public** constructors and destructor:
 - `BSTSet()`: initializes the `BSTSet` object to represent the empty set (an empty tree).
 - `BSTSet(const std::vector<int>& input)`: initializes the `BSTSet` object to represent the set containing all elements in vector `input`, without repetitions. For example, if the vector is: 5, 7, 4, 5, then the corresponding set is {5, 7, 4}. The vector `input` can be empty.
 - `~BSTSet()`: frees the memory allocated for the `BSTSet` object.
- Class `BSTSet` must contain the following **public** methods:
 - 1) `bool isIn(int v)`: returns `true` if integer `v` is an element of `this BSTSet`. It returns `false` otherwise.
 - 2) `void add(int v)`: adds `v` to `this BSTSet` if `v` was not already an element of `this BSTSet`. It does nothing otherwise.
 - 3) `bool remove(int v)`: removes `v` from `this BSTSet` if `v` was an element of `this BSTSet` and returns `true`. Returns `false` if `v` was not an element of `this BSTSet`.
 - 4) `void Union(const BSTSet& s)`: gets the union of `this BSTSet` and `s`. This method modifies `this BSTSet`, but it does not modify the input set `s`.
 - 5) `void intersection(const BSTSet& s)`: gets the intersection of `this BSTSet` and `s`. This method modifies `this BSTSet`, but it does not modify the input set `s`.
 - 6) `void difference(const BSTSet& s)`: gets the difference of `this BSTSet` and `s`. This method modifies `this BSTSet`, but it does not modify the input set `s`.
 - 7) `int size()`: returns the number of elements in `this BSTSet`.
 - 8) `int height()`: returns the height of `this BSTSet`. Height of the empty set is `-1`.
 - 9) `void printBSTSet()`: outputs the elements of `this BSTSet` to the console, in increasing order.
`void printBSTSet(TNode t)`: private helper function, outputs to the console the elements stored in the subtree rooted in `t`, in increasing order.For the two printing methods specified above you **must** use the following code:

```
void BSTSet::printBSTSet(){
    if (root == NULL)
        std::cout << "";
    else {
        printBSTSet(root);
    }
}

void BSTSet::printBSTSet(TNode* t){
    if (t != NULL) {
        printBSTSet(t->left);
        std::cout << t->element << ",";
        printBSTSet(t->right);
    }
}
```

- 10) void printNonRec(): prints the integers in **this** BSTSet in increasing order. This method is **nonrecursive** and uses a stack to implement the inorder traversal (use the class **MyStack**). See “Lab4Notes.pdf” for the algorithm.

Note: All print methods listed above, should print an empty string for the empty set, and print each element separated by a comma for the non empty set. For example, “1,2,3,”. Other characters and description words are not allowed.

NOTES:

- Compute the asymptotic run time and space complexity of all methods implemented as a function of the set size. Be prepared to present your derivations to the TA at demo time and provide verbal justification for your analysis.
- You are permitted to implement other **private** methods inside class **BSTSet** as required. However, you are not permitted to modify the class **TNode**. Additionally, class **BSTSet** must contain only one field which is an **TNode*** named **root**.
- You may use the code from the lecture notes on binary search trees and stack, or from the tutorial. However, you may need to adapt the code and provide complete references.
- To get credit for the lab you must demonstrate your code (i.e., classes **BSTSet** and **MyStack**) in front of a TA during your lab session.

SUBMISSION INSTRUCTIONS:

NO REPORT IS NEEDED. Submit the source code for each of the classes **BSTSet** and **MyStack** in a separate text file. Include your student number in the name of each file. For instance, if your student number is 12345 then the files should be named as follows: **BSTSet_12345.h.txt**, **BSTSet_12345.cpp.txt**, etc. Submit the files in the Assignment folder on Avenue by the end of your designated lab session.

BONUS:

A bonus of 1% of the course mark will be awarded if the second constructor creates a set

stored in a tree of **minimum height** and, additionally, methods **Union**, **intersection** and **difference** guarantee that the tree storing the result (in other words, the union, intersection or difference of the two input sets) has **minimum height** as well. You may write additional private methods for this purpose. You need to briefly describe in a comment at the beginning of the code of the method the main idea of your algorithm for each of the above methods and be prepared to justify this verbally to the TA during the demo.