# bayesian-filters-smoothers

None

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# 1. bayesian-filters-smoothers

A unified library for Bayesian filter and smoother algorithms based on the book "Bayesian Filtering and Smoothing" - Simo Sarkka

## Purpose of the Package

- To provide a collection of all the Bayesian Filters and Smoothers in a unified framework
- To be a building block for Bayesian Inference of state-space models
- To provide building blocks for state estimation algorithms
- To provide building blocks for parameter estimation algorithms

#### 1.0.1 Features

- Kalman Filter/Smoother
- Extended Kalman Filter/Smoother
- Unscented Kalman Filter/Smoother
- Gaussian Filter/Smoother
- Particle Filter/Smoother

## 1.0.2 Getting Started

The package can be found on pypi hence you can install it using pip

## Installation

pip install bayesian-filters-smoothers

#### 1.0.3 Documentation

You can check out the full documentation here

#### 1.0.4 Contribution

Contributions are welcome. Notice a bug let us know. Thanks!

#### 1.0.5 Author

• Ninad Kiran Gaikwad, PhD Student, Washington State University

# **2. API**

#### **API Reference**

This page gives an overview of all the Bayesian Filters and Smoothers implemented in the package

- Kalman Filter/Smoother
- Extended Kalman Filter/Smoother
- Unscented Kalman Filter/Smoother
- Gaussian Filter/Smoother
- · Particle Filter/Smoother

*Kalman\_Filter\_Smoother Class:* Kalman Filter/Smoother is the simplest Bayesian Filter/Smoother applied to a linear system with gaussian process/measurement errors

Creates an object to handle Kalman Filtering and Smoothing for Linear Time Invariant (LTI) System

- A ( numpy.array ) LTI system matrix
- B ( numpy.array ) LTI input matrix
- C ( numpy.array ) LTI output matrix
- m\_k ( numpy.array ) State mean vector

**Attributes:** 

- P\_k ( numpy.array ) State covariance matrix
- Q ( numpy.array ) Process error covariance matrix
- R ( numpy.array ) -

Measurement error covariance matrix

```
class Kalman_Filter_Smoother:
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    """Creates an object to handle Kalman Filtering and Smoothing for Linear Time Invariant (LTI) System Attributes: A (numpy.a.
 63
    """Initializes the instance of class Kalman_Filter_Smoother Args: A (numpy.array): LTI system matrix B (numpy.array): LTI in
    """Sets the A array for a linear time-varying (LTV) system Args: A (numpy.array): LTV system matrix """ self.A = A def set_
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    """Sets the B matrix for a linear time-varying (LTV) system Args: B (numpy.array): LTV input matrix """ self.B = B def set_0
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    """Sets the C matrix for a linear time-varying (LTV) system Args: C (numpy.array): LTV output matrix """ self.C = C def set
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    """Sets the Q matrix for the system Args: Q (numpy.array): Process error covariance matrix """ self.Q = Q def set_R(self, R
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    """Sets the R matrix for the system Args: R (numpy.array): Measurement error covariance matrix """ self.R = R def Kalman_Pro
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    """Performs the predict step of the Kalman Filter Args: u_k (numpy.array): Input to the system Returns: m_k_ (numpy.array):
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    """Performs the update step of the Kalman Filter Args: y k (numpy.array): New measurement from the system m k (numpy.array
    """Performs the smoothening step of the Kalman Smoother Args: u_k_list (list of numpy.array): List of inputs to the system
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```

# 2.0.1 Kalman\_Predict(u\_k)

Performs the predict step of the Kalman Filter

 $\bullet \ u\_k \ ( \ \texttt{numpy.array} \ ) \ -$ 

Parameters: Input to the system

• m\_k\_( numpy.array ) - Predicted state mean vector

 $\bullet \ P\_k\_( \ \, \texttt{numpy.array} \ ) \, - \,$ 

Returns:

Predicted state covariance matrix

```
Source code in bayesian-filters-smoothers\bayesian_filters_smoothers\bayesian_filters_smoothers.py
```

```
def Kalman Predict(self, u k):
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    """Performs the predict step of the Kalman Filter Args: u_k (numpy.array): Input to the system Returns: m_k_ (numpy.array):
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```

# 2.0.2 Kalman\_Smoother(u\_k\_list, y\_k\_list)

Performs the smoothening step of the Kalman Smoother

```
• u_k_{list} ( list of numpy.array ) — List of inputs to the system
```

• y\_k\_list ( list of numpy.array ) -

**Parameters:** 

List of measurements from the system

- $\cdot G_k_{list}([list of numpy.array]) List of Kalman Smoother Gain$
- m\_k\_s([list of numpy.array]) List of smoothed state vectors

Returns: • P\_k\_s( list of numpy.array )-

List of smoothed state covarivance matrices

 $Source\ code\ in\ \ \ \texttt{bayesian\_filters\_smoothers\_bayesian\_filters\_smoothers\_bayesian\_filters\_smoothers\_py\ \ }$ 

```
def Kalman_Smoother(self, u_k_list, y_k_list):
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    """Performs the smoothening step of the Kalman Smoother Args: u_k_list (list of numpy.array): List of inputs to the system
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```



# Performs the update step of the Kalman Filter

 $\bullet \ y\_k \ ( \ \texttt{numpy.array} \ ) \ -$ 

New measurement from the system

**Parameters:** 

- m\_k\_( numpy.array ) Predicted state mean vector
- P\_k\_(numpy.array) Predicted state covariance matrix
- $\mathbf{v_k}(\underline{\mathbf{numpy.array}}) Updated measurement error$
- $S_k([numpy.array]) -$

Returns:

Updated measurement covariance matrix

• K\_k( numpy.array ) - Updated Kalman Gain

```
Source code in bayesian-filters-smoothers\bayesian_filters_smoothers\bayesian_filters_smoothers.py
       def Kalman_Update(self, y_k, m_k_, P_k_):
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      """Performs the update step of the Kalman Filter Args: y_k (numpy.array): New measurement from the system m_k_ (numpy.array
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```

Initializes the instance of class Kalman Filter Smoother

2.0.4 \_\_init\_\_(A, B, C, m\_k, P\_k, Q, R)

```
• A ( numpy.array ) – LTI system matrix
```

- B ( numpy.array ) LTI input matrix
- . . . .
- $\cdot$  C ( numpy.array ) LTI output matrix
- $m_k (numpy.array)$  State mean vector

#### **Parameters:**

- P\_k ( numpy.array ) State covariance matrix
- Q (numpy.array) Process error covariance matrix
- R ( numpy.array ) -

Measurement error covariance matrix

```
Source\ code\ in\ |\ \texttt{bayesian\_filters\_smoothers\_bayesian\_filters\_smoothers\_bayesian\_filters\_smoothers.py\ |\ Source\ code\ in\ |\ Source\ code\ code\ in\ |\ Source\ code\ in\ |\ Source\ code\ code\ in\ |\ Source\ code\ co
```

```
def __init__(self, A, B, C, m_k, P_k, Q, R):
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   """Initializes the instance of class Kalman_Filter_Smoother Args: A (numpy.array): LTI system matrix B (numpy.array): LTI in
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```

2.0.5 set\_A(A)

Sets the A array for a linear time-varying (LTV) system

 $\bullet$  A ( numpy.array ) -

Parameters: LTV system matrix

Source code in | bayesian-filters-smoothers\bayesian\_filters\_smoothers.py |

```
def set_A(self, A):

"""Sets the A array for a linear time-varying (LTV) system Args: A (numpy.array): LTV system matrix """ self.A = A

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```

2.0.6 set B(B)

Sets the B matrix for a linear time-varying (LTV) system

 $\bullet \; B \; ( \; \texttt{numpy.array} \; ) \, - \,$ 

Parameters: LTV input matrix

 $Source\ code\ in\ |\ \texttt{bayesian-filters-smoothers} \setminus \texttt{bayesian\_filters\_smoothers.py}|$ 

```
def set_B(self, B):
    """Sets the B matrix for a linear time-varying (LTV) system Args: B (numpy.array): LTV input matrix """ self.B = B
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```

2.0.7 set\_C(C)

Sets the C matrix for a linear time-varying (LTV) system

• C ( numpy.array )-

Parameters: LTV output matrix

Source code in | bayesian-filters-smoothers\bayesian\_filters\_smoothers.py |

```
def set_C(self, C):

"""Sets the C matrix for a linear time-varying (LTV) system Args: C (numpy.array): LTV output matrix """ self.C = C

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```

2.0.8 set Q(Q)

Sets the Q matrix for the system

• Q ( numpy.array ) -

Parameters: Process error covariance matrix

Source code in | bayesian-filters-smoothers\bayesian\_filters\_smoothers\bayesian\_filters\_smoothers.py |

```
def set_Q(self, Q):

"""Sets the Q matrix for the system Args: Q (numpy.array): Process error covariance matrix """ self.Q = Q

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```

Sets the R matrix for the system

2.0.9 set R(R)

 $\bullet R$  ( numpy.array ) -

Parameters: Measurement error covariance matrix

# $Source\ code\ in \ \ \ \verb| bayesian-filters-smoothers \verb| bayesian_filters_smoothers \verb| bayesian_filters_smoothers \verb| py \ |$

```
def set_R(self, R):

"""Sets the R matrix for the system Args: R (numpy.array): Measurement error covariance matrix """ self.R = R

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```

#### **API Reference**

This page gives an overview of all the Bayesian Filters and Smoothers implemented in the package

- Kalman Filter/Smoother
- Extended Kalman Filter/Smoother
- Unscented Kalman Filter/Smoother
- Gaussian Filter/Smoother
- Particle Filter/Smoother

*Extended\_Kalman\_Filter\_Smoother Class:* Extended Kalman Filter/Smoother is the Bayesian Filter/Smoother applied to a nonlinear system with gaussian process/measurement errors and the gaussian approximation is achieved through linearization of the process and measurement models

Creates an object to handle Extended Kalman Filtering and Smoothing for Linear Time Invariant (LTI) System

- $\bullet$  A ( numpy.array ) LTI system matrix
- B ( numpy.array ) LTI input matrix
- C (numpy.array) LTI output matrix
- D ( numpy.array ) LTI feedforward matrix
- $m_k (numpy.array)$  State mean vector
- P\_k ( numpy.array ) State covariance matrix
- Q ( numpy.array ) Process error covariance matrix
- R ( numpy.array ) -

Measurement error covariance matrix

Attributes:

```
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    class Extended_Kalman_Filter_Smoother:
    """Creates an object to handle Extended Kalman Filtering and Smoothing for Linear Time Invariant (LTI) System Attributes: A
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    """Initializes the instance of class Extended_Kalman_Filter_Smoother Args: f (function(state,input) => numpy.array): Non-lim
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    """Sets the system dynamics function for a non-linear time-varying (LTV) system Args: f (function(state,input) => numpy.arr
    """Sets the linearized system dynamics function for a non-linear time-varying (LTV) system Args: F (function(state,input) =
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    """Sets the measurement function for a non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-l
    """Sets the linearized measurement function for a non-linear time-varying (LTV) system Args: H (function(state) => numpy.ar
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    """Sets the Q matrix for the system Args: Q (numpy.array): Process error covariance matrix """ self.Q = Q def set_R(self, R
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    """Sets the R matrix for the system Args: R (numpy.array): Measurement error covariance matrix """ self.R = R def Extended
285 """Performs the predict step of the Extended Kalman Filter Args: u k (numpy.array): Input to the system Returns: m k (numpy.array)
    """Performs the update step of the Extended Kalman Filter Args: y k (numpy.array): New measurement from the system m k (numpy.array)
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    """Performs the smoothening step of the Extended Kalman Smoother Args: u k list (list of numpy.array): List of inputs to the
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## 2.0.10 Extended Kalman Predict(u k)

Performs the predict step of the Extended Kalman Filter

 $\bullet u_k ([numpy.array]) -$ 

Parameters: Input to the system

• m\_k\_( numpy.array ) - Predicted state mean vector

• **P\_k\_(** numpy.array ) -

Returns:

Predicted state covariance matrix

 $Source\ code\ in\ \ \ \texttt{bayesian\_filters\_smoothers\_bayesian\_filters\_smoothers\_py}$ 

```
def Extended Kalman Predict(self, u k):
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     """Performs the predict step of the Extended Kalman Filter Args: u k (numpy.array): Input to the system Returns: m k
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```

#### 2.0.11 Extended\_Kalman\_Smoother(u\_k\_list, y\_k\_list)

Performs the smoothening step of the Extended Kalman Smoother

```
• u_k_list ( list of numpy.array ) - List of inputs to the system
```

•  $y_k_list(list of numpy.array) -$ 

**Parameters:** 

List of measurements from the system

• G\_k\_list( list of numpy.array ) - List of Extended Kalman Smoother Gain

 $\hbox{$^\bullet$m\_k\_s([list\ of\ numpy.array])$-$List\ of\ smoothed\ state\ vectors$}$ 

Returns: • P\_k\_s([list of numpy.array])-

List of smoothed state covarivance matrices

```
def Extended_Kalman_Smoother(self, u_k_list, y_k_list):
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    """Performs the smoothening step of the Extended Kalman Smoother Args: u_k_list (list of numpy.array): List of inputs to the
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```



Performs the update step of the Extended Kalman Filter

```
• y_k ( numpy.array ) -
```

New measurement from the system

**Parameters:** 

- $m_k_{\min}$  Predicted state mean vector
- P\_k\_(numpy.array) Predicted state covariance matrix
- $v_k(\underline{\quad \text{numpy.array}}) Updated measurement error$
- $S_k([numpy.array]) -$

Returns:

Updated measurement covariance matrix

• K\_k( numpy.array ) - Updated Extended Kalman Gain

```
Source code in bayesian-filters-smoothers\bayesian_filters_smoothers.py
 382
      def Extended_Kalman_Update(self, y_k, m_k_, P_k_):
     """Performs the update step of the Extended Kalman Filter Args: y_k (numpy.array): New measurement from the system m_k_ (nu
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```

2.0.13 \_\_init\_\_(f, F, h, H, m\_k, P\_k, Q, R)

Initializes the instance of class Extended Kalman Filter Smoother

- f (| function(state,input) => numpy.array ) Non-linear dynamics function which outputs state vector
- F ( function(state, input) => numpy.array ) Linearized system dynamics which outputs a matrix
- h ( function(state) => numpy.array ) Non-linear output function which outputs mesurement vector

**Parameters:** 

- H ( function(state) => numpy.array ) Linearized output function which outputs a matrix
- m\_k ( numpy.array ) State mean vector
- P\_k ( numpy.array ) State covariance matrix
- Q ( numpy.array ) Process error covariance matrix
- R ( numpy.array ) Measurement error covariance matrix

```
Source code in bayesian-filters-smoothers\bayesian_filters_smoothers.py
      def __init__(self, f, F, h, H, m_k, P_k, Q, R):
     """Initializes the instance of class Extended_Kalman_Filter_Smoother Args: f (function(state,input) => numpy.array): Non-li
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```

2.0.14 set\_F(F)

Sets the linearized system dynamics function for a non-linear time-varying (LTV) system

• F(| function(state,input) => numpy.array |) -

Parameters:

Linearized system dynamics which outputs a matrix

Sets the linearized measurement function for a non-linear time-varying (LTV) system

• H ( function(state) => numpy.array )-

Parameters: Linearized output function which outputs a matrix

```
Source\ code\ in\ \verb||\ bayesian-filters-smoothers\ bayesian_filters\_smoothers.py|
```

```
def set_H(self, H):

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"""Sets the linearized measurement function for a non-linear time-varying (LTV) system Args: H (function(state) => numpy.arg
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2.0.16 set Q(Q)
```

Sets the Q matrix for the system

• Q ( numpy.array ) -

Parameters: Process error covariance matrix

```
Source code in | bayesian-filters-smoothers\bayesian_filters_smoothers.py |
```

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def set_Q(self, Q):
"""Sets the Q matrix for the system Args: Q (numpy.array): Process error covariance matrix """ self.Q = Q

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```

2.0.17 set\_R(R)

Sets the R matrix for the system

• R ( numpy.array ) -

Parameters: Measurement error covariance matrix

Source code in bayesian-filters-smoothers\bayesian\_filters\_smoothers.py

```
def set_R(self, R):
    """Sets the R matrix for the system Args: R (numpy.array): Measurement error covariance matrix """ self.R = R

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```

2.0.18 set f(f)

Sets the system dynamics function for a non-linear time-varying (LTV) system

 $\bullet$  f ( function (state, input) => numpy.array ) - Non-linear dynamics function which outputs state

Parameters: vector

```
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```

```
def set_f(self, f):
    """Sets the system dynamics function for a non-linear time-varying (LTV) system Args: f (function(state,input) => numpy.arra
    """
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2.0.19 set h(h)
```

Sets the measurement function for a non-linear time-varying (LTV) system

• h (| function(state) => numpy.array |) - Non-linear output function which outputs mesurement

Parameters: vector

 $Source\ code\ in\ \ \ \verb|bayesian_filters_smoothers \ \ \verb|bayesian_filters_smoothers \ \ \verb|bayesian_filters_smoothers \ \ \verb|py||$ 

```
def set_h(self, h):
    """Sets the measurement function for a non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non
```

#### **API Reference**

This page gives an overview of all the Bayesian Filters and Smoothers implemented in the package

- Kalman Filter/Smoother
- Extended Kalman Filter/Smoother
- Unscented Kalman Filter/Smoother
- Gaussian Filter/Smoother
- Particle Filter/Smoother

*Unscented\_Kalman\_Filter\_Smoother Class:* Unscented Kalman Filter/Smoother is the Bayesian Filter/Smoother applied to a nonlinear system with gaussian process/measurement errors and the gaussian approximation is achieved through the unscented transform

Creates an object to handle Unscented Kalman Filtering and Smoothing for Linear Time Invariant (LTI) System

- f(| function(state,input) => numpy.array ) Non-linear dynamics function which outputs state vector
- h ( function (state) => numpy.array ) Non-linear output function which outputs mesurement vector
- n ( integer ) Number of states
- alpha (float) Parameter for the UKF algorithm

**Attributes:** 

- k ( float ) Parameter for the UKF algorithm
- beta (float) Parameter of the UKF algorithm
- $m_k (numpy.array)$  State mean vector
- P\_k ( numpy.array ) State covariance matrix
- Q ( numpy.array ) PRocess error covariance matrix
- R ( numpy.array ) Measurement error covariance matrix

```
class Unscented Kalman Filter Smoother:
503
    """Creates an object to handle Unscented Kalman Filtering and Smoothing for Linear Time Invariant (LTI) System Attributes:
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    """Initializes the instance of class Extended Kalman Filter Smoother Args: f (function(state,input) => numpy.array): Non-li
    """Sets the system dynamics function for a non-linear time-varying (LTV) system Args: f (function(state,input) => numpy.arr
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    """Sets the measurement function for a non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-l
    """Sets the Q matrix for the system Args: Q (numpy.array): Process error covariance matrix """ self.Q = Q def set_R(self, R)
508
    """Sets the R matrix for the system Args: R (numpy.array): Measurement error covariance matrix """ self.R = R def __UKF_Sign
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    """Computes Sigma Points for Unscented Kalman Filter Args: m (numpy.array): State mean vector P (np.array): State covariance
511
    """Computes Sigma Points through the dyanmic model for the Unscented Kalman Filter Args: Sigma_X_Points_list (list of numpy
512 """Computes Sigma Points through the measurement model for the Unscented Kalman Filter Args: Sigma X Points list (list of n
513 """Computes predict step state mean, covariance and cross-coavriance for the Unscented Kalman Filter Args: Sigma X Points 1.
514 """Computes predict step state mean and coavriance for the Unscented Kalman Filter Args: Sigma X Points list (list of numpy
515 """Performs the predict step of the Unscented Kalman Filter Args: u_k (numpy.array): Input to the system Returns: m_k_ (numpy.array)
    """Performs the update step of the Unscented Kalman Filter Args: y_k (numpy.array): New measurement from the system m_k_ (n
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    """Performs the smoothening step of the Unscented Kalman Smoother Args: u_k_list (list of numpy.array): List of inputs to t
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```

## 2.0.20 Unscented\_Kalman\_Predict(u\_k)

Performs the predict step of the Unscented Kalman Filter

• **u\_k** ( numpy.array ) -

Parameters: Input to the system

**Returns:** 

• m\_k\_( numpy.array ) - Predicted state mean vector

• P\_k\_( numpy.array ) - Predicted state covariance matrix

• D\_k( numpy.array ) - Predicted state cross-covariance

Source code in | bayesian-filters-smoothers\bayesian\_filters\_smoothers.py |

```
def Unscented_Kalman_Predict(self, u_k):
    """Performs the predict step of the Unscented Kalman Filter Args: u_k (numpy.array): Input to the system Returns: m_k_ (num
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```

## 2.0.21 Unscented Kalman Smoother (u\_k\_list, y\_k\_list)

Performs the smoothening step of the Unscented Kalman Smoother

•  $u_k_{list}$  ( list of numpy.array ) – List of inputs to the system

•  $y_k_list(|list of numpy.array|) -$ 

Parameters:

List of measurements from the system

• G\_k\_list( list of numpy.array ) - List of Extended Kalman Smoother Gain

•  $m_k_s([list of numpy.array]) - List of smoothed state vectors$ 

Returns: • P\_k\_s( list of numpy.array )-

List of smoothed state covarivance matrices

```
def Unscented_Kalman_Smoother(self, u_k_list, y_k_list):
898
     """Performs the smoothening step of the Unscented Kalman Smoother Args: u_k_list (list of numpy.array): List of inputs to the
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```



Performs the update step of the Unscented Kalman Filter

```
• y_k ( numpy.array ) -
```

New measurement from the system

Parameters:

- m\_k\_(numpy.array) Predicted state mean vector
- P\_k\_ ( numpy.array ) Predicted state covariance matrix
- mu\_k( numpy.array ) Predicted measurement mean
- $S_k(\underline{numpy.array})$  Predicted measurement covariance matrix
- C\_k( numpy.array )-

**Returns:** 

Predicted state-measurement covariance matrix

•  $K_k(\underline{\quad numpy.array})$  – Updated Extended Kalman Gain

```
Source\ code\ in\ |\ \texttt{bayesian-filters-smoothers} \setminus \texttt{bayesian\_filters\_smoothers.py}|
       def Unscented_Kalman_Update(self, y_k, m_k_, P_k_):
      """Performs the update step of the Unscented Kalman Filter Args: y_k (numpy.array): New measurement from the system m_k_ (n
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```

Computes predict step state mean, covariance and cross-coavriance for the Unscented Kalman Filter

2.0.23 UKF Predict State MeanCovariance(Sigma X Points list, Sigma X Points Tilde list)

```
• Sigma_X_Points_list ( list of numpy.array ) - List of Sigma points
```

Parameters:

• Sigma\_X\_Points\_Tilde\_list ( (list of numpy.array ) - List of Sigma points passed through the dynamic model

• m\_k\_( numpy.array ) - Predicted state mean vector

• **P\_k\_(** numpy.array ) -

**Returns:** 

Predicted state covariance matrix

• D\_k( numpy.array ) - Predicted state cross-covariance

```
691
     def __UKF_Predict_State_MeanCovariance(self, Sigma_X_Points_list, Sigma_X_Points_Tilde_list):
    """Computes predict step state mean, covariance and cross-coavriance for the Unscented Kalman Filter Args: Sigma_X_Points_1.
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2.0.24 UKF SigmPoints DynamicModel (Sigma X Points list, u k)
```

Computes Sigma Points through the dyanmic model for the Unscented Kalman Filter

• Sigma\_X\_Points\_list ( list of numpy.array ) - List of Sigma points

**Parameters:** 

• u\_k ( numpy.array ) - Input to the system

 $\hbox{$^\bullet$ Sigma\_X\_Points\_Tilde\_list($\tt list of numpy.array)$})-List of Sigma points passed through the$ 

Returns: dynamic model

 $Source\ code\ in\ \ \ \texttt{bayesian-filters-smoothers} \ \texttt{bayesian\_filters\_smoothers.py}$ 

```
def __UKF_SigmPoints_DynamicModel(self, Sigma_X_Points_list, u_k):
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     """Computes Sigma Points through the dyanmic model for the Unscented Kalman Filter Args: Sigma_X_Points_list (list of numpy
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```

```
2.0.25 __UKF_SigmPoints_Generator(m, P)
```

Computes Sigma Points for Unscented Kalman Filter

• m ( numpy.array ) - State mean vector

• **P** ( np.array ) -

**Parameters:** 

State covariance matrix

• Sigma\_X\_Points\_list( list of numpy.array )-

Returns: List of Sigma points

 $Source\ code\ in\ \verb|[bayesian_filters_smoothers]| bayesian\_filters\_smoothers.py|$ 

```
587
     def __UKF_SigmPoints_Generator(self, m, P):
588
     """Computes Sigma Points for Unscented Kalman Filter Args: m (numpy.array): State mean vector P (np.array): State covariance
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```

# 2.0.26 \_\_UKF\_SigmPoints MeasurementModel(Sigma\_X\_Points\_list)

Computes Sigma Points through the measurement model for the Unscented Kalman Filter

Source code in | bayesian-filters-smoothers\bayesian filters smoothers\bayesian filters smoothers.py |

• Sigma\_X\_Points\_list ( list of numpy.array ) -

Parameters: List of Sigma points

 $\bullet \textbf{Sigma} \textbf{Y} \textbf{Points} \textbf{Tilde} \textbf{list} ( \texttt{list of numpy.array} ) - List of Sigma points passed through the$ 

Returns: measurement model

def UKF SigmPoints MeasurementModel(self, Sigma X Points list): """Computes Sigma Points through the measurement model for the Unscented Kalman Filter Args: Sigma\_X\_Points\_list (list of n 

#### 2.0.27

\_\_UKF\_Update\_StateMeasurement\_MeanCovariance(Sigma\_X\_Points\_list, Sigma\_Y\_Points\_Tilde\_list, m\_k\_)

Computes predict step state mean and coavriance for the Unscented Kalman Filter

- Sigma\_Y\_Points\_Tilde\_list ( (list of numpy.array ) List of Sigma points passed through the

Parameters: measurement model

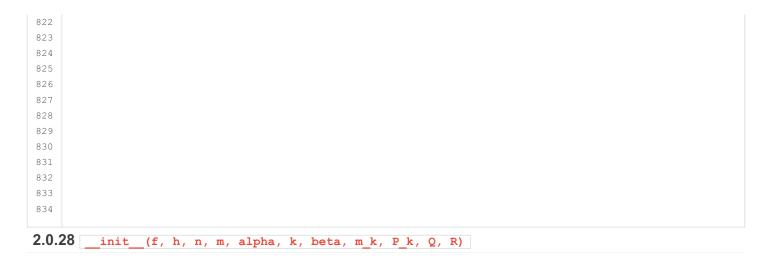
- m\_k\_( numpy.array ) Predicted state mean vector
- $mu_k(numpy.array)$  Predicted measurement mean
- S\_k( numpy.array ) Predicted measurement covariance matrix

Returns: • C\_k( numpy.array )-

Predicted state-measurement covariance matrix

 $Source\ code\ in\ \ \ \ \texttt{bayesian\_filters\_smoothers\_bayesian\_filters\_smoothers\_py}\ ]$ 

```
def __UKF_Update_StateMeasurement_MeanCovariance(self, Sigma_X_Points_list, Sigma_Y_Points_Tilde_list, m_k_):
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    """Computes predict step state mean and coavriance for the Unscented Kalman Filter Args: Sigma_X_Points_list (list of numpy
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```



Initializes the instance of class Extended\_Kalman\_Filter\_Smoother

- f([function(state,input) => numpy.array]) Non-linear dynamics function which outputs state vector
- h ( function (state) => numpy.array ) Non-linear output function which outputs mesurement vector
- n = Number of states
- m (integer) Number of outputs

Parameters:

- alpha ( float ) Parameter for the UKF algorithm
- k ( float ) Parameter for the UKF algorithm
- m\_k ( numpy.array ) State mean vector
- P k ( numpy.array ) State covariance matrix
- Q ( numpy.array ) PRocess error covariance matrix
- R ( numpy.array ) Measurement error covariance matrix

```
Source\ code\ in\ \verb|[bayesian_filters_smoothers]| bayesian\_filters\_smoothers.py|
       def __init__(self, f, h, n, m, alpha, k, beta, m_k, P_k, Q, R):
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      """Initializes the instance of class Extended_Kalman_Filter_Smoother Args: f (function(state,input) => numpy.array): Non-lin
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 2.0.29 set_Q(Q)
```

Sets the Q matrix for the system

 $\bullet \ Q \ ($  numpy.array ) -

Parameters: Process error covariance matrix

```
Source code in | bayesian-filters-smoothers\bayesian_filters_smoothers.py |
```

```
def set_Q(self, Q):

"""Sets the Q matrix for the system Args: Q (numpy.array): Process error covariance matrix """ self.Q = Q

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```

```
2.0.30 set R(R)
```

Sets the R matrix for the system

• R ( numpy.array ) -

Parameters: Measurement error covariance matrix

Source code in | bayesian-filters-smoothers\bayesian filters smoothers\bayesian filters smoothers.py |

```
def set_R(self, R):

"""Sets the R matrix for the system Args: R (numpy.array): Measurement error covariance matrix """ self.R = R

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```

2.0.31 set f(f)

Sets the system dynamics function for a non-linear time-varying (LTV) system

•  $f([function(state, input)] \Rightarrow numpy.array] - Non-linear dynamics function which outputs state$ 

Parameters: vector

 $Source\ code\ in\ \ \ \texttt{bayesian-filters-smoothers} \ \texttt{bayesian\_filters\_smoothers.py}\ \ ]$ 

```
def set_f(self, f):

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"""Sets the system dynamics function for a non-linear time-varying (LTV) system Args: f (function(state,input) => numpy.arra

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```

2.0.32 set h(h)

Sets the measurement function for a non-linear time-varying (LTV) system

•  $h = \frac{1}{2} - \frac{1}{2}$ 

Parameters: vector

Source code in bayesian-filters-smoothers\bayesian\_filters\_smoothers\bayesian\_filters\_smoothers.py

```
def set_h(self, h):

"""Sets the measurement function for a non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear time-varying (LTV) system Args: h (function(state) => numpy.array): Non-linear
```

#### **API Reference**

This page gives an overview of all the Bayesian Filters and Smoothers implemented in the package

- Kalman Filter/Smoother
- Extended Kalman Filter/Smoother
- Unscented Kalman Filter/Smoother
- Gaussian Filter/Smoother
- Particle Filter/Smoother

#### **API Reference**

This page gives an overview of all the Bayesian Filters and Smoothers implemented in the package

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- Extended Kalman Filter/Smoother
- Unscented Kalman Filter/Smoother
- Gaussian Filter/Smoother
- Particle Filter/Smoother

## 2.0.33 User Guide

# Examples

>>> from bayesian\_filters\_smoothers import addnum >>> addnum(10,5)

# **Jupyter Notebook Examples**

Coming soon...