

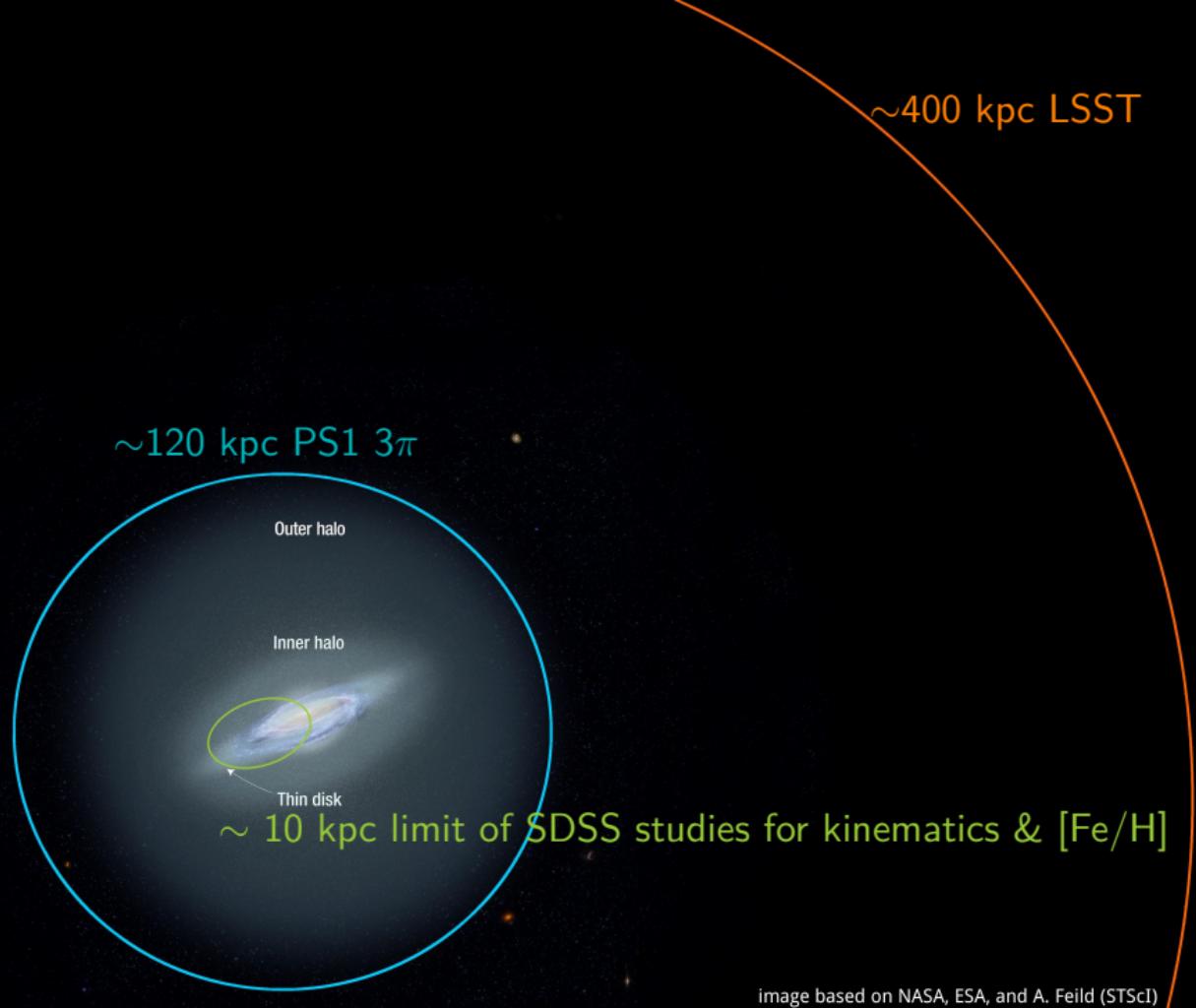
Iniciación en la Investigación (Semester 1 2025)

Lecture 1: The Blazhko effect

Nina Hernitschek

Centro de Astronomía CITEVA
Universidad de Antofagasta

May 9, 2025



Motivation

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

catalogs of variable sources from deep and wide all-sky surveys

to **model a survey**, tools are needed for

- describing data quality → outlier might fake or hide true variability
- describing light curve characteristics → “features” with scientific relevance
- classifying sources → catalogs others can use
- finding substructure → clumps, overdensities, ... the science we want to do

RR Lyrae stars

The Blazhko effect

Motivation

What?

How?

Why?

Simulations

prototype: RR Lyrae (variability discovered by Williamina Fleming, ~ 1900); RR Lyrae stars are old helium-burning variable stars of spectral type A5 to F5 with $0.5 M_{\odot}$

RRab

asymmetrical light curves
with steep ascend

- periods: 0.3 - 1.2 days
- amplitudes: 0.5 - 2 mag_V

RRc

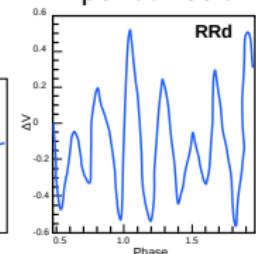
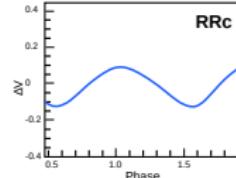
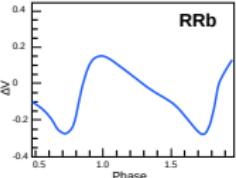
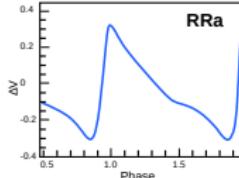
nearly symmetrical light
curves

- periods: 0.2 - 0.5 days
- amplitudes: < 0.8 mag_V

RRd

double-mode RR Lyrae
stars, fundamental
and first overtone

- fundamental period:
0.5 days
- period ratio: 0.74 days



RR Lyrae stars

The Blazhko
effect

Motivation

What?

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Simulations

RR Lyrae stars are considered textbook examples of **simple**, single-periodic radially pulsating stars.

RR Lyrae stars

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

RR Lyrae stars are considered textbook examples of **simple**, single-periodic radially pulsating stars.

In fact, they are **much more complex** and display phenomena that are not well understood.

The Blazhko effect

The Blazhko
effect

Motivation

What?

How?

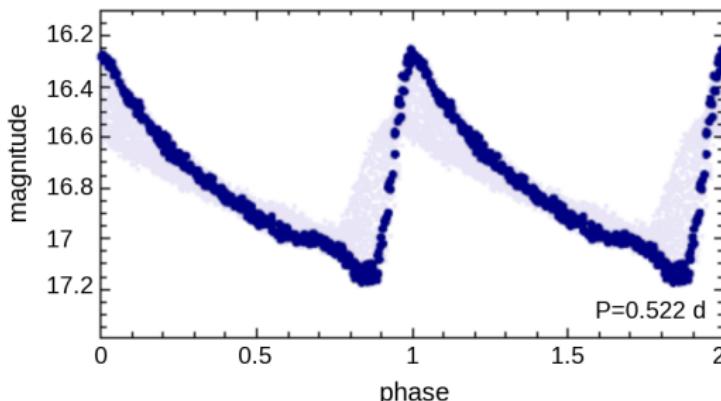
Why?

Simulations

A relevant fraction of RR Lyrae stars shows the **Blazhko effect**:
An amplitude and frequency modulation of the pulsations of a type of
classical pulsating stars called RR Lyrae.

In short: The period and/or amplitude changes.

Here we see an example of amplitude modulation:



source (animation):

<https://ogle.astrouw.edu.pl/atlas/lcurves/OGLE-BLG-RRLYR-09193.gif>

A simple light curve model for the Blazhko effect

The Blazhko
effect

Motivation

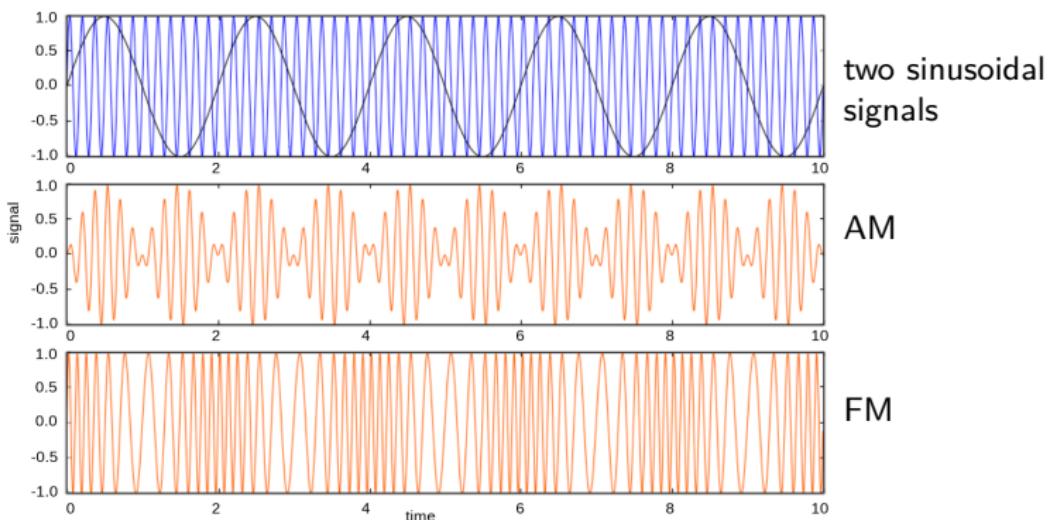
What?

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Why?

Simulations

schematic diagram of amplitude and frequency modulation:



A simple light curve model for the Blazhko effect

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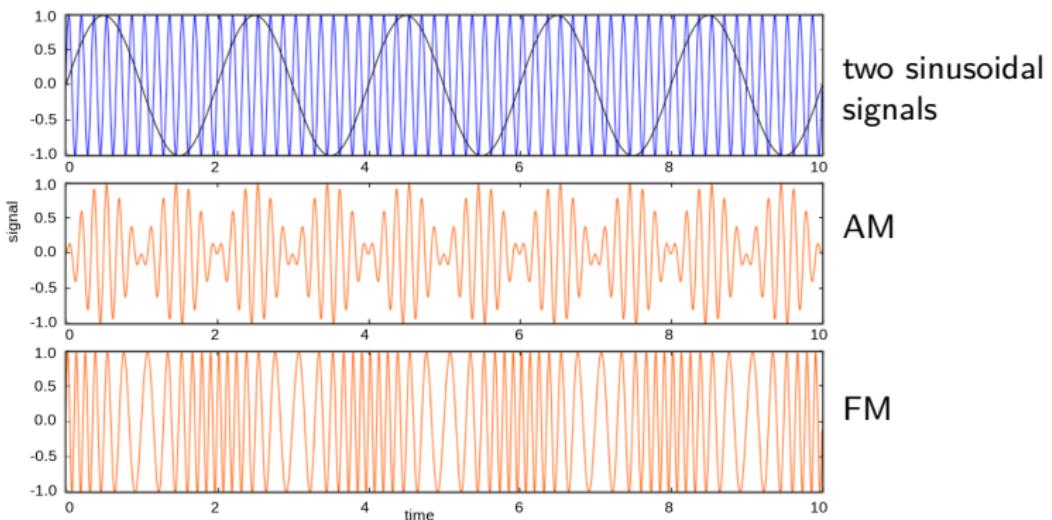
What?

How?

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Simulations

schematic diagram of amplitude and frequency modulation:



Amplitude modulation (AM) is achieved by multiplying two sinusoidal functions: $f = A \cos \Omega t \times a \cos \omega t$

A simple light curve model for the Blazhko effect

The Blazhko
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Motivation

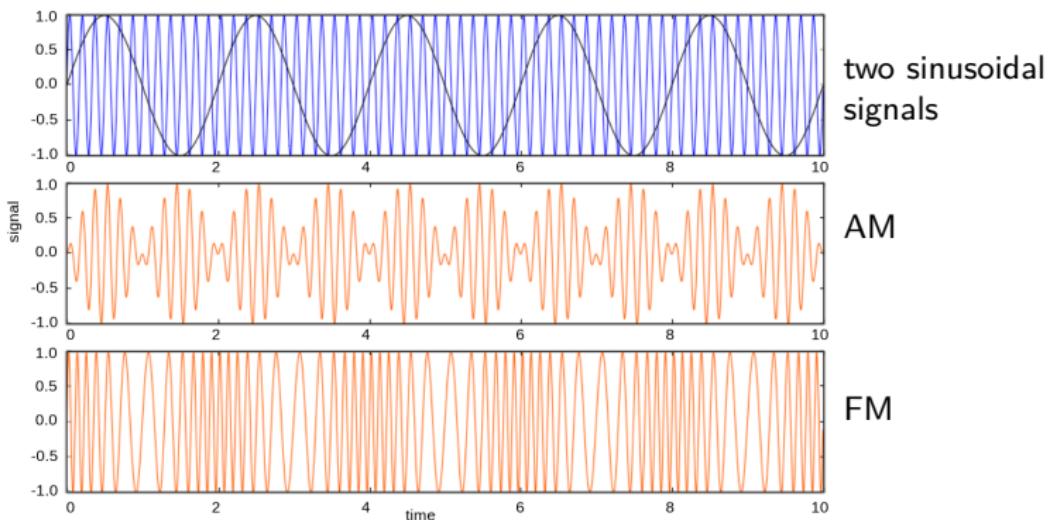
What?

How?

Why?

Simulations

schematic diagram of amplitude and frequency modulation:



Frequency modulation (FM) can be achieved by applying a sinusoidal signal to the frequency component of the carrier's sinusoidal waveform:
 $f = M \cos(\omega t \cos \Omega t)$

How to observe the Blazhko effect

The Blazhko
effect

Motivation

What?

How?

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Simulations

The Blazhko effect was discovered more than hundred years ago (Blažhko, 1907).

Since then, many Blazhko variables were discovered in the data gathered by different photometric sky surveys:

OGLE (e.g., Mizerski, 2003; Soszyński et al., 2011a)

MACHO (e.g. Alcock et al., 2003)

as well as targeted surveys such as by the Konkoly Blazhko Survey (e.g., Jurcsik et al., 2008; Sóder et al., 2011).

How to observe the Blazhko effect

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as well as targeted surveys such as by the Konkoly Blazhko Survey (e.g., Jurcsik et al., 2008; Sóder et al., 2011).

These observations also revealed that the Blazhko phenomenon might be **common**, at least in RRab stars, as it was detected in nearly 50 % of RRab stars for which high-quality photometry was gathered (Jurcsik et al., 2009).

Observations

The Blazhko effect

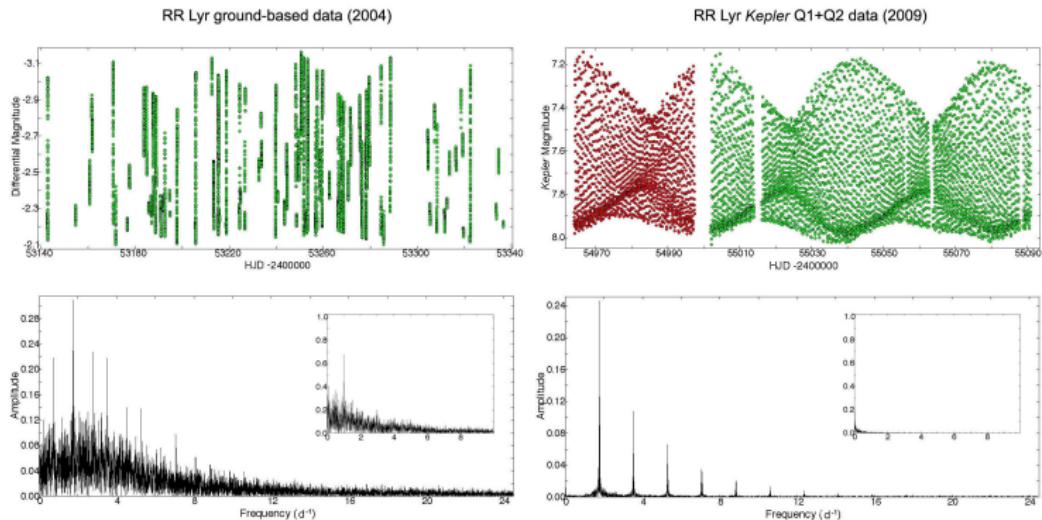
Motivation

What?

How?

Why?

Simulations



Comparison of the ground-based RR Lyrae data, gathered from six different observatories, published by Kolenberg et al. (2006) and the Kepler Q1 and Q2 data of the star transformed to the magnitude scale (top panels).
Bottom panels: Fourier transform of the data; the insert shows the window function.
From Kolenberg et al. (2011)

Observations

The Blazhko
effect

Motivation

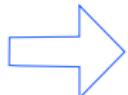
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Simulations

Observations also revealed that the Blazhko phenomenon might be **common**, at least in RRab stars, as it was detected in nearly 50 % of RRab stars for which high-quality photometry was gathered (Jurcsik et al. 2009).



something important to keep in mind when working with RR Lyrae stars, like e.g. predicting phases for spectroscopy

Observations

The Blazhko
effect

Motivation

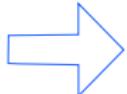
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something important to keep in mind when working with RR Lyrae stars, like e.g. predicting phases for spectroscopy

The incidence rate of the Blazhko effect is estimated as:

RRab stars: ~50% (Kovács 2015)

RRc stars: < 10% (Nagy & Kovács 2006; Mizerski 2003)

Modulation Patterns

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

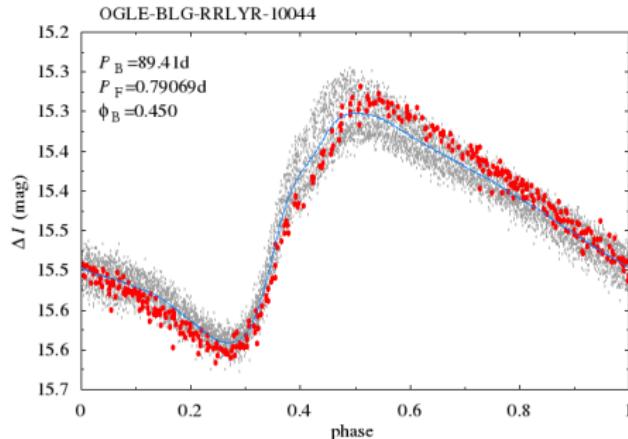
Among Blazhko stars a variety of modulation patterns are observed.

Modulation periods range from a few days to more than a thousand of days.

Typically, both pulsation amplitude and pulsation phase are modulated.

examples can be found in this online gallery:

<http://users.camk.edu.pl/smolec/blazhko/>



Modulation Patterns

The Blazhko
effect

Motivation

What?

How?

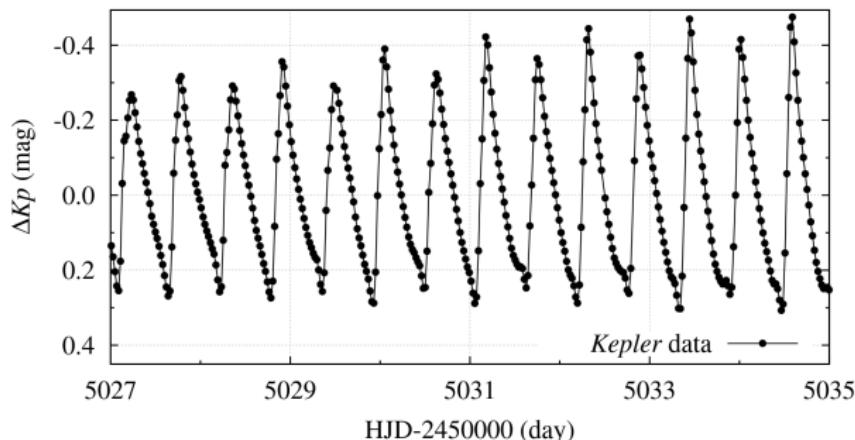
Why?

Simulations

Period doubling was detected in space observations.

Period doubling shows as alternating maxima and minima of the pulsation cycles in the light curve.

An in-depth study was done by Szabó et al. (2010).



On-/Offset of Pulsation

The Blazhko effect

Motivation

What?

How?

Why?

Simulations

Not directly related to the Blazhko effect, but also a change in pulsation behavior is the sudden on- or offset of pulsation in variable stars.

It is clear that each pulsating variable star, such as RR Lyrae stars, must have started pulsating at some time.

JOURNAL ARTICLE

HD 60435: the star that stopped pulsating ⓧ

Donald W Kurtz  , Gerald Handler , Daniel L Holdsworth , Margarida S Cunha , Hideyuki Saio , Thebe Medupe , Simon J Murphy , Joachim Krüger , E Brunsden , Victoria Antoci ... Show more

Monthly Notices of the Royal Astronomical Society, Volume 536, Issue 3, January 2025, Pages 2103–2126, <https://doi.org/10.1093/mnras/stae2708>

Published: 10 December 2024 Article history ▾



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ABSTRACT

HD 60435 is a well known rapidly oscillating (roAp) Ap star with a series of alternating even and odd degree modes, making it a prime asteroseismic target. It is also an oblique pulsator with rotational inclination, i , and magnetic/pulsation obliquity, β , such that both magnetic/pulsation poles are viewed over the rotation period, $P_{\text{rot}} = 7.679696$ d, determined from rotational light variations. While some roAp stars have stable pulsation mode amplitudes over decades, HD 60435 is known to have amplitude variations on time-scales as short as 1 d. We show from 5 years of TESS observations that there is strong amplitude modulation on this

Observations

The Blazhko
effect

Motivation

What?

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Why?

Simulations

Better understanding RR Lyrae stars with Blazhko effect requires:

- long-term monitoring of RR Lyrae stars
- nearly continuous monitoring (high cadence)

which is available e.g. from the upcoming LSST.

LSST Cadence

The Blazhko effect

Motivation

What?

How?

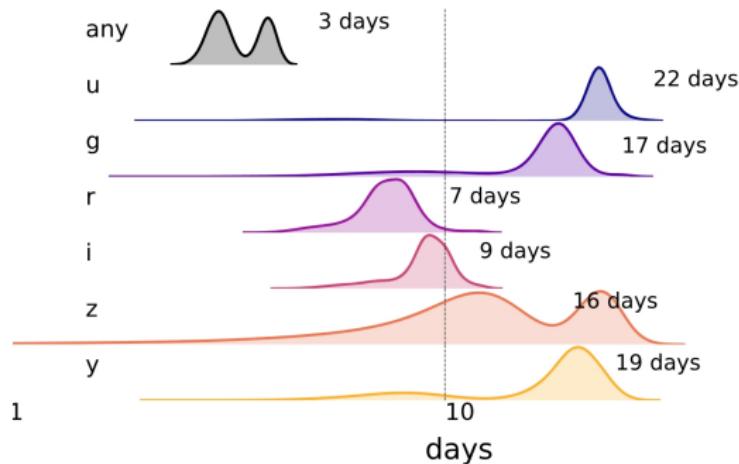
Why?

Simulations

To design LSST cadence in order to find and characterize variable stars:

Use **metrics** to measure the effect of various simulated survey strategies on science cases. They can be found in the *Survey Cadence Notes*:

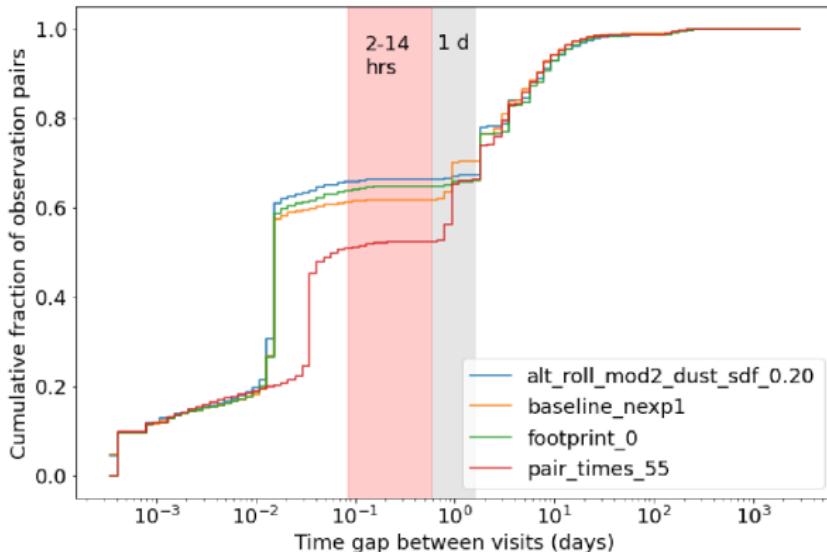
<https://www.lsst.org/content/survey-cadence-notes-2021>



Distribution of median time gaps between observations in different nights for 86 simulations of the Rubin LSST Wide Fast Deep Survey OpSim v1.5. Adapted from Li et al. (2022).

LSST Cadence

The Blazhko effect
Motivation
What?
How?
Why?
Simulations



Most LSST simulations have no observations between 2 and 14 hours and around 24 hours: normalized cumulative histogram (bottom) of the time gaps between visits to the same sky position, for several representative simulations (Bellm et al. 2021):

LSST Cadence

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

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<https://doi.org/10.3847/1538-4365/ac3baf>

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The Impact of Observing Strategy on the Reliable Classification of Standard Candle Stars: Detection of Amplitude, Period, and Phase Modulation (Blazhko Effect) of RR Lyrae Stars with LSST

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Abstract

The Vera C. Rubin Observatory will carry out its Legacy Survey of Space and Time (LSST) with a single-exposure depth of $r \sim 24.7$ and an anticipated baseline of 10 yr, allowing access to the Milky Way's old halo not only deeper than, but also with a longer baseline and better cadence than, e.g., PS1 3π . This will make the LSST ideal to study populations of variable stars such as RR Lyrae stars (RRL). Here, we address the question of observing strategy optimization of LSST, as survey footprint definition, single-visit exposure time, as well as the cadence of repeat visits in different filters are yet to be finalized. We present metrics used to assess the impact of different observing strategies on the reliable detectability and classification of standard candle variable stars, including detection of amplitude, period, and phase modulation effects of RRL (the so-called Blazhko effect), by evaluating metrics for simulated potential survey designs. So far, due to the depths and cadences of typical all-sky surveys, it has been nearly impossible to study this effect on a larger sample. All-sky surveys with relatively few observations over a moderately long baseline allow only for fitting phase-folded RRL light curves, thus integrating over the complete

LSST Cadence

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

THE ASTROPHYSICAL JOURNAL SUPPLEMENT SERIES, 258:4 (9pp), 2022 January

Hemitschek & Stassun

opsim night < 365*2: PeriodicStarModulationMetric

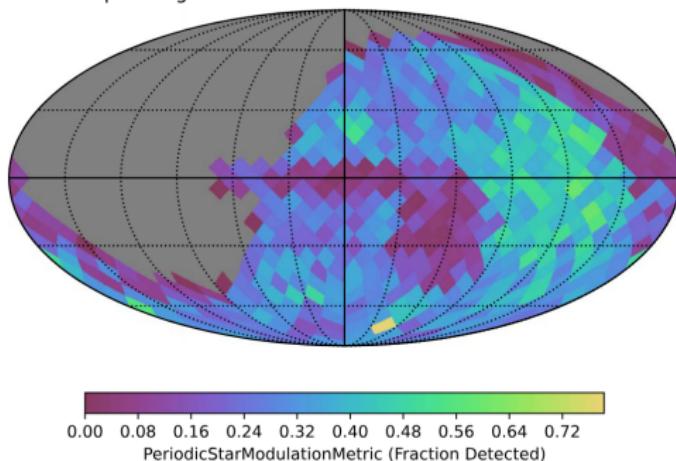


Figure 3. To illustrate how the histograms in Figure 1 and Figure 2 were calculated, this figure shows a single-metric result for a distance modulus of 18.0, and a time interval of 20 days for RRab-like light curves using the pair times cadence. This corresponds to the red histogram in the second panel of the second row in Figure 1. The sky map is plotted in Galactic coordinates. Each HEALPix cell covers $7^{\circ}33'$ (achieved using the HEALPix resolution parameter $Nside = 8$). We highlight that the fraction of correctly recovered period, phase, and amplitude (here as “Fraction Detected”) varies over the survey footprint due to coverage and light-curve length. The generation of sky maps as well as histograms is handled automatically within the `lsst.sims.maf.metricBundles` Python package provided by the MAF. For

LSST Cadence

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

This was a first analysis. We have now better LSST simulations to investigate this in more detail - your task to investigate this more closely :)

(We will see more on LSST in the next lectures.)

Possible explanations for the Blazhko effect

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

We have seen how the light curves from RR Lyrae stars with Blazhko effect look like, and what are possible methods to detect them.

What are possible **explanations** for the observed light-curve modulations?

Possible explanations for the Blazhko effect

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

Several models were proposed to explain the Blazhko phenomenon. Some of them are rather ideas, as they lack rigorous physical description.

Testing of the models faces a basic difficulty: we still lack realistic, 3D models that could correctly describe turbulent convection present in the envelopes of RR Lyrae stars and could describe the nonlinear interaction between the radial modes, and radial and nonradial modes.

Possible explanations for the Blazhko effect

The Blazhko
effect

Motivation

What?

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Simulations

Nevertheless, some models could be ruled out on observational and/or theoretical grounds.

Here, a list of a few of those models is given.

For extensive review of some models, see Kovács (2009).

Possible explanations for the Blazhko effect

The Blazhko
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Motivation

What?

How?

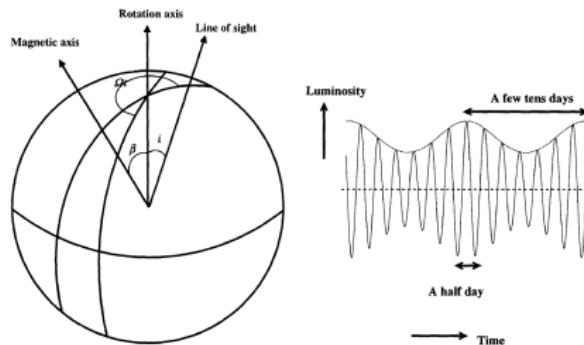
Why?

Simulations

Magnetic oblique rotator/pulsator model (Shibahashi 2000)

Assumption: RR Lyrae stars have substantial magnetic fields, and their magnetic symmetry axis is inclined to the rotation axis of the star. The model is inspired by the observation that the modulation periods are of the same order as the rotation periods of those stars.

An rigid rotating star with angular frequency Ω and a dipole magnetic field is assumed, its symmetry axis passes through the stellar axis.



This model requires strong dipole magnetic field of 1 kG which is not detected (e.g. Kolenberg & Bagnulo 2009). Also, it predicts strictly periodic modulation, despite observed modulation can be strongly irregular.

Possible explanations for the Blazhko effect

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

Resonant nonradial rotator/pulsator model (Nowakowski & Dziembowski 2001)

Explains modulation as due to rotational splitting of nonradial modes that are in 1:1 resonance with the fundamental mode. The model predicts strictly periodic modulation which is not the case.

Possible explanations for the Blazhko effect

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

Magnetic field variability (Stothers 2006)

Explains modulations by a variable magnetic field affecting the efficiency of envelope convection and causes the modulation of pulsation. In this interpretation of the modulating Blazhko effect in RR Lyrae stars, turbulent convection inside the hydrogen and helium ionization zones becomes cyclically weakened and strengthened owing to the presence of a transient magnetic field that is generated *in situ* by either a turbulent or a rotational dynamo mechanism.

The idea lacks rigorous elaboration. For recent critique of this idea see Smolec et al. (2011) and Molnár et al. (2012a) who test variable turbulent convection as the cause of the Blazhko effect (the Stothers model).

Possible explanations for the Blazhko effect

The Blazhko
effect

Motivation

What?

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Simulations

9:2 radial mode resonance model (Buchler & Kolláth 2011)

The 9:2 radial mode resonance model explains period doubling in RR Lyrae stars by proposing that a resonance between the fundamental mode and the ninth radial overtone causes the observed phenomenon. This resonance shifts the period of the overtone by up to 10%, leading to the characteristic alternation of pulsation cycles with higher and lower amplitudes. Hydrodynamic models have successfully reproduced this period doubling and identified the 9:2 resonance as the underlying cause

This conclusion is based on the analysis of amplitude equations. The resulting modulation may be quasi-periodic or chaotic. There are no realistic hydrodynamic calculations confirming the hypothesis.

Possible explanations for the Blazhko effect

The Blazhko
effect

Motivation

What?

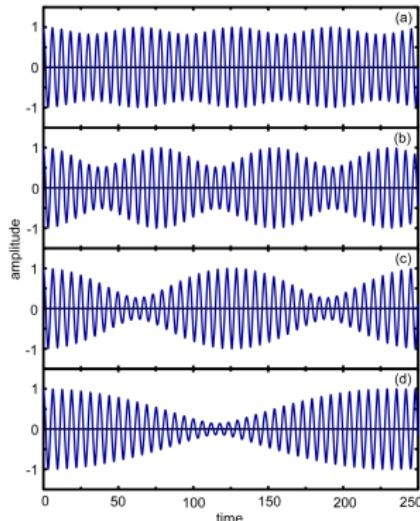
How?

Why?

Simulations

Nonresonant radial-nonradial mode interaction (Cox 2013, Bryant 2015b)

Assumes excitation of two modes, radial and nonradial, of nearly the same frequency, that are not phase-locked.



Normal mode displacement x for different coupling strengths C , where phase-locking would occur for $C \gtrsim 0.05$. Source: Bryant et al. (2016)

Simulating the Blazhko effect

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

We can (quite easily) simulate light curve shapes, also such that show an amplitude or period modulation.

Simulating the Blazhko effect

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

We can (quite easily) simulate light curve shapes, also such that show an amplitude or period modulation.

However: A hydrodynamic simulation that automatically generates the Blazhko effect would be important.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
effect

Motivation

What?

How?

Why?

Simulations

The "Warsaw code" refers to computational models and codes developed in Poland, particularly by researchers at the Nicolaus Copernicus Astronomical Center.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
effect

Motivation

What?

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Simulations

The "Warsaw code" refers to computational models and codes developed in Poland, particularly by researchers at the Nicolaus Copernicus Astronomical Center.

The codes are used to simulate the internal processes of stars, including their convection, radiation, and pulsation dynamics. They can be used to predict the periods, amplitudes, and light curves of RR Lyrae stars.

Convective Hydrocodes for Radial Stellar Pulsation

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The codes are used to simulate the internal processes of stars, including their convection, radiation, and pulsation dynamics. They can be used to predict the periods, amplitudes, and light curves of RR Lyrae stars.

The predictions from the Warsaw codes are compared with actual observations of RR Lyrae stars, allowing researchers to refine their models and understand the physical processes driving these stellar pulsations.

See e.g. Smolec & Moskalik (2008).

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko effect

Motivation

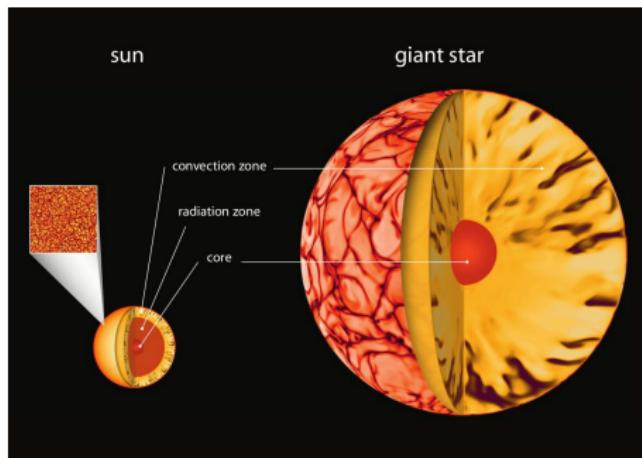
What?

How?

Why?

Simulations

Turbulent convection is an important physical process acting in many types of stars.



Turbulent convection is a **three-dimensional process** transporting energy through many length-scales: from macroscopic eddy cells to microscopic molecular scales, where energy is dissipated.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
effect

Motivation

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Simulations

Stellar convection is complicated to model due to the turbulence.

However, many essential features of convection may be described with simple **one-dimensional models**.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
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Simulations

In pulsating variable stars, large-scale motions of gas interact with smaller-scale turbulent motions and time-dependent models are necessary to describe the coupling between them.

In the code, all quantities are decomposed into mean and fluctuating parts, for example for velocity and temperature we have
 $\mathbf{U} = \bar{\mathbf{U}} + \mathbf{U}'$ and $\mathbf{T} = \bar{\mathbf{T}} + \mathbf{T}'$ respectively.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
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Motivation

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Simulations

The convective hydrocodes implement the time-dependent turbulent convection model.

In the following, U stands for the fluid velocity, which is the time derivative of the radius R :

$$U = \frac{dR}{dt}$$

M_R is the mass enclosed in radius R , V is the specific volume (which is inverse of density ρ). E and P are energy and pressure of the gas including radiation, where E_t and P_t are turbulent energy and turbulent pressure. The viscous energy and momentum transfer rates are denoted by E_q and U_q . F_r , F_c and F_t are radiative, convective and turbulent flux, respectively. The C term describes the coupling between gas energy and turbulent energy equations.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
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Simulations

Momentum and energy equations are then given by

$$\frac{dU}{dt} = -\frac{1}{\rho} \frac{\partial}{\partial R} (P + P_t) + U_q - \frac{GM_R}{R^2}$$

$$\frac{dE}{dt} + P \frac{dV}{dt} = -\frac{1}{\rho} \frac{\partial [R^2(F_r + F_c)]}{R^2 \partial R} - C$$

$$\frac{de_t}{dt} + P_t \frac{dV}{dt} = -\frac{1}{\rho} \frac{\partial (R^2 F_t)}{\partial R} + E_q + C$$

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
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$$\frac{de_t}{dt} + P_t \frac{dV}{dt} = -\frac{1}{\rho} \frac{\partial (R^2 F_t)}{\partial R} + E_q + C$$

The sum of the last two equations form the total energy equation:

$$\frac{d(E + e_t)}{dt} + (P + P_t) \frac{dV}{dt} = -\frac{1}{\rho} \frac{\partial [R^2(F_r + F_c + F_t)]}{R^2 \partial R} + E_q$$

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
effect

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Simulations

Momentum and energy equations are then given by

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$$\frac{de_t}{dt} + P_t \frac{dV}{dt} = -\frac{1}{\rho} \frac{\partial (R^2 F_t)}{\partial R} + E_q + C$$

The sum of the last two equations form the total energy equation:

$$\frac{d(E + e_t)}{dt} + (P + P_t) \frac{dV}{dt} = -\frac{1}{\rho} \frac{\partial [R^2(F_r + F_c + F_t)]}{R^2 \partial R} + E_q$$

A more detailed description can be found in Smolec & Moskalik (2008).

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
effect

Motivation

What?

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Why?

Simulations

For the radiative transfer one may use time-dependent, detailed treatment (Vienna code), or simpler models, like diffusion approximation (Florida-Budapest code).

The first approach has higher accuracy and leads to better physical description of the model's structure, especially in the outer parts.

However, in classical pulsator's models, time dependent treatment gives essentially the same results as simple diffusion approximation (Kovács and Kanbur 1998, Feuchtinger, Buchler and Kolláth 2000).

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Thus, the **diffusion approximation** is used in the hydrocode, which has the advantage of very low numerical costs.

In this approximation, the radiative flux F_r is given by

$$F_r = -\frac{4\sigma}{3}4\pi R^2 \frac{1}{\kappa} \frac{\partial T^4}{\partial M}$$

Radiation pressure P_r and radiative energy E_r are included in P and E together with gas contribution: $P = P_g + P_r$, $E = E_g + E_r$. We have $P_r = aT^4/3$ and $E_r = aT^4/\rho$ where a is the radiation constant.

Pressure, energy as well as other thermodynamic quantities are calculated as function of T and V from the equation-of-state (EOS).

Convective Hydrocodes for Radial Stellar Pulsation

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Motivation

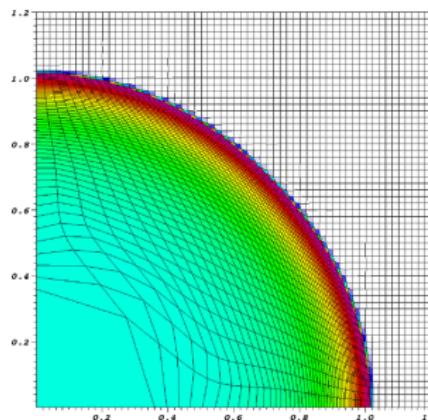
What?

How?

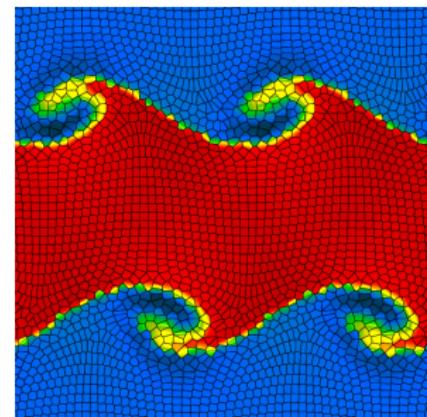
Why?

Simulations

In pulsation hydrocodes, hydrodynamic equations are **discretized on a mesh**, which is either Lagrangian (fixed mass zones) or adaptive.



Lagrangian mesh



AREPO adaptive mesh

Convective Hydrocodes for Radial Stellar Pulsation

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Simulations

The more sophisticated adaptive grid is very useful in resolving the narrow features present in classical pulsator's models such as shocks or hydrogen partial ionization regions (PIR). These are not very well resolved by Lagrangian mesh.

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The more sophisticated adaptive grid is very useful in resolving the narrow features present in classical pulsator's models such as shocks or hydrogen partial ionization regions (PIR). These are not very well resolved by Lagrangian mesh.

However, the use of adaptive mesh in purely radiative models just smoothed the light curves, not changing their overall shape (Buchler 1998). In convective models, hydrogen PIR is widened by the convective motions and therefore, is numerically less troublesome.

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However, the use of adaptive mesh in purely radiative models just smoothed the light curves, not changing their overall shape (Buchler 1998). In convective models, hydrogen PIR is widened by the convective motions and therefore, is numerically less troublesome.

Therefore, the "Warsaw code" uses the Lagrangian mesh.

Convective Hydrocodes for Radial Stellar Pulsation

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Simulations

In classical pulsators, inner parts of the star do not participate in the oscillations.

Thus, only the outer parts of the star, so-called **envelope**, are modeled.
Rotation and magnetic fields are neglected.

The model is specified by:

- mass M
- luminosity L
- effective temperature T_{eff}
- chemical composition X and Z
- mixing-length parameter α , a free parameter that represents the efficiency of convection.

Convective Hydrocodes for Radial Stellar Pulsation

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Motivation

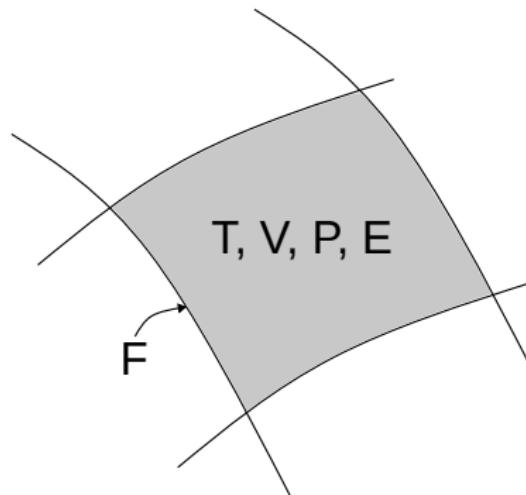
What?

How?

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Simulations

The model is divided into N mass zones according to the Lagrangian mesh. All quantities are defined either at the zones (thermodynamic quantities: T, V, P, E) or in between, at so-called interfaces (the fluxes).



Convective Hydrocodes for Radial Stellar Pulsation

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Motivation

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Simulations

The static model is constructed in **two steps**.

In the first step, an initial model is constructed without turbulent pressure and turbulent flux ($\alpha_p = \alpha_t = 0$), with turbulent energy and coupling term defined at the interfaces.

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The static model is constructed in **two steps**.

In the first step, an initial model is constructed without turbulent pressure and turbulent flux ($\alpha_p = \alpha_t = 0$), with turbulent energy and coupling term defined at the interfaces.

This initial model is constructed by integration of the static equilibrium equations from the surface inward.

Convective Hydrocodes for Radial Stellar Pulsation

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Simulations

The static model is constructed in **two steps**.

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This initial model is constructed by integration of the static equilibrium equations from the surface inward.

The final model, with turbulent pressure and turbulent flux included and with turbulent energy and coupling term defined at the zones, is constructed through the **multivariate Newton-Raphson iterations**.

Newton's method (also called Newton-Raphson) is an iterative method for finding the roots of a differentiable function f , which are solutions to the equation $f(x) = 0$.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko effect

Motivation

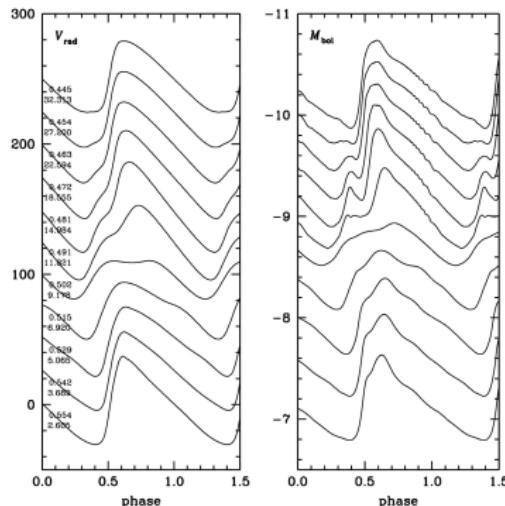
What?

How?

Why?

Simulations

For **testing the code**, Smolec & Moskalik (2008) use Galactic chemical composition, $X = 0.7$ and $Z = 0.02$, and mass-luminosity relation:
 $\log(L/L_\odot) = 3.56 \log(M/M_\odot) + 0.7328$ (Szabó et al. 2007).



Full amplitude radial velocity curves (left panel) and bolometric light curves (right panel). Model masses are increasing by $0.5 M_\odot$, starting from $4.0 M_\odot$ at the bottom of the figures up to $9 M_\odot$ at the top. Source: Smolec & Moskalik (2008), Fig. 5.

Concerning ϕ_{21} the model curves are shifted toward shorter periods in comparison to observations. This is connected with the location of the $2\omega_0 = \omega_2$ resonance center.

Convective Hydrocodes for Radial Stellar Pulsation

The Blazhko
effect

Motivation

What?

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Simulations

Period-amplitude modulations, period doubling etc. can be found in some simulations,

e.g.:

Smolec, R.; Survey of non-linear hydrodynamic models of type-II Cepheids; MNRAS, 456, 3475 (2016); PDF, arXiv:1512.01550

Smolec, R., Moskalik, P.; Chaos in hydrodynamic BL Herculis models; MNRAS, 441, 101 (2014); PDF, arXiv:1403.4937

Convective Hydrocodes for Radial Stellar Pulsation

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Simulations

The possible models are constrained by **observational facts** and by the laws of physics.

According to Zoltán Kolláth (2018)¹, the major observational constraints that one should take into consideration are the following:

- The amplitude of the modulation is comparable to the amplitude of the pulsation mode itself. Most of the mechanisms in models are weak in generating large amplitude modulations.
- The incidence rate of modulated stars are high, about 50% (see e.g. Jurcsik et al., 2009; Prudil & Skarka, 2017). The models should also answer what is the selection process between modulated and stable pulsations.
- The observed time scale of the modulation is an important empirical parameter of the Blazhko effect - all modulation scales can be handled by the theory. In addition, multiple modulation scales present another restriction for most of the models.

¹ <https://www.pta.edu.pl/pliki/proc/vol16/v6p137.pdf>

Convective Hydrocodes for Radial Stellar Pulsation

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Simulations

- Structure of the side lobes, asymmetries, complex frequency displacements excludes lots of the mechanism.
- Extra (Additional) modes or peaks in the Fourier spectra can be a feature independent from the Blazhko effect, but the pulsation models should provide some clues on the multi-mode properties of RR Lyrae stars.
- Anomaly of the infrared and the radius modulation strength is a very recent constraint (Jurcsik & Hajdu, 2017; Jurcsik et al., 2018) on theory. It is also a dichotomy between radius variation and the light curve or it can be simply treated as the dependence of modulation amplitude on the depth of the stellar atmosphere.
- The occurrence of period doubling in Blazhko modulated light curves present another possible constraint on models. Note that it appears with high amplitude only at specific phases of the Blazhko cycle.
- Finally any idea that is not compatible with the known physics of stellar pulsation should be ruled out.

Outlook - Monday session

The Blazhko
effect

Motivation

What?

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Simulations

The Monday session (10 - 11h) is for QA.

We can also use it to discuss a paper of your choice.

If you want to do so, please provide me the link to the paper before.