

Scale of Fluctuation(SoF)

Ningxin Yang, PhD student

Concept of SoF

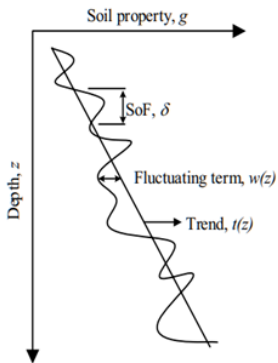
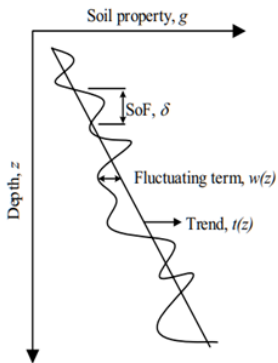


Figure 1: Illustration of the soil inherent variability[1]

Concept of SoF



The random field can be expressed as:

$$g(z) = t(z) + w(z) \quad (1)$$

Figure 1: Illustration of the soil inherent variability[1]

Concept of SoF

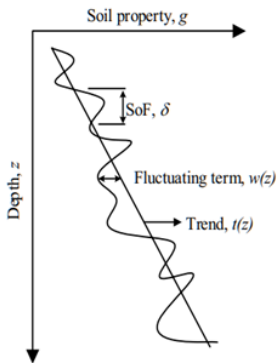


Figure 1: Illustration of the soil inherent variability[1]

The random field can be expressed as:

$$g(z) = t(z) + w(z) \quad (1)$$

Some bullet point list for SoF:

Concept of SoF

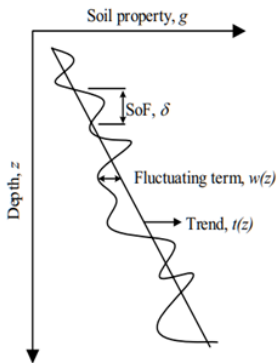


Figure 1: Illustration of the soil inherent variability[1]

The random field can be expressed as:

$$g(z) = t(z) + w(z) \quad (1)$$

Some bullet point list for SoF:

- soil are rarely homogeneous

Concept of SoF

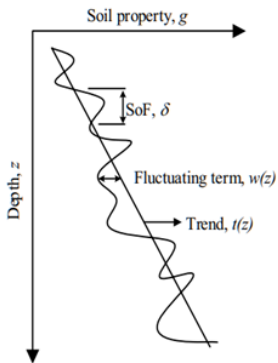


Figure 1: Illustration of the soil inherent variability[1]

The random field can be expressed as:

$$g(z) = t(z) + w(z) \quad (1)$$

Some bullet point list for SoF:

- soil are rarely homogeneous
- $g(z)$ can be detrended into a stationary random function $w(z)$

Concept of SoF

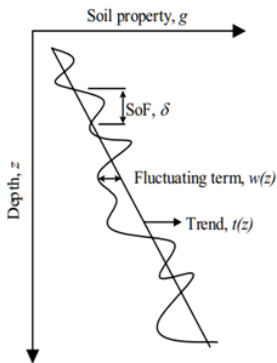


Figure 1: Illustration of the soil inherent variability[1]

The random field can be expressed as:

$$g(z) = t(z) + w(z) \quad (1)$$

Some bullet point list for SoF:

- soil are rarely homogeneous
- $g(z)$ can be detrended into a stationary random function $w(z)$
- indicator of the estimated distance over a soil property

Concept of SoF

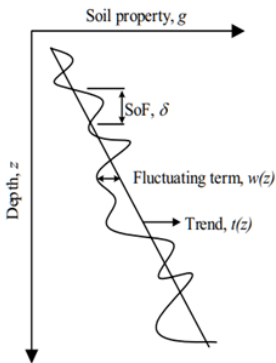


Figure 1: Illustration of the soil inherent variability[1]

The random field can be expressed as:

$$g(z) = t(z) + w(z) \quad (1)$$

Some bullet point list for SoF:

- soil are rarely homogeneous
- $g(z)$ can be detrended into a stationary random function $w(z)$
- indicator of the estimated distance over a soil property
- measure for spatial variability of a soil property in a random field

Characteristics of SoF

Characteristics of SoF

- 1 For the SoF reported, horizontal SoF is generally larger than the vertical SoF

Characteristics of SoF

- ① For the SoF reported, horizontal SoF is generally larger than the vertical SoF
- ② Vertical SoF is relatively narrow, from 0.06 to 2.6 m

Characteristics of SoF

- ① For the SoF reported, horizontal SoF is generally larger than the vertical SoF
- ② Vertical SoF is relatively narrow, from 0.06 to 2.6 m
- ③ horizontal SoF for CPT is fairly broad compared with Vertical SoF, from 0.14 to 80 m.

Calculation of SoF-ACFM method

$$\hat{\rho}(\tau) = \frac{\sum_{i=1}^{n(\tau)} [w(z_i) - \bar{w}] [w(z_i + \tau) - \bar{w}]}{[n(\tau) - 1] \hat{\sigma}^2} \quad (2)$$

where $\hat{\rho}(\tau)$ is autocorrelation function, \bar{w} and $\hat{\sigma}^2$ denote the sample mean and the sample variance of $w(z)$, $n(\tau)$ is number of lag distance τ

- Autocorrelation fitting method (ACFM) is to be one of the most widely used methods for estimating SoF.
- The main idea of ACFM is to fit theoretical models to the sample autocorrelation function $\hat{\rho}(\tau)$ based on an ordinary least squares approach

Table 1: Theoretical autocorrelation models

Model	Autocorrelation function
Triangular	$\rho(\tau) = \begin{cases} 1 - \tau /\delta & \tau \leq \delta \\ 0 & \tau > \delta \end{cases}$
Exponential	$\rho(\tau) = \exp\left(-\frac{2 \tau }{\delta}\right)$
Squared exponential	$\rho(\tau) = \exp\left(-\pi\left(\frac{\tau}{\delta}\right)^2\right)$
Cosine exponential	$\rho(\tau) = \cos\left(\frac{\tau}{\delta}\right) \exp\left(\frac{- \tau }{\delta}\right)$
Second-order Markov	$\rho(\tau) = \left(1 + \frac{4 \tau }{\delta}\right) \exp\left(-\frac{4 \tau }{\delta}\right)$

¹Note: τ is the separation distance and δ is the scale of fluctuation.

Five common theoretical autocorrelation models are given above

Imperial College
London

Calculation of SoF-Fitting

Calculation of SoF-Fitting

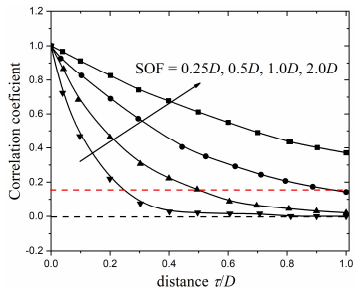
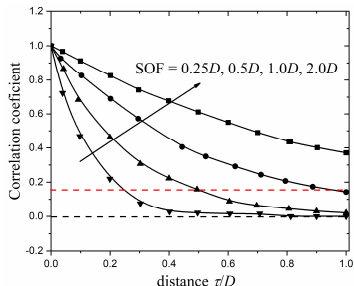


Figure 2: Illustration of the soil inherent variability followed [1]

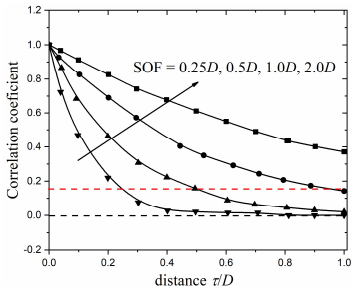
Calculation of SoF-Fitting



- Get autocorrelation coefficients for varying τ

Figure 2: Illustration of the soil inherent variability followed [1]

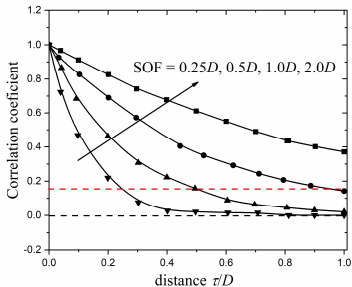
Calculation of SoF-Fitting



- Get autocorrelation coefficients for varying τ
- Utilize the autocorrelation function to fit the coefficients

Figure 2: Illustration of the soil inherent variability followed [1]

Calculation of SoF-Fitting



- Get autocorrelation coefficients for varying τ
- Utilize the autocorrelation function to fit the coefficients
- Obtain the distance as the intersection with the redline

Figure 2: Illustration of the soil inherent variability followed [1]

Reference

- [1] X Nie et al. “Scale of fluctuation for geotechnical probabilistic analysis scale of fluctuation for geotechnical probabilistic analysis”. In: *Proc. of the 5th International Symposium on Geotechnical Safety and Risk*. Vol. 1. 2015, pp. 834–40.