

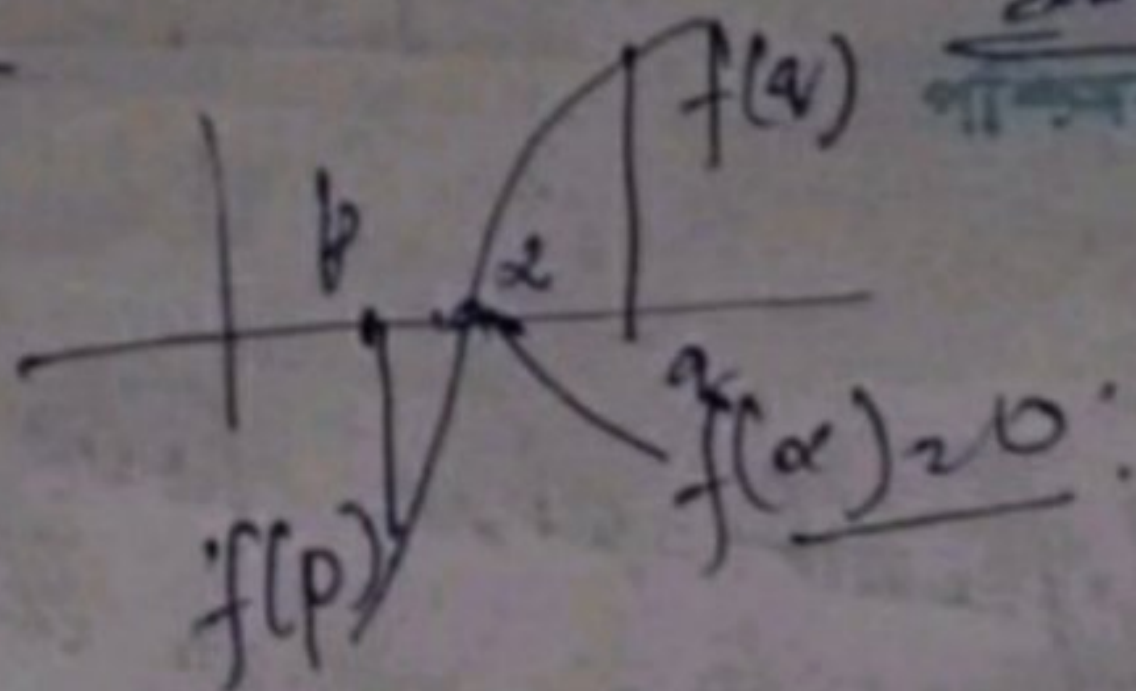
18/9/2020

Algebraic Eqⁿ - Eqⁿ containing polynomial terms.

Transcendental Equation :-

$$x_n \rightarrow \alpha \text{ as } n \rightarrow \infty$$

$$h_n = x_{n+1} - x_n \approx E_n - E_{n+1}$$



Saha Roy, Institute

Numerical analysis with algorithm & programming

$$\frac{f(a)f(p) < 0}{f(a)f(p) > 0} \rightarrow \text{either no root or even no. of roots}$$

$$y = x = \sin x$$

2.3 Initial App.



2.3.1 Graphical Method

Example 2.1

Example 2.2

2.4 Iterative Method

Theorem 2.2 Bisection Method:

2.4.3

Fixed point Iteration

Condition of Convergence for fixed-point Iteration Method

Example 2.6

$$f(x) = x^3 + x + 1 = 0$$

Table 2.8

2.44 NR Method

Initial guess

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)} \quad (2.21) \quad \frac{f(x_0) \neq 0}{\text{অন্যভাবে লিখা: } f(x_0) \neq 0}$$

2.4.4.2 Order of Convergence for NR Method ..

↳ (2) ..

Table 2.14 \Rightarrow Problem ..

Santanu Saha Ray

25.09.2020
Uttam Ghosh

1.3 { Approx. Method and
Significant figure }

1.3 Numerical Analysis

i) Absolute error $|x_T - x_A|$

$$\text{Relative Error} = \frac{|x_T - x_A|}{(x_T)}$$

Since, the another three types of error are -

i) Inherent Error

ii) Truncation Error

iii) Rounding off Error.

1.4 Rounding Off

1.4.3 Inherent Error

1.4.3.1

2.4.3 Fixed Point Iteration

$$f(x) = 0$$

Example 2.6

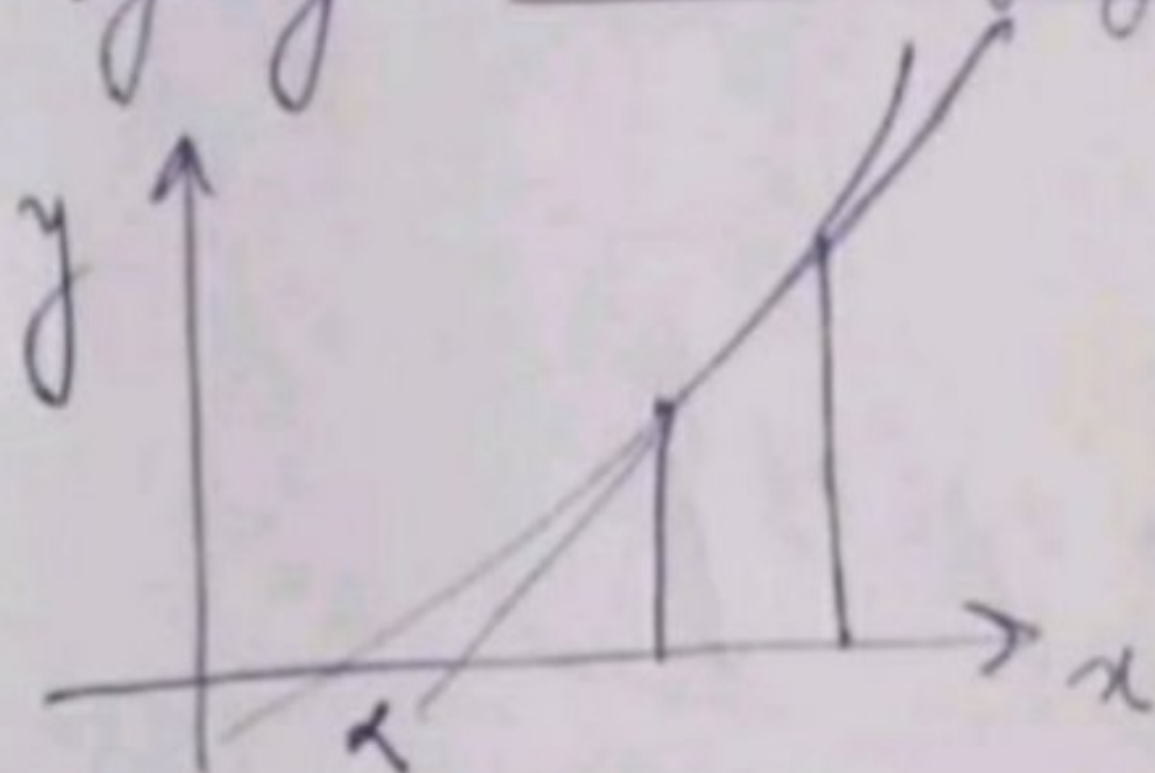
2.4.4 → Newton Raphson Method

Equation 2.21

Condition of Convergence

8-10-2020

for geometrical significance of NR



2.4.4.4 Advantages & Disadvantages of N-R Method

Ex: 2.9 $10^x + x - 4 = 0$

Hence the root is 0.5391791

Ex: 2.10 $x^2 - 10 \log_{10} x - 3$

2.4.5 Secant Method (Not in Syllabus).

2.4.5.2 Order of Convergence for the Secant Method.

"Bokrolekha"??
"Dhubak"

2.5 Generalized Newton Method (Modified)

$$f(x) = (x - \alpha)^r g(x) ; g(\alpha) \neq 0$$

$$\phi(x) = x - r \frac{f(x)}{f'(x)} \quad \text{such that} \quad \phi'(\alpha) \neq 0$$

$$f(x) \rightarrow (x - \alpha)^r g(x)$$

$$f'(x) \rightarrow (x - \alpha)^{r-1} \{ (x - \alpha) g'(x) + r g(x) \}$$

$$\frac{f(x)}{f'(x)} = (x - \alpha) \phi_1(x)$$

2.5.1.1 Newton's Method

Let (x_0, y_0) be an initial approx. of roots

On Taylor Expansion,

$$f(x_0, y_0) + \left(\Delta x \frac{\partial}{\partial x} + \right. \\ \left. g(x_0, y_0) \right)$$

Numerical

6.4.1 Guass Jacobi

6.4.1.1 Convergence

Example 6.9

6.4.2 Guass Seidel

Example 6.1.1

Book -Santanu

9:16 pm

Maths

VLG 08-01-2020

Properties

1. $K_n^{(m)} = K_{n-1}^{(m)}$

5.3.1 Deduction of Trapezoidal, Simpson's Qu. Third, + 174

Weddle's and

Pg-125. $\int_a^b f(x) dx = (b-a)$

Pg-127

Richardson Extrapolation \rightarrow 5.6

Uttam Sir

Gauss Elimination Method

Numerical Methods for Scientific and Engineering Computation

$$[A|b] \xrightarrow{\text{Gauss Elimination}} [U|c]$$

Partial Pivoting

Example 3.5

$$10x_1 - x_2 + 2x_3 = 4$$

Ex 3.7 $x_1 + x_2 + x_3 = 6$

Pg-113

zuo-hkx3-xdg

Uttam Sir

zuo-hkx2-xdg

5 (Numerical Integration with Algorithms and Programming) ✓

Ex. 1 $\int_a^b f(x) dx$ $\int_0^{\sqrt{\pi/2}} \sin^2(x) dx$ \rightarrow not differentiable \rightarrow Integrable \rightarrow Primitive function

Integrable functions \rightarrow Primitive function

$f(x) = \phi'(x)$
 $[f(x) = \phi'(x)]$ $\phi(x)$ is called Primitive function

② Only some functions can be integrated

$\sin^2(x)$ \rightarrow Integrate to a polynomial

$f(x) = P_n(x) + \frac{\pi(x) f^{(n+1)}(\xi)}{(n+1)!}$, where $a < \xi < b$.

$f(x) = \sum_{i=0}^n$

$\pi(x) = (x-x_0) \cdot \dots \cdot (x-x_n)$

5.3 Numerical Integration from Lagrange's Interpolation

$$R_{n+1}(f) = \int_a^b \frac{\pi(x)}{(n+1)!} dx.$$

प्राप्त किया गया

$$\pi(x) = (x-x_0) \cdots (x-x_n)$$

Definition 5.2 : Degree of Precision

5.3 Newton-Cotes formula for Numerical Interpolation

$$f(x) = \sum_{i=0}^n \frac{\pi(x)}{(x-x_i)\pi'(x_i)} y_i + \frac{\pi(x) f^{(n+1)}(\xi)}{(n+1)!}$$

$$\text{and } \int_a^b f(x) dx = \sum_{i=0}^n H_i^{(n)} y_i + R_n(f).$$

where $H_i^{(n)}$ and $R_n(f)$ are -

$$\begin{array}{l} \text{5.3} \\ \text{5.6} \\ \text{5.7} \end{array}$$

5.8

$$\int_a^b f(x) dx = \sum_{i=0}^n H_i^{(n)} y_i + R_n(f) = (b-a) \sum_{i=0}^n K_i^{(n)} y_i + R_n(f). \quad \text{Eq. 5.8}$$

Q. 2

(134)

गणित, नई दिल्ली

(5.24) $R_2(h) = \int_0^h f(x) dx = \frac{h}{2} ($

5.24

$I = I_1\left(\frac{h}{2}\right) + c_1\left(\frac{h^2}{4}\right) + c_2 \frac{h^4}{16} + c_3 \left(\frac{h^6}{64}\right) + \dots$ - 5.24

$I = (5.24) \rightarrow$ Fourth Order Error Term

Replacing h by $(h/2)$ in Eq. 5.24

$I = I_1\left(\frac{h}{2}\right)$

Example 55 Pg 228

16/15.01.2020

Pg. - 229

$$I = \int_a^b w(x) f(x) dx = \int_a^b w(x) f(x) dx \quad \text{--- (5.85)}$$

$$x = \left[\frac{b-a}{2} \right] u + \left[\frac{b+a}{2} \right]$$

$w(x) > 0$ ($a \leq x \leq b$)
the weight
function

$$y = f(x) = f\left(\frac{b-a}{2} u + \frac{b+a}{2}\right) = \phi(u)$$

$$w(x) = w\left(\frac{b-a}{2} u + \frac{b+a}{2}\right) = \psi(u)$$

$$w_1 \phi(u) + w_2 \phi(u)$$

~~5.8.1 Gauss Legendre Integration Method~~

5.8.1 Gauss Legendre Integration Method

(Pg)
(231)

$$\int_a^b f(x) dx \approx (b-a) f\left(\frac{a+b}{2}\right) \quad \text{--- 5.94}$$

5.9 Gaussian Quadrature

Theorem 5.3 :-

2.1, 2.2, 2.3, 2.4.3, 2.4.3.1, 2.4.4, 2.4.4.1, 2.4.4.2
2.4.4.3, 2.4.4.4, 2.4.5, 2.4.5.1, 2.4.5.2, 2.4.5.3, 2.5

2.5.1, Game elimination

6.4.1, 6.4.1.1, 6.4.2

5.2, 5.3, 5.7, 5.8, 5.9