

# Distributed Mutual Exclusion Algorithms II

Different Approaches



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## Outline

- Ricart-Agrawala algorithm
- Token based algorithm for Ring topology
- Raymond's algorithm
- Limitations of Raymond's algorithm
- Quorum based algorithm

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## Latency and Raymond's Algorithm



- The process of decision making takes place in multiple number of nodes.
  - There could be a high latency involved in the process.
  - The amount of latency depends on number of concurrent requests and height of the tree.
  - It may be worth keeping in mind that the inverted tree structure does not assume that it's a height-balanced tree.

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## Deadlock and Raymond's Algorithm



- Deadlock may occur if and only if one or more of the following conditions are true:
  1. Token cannot be transferred to a node because no node holds the privilege.
  2.  $P_{\text{hold}}$  is unaware that there are other nodes requiring the token.
  3. The token does not reach the requesting node.

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## Deadlock and Raymond's Algorithm



1. Token cannot be transferred to a node because no node holds the token.
  - This scenario can not occur for Raymond's algorithm because we have assumed that the network is reliable, and messages are not lost.

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## Deadlock and Raymond's Algorithm



2.  $P_{hold}$  is unaware that there are other nodes requiring the token.
  - The algorithm ensures that a node that needs the token sends a REQUEST message either to  $P_{hold}$  directly or to a node that has a path to  $P_{hold}$ .
  - Thus condition 2 can never occur.

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## Deadlock and Raymond's Algorithm

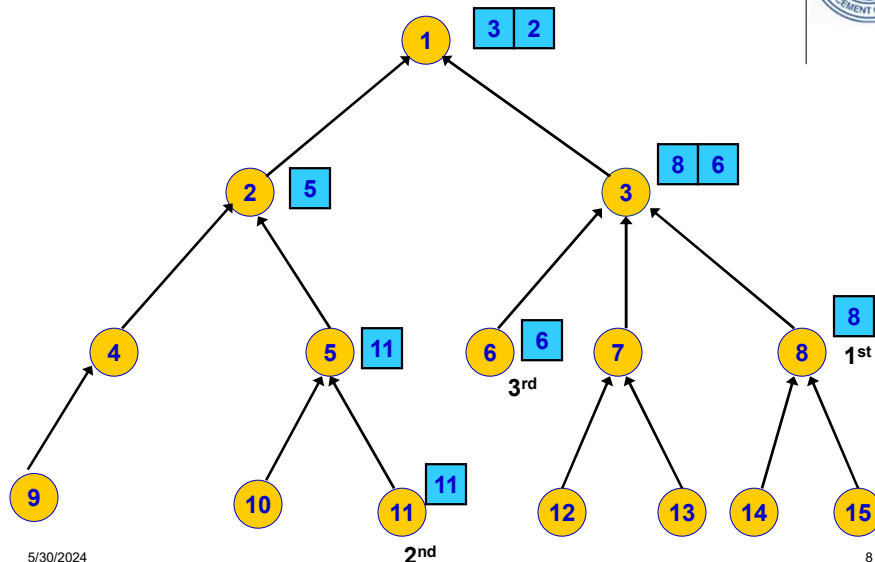


3. The token does not reach the requesting node.

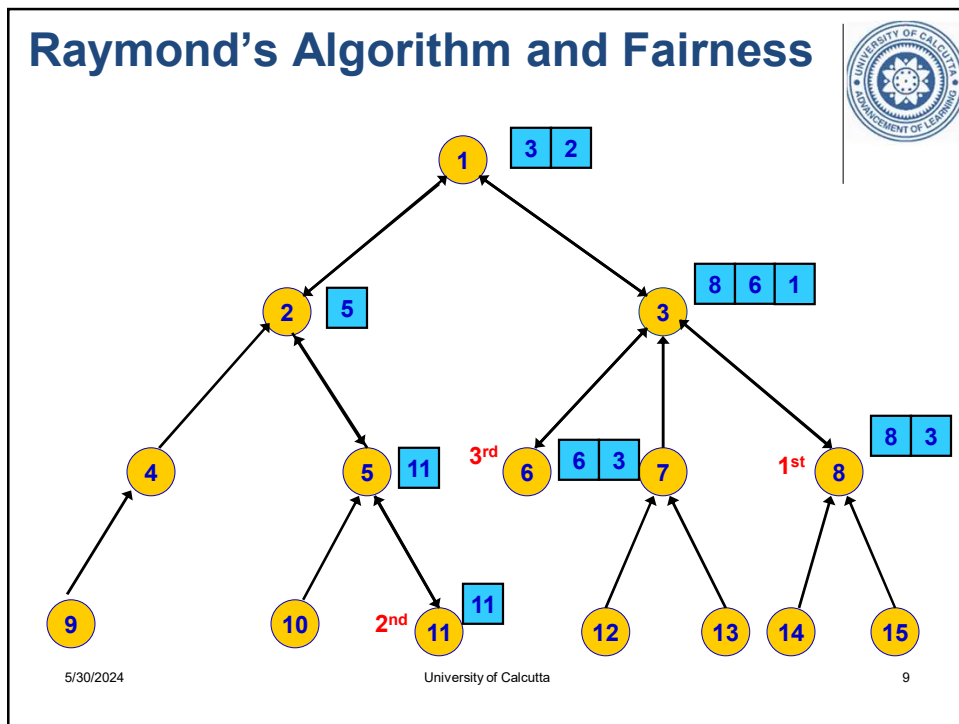
- The series of REQUEST messages are saved in the local Qs in various nodes such that the REQUEST Qs of those nodes collectively provide a logical path for the transfer of the token from  $P_{hold}$  to the requesting nodes.
- Thus, scenario 3 too can never occur.

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## Raymond's Algorithm and Fairness



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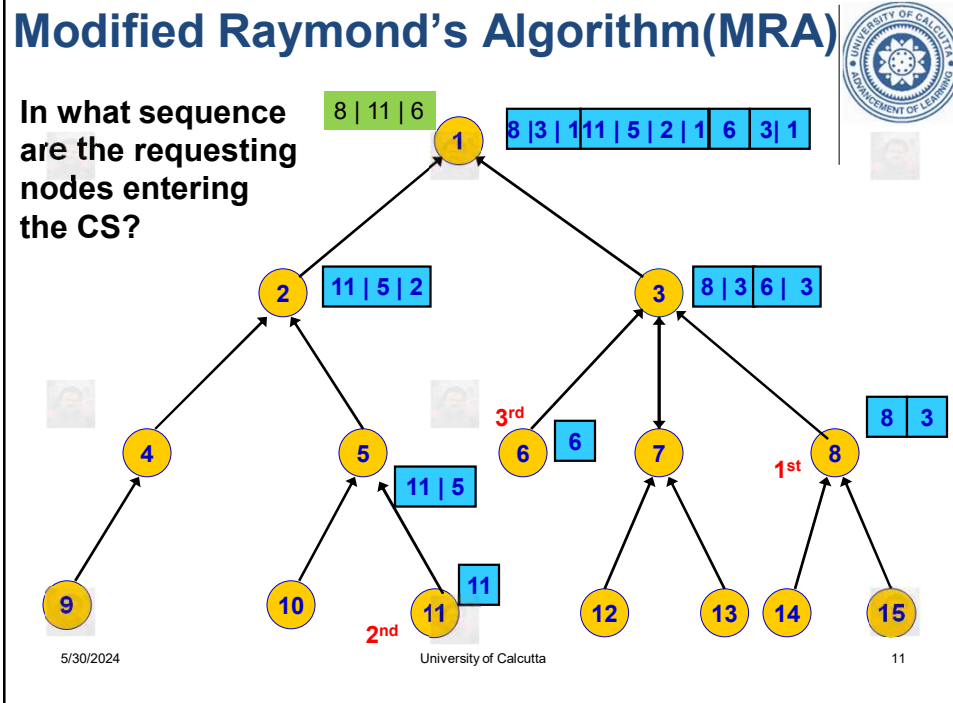


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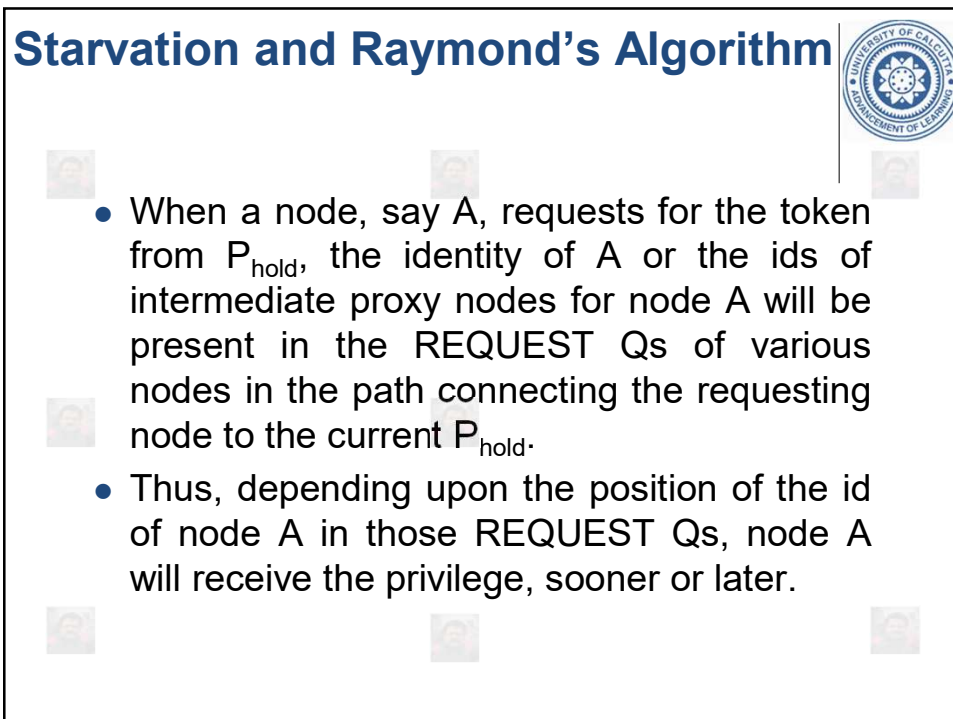
## How do you solve?

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## Outline



- Ricart-Agrawala algorithm
- Token based algorithm for Ring topology
- Raymond's algorithm
- Limitations of Raymond's algorithm
- **Quorum based algorithm**

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## Coterie and Quorums



- A Coterie  $C$  is defined as a set of sets, where each set  $g \in C$  is called a Quorum.
- The following two properties hold for Quorums in a Coterie:
  - Intersection Property
  - Minimality Property

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## Properties of Quorums



- Intersection Property
  - $\forall g \forall h \in C, g \cap h \neq \phi$ .
  - e.g., sets  $\{1,2,3\}$ ,  $\{2,5,7\}$  and  $\{5,8,9\}$  cannot be quorums in a coterie as the first and third sets do not have a common element.
- Minimality Property
  - No quorums  $g, h \notin C: (g \supseteq h) \vee (h \supseteq g)$ .
  - e.g., sets  $\{1,2,3\}$  and  $\{1,3\}$  cannot be quorums in a coterie as  $\{1, 2, 3\} \supseteq \{1, 3\}$ .

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## Basic Idea for Quorum-based DME



- Let  $a$  be a site in quorum  $A$ .
- If  $a$  wants to invoke mutual exclusion, it requests permission from all sites in its quorum  $A$ .
- Every site does the same to invoke mutual exclusion.

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## Basic Idea for Quorum-based DME



- As per Intersection property, quorum A contains at least one common site included in a quorum for every other site in the coterie.
- These common sites send permission to only one site at any time.

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## Basic Idea for Quorum-based DME



- Thus, safety in execution is guaranteed.
- Minimality property ensures efficiency rather than correctness
- While designing for individual Quorum-based algorithms, one has to ensure
  - Liveness
  - Deadlock-free execution

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## Quorum based DME Algorithms



- Let's assume two lists in every site  $S_k$ :
  - The first list  $R_k$  is called request set.
  - It contains IDs of the sites from which  $S_k$  must acquire permission before its CS.
  - The second list  $RP_k$  is called response set.
  - It contains IDs of the sites to which  $S_k$  must send its permission to execute CS after executing its own CS.

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## Quorum based DME Algorithms



- Quorum-based DME algorithms are different in the following two ways:
  - A site does not request permission from all other sites, but only from a subset.
  - The request set of sites are chosen such that  $\forall m \forall n: 1 \leq m, n \leq N :: R_m \cap R_n \neq \phi$ .
  - Consequently, every pair of sites has at least one site that arbitrates between that pair.

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## Quorum based DME Algorithms



- A site can send out only one REPLY message at any time.
- A site can send a REPLY message only after it has received a RELEASE message for the previous REPLY message.

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**Thanks for your kind attention**

**Questions??**

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