$$\alpha_{t}(i) = P(X_{1:t}|z_{t} = i)$$