$$\beta_{\mathbf{t}}(i) = P(X_{\mathbf{t+1:T}}|z_{\mathbf{t}} = i)$$