$$\alpha_t(i) = P(X_{1:t}|z_t = i)$$