$$\beta_t(i) = P(X_{t+1:T} | z_t = i)$$