

SUPERVISED LEARNING

[HTTPS://WWW.LINKEDIN.COM/IN/KETANKOTECHA/](https://www.linkedin.com/in/ketankotecha/)



An example application

2

- An emergency room in a hospital measures 17 variables (e.g., blood pressure, age, etc) of newly admitted patients.
- A decision is needed: whether to put a new patient in an intensive-care unit.
- Due to the high cost of ICU, those patients who may survive less than a month are given higher priority.
- Problem: to predict high-risk patients and discriminate them from low-risk patients.

Another application

3

- A credit card company receives thousands of applications for new cards. Each application contains information about an applicant,
 - age
 - Marital status
 - annual salary
 - outstanding debts
 - credit rating
 - etc.
- Problem: to decide whether an application should be approved, or to classify applications into two categories, approved and not approved.

Machine learning

4

- Like human learning from past experiences.
- A computer does not have “experiences”.
- A computer system learns from data, which represent some “past experiences” of an application domain.
- Our focus: learn a target function that can be used to predict the values of a discrete class attribute, e.g., approve or not-approved, and high-risk or low risk.
- The task is commonly called: Supervised learning, classification, or inductive learning.

The data and the goal

5

- Data: A set of data records (also called examples, instances or cases) described by
 - k attributes: A_1, A_2, \dots, A_k .
 - a class: Each example is labelled with a pre-defined class.
- Goal: To learn a classification model from the data that can be used to predict the classes of new (future, or test) cases/instances.

An example: data (loan application)

Approved or not

6

ID	Age	Has_Job	Own_House	Credit_Rating	Class
1	young	false	false	fair	No
2	young	false	false	good	No
3	young	true	false	good	Yes
4	young	true	true	fair	Yes
5	young	false	false	fair	No
6	middle	false	false	fair	No
7	middle	false	false	good	No
8	middle	true	true	good	Yes
9	middle	false	true	excellent	Yes
10	middle	false	true	excellent	Yes
11	old	false	true	excellent	Yes
12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

An example: the learning task

- Learn a classification model from the data
- Use the model to classify future loan applications into
 - ▣ Yes (approved) and
 - ▣ No (not approved)
- What is the class for following case/instance?

Age	Has_Job	Own_house	Credit-Rating	Class
young	false	false	good	?

Supervised vs. unsupervised Learning

8

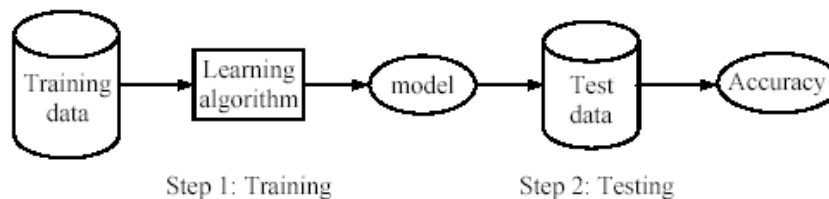
- Supervised learning: classification is seen as supervised learning from examples.
 - ▣ Supervision: The data (observations, measurements, etc.) are labeled with pre-defined classes. It is like that a “teacher” gives the classes (supervision).
 - ▣ Test data are classified into these classes too.
- Unsupervised learning (clustering)
 - ▣ Class labels of the data are unknown
 - ▣ Given a set of data, the task is to establish the existence of classes or clusters in the data

Supervised learning process

9

- Learning (training): Learn a model using the training data
- Testing: Test the model using unseen test data to assess the model accuracy

$$Accuracy = \frac{\text{Number of correct classifications}}{\text{Total number of test cases}},$$



What do we mean by learning?

10

- Given

- a data set D ,
- a task T , and
- a performance measure M ,

a computer system is said to **learn** from D to perform the task T if after learning the system's performance on T improves as measured by M .

- In other words, the learned model helps the system to perform T better as compared to no learning.

An example

11

- Data: Loan application data
- Task: Predict whether a loan should be approved or not.
- Performance measure: accuracy.

No learning: classify all future applications (test data) to the majority class (i.e., Yes):

$$\text{Accuracy} = 9/15 = 60\%.$$

- We can do better than 60% with learning.

Fundamental assumption of learning

■ 12

Assumption: The distribution of training examples is identical to the distribution of test examples (including future unseen examples).

- In practice, this assumption is often violated to certain degree.
- Strong violations will clearly result in poor classification accuracy.
- To achieve good accuracy on the test data, training examples must be sufficiently representative of the test data.

Decision Tree

■13

- Decision tree learning is one of the most widely used techniques for classification.
 - ▣ Its classification accuracy is competitive with other methods, and
 - ▣ it is very efficient.
- The classification model is a tree, called decision tree.
- C4.5 by Ross Quinlan is perhaps the best known system. It can be downloaded from the Web.

The loan data (reproduced)

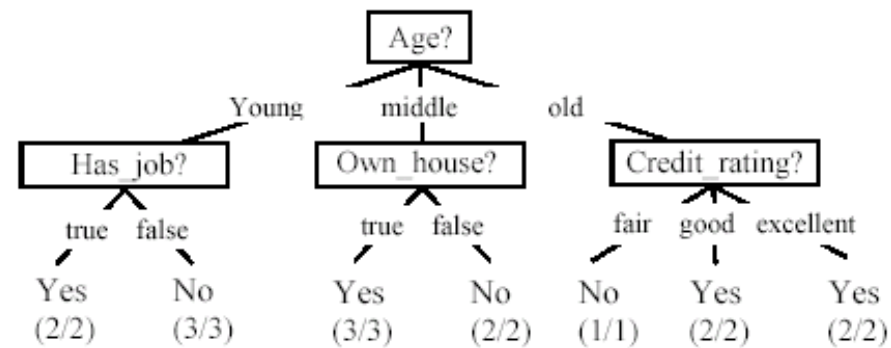
Approved or not

ID	Age	Has_Job	Own_House	Credit_Rating	Class
1	young	false	false	fair	No
2	young	false	false	good	No
3	young	true	false	good	Yes
4	young	true	true	fair	Yes
5	young	false	false	fair	No
6	middle	false	false	fair	No
7	middle	false	false	good	No
8	middle	true	true	good	Yes
9	middle	false	true	excellent	Yes
10	middle	false	true	excellent	Yes
11	old	false	true	excellent	Yes
12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

A decision tree from the loan data

■ 15

- Decision nodes and leaf nodes (classes)

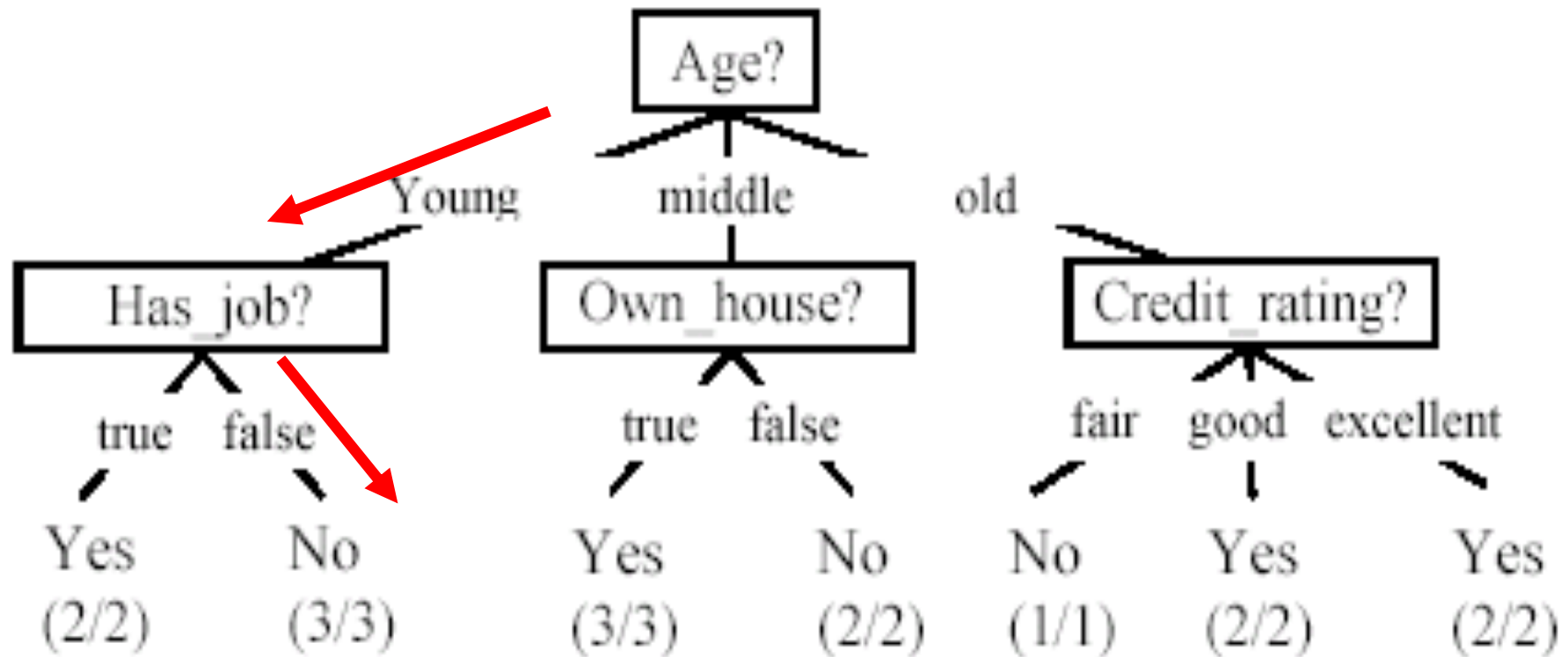


Use the decision tree

16

Age	Has_Job	Own_house	Credit-Rating	Class
young	false	false	good	?

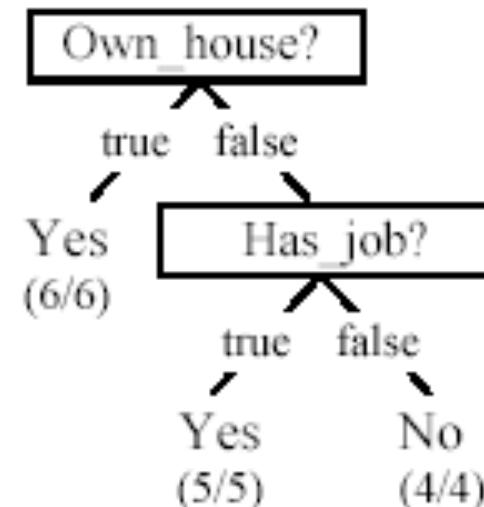
No



Is the decision tree unique?

■ 17

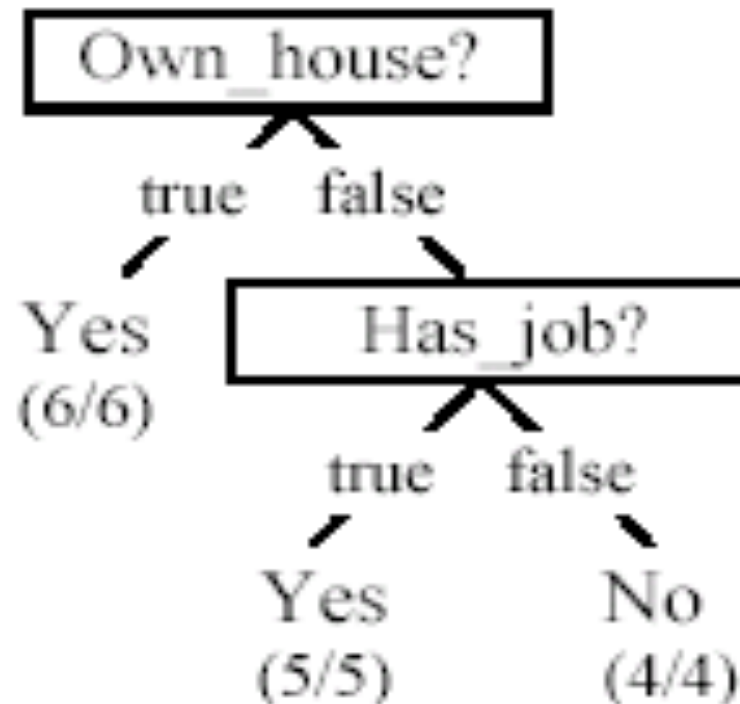
- No. Here is a simpler tree.
- We want smaller tree and accurate tree.
 - Easy to understand and perform better.
- Finding the best tree is NP-hard.
- All current tree building algorithms are heuristic algorithms



From a decision tree to a set of rules

18

- A decision tree can be converted to a set of rules
- Each path from the root to a leaf is a rule.



Own_house = true → Class = Yes [sup=6/15, conf=6/6]

Own_house = false, Has_job = true → Class = Yes [sup=5/15, conf=5/5]

Own_house = false, Has_job = false → Class = No [sup=4/15, conf=4/4]

Algorithm for decision tree learning

1

- Basic algorithm (a greedy **divide-and-conquer** algorithm)
 - ▣ Assume attributes are categorical now (continuous attributes can be handled too)
 - ▣ Tree is constructed in a top-down recursive manner
 - ▣ At start, all the training examples are at the root
 - ▣ Examples are partitioned recursively based on selected attributes
 - ▣ Attributes are selected on the basis of an impurity function (e.g., information gain)
- Conditions for stopping partitioning
 - ▣ All examples for a given node belong to the same class
 - ▣ There are no remaining attributes for further partitioning – majority class is the leaf
 - ▣ There are no examples left

Decision tree learning algorithm

. **Algorithm** decisionTree(D, A, T)

```
1  if  $D$  contains only training examples of the same class  $c_j \in C$  then
2      make  $T$  a leaf node labeled with class  $c_j$ ;
3  elseif  $A = \emptyset$  then
4      make  $T$  a leaf node labeled with  $c_j$ , which is the most frequent class in  $D$ 
5  else //  $D$  contains examples belonging to a mixture of classes. We select a single
6      // attribute to partition  $D$  into subsets so that each subset is purer
7       $p_0 = \text{impurityEval-1}(D)$ ;
8      for each attribute  $A_i \in \{A_1, A_2, \dots, A_k\}$  do
9           $p_i = \text{impurityEval-2}(A_i, D)$ 
10     end
11     Select  $A_g \in \{A_1, A_2, \dots, A_k\}$  that gives the biggest impurity reduction,
        computed using  $p_0 - p_i$ ;
12     if  $p_0 - p_g < \text{threshold}$  then //  $A_g$  does not significantly reduce impurity  $p_0$ 
13         make  $T$  a leaf node labeled with  $c_j$ , the most frequent class in  $D$ .
14     else //  $A_g$  is able to reduce impurity  $p_0$ 
15         Make  $T$  a decision node on  $A_g$ ;
16         Let the possible values of  $A_g$  be  $v_1, v_2, \dots, v_m$ . Partition  $D$  into  $m$ 
            disjoint subsets  $D_1, D_2, \dots, D_m$  based on the  $m$  values of  $A_g$ .
17         for each  $D_j$  in  $\{D_1, D_2, \dots, D_m\}$  do
18             if  $D_j \neq \emptyset$  then
19                 create a branch (edge) node  $T_j$  for  $v_j$  as a child node of  $T$ ;
20                 decisionTree( $D_j, A - \{A_g\}, T_j$ ) //  $A_g$  is removed
21             end
22         end
23     end
24 end
```

Choose an attribute to partition data

21

- The *key* to building a decision tree - which attribute to choose in order to branch.
- The objective is to reduce impurity or uncertainty in data as much as possible.
 - ▣ A subset of data is pure if all instances belong to the same class.
- The *heuristic* in C4.5 is to choose the attribute with the maximum Information Gain or Gain Ratio based on information theory.

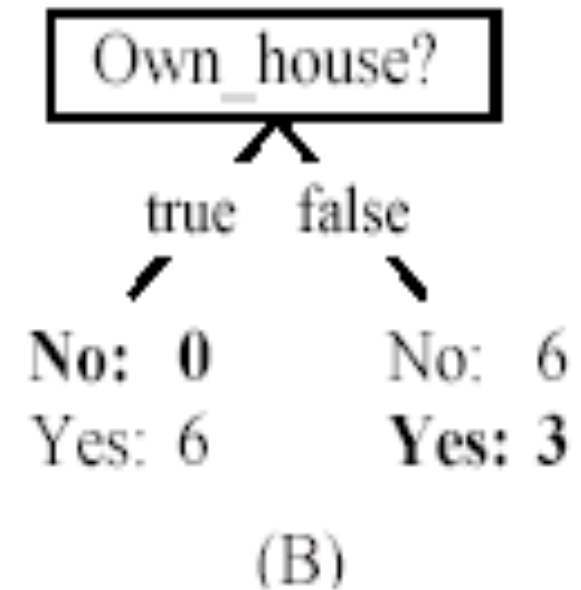
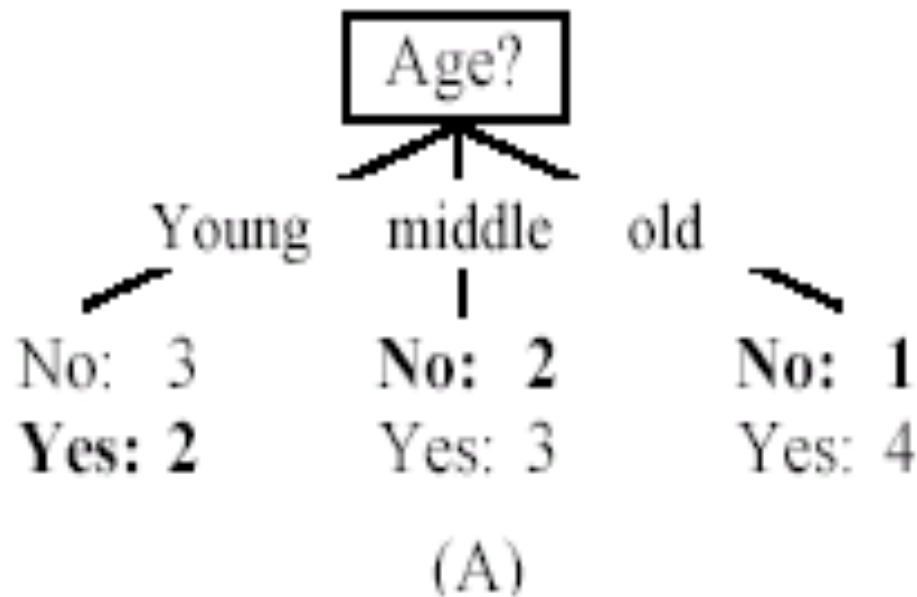
The loan data (reproduced)

Approved or not

ID	Age	Has_Job	Own_House	Credit_Rating	Class
1	young	false	false	fair	No
2	young	false	false	good	No
3	young	true	false	good	Yes
4	young	true	true	fair	Yes
5	young	false	false	fair	No
6	middle	false	false	fair	No
7	middle	false	false	good	No
8	middle	true	true	good	Yes
9	middle	false	true	excellent	Yes
10	middle	false	true	excellent	Yes
11	old	false	true	excellent	Yes
12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

Two possible roots, which is better?

23



- Fig. (B) seems to be better.

Information theory

■24

- Information theory provides a mathematical basis for measuring the information content.
- To understand the notion of information, think about it as providing the answer to a question, for example, whether a coin will come up heads.
 - ▣ If one already has a good guess about the answer, then the actual answer is less informative.
 - ▣ If one already knows that the coin is rigged so that it will come with heads with probability 0.99, then a message (advanced information) about the actual outcome of a flip is worth less than it would be for a honest coin (50-50).

Information theory (cont ...)

25

- For a fair (honest) coin, you have no information, and you are willing to pay more (say in terms of \$) for advanced information - less you know, the more valuable the information.
- Information theory uses this same intuition, but instead of measuring the value for information in dollars, it measures information contents in **bits**.
- One bit of information is enough to answer a yes/no question about which one has no idea, such as the flip of a fair coin

Information theory: Entropy measure

- The entropy formula,

$$\text{entropy}(D) = - \sum_{j=1}^{|C|} \text{Pr}(c_j) \log_2 \text{Pr}(c_j)$$

$$\sum_{j=1}^{|C|} \text{Pr}(c_j) = 1,$$

- $\text{Pr}(c_i)$ is the probability of class c_i in data set D
- We use entropy as a measure of impurity or disorder of data set D . (Or, a measure of information in a tree)

Entropy measure: let us get a feeling

■ 27

1. The data set D has 50% positive examples ($\Pr(\text{positive}) = 0.5$) and 50% negative examples ($\Pr(\text{negative}) = 0.5$).

$$\text{entropy}(D) = -0.5 \times \log_2 0.5 - 0.5 \times \log_2 0.5 = 1$$

2. The data set D has 20% positive examples ($\Pr(\text{positive}) = 0.2$) and 80% negative examples ($\Pr(\text{negative}) = 0.8$).

$$\text{entropy}(D) = -0.2 \times \log_2 0.2 - 0.8 \times \log_2 0.8 = 0.722$$

3. The data set D has 100% positive examples ($\Pr(\text{positive}) = 1$) and no negative examples, ($\Pr(\text{negative}) = 0$).

$$\text{entropy}(D) = -1 \times \log_2 1 - 0 \times \log_2 0 = 0$$

- As the data become purer and purer, the entropy value becomes smaller and smaller. This is useful to us!

Information gain

- Given a set of examples D , we first compute its entropy:

$$\text{entropy}(D) = - \sum_{j=1}^{|C|} \text{Pr}(c_j) \log_2 \text{Pr}(c_j)$$

- If we make attribute A_i , with v values, the root of the current tree, this will partition D into v subsets D_1, D_2, \dots, D_v . The expected entropy if A_i is used as the current root:

$$\text{entropy}_{A_i}(D) = \sum_{j=1}^v \frac{|D_j|}{|D|} \times \text{entropy}(D_j)$$

Information gain (cont ...)

- Information gained by selecting attribute A_i to branch or to partition the data is

$$\text{gain}(D, A_i) = \text{entropy}(D) - \text{entropy}_{A_i}(D)$$

- We choose the attribute with the highest gain to branch/split the current tree.

An example

ID	Age	Has_Job	Own_House	Credit_Rating	Class
1	young	false	false	fair	No
2	young	false	false	excellent	No
3	young	true	false	good	Yes
4	young	true	true	good	Yes
5	young	false	false	fair	No
6	middle	false	false	fair	No
7	middle	false	false	good	No
8	middle	true	true	good	Yes
9	middle	false	true	excellent	Yes
10	middle	false	true	excellent	Yes
11	old	false	true	excellent	Yes
12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

$$entropy(D) = -\frac{6}{15} \times \log_2 \frac{6}{15} - \frac{9}{15} \times \log_2 \frac{9}{15} = 0.971$$

$$\begin{aligned}
 entropy_{Own_house}(D) &= -\frac{6}{15} \times entropy(D_1) - \frac{9}{15} \times entropy(D_2) \\
 &= \frac{6}{15} \times 0 + \frac{9}{15} \times 0.918 \\
 &= 0.551
 \end{aligned}$$

$$\begin{aligned}
 entropy_{Age}(D) &= -\frac{5}{15} \times entropy(D_1) - \frac{5}{15} \times entropy(D_2) - \frac{5}{15} \times entropy(D_3) \\
 &= \frac{5}{15} \times 0.971 + \frac{5}{15} \times 0.971 + \frac{5}{15} \times 0.722 \\
 &= 0.888
 \end{aligned}$$

Age	Yes	No	entropy(Di)
young	2	3	0.971
middle	3	2	0.971
old	4	1	0.722

$$gain(D, Age) = 0.971 - 0.888 = 0.083$$

$$gain(D, Own_house) = 0.971 - 0.551 = 0.420$$

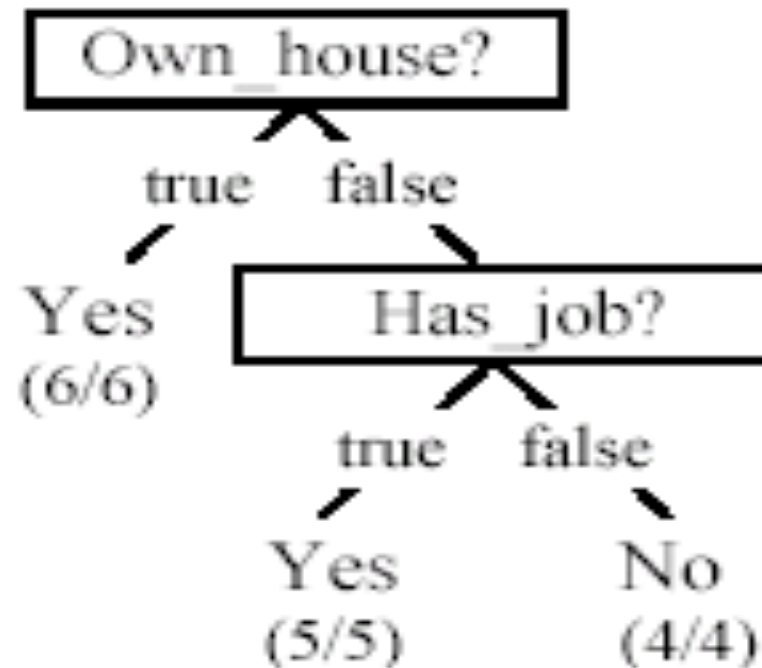
$$gain(D, Has_Job) = 0.971 - 0.647 = 0.324$$

$$gain(D, Credit_Rating) = 0.971 - 0.608 = 0.363$$

- Own_house is the best choice for the root.

We build the final tree

■ 31



- We can use information gain ratio to evaluate the impurity as well