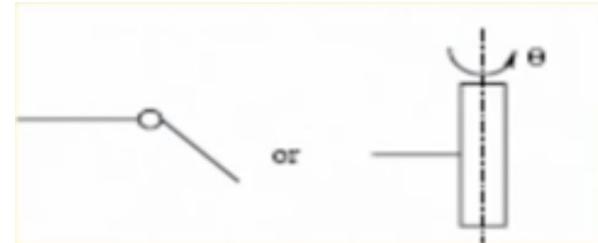


Introduction to robots and robotics

Representation of the joints

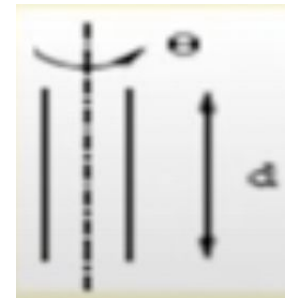
Revolute Joint (R)



Prismatic Joint (p)



Cylindrical Joint (C)

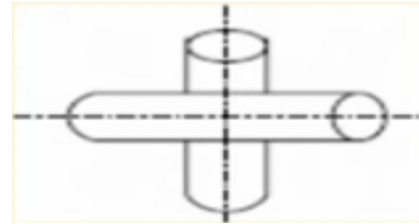


Representation of the Joints

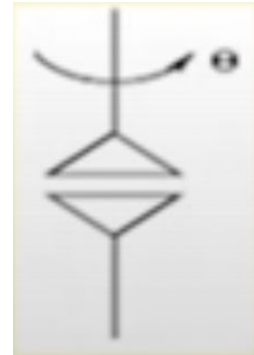
Spherical Joint (S')



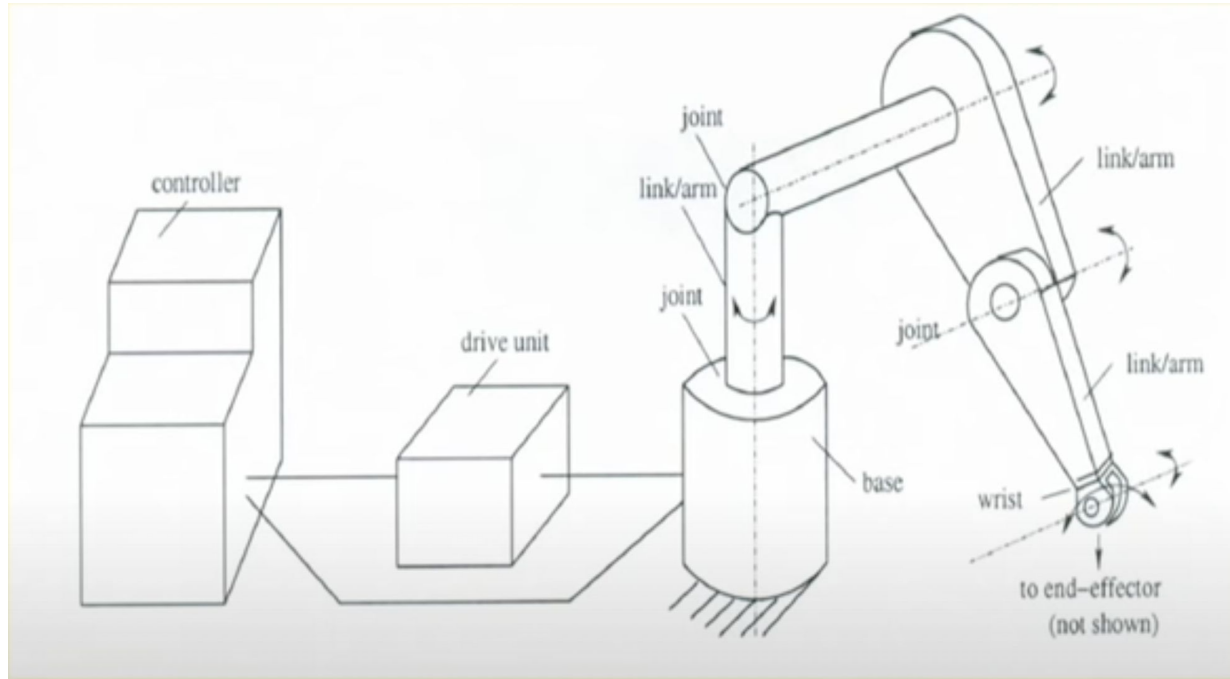
Hooke Joint (U)



Twisting Joint (T)



Kinematic Diagram



Degrees of Freedom of a system

It is defined as the minimum number of independent parameters/variables/coordinates needed to describe a system completely.

Notes:

- ❖ A point in 2-D: 2dof; In 3-D space:3 dof
- ❖ A rigid body in 3-D: 6 dof
- ❖ Spatial Manipulator:6 dof
- ❖ Planar Manipulator: 3 dof

Redundant Manipulator

Either a spatial manipulator with more than 6 dof or a planar manipulator with more than 3 dof

Under-actuated Manipulator

Either a spatial manipulator with less than 6 dof or a planar manipulator with less than 3 dof

- Mini Mover 5 dof

Mobility/ dof of spatial Manipulator

Let us consider a manipulator with n rigid moving links and m joints

C_i : connectivity of i -th joints; $i=1,2,3,\dots,m$

No. of constraints put by i -th joint $= 6 - C_i$

Total number of constraints $= \sum_{i=1}^m (6 - C_i)$

Mobility of the manipulator $M = 6n - \sum_{i=1}^m (6 - C_i)$

It is known as Grubler's criterion.

Mobility/ dof of planar Manipulator

Let us consider a manipulator with n rigid moving links and m joints

C_i : connectivity of i -th joints; $i=1,2,3,\dots,m$

No. of constraints put by i -th joint $= 3 - C_i$

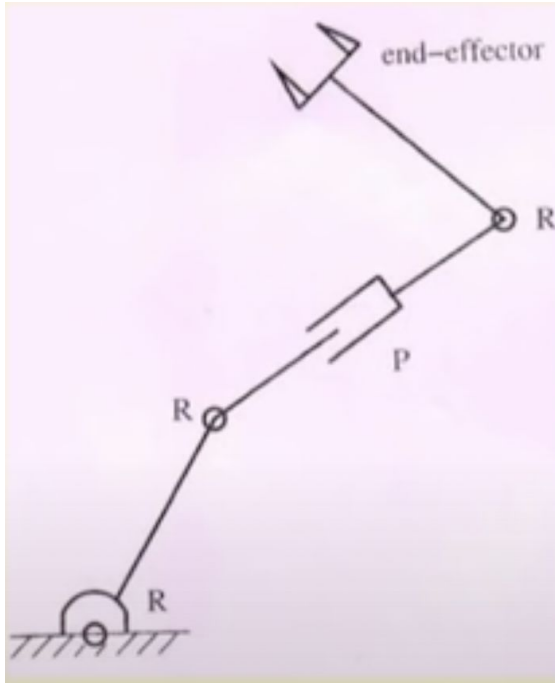
Total number of constraints $= \sum_{i=1}^m (3 - C_i)$

Mobility of the manipulator $M = 3n - \sum_{i=1}^m (3 - C_i)$

It is known as Grubler's criterion.

Numerical example

Serial Planar Manipulator



$$n=4, m=4$$

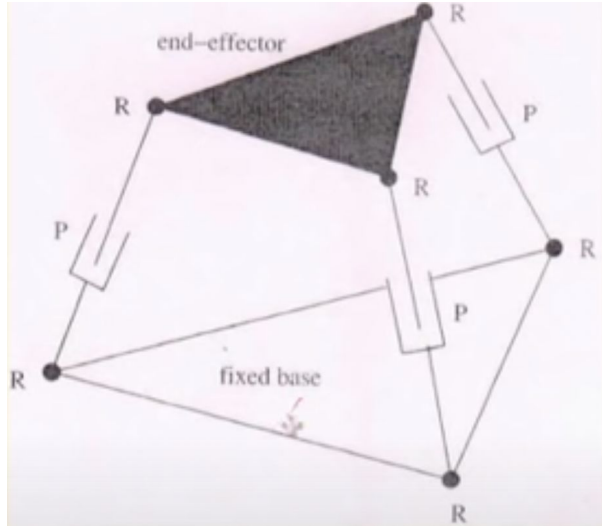
$$c_1=c_2=c_3=c_4=1$$

Mobility/dof:

$$M=3n-\sum_{i=1}^m(3-C_i)=3*4-8=4$$

Numerical example

Parallel I Planar Manipulator



$$n=7, m=9$$

$$c_i=1 \text{ where } i=1, \dots, 9$$

Mobility/dof:

$$M=3n-\sum_{i=1}^m(3-C_i)=3*7-18=3$$

References

- <https://www.instructables.com/Arduino-Controlled-Robotic-Biped/>
- <https://www.youtube.com/watch?v=xrwz9lxpMJg&t=893s>
- [https://en.wikipedia.org/wiki/Optimus_\(robot\)](https://en.wikipedia.org/wiki/Optimus_(robot))