# Models with multiple predictors

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# The linear model with multiple predictors



## Data: Book weight and volume

The allbacks data frame gives measurements on the volume and weight of 15 books, some of which are paperback and some of which are hardback

- Volume cubic centimetres
- Area square centimetres
- Weight grams

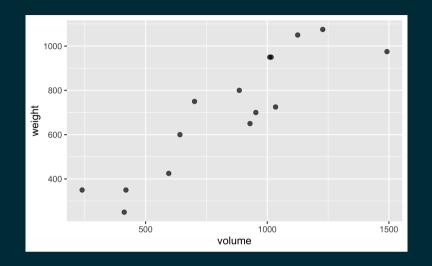
```
## # A tibble: 15 \times 4
      volume
             area weight cover
       <dbl> <dbl>
                     <dbl> <fct>
         885
               382
                       800 hb
        1016
               468
                       950 hb
        1125
               387
                      1050 hb
         239
                       350 hb
                371
         701
                       750 hb
         641
                       600 hb
        1228
                      1075 hb
         412
                       250 pb
         953
                       700 pb
         929
                       650 pb
        1492
                       975 pb
         419
                       350
        1010
                       950 pb
         595
                       425 pb
        1034
                       725 pb
```

These books are from the bookshelf of J. H. Maindonald at Australian National University.

# Book weight vs. volume

```
linear_reg() %>%
  set_engine("lm") %>%
  fit(weight ~ volume, data = allbacks) %>
  tidy()
```

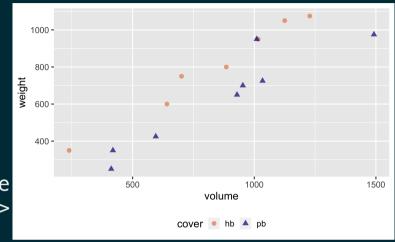
```
A tibble: 2 \times 5
##
               estimate std.error statistic
                                             p.value
    term
##
                  <dbl>
                           <dbl>
                                     <dbl>
                                               <dbl>
    <chr>
                        88.4
  1 (Intercept) 108.
                                     1.22 0.245
## 2 volume
                  0.709
                        0.0975
                                      7.27 0.00000626
```



### Book weight vs. volume and cover

```
linear_reg() %>%
  set_engine("lm") %>%
  fit(weight ~ volume + cover, data = allk
  tidy()
```

```
A tibble: 3 \times 5
                estimate std.error statistic
                                                  p.value
##
     term
                                                   <dbl>
##
                   <dbl>
                            <dbl>
                                       <dbl>
    <chr>
                          59.2
                                        3.34 0.00584
  1 (Intercept) 198.
  2 volume
                   0.718
                         0.0615
                                       11.7 0.0000000660
## 3 coverpb
                           40.5
                                       -4.55 0.000672
                -184.
```



### Interpretation of estimates

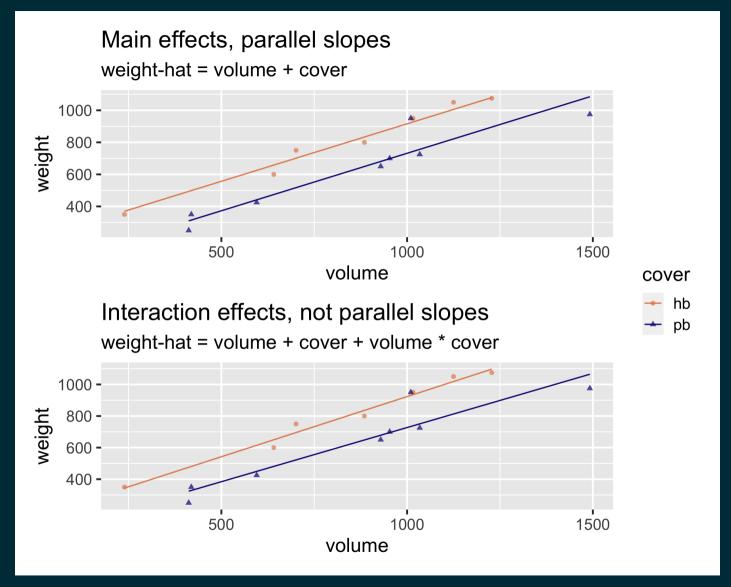
```
## # A tibble: 3 \times 5
               estimate std.error statistic
                                               p.value
    term
                  <dbl>
                         <dbl>
                                    <dbl>
                                                <dbl>
    <chr>
                         59.2
                                   3.34 0.00584
  1 (Intercept) 198.
## 2 volume
                  0.718
                        0.0615 11.7 0.0000000660
               -184.
                         40.5
                                    -4.550.000672
## 3 coverpb
```

- **Slope volume:** *All else held constant*, for each additional cubic centimetre books are larger in volume, we would expect the weight to be higher, on average, by 0.718 grams.
- **Slope cover:** *All else held constant*, paperback books are weigh, on average, by 184 grams less than hardcover books.
- Intercept: Hardcover books with 0 volume are expected to weigh 198 grams, on average. (Doesn't make sense in context.)

#### Main vs. interaction effects

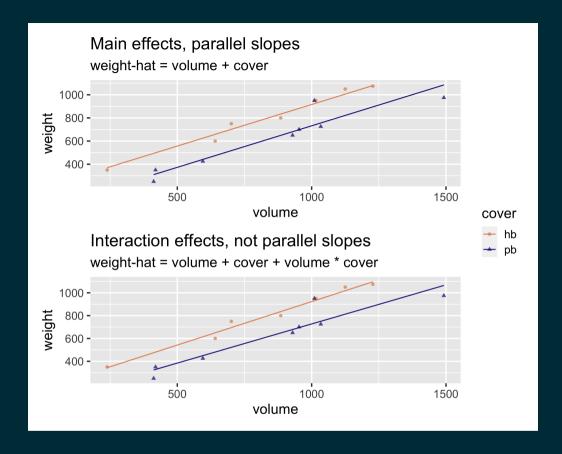
Suppose we want to predict weight of books from their volume and cover type (hardback vs. paperback). Do you think a model with main effects or interaction effects is more appropriate? Explain your reasoning.

**Hint:** Main effects would mean rate at which weight changes as volume increases would be the same for hardback and paperback books and interaction effects would mean the rate at which weight changes as volume increases would be different for hardback and paperback books.



### In pursuit of Occam's razor

- Occam's Razor states that among competing hypotheses that predict equally well, the one with the fewest assumptions should be selected.
- Model selection follows this principle.
- We only want to add another variable to the model if the addition of that variable brings something valuable in terms of predictive power to the model.
- In other words, we prefer the simplest best model, i.e. parsimonious model.



Visually, which of the two models is preferable under Occam's razor?

### R-squared

 $lacksquare R^2$  is the percentage of variability in the response variable explained by the regression model.

```
glance(book_main_fit)$r.squared
```

```
## [1] 0.9274776
```

```
glance(book_int_fit)$r.squared
```

```
## [1] 0.9297137
```

- Clearly the model with interactions has a higher  $\mathbb{R}^2$ .
- However using  $\mathbb{R}^2$  for model selection in models with multiple explanatory variables is not a good idea as  $\mathbb{R}^2$  increases when **any** variable is added to the model.

# Adjusted R-squared

... a (more) objective measure for model selection

- Adjusted  $\mathbb{R}^2$  doesn't increase if the new variable does not provide any new information or is completely unrelated, as it applies a penalty for number of variables included in the model.
- lacktriangle This makes adjusted  $R^2$  a preferable metric for model selection in multiple regression models.

## Comparing models

```
glance(book_main_fit)$r.squared

## [1] 0.9274776

glance(book_int_fit)$r.squared
```

Is R-sq higher for int model?

[1] 0.9297137

glance(book\_int\_fit)\$r.squared > glance(book\_main\_fit)\$r.squared

## [1] TRUE

■ Is R-sq adj. higher for int model?

glance(book\_int\_fit)\$adj.r.squared > glance(book\_main\_fit)\$adj.r.squared

## [1] FALSE

```
glance(book_main_fit)$adj.r.squared
```

```
## [1] 0.9153905
```

```
glance(book_int_fit)$adj.r.squared
```

**##** [1] **0.**9105447