

## Insertion Sort

75, 90, 100, 95, 85, 80  
0 1 2 3 4 5

$$\text{key} = 90$$

$$j = i - 1$$

0 1 2 3 4 5  
 75, 90, ~~100~~, ~~95~~, 85, 80  
95 100

$$i = 1$$

$$90 < 75$$

$$\begin{array}{c} i = 3 \\ \cancel{j = 2} \\ j = 1 \end{array}$$

$$\begin{array}{c} \text{key} = 95 \\ \cancel{j} \end{array}$$

$$\begin{array}{c} \text{true} \\ 95 < 100 \\ j = 1 \end{array}$$

$$\begin{array}{c} i = 2 \\ \text{key} = 100 \end{array}$$

$\text{while } j \geq 0 \text{ and } \text{key} < \text{arr}(j) :$

$$\left\{ \begin{array}{l} \text{arr}(j+1) = \underline{\text{arr}(j)} \\ j = j - 1 \end{array} \right.$$

$$\text{arr}(j+1) = \underline{\text{key}}$$

0 1 2 3 4 5  
 75, ~~90~~, ~~95~~, ~~100~~, ~~85~~, 80  
85 90 100  
 $i = 4 \quad \text{key} = \text{arr}(i) = 85$

$$\cancel{j = 3} \neq 0$$

T

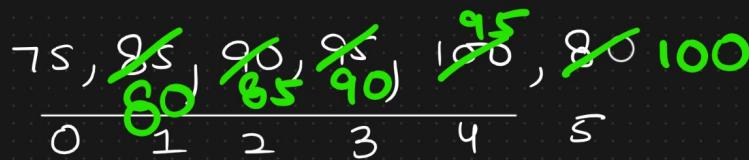
$$85 < 75$$

$\text{while } j \geq 0 \text{ and } \text{key} < \text{arr}(j)$

$$\text{arr}(j+1) = \underline{\text{arr}(j)}$$

$$j = j - 1$$

$$\text{arr}(j+1) = \underline{\text{key}}$$



$$i = 5$$

$$\text{key} = 80$$

$$J = \cancel{4} \cancel{3} \cancel{2} \cancel{1} \\ 80 < 75$$

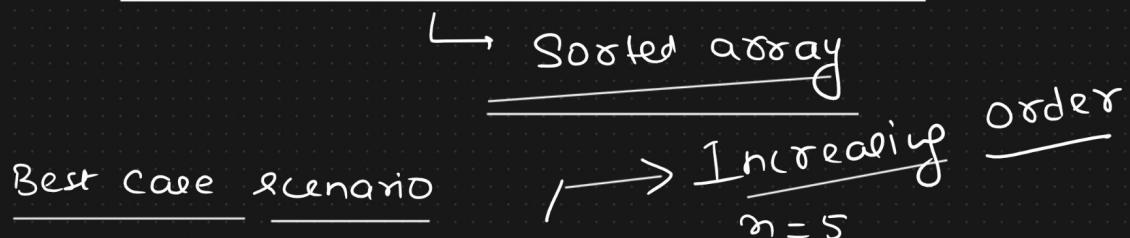
while  $J \geq 0$   $\&$   $\text{key} < arr(J)$ :

$$arr(J+1) = arr(J) \quad \text{--- } \checkmark$$

$$J = J - 1 \quad \text{--- }$$

$$arr(J+1) = \text{key}$$

$$75, 80, 85, 90, 95, 100$$



$$10, 20, 30, 40, 50 \quad \text{--- } \begin{matrix} \text{comparisons} \\ \Rightarrow 4 \end{matrix}$$

Time complexity  $\rightarrow$  # comp + # swaps

$$\Rightarrow (n-1) + 0$$

$$\frac{10}{J} \quad \frac{20}{i}$$

$$\Rightarrow O(n)$$

$$\underline{\text{key} = 20}$$

$$20 < 10$$

\* Given a scenario, array is sorted or almost sorted →

which sorting algorithm is preferable & why??

## Insertion Sort → O(n)

$$\begin{array}{ccccccc}
 0 & 1 & 2 & 3 & 4 & 5 & n=6 \\
 \cancel{10}, \cancel{20}, \cancel{30}, \cancel{40}, \cancel{50}, \cancel{5} & & & & & & \underline{n=6} \\
 \underline{5} & \underline{10} & \underline{20} & \underline{30} & \underline{40} & \underline{50} & \\
 \# \text{ comparisons} + \# \text{ swaps} & & & & & & \\
 (n-1) & & & & & & \\
 & & & & & & \\
 10, 20 & & & & & & \hookrightarrow \underline{O(n)} \\
 20, 30 & & & & & & J=4 \\
 30, 40 & & & & & i=5 & \text{key}=5 \\
 40, 50 & & & & & & \\
 50, 5 & & & & & & 5 < 50 \\
 & & & & & & \\
 & & & & & & \nearrow \text{Decreasing Order}
 \end{array}$$

key = 40	40	50	C	S
50, 40	50	40	1	1
	40	50	2	2
30, 50	30	50		
key = 30	30	30		
30, 40	20	30	40	50
	30	40	80	20
key = 20			3	3

20 50

20 40

20 30

10	20	30	40	50	4	4
20	30	40	80	10		

(n-1)

(n-1)

Key = 10

# comp. & # swaps

$$\frac{1+2+3+4+\dots+(n-1)}{(n-1)}$$

10 50

10 40

10 30

10 20

$$\frac{n^2 - n}{2} = \frac{(n-1)n}{2} \Rightarrow O(n^2)$$

which sorting algo is preferable when the array is highly unsorted??

↳ Quicksort

HeapSort

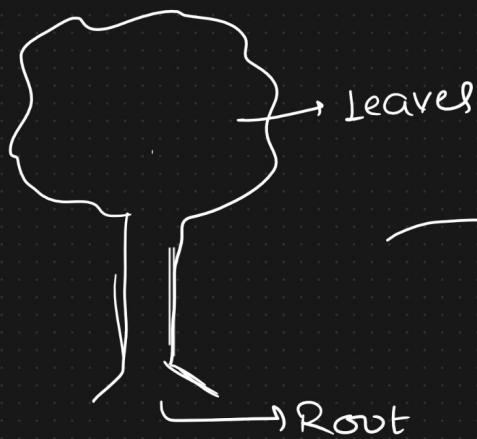
→ heapq

↳ Heap Data Structure

Maxheap

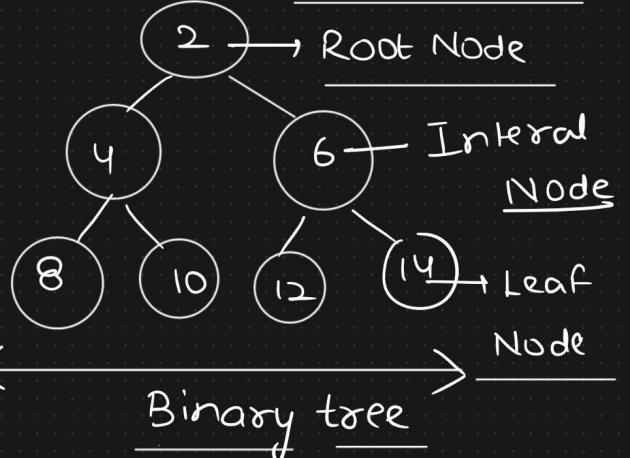
Minheap

Tree Data Structure → Non-Linear



Data Structure

→ Root Node



Internal Node

Node

↳ Binary Tree → 0, 1, 2

↳ Atmost 2 child model

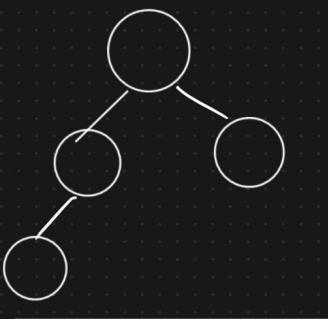
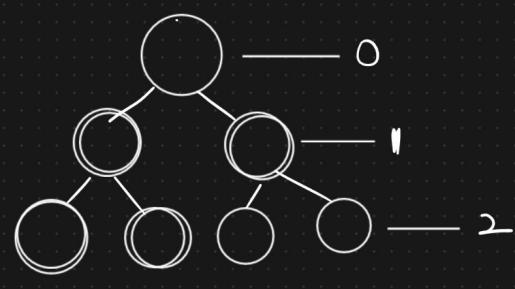
2) full Binary Tree vs Almost complete

or

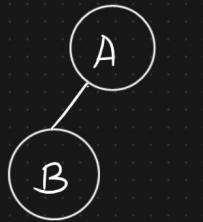
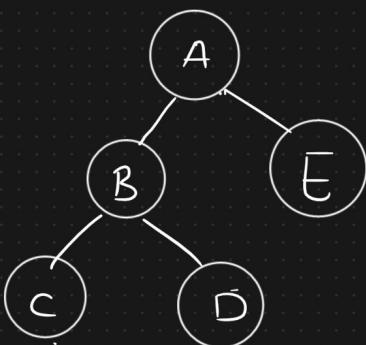
Perfect Binary Tree vs

Binary tree

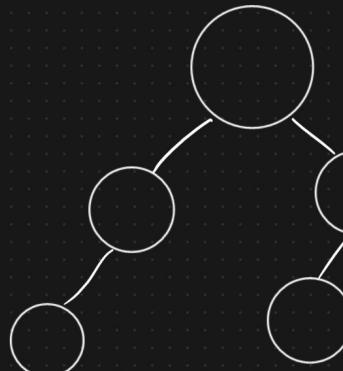
Complete Binary tree



- ↳ Insertion of nodes → (Left to right) }  
 2) upper Level nodes will be filled up before }  
 coming to the lower level } ↓  
 common for  
 above three  
 different binary tree



→ valid ACBT

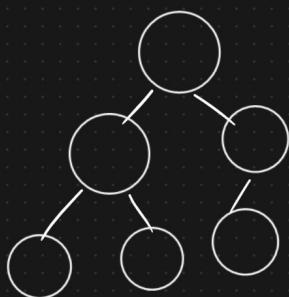
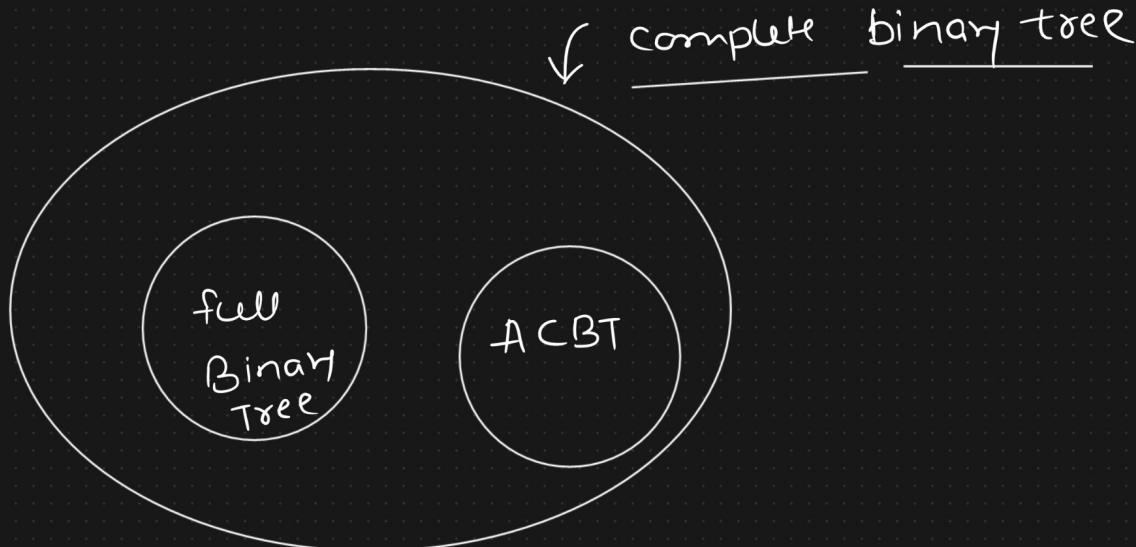


→ Not ACBT

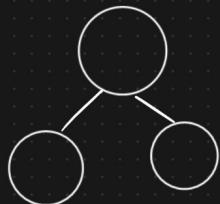
Complete Binary Tree  $\rightarrow$  full Binary Tree

LR

Almost CBT



$\rightarrow$  CBT  $\rightarrow$  Yes  
ACBT  $\rightarrow$  Yes  
fBT  $\rightarrow$  No

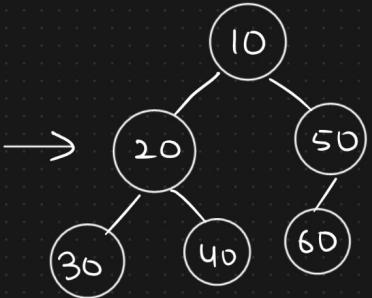


$\rightarrow$  CBT  $\rightarrow$  Yes  
ACBT  $\rightarrow$  No  
fBT  $\rightarrow$  Yes

Heap  
↳ Complete Binary Tree  
1) Minheap

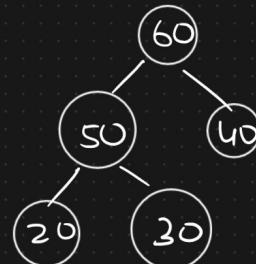
↳ Parent mode  
2)

data < child mode data



$10 < 20 \& 50$  T  
 $20 < 30 \& 40$  T  
 $50 < 60$  T

2) Maxheap  
2)  
↳ Parent mode  
data > child  
mode data



T  
T  
T

Valid Minheap



minimum element

from the given

array



O(1)

T  
T

Valid Maxheap



max-element

from the

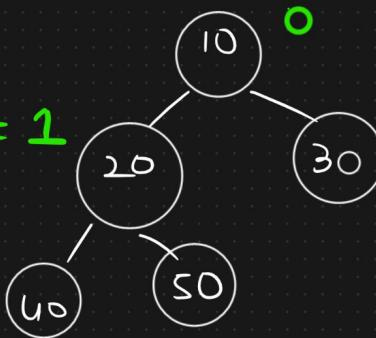
given array



O(1)

CBT

$$2 \times i + 1 = 1$$



$$2 \times i + 2 = 2$$

parent index

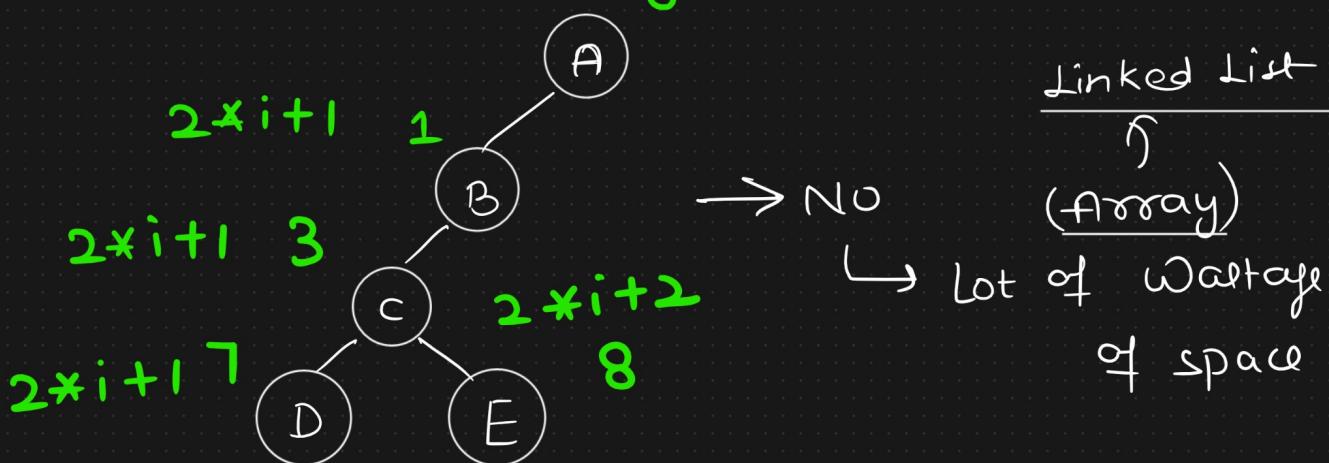
0	1	2	3	4
10	20	30	40	50

↙ array

↳ no wastage  
cf

Space

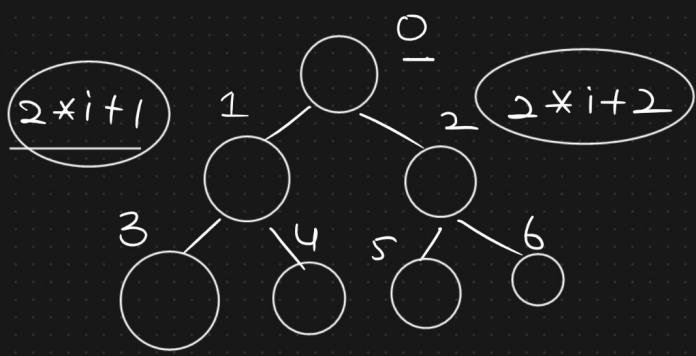
Skewed binary tree



0	1	2	3	4	5	6	7	8
A	B		C				D	E

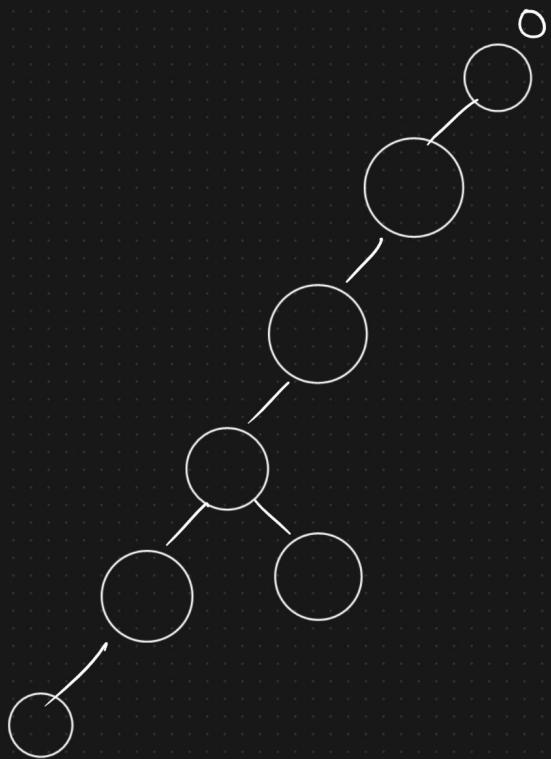
{ }

{ }



$\rightarrow 2*i+1 \text{ (L.I.)}$

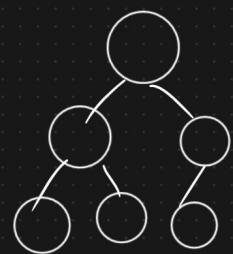
$\rightarrow 2*i+2 \text{ (R.I.)}$



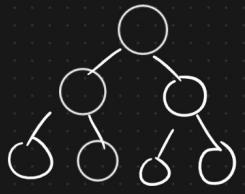
Linked List  
Skewed BT

↓

Not a contiguous  
allocation of  
memory

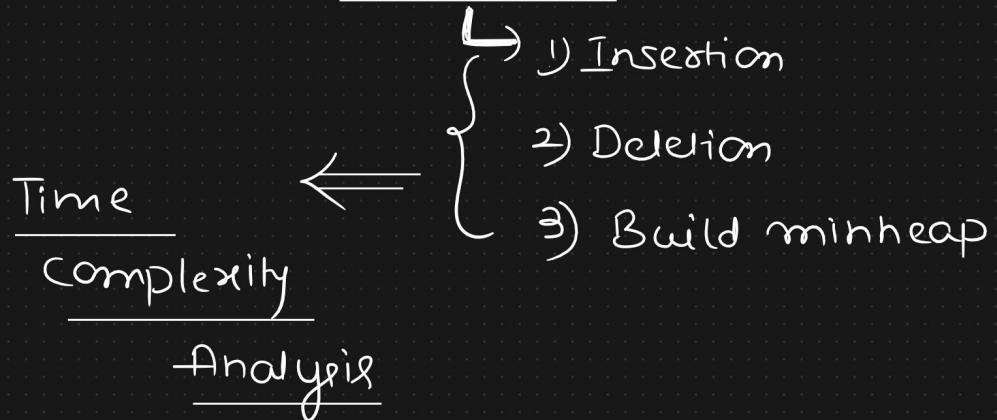


$\rightarrow$  CBT, ACBT



$\rightarrow$  CBT, fBT

## Operations



## Analysis