DSB Portfolio 1

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1 Draw the double sided spectrum of the amplitudes for the signal $\mathbf{x}(t)$

By using Eulers princible x(t) can be rewritten as:

$$\begin{array}{lll} x(t) & = & 2 \cdot \frac{e^{i2\pi \cdot 1000t} + e^{i2\pi \cdot 1000t}}{2} + \frac{e^{i2\pi \cdot 3000t} + e^{i2\pi \cdot 3000t}}{2} + \frac{e^{i2\pi \cdot 3000t} + e^{i2\pi \cdot 19000t} + e^{i2\pi \cdot 19000t}}{2} \\ x(t) & = & e^{i2\pi \cdot 1000t} + e^{i2\pi \cdot 1000t} + \frac{1}{2} \cdot e^{i2\pi \cdot 3000t} + \frac{1}{2} \cdot e^{-i2\pi \cdot 3000t} + \frac{1}{2} \cdot e^{i2\pi \cdot 19000t} + \frac{1}{2} \cdot e^{-i2\pi \cdot 19000t} \end{array}$$

Which gives us the coefficients:

$$c_{1} = 1$$

$$c_{-1} = 1$$

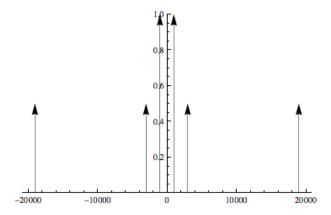
$$c_{3} = 0.5$$

$$c_{-3} = 0.5$$

$$c_{19} = 0.5$$

$$c_{-19} = 0.5$$
(2)

And the double sided spectrum:



Figur 1: Double Sided Spectrum without aliasing

2 Draw the double sided spectrum xs1(t) for the sampled signal without the anti-aliasing filter

The sample rate of the A/D-converter is $20 \mathrm{kHz}$. The new coefficients will be calculated by by multiplying them with the sample rate. Which gives:

$$c_1 = 20000$$

$$c_{-1} = 20000$$

$$c_3 = 10000$$

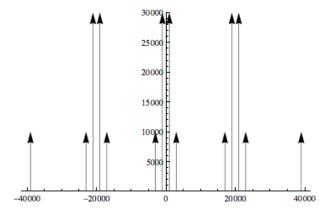
$$c_{-3} = 10000$$

$$c_{19} = 10000$$

$$c_{-19} = 10000$$

(3)

And a plot of the double sided spectrum:



Figur 2: Double Sided Spectrum with aliasing

3 Calculate the A/D converter signal in dB

A/D-converter signal can be calculated by using:

$$SNR_{dB} = 10,79 + 20 \cdot Log_{10}(\frac{x_{rms}}{\Delta}) \tag{4}$$

Where:

$$\Delta = \frac{x_{max} - x_{min}}{2^m} \tag{5}$$

 x_{max} and x_{min} is the maximum and minimum voltage for the A/D-converter and m is the bitsize. x_{rms} is given by:

$$x_{rms} = \sqrt{\frac{1}{T} \int_0^T x(t)^2 dT} \tag{6}$$

We can then start calcualting:

$$\begin{array}{rcl} x_{rms} & = & \sqrt{3} \\ \Delta & = \frac{2-(-2)}{2^8} & = & \frac{1}{64} \\ SNR_{dB} & = & 10,79+20 \cdot Log_{10}(\frac{\sqrt{3}}{\frac{1}{64}}) & = & 51,6848dB \end{array}$$

 SNR_{dB} is the strength of the signal.

4 Determine the quantization voltage for the A/D converter

Quantization is the steps in which the A/D-converter moves. It is the same as Δ which we calculated in the previous section:

$$\Delta = \frac{2 - (-2)}{2^8} = \frac{1}{64}$$

5 Determine the order of the filter for the analog Butterworth

The equation can be converted to dB and solved with regards to n:

$$-48dB = 20 \cdot log_{10} \left(\frac{1}{\sqrt{1 + \left(\frac{10000}{3000}\right)^{2n}}}\right)$$

$$n = 4,58997 \sim 5$$

The order of the filter is 5.