

DSB Portfolio 1

Nis Sarup

2. november 2010

1 Draw the double sided spectrum of the amplitudes for the signal $x(t)$

By using Eulers principle $x(t)$ can be rewritten as:

$$x(t) = 2 \cdot \frac{e^{i2\pi \cdot 1000t} + e^{-i2\pi \cdot 1000t}}{2} + \frac{e^{i2\pi \cdot 3000t} + e^{-i2\pi \cdot 3000t}}{2} + \frac{e^{i2\pi \cdot 19000t} + e^{-i2\pi \cdot 19000t}}{2}$$

$$x(t) = e^{i2\pi \cdot 1000t} + e^{-i2\pi \cdot 1000t} + \frac{1}{2} \cdot e^{i2\pi \cdot 3000t} + \frac{1}{2} \cdot e^{-i2\pi \cdot 3000t} + \frac{1}{2} \cdot e^{i2\pi \cdot 19000t} + \frac{1}{2} \cdot e^{-i2\pi \cdot 19000t} \quad (1)$$

Which gives us the coefficients:

$$\begin{aligned} c_1 &= 1 \\ c_{-1} &= 1 \\ c_3 &= 0,5 \\ c_{-3} &= 0,5 \\ c_{19} &= 0,5 \\ c_{-19} &= 0,5 \end{aligned} \quad (2)$$

And the double sided spectrum:

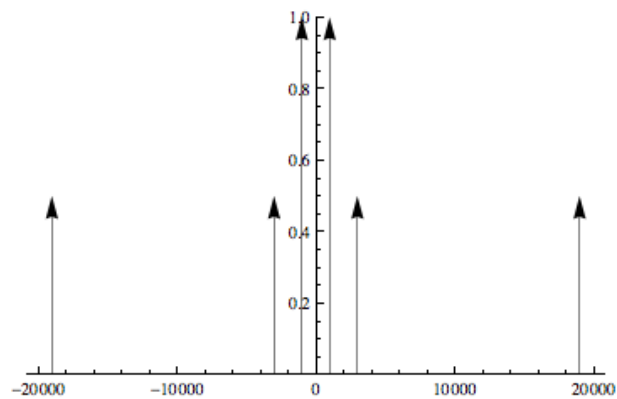


Figure 1: Double Sided Spectrum without aliasing

2 Draw the double sided spectrum $xs_1(t)$ for the sampled signal without the anti-aliasing filter

The samplerate of the A/D-converter is 20kHz. The new coefficients will be calculated by multiplying them with the samplerate. Which gives:

$$\begin{aligned} c_1 &= 20000 \\ c_{-1} &= 20000 \\ c_3 &= 10000 \\ c_{-3} &= 10000 \\ c_{19} &= 10000 \\ c_{-19} &= 10000 \end{aligned}$$

(3)

And a plot of the double sided spectrum:

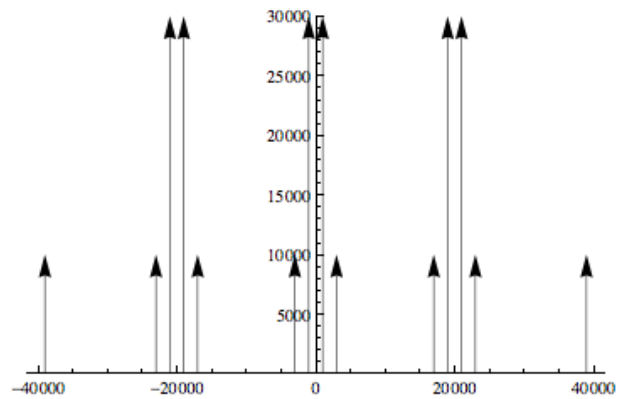


Figure 2: Double Sided Spectrum with aliasing

3 Calculate the A/D converter signal in dB

A/D-converter signal can be calculated by using:

$$SNR_{dB} = 10,79 + 20 \cdot \text{Log}_{10}\left(\frac{x_{rms}}{\Delta}\right) \quad (4)$$

Where:

$$\Delta = \frac{x_{max} - x_{min}}{2^m} \quad (5)$$

x_{max} and x_{min} is the maximum and minimum voltage for the A/D-converter and m is the bitsize. x_{rms} is given by:

$$x_{rms} = \sqrt{\frac{1}{T} \int_0^T x(t)^2 dT} \quad (6)$$

We can then start calculating:

$$\begin{aligned} x_{rms} &= \sqrt{3} \\ \Delta &= \frac{2 - (-2)}{2^8} = \frac{1}{64} \\ SNR_{dB} &= 10,79 + 20 \cdot \text{Log}_{10}\left(\frac{\sqrt{3}}{\frac{1}{64}}\right) = 51,6848dB \end{aligned}$$

SNR_{dB} is the strength of the signal.

4 Determine the quantization voltage for the A/D converter

Quantization is the steps in which the A/D-converter moves. It is the same as Δ which we calculated in the previous section:

$$\Delta = \frac{2 - (-2)}{2^8} = \frac{1}{64}$$