CS174 Assignment 3 - Part 1 Writing Section

1 Clipping

a The top of the box is y=1 (+(xx(1))). Apparently, line AC intersects with top of the box at D(0,1) olue to the answer of (y=1) (-(xx(1))) (x=0) (x=0)

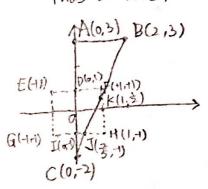
According to piazza, professor says "You do not need to provide outcodes".

b. $A^{(o)} \vee B^{(2)3)}$ Assume the bottom edge of the box is GH with G(-1,+), H(1,+) $E^{(-1,1)} \longrightarrow E^{(-1,1)} \longrightarrow X$ The BC intersects with GH at point J $Y = \frac{1}{2}X - 2 \ (0 \le X \le 2) \longrightarrow J(\frac{2}{5}, +)$ $Y = -1(-1 \le X \le 1)$

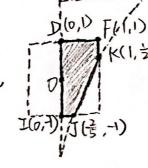
C. A(0,3) Y B(2,3), $E(-1,0) \to (0,1) \to (1,-1)$ $G(-1,-1) \to (1,-1) \to (1,-1)$ C(0,-2) $G(-1,-1) \to (1,-1)$

Apparently, Line AC. AB about intersect with the right edge FH, which is x=1 ($1 \le y \le 1$). Let K be the intersection point of BC and FH, we have $\begin{cases} y = \frac{5}{2}x - 2 \ (0 \le x \le 2) \Rightarrow K(1, \frac{1}{2}) \\ X = 1 \ (-1 \le y \le 1) \end{cases}$

d. the left edge EG $(X=1, (-1 \le y \le 1))$ does not intersect with any part of ABC. Thus we have,

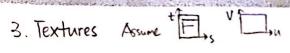


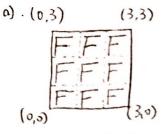
After clipping,

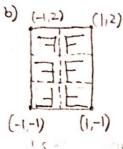


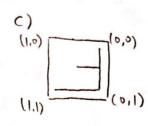
the shading part is what we got.

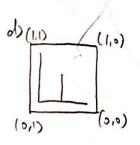
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2. Rasterization / Scan-conversion
 a. The implicit equation of the circle is
                (x-x_0)^2 + (y-y_0)^2 = r^2, We have F(x,y) = (x-x_0)^2 + (y-y_0)^2 - r^2
 b. For the naive thought, for every x, we have y = y_0 + \sqrt{r^2 - (x - x_0)^2}
                                                     or y= y - 5 [2-(x-x))
   thus for & from round(x-r) to round (x.+r) do
              (a)culte y=round (y0+ Sqrt(r*r-(x-x0) x(x-x0)))
                        Ydown = round (yo - Sart (rxr - (x-x0)*(x-x)))
             Set Pixel (x, yup)
             Set Pixel (X. Ydown)
         end
C. Bresen ham approach. (work by octants and uses symmetry)
    We first start with x=xo, y= round (y.+r)
     we have next candidate point
      M(x+1, y-0.5) d=F(M)=(x+1-x)+(y-0.5-y0)2-r2=
      if dco choose E.
                        d_{\text{next}} = F(x+1+1, y-0.5) = (x+1-x_0+1)^2 + (y-0.5-x_0)^2/2 = d+2(x+1-x_0)+1
= d+2(x+x_0)+3
      if d>0 choose SE
                        Chext = F(x+1+1, y-1-0.5) = (x+1-x+1)2+ (y-4.-1-0.5)2-y2 = d+2(x-x+1+3)+3
                                                                              -2(y-y0-015)+1
                                                                             = d+2(x-x0)-2(y-y0)+5
       Start with X = Xo
                                                                             = d + 2(x-y) + 5
                   y = round (y,+r), sortisfying x < y, setfixel (x, y)
                    d = (X,+1-1,0)2+ (4-0.5-40)2-12= 1+ (4-0.5-40)2-12
            while (x <y).
                                                                 set Pixel (Y-1/6+X0, X-1/6+1/6)
                 if d<=0
                      d = d+2(x-x0)+3
                                                                  set Pixel ( Y-Y6+X0, X0-X+Y6)
                      X=X+1
                                                                  set Pixel ( Yo-y+xo, X-Xo+xo)
                 if d70
                                                                  Set fixed ( 40-Y+X, x0-X+40)
                      d = d + 2(x - y) + 5
                      X = X+1
                      Y=y-1
                SetPixel (x, y) SetPixel (2X6-X, Y) SetPixel (X, ZY6-Y) SetPixel (2X6-X, ZY6-Y)
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4. Interpolation

The barycentric coordinate for Pis

The barycentric coordinate for P is

$$R_{2}(s,8) = \frac{(V_{1}-V_{new})\times(V_{K}-V_{new})}{(V_{1}-V_{1})\times(V_{K}-V_{new})} \times \frac{(V_{1}-V_{1})\times(V_{K}-V_{new})}{(V_{1}-V_{1})\times(V_{K}-V_{1})} = \frac{(V_{1}-V_{1})\times(V_{K}-V_{new})}{(V_{1}-V_{1})\times(V_{K}-V_{1})} = \frac{(V_{1}-V_{1})\times(V_{K}-V_{1})}{(V_{1}-V_{1})\times(V_{K}-V_{1})} = \frac{(V_{1}-V_{1})\times(V_{K}-V_{1})}{(V_{1}-V_{1})\times(V_{K}-V_{1})} = \frac{(V_{1}-V_{1})\times(V_{K}-V_{1})}{(V_{1}-V_{1})\times(V_{K}-V_{1})} = \frac{(V_{1}-V_{1})\times(V_{1}-V_{1})}{(V_{1}-V_{1})\times(V_{1}-V_{1})} =$$

thus
$$(a, \beta, r) = (\frac{9}{16}, \frac{3}{8}, \frac{1}{16})$$
.

$$\Delta t_i = \frac{(V_j - V_{new}) \times (V_k - V_{new})}{(V_j - V_i) \times (V_k - V_i)}$$
$$= \frac{(2, -3) \times (-3, 0)}{(2, -3) \times (-3, 0)} = \frac{(-3, -3) \times (-3, 0)}{(-3, 0)}$$

$$= \frac{(2,3) \times (-2,2)}{(3,-5) \times (-2,-2)} = \frac{9}{16}$$

$$i = \frac{(V_{j} - V_{new}) \times (V_{k} - V_{new})}{(V_{j} - V_{i}) \times (V_{k} - V_{i})}$$

$$= \frac{(V_{j} - V_{i}) \times (V_{k} - V_{i})}{(V_{j} - V_{j}) \times (V_{k} - V_{j})}$$

$$= \frac{(2, -3) \times (-3, 0)}{(3, -1) \times (-2, -2)} = \frac{9}{16}$$

$$= \frac{(-1, 2) \times (-3, 0)}{(-3, 5) \times (-5, 3)} = \frac{6}{16} = \frac{3}{8}$$

$$\Delta t_{K} = \frac{(V_{i} - V_{rew}) \times (V_{j} - V_{rew})}{(V_{i} - V_{K}) \times (V_{j} - V_{K})} = \frac{(-1, 2) \times (2, -3)}{(2, 2) \times (3, -3)} = \frac{1}{16}$$

$$\frac{\partial \mathcal{L}}{\partial w} + \frac{1}{W_1} + \frac{1}{W_2}$$
Since $W_0 = W_1 = W_2 = 1$

$$\frac{\partial}{\partial w} + \frac{\partial}{\partial w} + \frac{1}{W_1} + \frac{1}{W_2}$$
We have $S = \frac{\partial}{\partial w} + \frac{\partial}{\partial w} + \frac{1}{\partial w} + \frac{1}{W_2}$
So $\frac{\partial}{\partial w} + \frac{\partial}{\partial w} + \frac{1}{W_2} + \frac{1}{W_2}$
We have $S = \frac{\partial}{\partial w} + \frac{\partial}{\partial w} + \frac{1}{W_2} + \frac{1}{W_2}$

As for (r.g.b)
$$r = \frac{16 \times 0.5 + \frac{6}{16} \times 0.7 + \frac{1}{16} \times 0.3}{16 \times 0.5625} = \frac{9}{16} = 0.5625$$

$$9 = \frac{9}{16} \times 0.5 + \frac{1}{16} \times 0.2 + \frac{1}{16} \times 0.9 = \frac{33}{80} = 0.4125$$

$$b = \frac{16 \times 0.9 + \frac{1}{16} \times 0.7 + \frac{1}{16} \times 0.7}{1} = \frac{25}{32} = 0.78125$$

$$b = \frac{6 \times 0.9 + \frac{6}{16} \times 0.7 + \frac{1}{16} \times 0.2}{1} = \frac{25}{32} = 0.78125$$
, the answer is (0.5625, 04125, 0.78125)



5. Local Illumination (18 pts)

a) (16 pts) Sketch the illumination that would be computed for the above scene using the Phong illumination model. The scene is lit from above using a directional light source that is coming directly from above. Use 4 sketches: one for ambient, one for diffuse, one for specular and one for the total illumination. The Phong illumination model is given by:

$$I = I_{d}k_{d}(\mathbf{n} \cdot \mathbf{l}) + I_{s}k_{s}(\mathbf{r} \cdot \mathbf{v})^{n} + I_{a}k_{a}$$

Solution: For ombient, I = Taka = 0,2

eye

where $I_d = I_a = I_s = 1.0$, $k_a = 0.2$, $k_d = 0.8$, $k_s = 0.7$, n = 100.

For diffuse, when I and I has Dangle, it reaches max Id Kd = 0.8 from left to right in semicircle A>B>C

angle in Til decrease from 90 to 0° thus cost of increases.

from B+C. O increases and cost decrease

For specular, the peak value is 0.7(1.0700, When F, I has Dargle

The peak is at D and E.

since n=100, Igecular will decrease rapidly in both directions from peak to right, aid from peak to left.

For total curves, we odd the above curves together. total I(x)diffuse specular specular ambrent. ambient veny thin!

a) We first project B on Ac to get B'
according to piazza.

Ye = $\frac{5-2(x-1)}{8-1} + 2 \Rightarrow y_{Ac} = \frac{3}{7} \times + \frac{11}{7} \Rightarrow B'(\frac{16}{29})$

 $y_{c} = \frac{1}{8-7}(x-1) + 2 \Rightarrow y_{Ac} = \frac{3}{7}x + \frac{1}{7}$ $\Rightarrow B'(\frac{1}{7}, \frac{1}{7})$ $y_{BB}' = -\frac{7}{3}(x-6) + 3$ $y_{BB}' = -\frac{7}{3}x + 17$ $\Rightarrow B'(\frac{1}{7}, \frac{1}{7})$ $t = AB' = \frac{1}{12} - \frac{1}{12} + \frac{1}{12}$

 $t = AR' = \frac{|(1.2) - (\frac{162}{27}, \frac{115}{29})|}{|(1.2) - 8.5)||} = \frac{19}{29}$

NB= (1-t)M++Nc= 10/4+ 19/1c

Normalize Na = (-\$\vec{1}, -\$\vec{1}) Not(1.0).

No= (195/2 5/2) = (0.41,-024)

Normalie NB = (19-5/2) , -5/2 , 194-19012)

= (0.86, -0.51)

b) ambient illumination: BCD: IaKa = (01,0201)

specular illumination:

Is = ILKs (H-N)", H=1+V

后的 La=信,意) VB=(店,意)

HB = (17-15, - 5+2E) Norwhite HB= (10-110, - 10+110, 0)

= (0.58, -0.8/0)

NAB=(点, 流) NE=(点,一点) NB= NAB+NEE (红版 斯肠)

NB = NAB+NBC = (545, -5545)0)

Normalize NB = (2/13+3/13) - 5+1/13 = (0,47,-0,88,0)

Is = (1.0, 1.0, .9) (HBNB)20 = (1.0, 1.0, 9) (0,9854)20 (0.75,075,0.67)

diffusion: I=ILKd (成記)=(1.0,1.0,9)(3,0,0,9)[0.47,-0.88,0)·(虚,-龙》] =(3,8,81)·0.95=(0.29,0.76,0.77)

Itotal = Iaka+Is+I= (1.05, 1.53, 1.45) > Itotal = (1.0, 1.0, 1.0)

b) Continue 1) I ambient = (.01, .02, .01). For C. Nc=(1,0,0). Lc=(0,-1) Vc=(0,-1). H=(0,-1)Is= I₁ K₅ (H N)ⁿ= $(1,1,9)(0)^{20}=0$ For diffusion,

I total = I ambient + Is + I = (.01,.02,.01)_

I=ILKd (TETC)=(.3,8,81).0=0.

Since it is flat shading model,
let D be either B or C.
Here, we let D equals with C.

Iambient = (.0|, .0L, .01)

Is = Idiffusion = 0

Itotal = Iambient = (.0|, .02, .01)

c). We have

C (.ol, i02, .ol)

Ambient (.01,-02,-01) (.01,02,-01) Specular (.75,.75,-67) (0,0,0)

diffuse (,29,76,77) (0,0,0)

total (1.0,1.0,1.0) (.01,02,01)

Since it is governed shooting model BD=DC

D: Ambient (.01, .02, .01)

Specular (.375,.375,.335)

diffuse (.145,.38,.385)

total (.53, .775, .73)

NB=(0.47,-0.88,0), NE=(1.0,0)

linearly interpolate ND=NB+NKI =(0.86,-0.51)

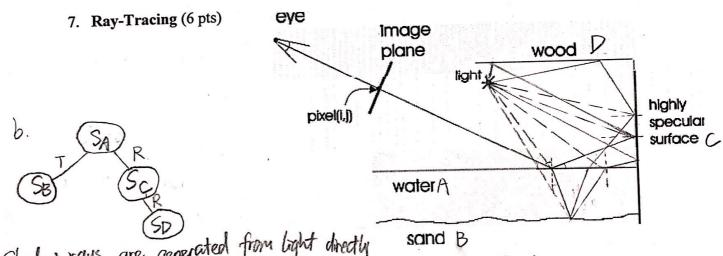
Lp = (8.1.0)-(7.4.0) = (\$\frac{1}{10}, -\frac{1}{10}, 0) \quad \qu

() Is = (1.0, 1.0, -9) (HOND)=(1.0, 1.0, -9) x(0, 7183) = (0,0013,

@ Id=ILKd(成员)=(.3,.8,.8)×0.76

= (0.23, 0.6, 0.61) @ Jambed=(0.01,0.02,001)

@ Itotal=Iambert +Ix+ ID=(0,2413, 0,6213, 0,6212).



Shadow rows are generated from light directly sand B

to each reflect of diffuse point as the "--" in graph indicates.

to each reflect a. (3 pts) For the following scene, sketch all the ray paths and shadow rays that would be generated by a raytracer in order to compute the color for the given pixel, (i,j).

b. (3 pts) Draw the ray tree corresponding to the above ray paths. Draw the reflected paths to the right and the transmitted paths to the left. Also indicate where the

- a) Give the polynomial representation for a parametric cubic curve. $p(t) = a_0 + a_1 t + a_2 t^2 + a_3 t^3$
- b) Compute the first and second derivative representation $P'(t) = a_1 + 2a_2t + 3a_3t^2$ $P''(t) = 2a_2 + 6a_3t$

C) Determine the basis matrix for the parametric cubic curve,
$$P(t) = \begin{bmatrix} 1 + t^2 + t^3 \end{bmatrix} \begin{bmatrix} a_0^{-1} \\ a_1^{-1} \end{bmatrix} P_0 = P(0) = 0 A_0 = P'(0) = 202$$

$$P(0) = A_0 = P'(0) = 20$$

$$P(0) = A_0 = P'(0) = 202$$

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