CS 174A Assignment 2 - Part 1.

- 1. a) Since the hint says Peacin_head-coord = D*Pear, We have Pear_in_comera = ACD Pear
 - b). Since Tailcommera let us see from the end of the cost tail, Ptaltp= B * Ptoiso, According to the hint in a), we have Ptors= KLM Ptailtip, thus B = M-12 K-1
- 2. According to the slide 6,

$$F_{total} = g - rv + f_{ext}$$

 $a(t) = f_{total}$

V(t+ot) = V(t) + ota(t)

 $\chi(t+\Delta t) = \chi(t) + \Delta t V(t+\Delta t)$

where V is the damping coeff.
f is the external force.

By computing iteratively, we get the position of a certain particle

3. According to the stide 6,

$$g_i(t) = \sum_{j \in N_i} g_{ij}$$

Jij = kij eij dij

gi is total force on node i due to springs connecting it to neighboring nodes jeNi

gij is the fince spring ij exerts on node i.

 $dij = X_j - X_i$

ej= | dij | - lij

olij is separation of nodes Il dijl is actual length of sprty eij is deformation of spring

Function calls as specified in lecture: void spring_forces (int num_springs, spring *sprs) { int i; for (i=0; i<num.springs; i++) spring-force (& sprs[i]);}

void spring-force (spring *s)

{ node * node1, * node2; double length, extension, scale-factor; vector direction, force;

node1 = s→n1; node2=S→n2;

VMinus (node2-> position, node1-> position, direction); length = Vlength (direction);

vdecifore, node2-forces; deformation=length - s > rest - length; Scale-factor = ((deformation * S+spring-constant) Vscale (scale-factor, direction, force);

vinc (force, nodel force);

4. a Mass-spring model with a non-zero length spring b. Cloth - Viscoelasticity - Mass-Springs Model C. Heating and Melting Deformable Models - Mass-Springs Model d Liquids-Particle Models Solution: a gij = kijej dij = kij (||xj-xi||-lij) xj-xi (where dij = xj-xi is node distance, · eij = Ildijll - Uj is deformation, (Page 10) Lij is natural spring length, (Page17) Mixi+rixi+cij dij=fi where cij= kijeij+rijeij
(Page17) Mjxj+rjxj-cij dij=fi kij is the spring constant for ij) where dij=xj-xi, eij=||dij||-lij, rij is damply coeff, kij is stiffness: C. Since the only difference is kij. where 2 (100)-V(CVD)=9 V-(30,3V,3W) 9 is the vate of heat generation. Mismass density o is specific heat the istemperature C is thermal conductivity matrix d. The total force on a particle i, repulsion $g_i(t) = \sum_{j \neq i} g_{ij}(t)$ attraction (Page 16) gij (t) = mim (x-xj) (- dij+8) + (3) , a=2, b=4 I and & determine the strength of the attraction & pepulsion forces dij=11xj-xill. Is is minimum required separation between particles

5 According to 2 fext = [147] m=1 at=1 g=9.8 flotal = 9-10+ fext where a(t) = from assume Y=D for particle. $V(t+d) = v(+) + \Delta t N(t)$ $\gamma(t+ot)=\gamma(t)+ot\cdot V(t+ot)$ thus feetal = [4,9] at t=0. $\alpha(0) = [2,4.7,-5]^{\mathsf{T}}, \ V(0) = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}, \ \chi(0) = [0,0,0]^{\mathsf{T}}$ Since ot=1, t=1s, V(1) = V(0) + 1.0(0) = [2,49,-5]T $X(1) = X(0) + 1 V(1) = [2,49,-5]^{T}$ ftotal = g and a(1) = 9 = [0, -9.8, D] V(2) = V(1) + 1.a(1) = [2, -4.9, -5] $\chi(2) = \chi(1) + 1 \cdot V(2) = [4, 0, -10]^T$ Since $\chi_y = 0$, it hits the ground of $\begin{bmatrix} 4 \\ 0 \\ -10 \end{bmatrix}$ 6. According to lecture 7, Peye = [=,10,3], Pref = [-2,2,0], Vup=[-1,-1,0]. thus $K = \frac{\text{Peye-Pref}}{|\text{Peye-Pref}|} = \frac{[4, 8, 3]^{T}}{|4^{2} + 8^{2} + 3^{2}} = [\frac{4}{189}, \frac{8}{187}, \frac{3}{189}]^{T}$ i = Vypxk = (-滿, 黃,-貴) = (黃,承,丁) $\hat{J} = k \times \hat{i} = (\frac{-41}{300}, \frac{7}{3000}, \frac{36}{13000})$ which is the camera coordinate system. Man transform world coordicate system to view wordinate system. $M_{\text{cam}} = \begin{bmatrix} \frac{1}{\sqrt{100}} & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} I - P_{\text{ex}} \\ 0 & 0 \end{bmatrix} = \begin{bmatrix} -\frac{2}{\sqrt{100}} & \frac{2}{\sqrt{100}} & \frac{2}{\sqrt{100}} \\ \frac{2}{\sqrt{100}} & \frac{2}{\sqrt{100}} & \frac{2}{\sqrt$ 7. According to Lecture 7. The projection Matrix is, n=-1 f=-100 r=2-13 l=-2+13 $Mp = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$ since ospect ratio = \frac{r-L}{t-b} = \frac{1}{2}, b=-4+213, t=4-213 $M_{0} = \begin{bmatrix} \frac{1}{215}, & 0, & 0, & 0 \\ 0, & \frac{1}{4725}, & 0 & 0 \\ 0 & 0 & -\frac{2}{99}, & \frac{101}{99} \end{bmatrix}$ $+ \text{this.} \quad M_{prij} = M_{0}M_{p} = \begin{bmatrix} \frac{1}{15-2} & 0 & 0 & 0 \\ 0 & 215-4 & 0 & 0 \\ 0 & 0 & \frac{1}{49} & \frac{210}{99} \end{bmatrix} = \begin{bmatrix} 2+\sqrt{15} & 0 & 0 \\ 0 & -\frac{1}{245} & 0 & 0 \\ 0 & 0 & \frac{1}{49} & \frac{2}{49} \end{bmatrix}$