1. Hint:  $\Delta \log f(x) = \log f(x+h) - \log f(x)$ 

2. Hint: 
$$\Delta \binom{n}{x+1} = \binom{n+1}{x+1} - \binom{n}{x+1}$$

3. Hints:

$$\bullet \ E^{-k}f(x) = f(x - kh).$$

• Use mathematical induction.

4. **Hint:** Use the basic error formula of interpolation.

5. **Ans:** 
$$x^3 + x^2 - 3x + 1$$

6. **Ans:** 48

Hint: Use Newton's forward interpolation formula

7. **Ans:** 96.6352 thousands

Hint: Use Newton's backward interpolation formula

8. **Ans:** f(5) = 32.9333

**Hint:** Use Lagrange's interpolation formula for five nodal points.

9. Ans:  $\frac{5}{2(x-1)} - \frac{15}{(x-2)} + \frac{31}{2(x-3)}$ Hint: Take  $f(x) = 3x^2 + x + 1$  and use Lagrange's interpolation formula for f(x).

10. **Hints:** Use Lagrange's formula for the arguments -3, -1, 1, 3 and then put x = 0.

11. **Ans:** 4.07152

12. **Ans:** 9855 feet

**Hint:** Use trapezoidal formula for n = 14.

13. **Ans:**  $h \le 0.0047$ 

**Hint:** Error,  $E = -\frac{(b-a)h^2}{12}f''(\zeta), \zeta \in (a,b)$ 

14. **Hint:** Actual area =  $\int_{-h}^{h} y \, dx$ 

15. **Ans:** 1.8278472