1.
$$\frac{dz}{dt} =$$

(a)
$$(2x + y)e^t + x(\cos t)$$
.

(b)
$$(x\cos t - y\sin t)$$

2.
$$\frac{\partial z}{\partial u} = 2(x\cos v + y\sin v)$$
 and $\frac{\partial z}{\partial v} = 2u(y\cos v - x\sin v)$

3. (a)
$$\frac{dy}{dx} =$$
i. $\frac{yx^{y-1} - y^x \ln(y)}{xy^{x-1} - x^y \ln(x)}$
iii. $= -\frac{e^y + ye^x - ye^{xy}}{xe^y + e^x - xe^{xy}}$
iii. $-\frac{y}{x} \left(\frac{\cos xy - e^{xy} - 2x}{\cos xy - e^{xy} - x} \right)$
iv. $-\left(\frac{y}{x} \right)^{\frac{1}{3}}$

(b) i.
$$\frac{\partial z}{\partial x} = \frac{z^2 e^{xz^2} - y^2 z^2}{2xy^2 z + y \cos yz - 2xz e^{xz^2}},$$

$$\frac{\partial z}{\partial y} = -\frac{2xyz^2 + z \cos yz}{2xy^2 z + y \cos yz - 2xz e^{xz^2}}$$
ii.
$$\frac{\partial z}{\partial x} = -\frac{tan^{-1}(\frac{y}{z}) - \frac{yz}{x^2 + z^2} + \frac{yz}{x^2 + y^2}}{tan^{-1}(\frac{x}{y}) - \frac{yx}{y^2 + z^2} + \frac{xy}{z^2 + x^2}}$$

$$\frac{\partial z}{\partial y} = -\frac{tan^{-1}(\frac{z}{x}) - \frac{xz}{x^2 + y^2} + \frac{xz}{y^2 + z^2}}{tan^{-1}(\frac{x}{y}) - \frac{xy}{y^2 + z^2} + \frac{xy}{x^2 + z^2}}$$
(a) Homogeneous of degree 0. (d) Not 1

- 4. (a) Homogeneous of degree 0. (d) Not Homogeneous.
 - (b) Homogeneous of degree 2.
 - (c) Homogeneous of degree $\frac{1}{20}$. (e) Homogeneous of degree 2.
- 5. Use chain rule differentiation with two variables.
- 6. Use Euler's theorem.
- 7. Use Euler's theorem to the function $z = \sin u$.
- 8. Use Euler's theorem to the function z = fu.
- 9. Compute first and second order partial derivatives.
- 10. Use Euler's theorem to the function z.

- 11. Use Euler's theorem to the function $f = \tan u$.
- 12. Use Euler's theorem to the function $f = \sin u$.
- 13. Use Euler's theorem to the function $U = \frac{(ax^3 + by^3)^n}{3n(3n-1)}$ and $V = xf(\frac{y}{x})$.
- 14. Use Euler's theorem to the function $\alpha = x^m f(\frac{y}{x})$ and $\beta = y^n g(\frac{x}{y})$.
- 15. Compute first and second order partial derivatives of u.
- 16. Use Euler's theorem to the function $\alpha = x\phi(\frac{y}{x})$ and $\beta = \psi(\frac{x}{y})$.
- 17. Use Euler's theorem to the function $\alpha = \frac{(x^2 + y^2)^n}{2n(2n-1)}$ and $\beta = x\phi(\frac{y}{x})$ and $\gamma = \psi(\frac{y}{x})$.
- 18. Compute partial derivatives of u with respect to r and θ .
- 19. Compute partial derivatives of z with respect to r and θ .