

## Basics of R software.

- R is a software for data analysis and statistical computing.
- 1) This software is used for effective data handling and output storage is possible.
  - 2) It is capable of graphical display.
  - 3) It is a free software.

1)  $2^2 + \sqrt{25} + 35$   
 $> (2^{**2}) + \text{sqrt}(25) + 35 =$   
 [1] 44

2)  $2 \times 5 \times 3 + 62 \div 5 + \sqrt{49}$   
 $> (2 * 5 * 3) + (62 / 5) + \text{sqrt}(49)$   
 [1] 49.4

3)  $\sqrt{76 + 4 \times 2 + 9 \div 5}$   
 $> \text{sqrt}(76 + (4 * 2) + (9 / 5))$   
 [1] 9.262829

4)  $4^2 + 1 - 101 + 7^2 + 3 \times 9$   
 $> 4^2 + \text{abs}(-101 + (7^{**2}) + (3 * 9))$   
 [1] 128

P.E

Q.1)  $x = 20$

$y = 30$

Find  $x+y$ ,  $x^2+y^2$ ,  $\sqrt{y^3-x^3}$ ,  $|x-y|$

$x+y$

[i] 50

$x^{**2} + y^{**2}$

[i] 1300

$\sqrt{(y^{**3}) - (x^{**3})}$

[i] 137.8405

$|x-y|$

[i] 10

Q.3)  $c([2, 3, 4, 5])^2$

[i] 4 9 16 25

$c([4, 5, 6, 8])^3$

[i] 12 15 18 24

$c([2, 3, 5, 7]) * c([-2, -3, -4, -5])$

[i] -4 -9 -25 -28

$c([2, 3, 5, 7]) * c([8, 9])$

[i] 16 27 40 63

$c([1, 2, 3, 4, 5]) * c([2, 3, 4])$

c(1, 2, 3, 4, 5, 6) ^ c(2, 5)

[1] 1 8 9 64 25 216

Q) Find the sum , product , maximum , minimum of the values.

5, 8, 6, 7, 9, 10, 15, 5.

> x = c(5, 8, 6, 7, 9, 10, 15, 5)

> length(x)

[1] 8

> sum(x)

[1] 65

> prod(x)

[1] 11340000

> max(x)

[1] 15

> min(x)

[1] 5

> z <- matrix(nrow=4, ncol=2, data=c(1, 2, 3, 4, 5, 6, 7, 8))

> z [,1] [,2]

[1,] 1 5

[2,] 2 6

[3,] 3 7

[4,] 4 8

18

$$x = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

$$y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix}$$

>  $x \leftarrow \text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8, 9))$

>  $y \leftarrow \text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(2, -2, 10, 4, 6, 1, -11, 12))$

>  $x + y$

$$\begin{bmatrix} [1] & [2] & [3] \\ [1] & 3 & 8 & 17 \\ [2] & 0 & 13 & -3 \\ [3] & 13 & 12 & 21 \end{bmatrix}$$

>  $x * y$

$$\begin{bmatrix} [1] & [2] & [3] \\ [1] & 2 & 16 & 70 \\ [2] & -4 & -40 & -88 \\ [3] & 30 & 36 & 108 \end{bmatrix}$$

>  $x^2 + y^3$

$$\begin{bmatrix} [1] & [2] & [3] \\ [1] & 8 & 20 & 44 \\ [2] & -2 & 34 & -17 \\ [3] & 36 & 30 & -84 \end{bmatrix}$$

>  $x = c(2, 4, 6, 1, 3, 5, 7, 18, 16, 14, 17, 19, 3, 3, 2,$   
 $5, 0, 15, 99, 14, 18, 10, 12)$

> length(x)

[1] 23

> a = table(x)

> a

x

0	1	2	3	4	5	6	7	8	9	10	12	14	15	16	17	18
1	1	2	3	1	2	1	1	1	1	1	1	1	2	1	1	2

> transform(a)

x freq

0	1
---	---

1	1
---	---

2	2
---	---

3	3
---	---

4	1
---	---

5	2
---	---

6	1
---	---

7	1
---	---

9	1
---	---

10	1
----	---

12	1
----	---

14	2
----	---

15	1
----	---

16	1
----	---

17	1
----	---

18	2
----	---

19	1
----	---

> breaks = seq(0, 20, 5),  
> s = cut(x, breaks, right = FALSE)  
> c = table(s)  
> transform(c)

	s	Freq.
1	[0, 5)	8
2	(5, 10]	5
3	(10, 15)	14
4	(15, 20)	6

PM

Can the following be p.d.f?

$$f(x) = \begin{cases} 2-x & ; 1 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

$$\Rightarrow \int_1^2 (2-x) dx$$

$$= \int_1^2 2dx - \int_1^2 x dx$$

$$= 2x \Big|_1^2 - \frac{x^2}{2} \Big|_1^2$$

$$= (4-2) - (2 - 0.5)$$

$$\neq 1$$

$\Rightarrow$  Not a p.d.f.

$$f(x) = \begin{cases} 3x^2 & ; 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\Rightarrow \int_0^1 (3x^2) dx$$

$$= \int_0^1 \frac{3x^3}{3}$$

$$= x^3 \Big|_0^1$$

$\Rightarrow$  It is a p.d.f.

$$\text{iii) } f(x) = \begin{cases} \frac{3x}{2} \left(1 - \frac{x}{2}\right); & 0 \leq x \leq 2 \\ 0, & \text{otherwise} \end{cases}$$

$$\Rightarrow \int_0^2 \left( \frac{3x}{2} - \frac{3x^2}{4} \right) dx$$

$$= \frac{3}{2} \int_0^2 x \, dx - \frac{3}{4} \int_0^2 x^2 \, dx.$$

$$= \frac{3}{2} \left[ \frac{x^2}{2} \right]_0^2 - \frac{3}{4} \left[ \frac{x^3}{3} \right]_0^2$$

$$= \frac{3}{4} [x^2]_0^2 - \frac{1}{4} [x^3]_0^2$$

$$= \frac{3}{4} [4] - \frac{1}{4} [8]$$

$$= 1$$

$T^4$  is a p.d.f.

Can the following be p.m.f

$x$	1	2	3	4	5
$p(x)$	0.2	0.3	-0.1	0.5	0.1

Since, 1 of the probability is negative, it is not a p.m.f.

$x$	0	1	2	3	4	5
$p(x)$	0.1	0.3	0.2	0.2	0.1	0.1

Since  $p(x) \geq 0 \ \forall x$

$$\text{and } \sum p(x) = 1$$

$\therefore$  It is a p.m.f

$x$	10	20	30	40	50
$p(x)$	0.2	0.3	0.3	0.6	0.2

Since  $p(x) \geq 0 \ \forall x$

$$\text{and } \sum p(x) \neq 1$$

$\therefore$  It is not a p.m.f.

Since  $p(x) \geq 0 \ \forall x$

Find  $P(x \leq 2)$ ,  $P(2 \leq x \leq 4)$ ,  $P(\text{at least } 4) \quad P(3 < x < 6)$

$x$	0	1	2	3	4	5	6
$p(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\rightarrow P(2 \leq x \leq 2)$$

$$\begin{aligned} &= P(0) + P(1) + P(2) \\ &= 0.1 + 0.1 + 0.2 \\ &= 0.4 \end{aligned}$$

$$P(2 \leq x \leq 4)$$

$$\begin{aligned} &= P(2) + P(3) \\ &= 0.2 + 0.2 \\ &= 0.4 \end{aligned}$$

$$P(\text{at least } 4)$$

$$\begin{aligned} &= P(4) + P(5) + P(6) \\ &= 0.1 + 0.2 + 0.1 \\ &= 0.4 \end{aligned}$$

$$P(3 < x < 6)$$

$$\begin{aligned} &= P(4) + P(5) \\ &= 0.1 + 0.2 \\ &= 0.3 \end{aligned}$$

RM

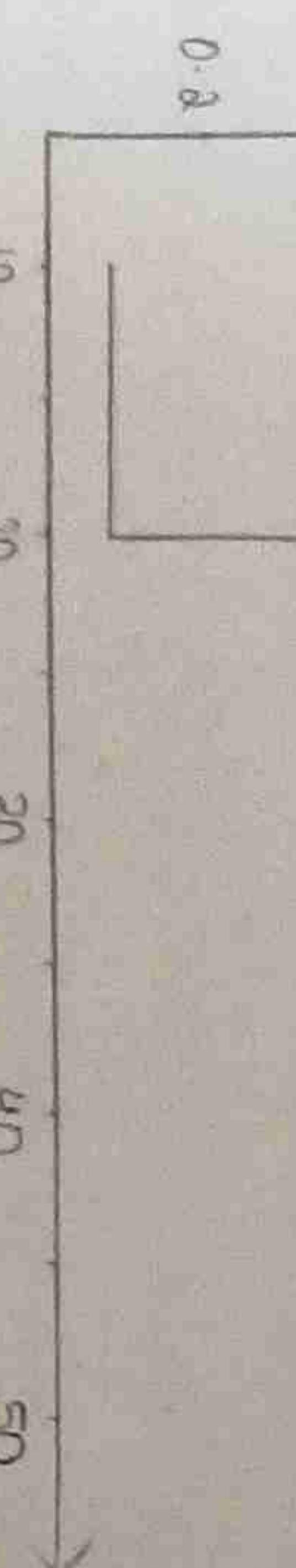
## Probability Distribution

Find c.d.f.s of the following p.m.t draw the graph

$x$	10	20	30	40	50
$p(x)$	0.15	0.25	0.3	0.2	0.1

$$\begin{aligned}
 f(x) &= 0 && \text{if } x < 10 \\
 &= 0.15 && 10 \leq x < 20 \\
 &= 0.40 && 20 \leq x < 30 \\
 &= 0.70 && 30 \leq x < 40 \\
 &= 0.90 && 40 \leq x < 50 \\
 &= 1.0 && x \geq 50
 \end{aligned}$$

Probability



```

> x = c(10, 20, 30, 40, 50)
> prob = c(0.15, 0.25, 0.3, 0.2, 0.1)
> cumsum(prob)
[1] 0.15 0.40 0.70 0.90 1.00
> plot(x, cumsum(prob), xlab = "Values", ylab = "Probability",
      main = "graph of c.d.f.", "s")
    
```

Values

## Binomial Distribution

Suppose there are 12 mcq's in a test each question has 5 options and only one of them is correct. Find probability of having (1) 5 correct answers (2) At least 4 correct answers.

→ Given that

$$n = 12, p = 1/5, q = 4/5$$

$x$ : Total no. of correct answers

$$x \sim B(n, p)$$

$$n = 12, p = 1/5, q = 4/5, x = 5$$

>  $n = 12; p = 1/5; q = 4/5; x = 5$

> sum ln, p, q, x)

[1] 18

> dbinom(5, 12, 1/5)

[1] 0.05315022

> pbinom(4, 12, 1/5)

[1] 0.9274445

There are 10 members in a committee, the probability of any member attending a meeting is 0.9. Find the probability 7 members attended.

At least 5 members attended.

At most 6 members attended.

> Given that

$$n = 10, p = 0.9 \quad \therefore q = 0.1$$

$x$  = Total no. of members attended

$$x \sim B(n, p)$$

$$n = 10, p = 0.9, q = 0.1$$

$$> n = 10, p = 0.9, q = 0.1$$

$$> \text{dbinom}(7, 10, 0.9)$$

$$[1] 0.05739563$$

$$> 1 - \text{qbinom}(5, 10, 0.9)$$

$$[1] 0.9983651$$

$$> \text{qbinom}(6, 10, 0.9)$$

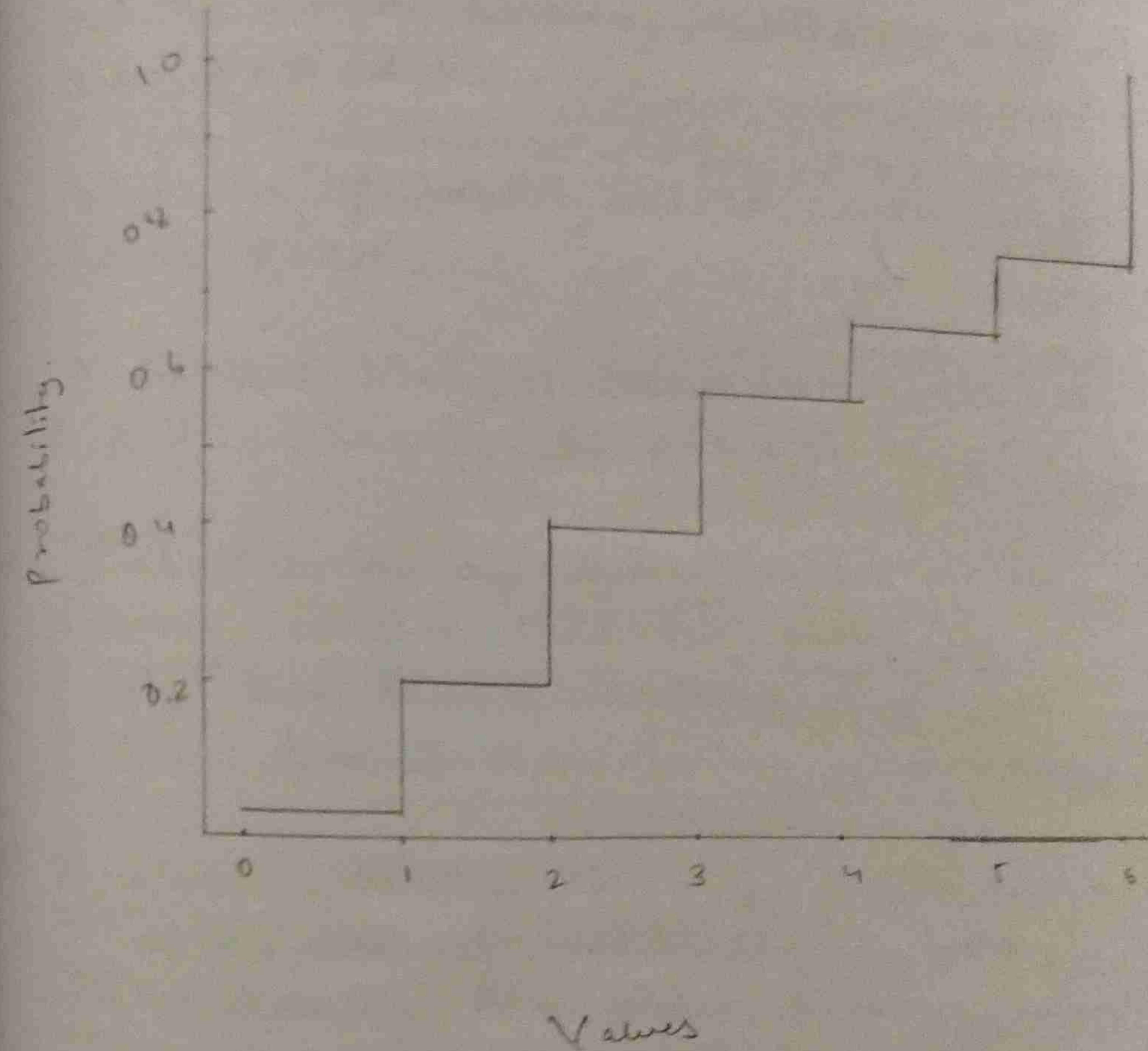
$$[1] 0.0127952$$

4 Find the c.d.f and draw the graph.

$x$	0	1	2	3	4	5	6
$p(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

```
> x = c(0,1,2,3,4,5,6)
> prob = c(0.1,0.1,0.2,0.2,0.1,0.2,0.1)
> cumsum(prob)
[1] 0.1 0.2 0.4 0.6 0.7 0.8 1.0
> plot(x, wsum(prob), xlab="values", ylab="probability",
       main="graph of C.d.F.", "s")
```

graph c.d.f



AM  
11/12/19

## Binomial Distribution

Find the complete binomial distribution when  $n = 5$  and  $p = 0.1$ .

Find the probability of 10 success in 100 times where  $p = 0.1$

$x$  follows binomial distribution with  $n = 12$ ,  $p = 0.25$   
find (1)  $P(x=5)$  (2)  $P(x \leq 5)$ , (3)  $P(x > 7)$  (4)  $P(5 \leq x \leq 7)$

Probability of a salesman makes a sell to a customer is 0.15 Find the probability.

1) No sale for 10 customers.

2) More than 3 sales in 20 customers.

3) A student writes 5 mcq's each question has 4 option out of which one is correct. Calculate the probability for atleast 3 correct answer.

$x$  follows binomial distribution with  $n = 10$ ,  $p = 0.2$   
Plot the graph of p.m.f. and c.d.f.

# Note

$$p(x=x) = \text{dbinom}(x, n, p)$$

$$p(x \leq x) = \text{pbinom}(x, n, p)$$

$$p(x > x) = 1 - \text{binoml}(x, n, p)$$

To find the value of  $x$  for which the probability is given as  $P_1$ , command is  $\text{qbinom}$ .

$$\Rightarrow \text{qbinom}(P_1, n, p)$$

\* Answers :-

1.  $n=5, p=0.1$

$$\text{dbinom}(0.5, 5, 0.1)$$

[1] 0.59049 0.32805 0.07290 0.00810 0.00045

2  $x=10, n=100, p=0.1$

$$\text{dbinom}(10, 100, 0.1)$$

[1] 0.1318653

3.  $n=12, p=0.25$

1)  $p(x=5) = \text{dbinom}(x, n, p)$

$$> \text{dbinom}(5, 12, 0.25)$$

[1]

2)  $p(x \leq 5) = \text{pbinom}(x, n, p)$

$$> \text{pbinom}(5, 12, 0.25)$$

[1] 0.9455978

$$P(5 < x < 7) = \text{dbinom}(x, n, p)$$

$$> \text{dbinom}(6, 12, 0.25)$$

[i] 0.04014945

$$P(x \geq 7) = 1 - P(\text{binom}, (x, n, p))$$

$$= 1 - \text{pbinom}(7, 12, 0.25)$$

[i] 0.00278151

$$p = 0.15$$

$$1) n = 10, P = 0.15, x = 0$$

$$> \text{dbinom}(0, 10, 0.15)$$

[i] 0.1968744

$$p = 0.15, n = 20$$

$$P(x > 3) = 1 - P(x \leq 3)$$

$$> 1 - \text{pbinom}(3, 20, 0.15)$$

[i] 0.3522748.

$$n = 5, p = 1/4$$

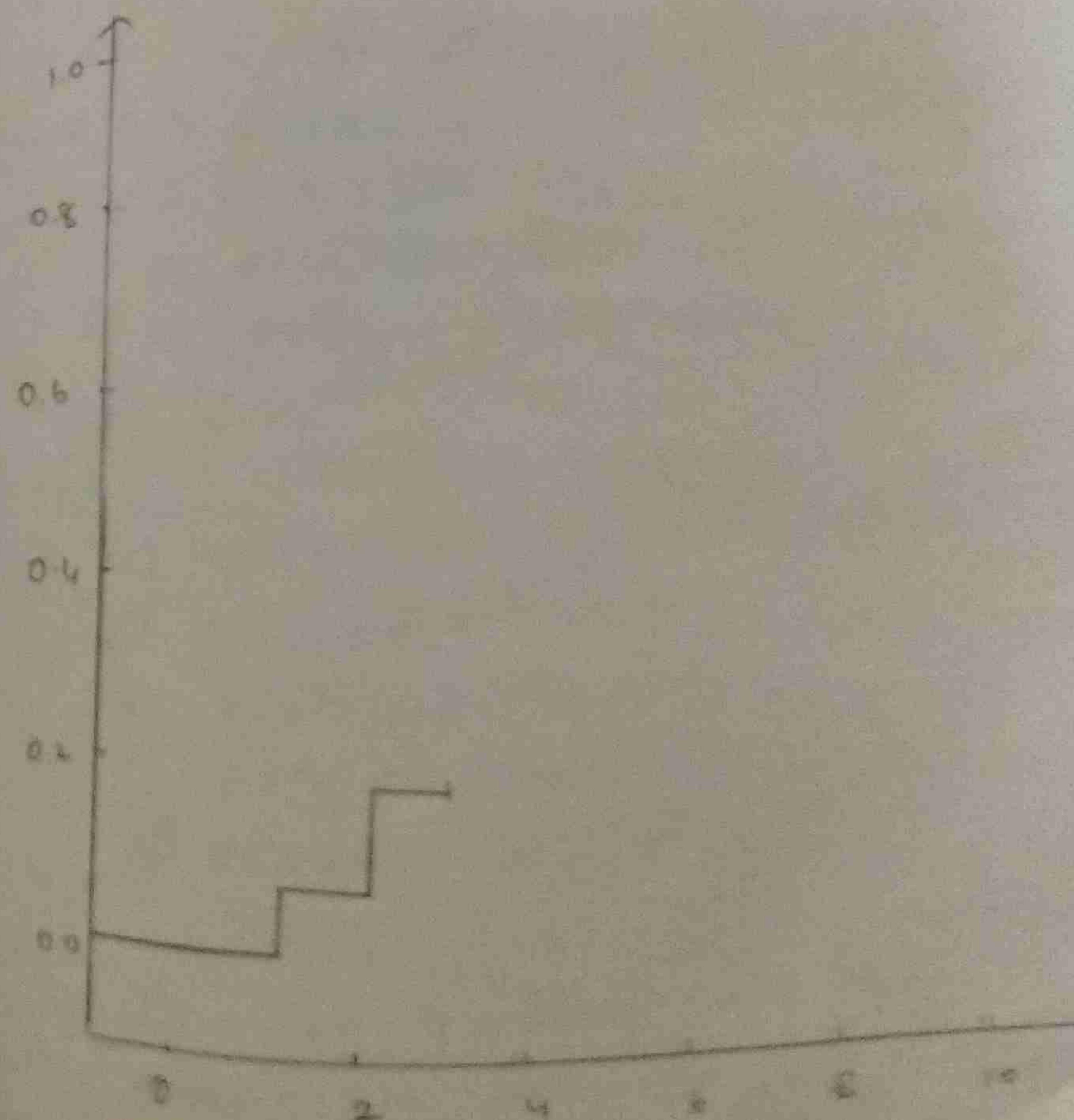
$$P(x \geq 3)$$

$$< 1 - P(x \leq 2)$$

$$> 1 - \text{pbinom}(3, 5, 1/4)$$

[i] 0.015625

6.  $n=10, p=0.4$   
 $x = 0:n$   
 $> prob = dbinom(x, n, p)$   
 $> cumprob = pbisnom(0:10, 10, 0.4)$   
 $> d = data.frame("x values" = 0:10, "probability" = prob)$   
 $> print(d)$   
 $> plot(0:10, prob, "n")$



PRACTICAL - 5

Note :-

1.  $P[X = x] = \text{dnorm}(x, \mu, \sigma)$
2.  $P[X \leq x] = \text{pnorm}(x, \mu, \sigma)$
3.  $P[X > x] = 1 - \text{pnorm}(x, \mu, \sigma)$
4.  $P[x_1 < x < x_2] = \text{pnorm}(x_2, \mu, \sigma) - \text{pnorm}(x_1, \mu, \sigma)$

5. To find the value of K so that

$$P[X \leq K] = P_i ; \text{pnorm}(P_i, \mu, \sigma)$$

6. Two generation random no. the command is  
 $\text{rnorm}(n, \mu, \sigma)$ 

$$X \sim N(\mu = 50, \sigma^2 = 100)$$

Find (1)  $P(X \leq 40)$

(2)  $P(X > 55)$

(3)  $P(42 \leq X \leq 60)$

(4)  $P(X \leq K) = 0.7, K = ?$

$$X \sim N$$

Find (1)  $P(X \leq 110)$

(2)  $P(X \leq 95)$

(3)  $P(X > 115)$

(4)  $P(95 \leq X \leq 105)$

(5)  $P(X \leq K) = 0.4, K = ?$

Generate 10 random nos from a normal distribution with mean ( $\mu = 60$ ) and S.D ( $\sigma = 5$ )  
 calculate the sample mean, median, variance and standard deviation

Solution:

1. > a = pnorm(40, 50, 10)

> cat ("P(X ≤ 40) is = ", a)

[1] 0.1886553

2. > b = 1 - pnorm(35, 50, 10)

[1] 0.3085375

3. > c = pnorm(60, 50, 10) - pnorm(42, 50, 10)

[1] 0.6294893

4. > d = qnorm(0.7, 50, 10)

[1] 55.24401

2) 1. > a = pnorm(110, 100, 6)

> a

[1] 0.9522096

> b = pnorm(98, 100, 6)

> b

[1] 0.2023284

>c = 1 - pnorm(115, 100, 6)

>c  
[1] 0.006209665

>d = pnorm(105, 100, 6) - pnorm(95, 100, 6)

>d  
[1] 0.5953432

>e = qnorm(0.4, 100, 6)

>e

[1] 98.47992

>x = rnorm(10, 60, 5)

>x

[1] 64.30801 56.28556 51.12444 62.66236 57.07212  
52.90556 63.04319 59.37558 59.78091 56.48464

>am = mean(x)

>am

[1] 58.30124

>me = median(x)

>me

[1] 58.22385

>n = 10

>variance = (n-1) \* var(x) / n

[1] 17.05339

>sq = sqrt(variance)

[1] 4.129575

4.  $> x = seq(-3, 3, by = 0.1)$

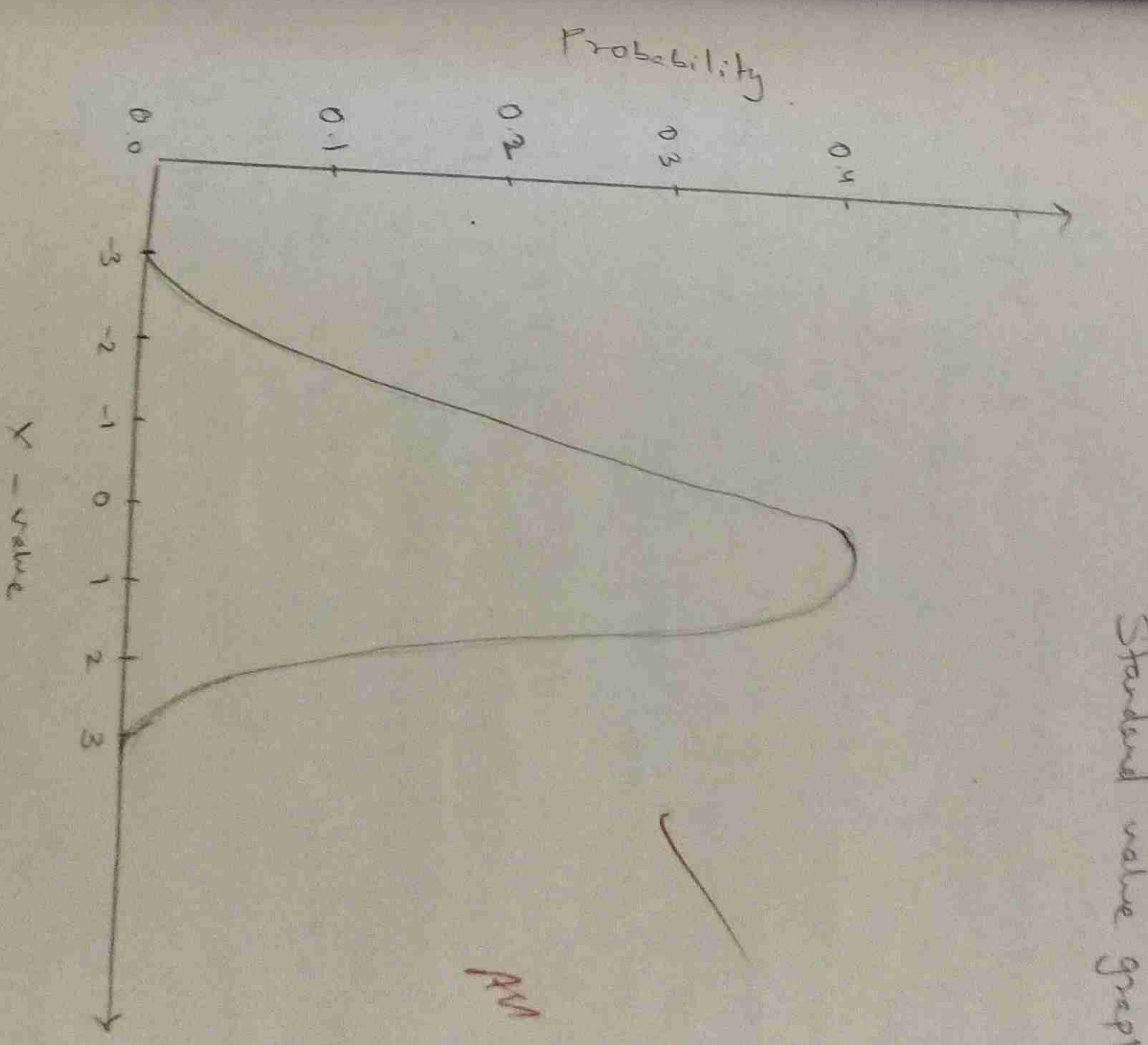
$> x$

```
[1] -3.0 -2.9 -2.8 -2.7 -2.6 -2.5 -2.4 -2.3 -2.2 -2.1
-2.0 -1.9 -1.8 -1.7 -1.6 -1.5 -1.4 -1.3 -1.2 -1.1
-1.0 -0.9 -0.8 -0.7 -0.6 -0.5 -0.4 -0.3 -0.2 -0.1
```

$> y = dnorm(x)$

$> y$

$> plot(x, y, xlab = "x values", ylab = "probability", main =$   
 , standard normal graph")



Standard value graph

Topic -  $Z$  distribution.

Test the hypothesis ( $H_0$ )  $H_0: \mu = 10$  against  $H_1: \mu \neq 10$ . A sample of size 400 is selected which gives the mean 10.2 and standard deviation 2.25. Test the hypothesis at 5% level of significance.

$> m_0 = 10; mx = 10.2; sd = 2.25; n = 400$

$> z_{\text{cal}} = (mx - m_0) / (sd / \sqrt{n})$

$> z_{\text{cal}}$

[1] 1.777778

$> cat ("z_{\text{cal}} \text{ is } ", z_{\text{cal}})$

$> [1] z_{\text{cal}} \text{ is } = 1.777778$

$> pvalue = 2 * (1 - pnorm (abs (z_{\text{cal}})))$

$> pvalue$

[1] 0.07544036

: The answer is more than 0.05, the value of the  $H_0$  is correct.

Test the hypothesis  $H_0: \mu = 75$  against  $H_1: \mu \neq 75$ . A sample of size 100 is selected and sample mean is 80 with standard deviation of 3. Test the hypothesis at 5% level of significance.

$> m_0 = 75; mx = 80; sd = 3; n = 100$

$> z_{\text{cal}} = (mx - m_0) / (sd / \sqrt{n})$

$> z_{\text{cal}}$

[1] 16.66667

> cat ("zcal is = ", zcal)

zcal is = 16.66667

> pvalue = 2 \* (1 - pnorm (abs(zcall)))

> pvalue

[1] 0.

Since, the value of is less than 0.05, the value of  $H_0$  is incorrect.

- 3) Test the hypothesis  $H_0: \mu = 25$  against  $H_1: \mu \neq 25$  at 5% level of significance. Following sample of 30 is selected.

$x = 20, 24, 27, 35, 30, 46, 26, 27, 10, 20, 30, 37, 35, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 39, 27, 15, 19, 22, 20, 18.$

> mx = mean(x)

> mx

[1] 26.06667

> n = length(x)

> n

[1] 30

> variance = (n-1) \* var(x) / n

> variance

[1] 52.99556

> sd = sqrt(variance)

> sd

[1] 7.279805

> m0 = 25; mx = 26.07; sd = 7.28; n = 30

> zcal = (mx - m0) / (sd / sqrt(n))

$z_{\text{cal}}$ 

[1] 0.8050318

&gt; cat, ("zcal is", "zcal")

zcal is = 0.8050318, &gt; pvalue = 2 \* (1 - pnorm(abs(zcal)))

&gt;pvalue

[1] 0.4208013.

$\therefore$  The value is more than 0.05, the value of  $H_0$  is correct.

Experience has shown that 20% student of a college smoke. A sample of 400 students reveal that out of 400 only 50 smoke. Test the hypothesis that the experience gives the correct proportion, or not.

&gt;p = 0.2

&gt;Q = 1 - p

&gt;Q

[1] 0.8

&gt;p = 50 / 400

&gt;p

[1] 0.125

&gt;n = 400

&gt;zcal = (p - Q) / (sqrt(p \* Q / n))

&gt;zcal

[1] -3.75

$\therefore$  The value is less than 0.05, the value of  $H_0$  is not accepted.

8.3

5) Test the hypothesis  $H_0: P = 0.5$  against  $H_1: P \neq 0.5$ . A sample of 200 is selected and the sample proportion is calculated  $\hat{P} = 0.36$ . Test the hypothesis at 2% level of significance.

$$> P = 0.5$$

$$> Q = 1 - P$$

$$> Q = 0.5$$

$$> P = 0.56$$

$$> n = 200$$

$$> z_{\text{cal}} = (\hat{P} - P) / (\sqrt{P \cdot Q / n})$$

$$(1) -1.697056$$

$$> p_{\text{value}} = 2 * \text{1-pnorm}(|z_{\text{cal}}|))$$

$$(1) 0.89688$$

$\therefore$  The value is more than 0.05, the value of  $H_0$  is accepted.

P

$$((n \cdot 0.5^2) + 0.5) / (0.5 \cdot 0.5)$$

## PRACTICAL - 7

## Large Sample Test

A study of noise level into hospital is calculated below.  
 Test the hypothesis that the noise level into hospital. Test  
 the hypothesis that the noise level in 2 hospital are  
 same or not.

	Hos A	Hos B
No. of sample obj.s	84	34
Mean	61	59
S.D	7	8

$H_0$ : The noise level are same

$$n_1 = 84$$

$$n_2 = 34$$

$$m_x = 61$$

$$m_y = 59$$

$$s_{dx} = 7$$

$$s_{dy} = 8$$

$$z = (m_x - m_y) / \sqrt{s_{dx}^2/n_1 + s_{dy}^2/n_2}$$

> z

$$[1] 1.273682$$

> cat("z calculated is = ", z)

2 calculated is = 2 > pvalue = 2 \* (1 - pnorm(abs(z)))

pvalue

$$[1] 0.1291361$$

Since the pvalue is 0.1291361, we reject  $H_0$  at 5% level of significance.

Q3.

2. Two random sample of size 1000 and 2000 are drawn from 2 population with the means 67.5 and 68 respectively and with same S.D of 2.5. Test the hypothesis the mean of 2 population are equal.

$H_0$ : 2 population are equal

$n_1 = 1000$

$n_2 = 2000$

$m_x = 67.5$

$m_y = 68$

$s_{dx} = 2.5$

$s_{dy} = 2.5$

$$z = (m_x - m_y) / \sqrt{(\frac{s_{dx}^2}{n_1} + \frac{s_{dy}^2}{n_2})}$$

[1] -5.1

> cat("z calculated is = ", 2)

2 calculated

> pvalue = 2 \* (1 - pnorm (abs(z)))

[1] 2.417

Since the p-value is 2.417 which is less than level of significance, we reject at 5% level.

In PIBSC 2014 of a random sample of 400 students had defective eye sight in class 15.5% of 500 sample had the same defect. Is the difference of proportion is same?

$H_0$  = The proportion of population is equal.

$$> n_1 = 400$$

$$> n_2 = 500$$

$$> p_1 = 0.2$$

$$> p_2 = 0.155$$

$$> p = (n_1 \times p_1 + n_2 \times p_2) / (n_1 + n_2)$$

$$> p$$

$$(i) 0.175$$

$$> q = 1 - p$$

$$> q$$

$$(ii) 0.825$$

$$> z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$z$$

$$(i) 1.76547$$

$$> \text{cal } z^2 \text{ calculated is } z^2$$

$$2 \text{ calculated is } z^2 = 1.76547^2 \text{ pvalue} = 2 \times (1 - \text{norm.pdf}(z))$$

$$> \text{pvalue}$$

$$(ii) 0.7748487$$

Since pvalue of 0.7748487, we accept  $H_0$  at 5% level of significance.

Q) From each of the box of the apple, a sample size of 200 is collected. It is found that there are 44 bad apple in the 1st sample and 36 bad apple in 2 sample test the hypothesis that the 2 boxes are equivalent in terms of number of bad apple.

$H_0$  = The proportion of boxes is same.

$$> n_1 = 200$$

$$> n_2 = 200$$

$$> p_1 = 44/200$$

$$> p_2 = 36/200$$

$$> p_1 = 0.22$$

$$> p_2 = 0.15$$

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$[1] 0.185$$

$$> q = 1 - p$$

$$> q$$

$$[1] 0.815$$

$$> z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> z$$

$$[1] 1.802741$$

> cat("calculated is = ", z)

? calculated is = 1.802741 > pvalue = 2 \* pnorm(abs(z))

> pvalue

$$[1] 0.714288$$

Since pvalue is 0.714, we accept at 5% of level significance.

In a MA class out of the sample of 60 mean height is 63.5 inch with a SD 2.5. In an M.com class out of 50 student mean height 69.5 inch with SD of 2.5. Test the hypothesis that the means of MA & M.com classes are same.

$H_0$  = Mean height of MA and Mean Students are equal

$$>n1 = 60$$

$$>n2 = 50$$

~~$>m_x = 63.5$~~

~~$>m_y = 69.5$~~

~~$>sdx = 2.5$~~

~~$>sdy = 2.5$~~

$$>z = (m_x - m_y) / \sqrt{((sdx^2/n1) + (sdy^2/n2))}$$

$$>z$$

$$(1) -12.4335$$

Cat ("z calculated is = ", z)

$$? pvalue = 2 * (1 - pnorm (abs(z)))$$

? pvalue

$$(2) 0.09500026$$

Since, pvalue is 0.09, we reject 1.5 level of significance.

AM

7.21.20

Practical - 8

## Small Sample Test

Q.I. Tens are selected & height are found to be 63, 63, 68, 69, 71, 71, 72 cms. Test hypothesis that mean height  $x$  are 66 cm or not at 1%.

$$H_0: \text{Mean} = 66 \text{ cms.}$$

> mean = 66  
>  $x = [63, 63, 68, 69, 71, 71, 72]$

> t-test ( $x$ )

One Sample t-test

data :  $x$

$t = 4.744$ , df = 6, p-value = 5.22e-09.

alternative hypothesis : true mean is not equal to 66  
95 percent confidence Interval:

64.6499 : 71.12091

Sample estimates :

mean of  $x$

68.14286

: p-value < 0.01 is rejected on H<sub>0</sub> in 1% level of significance.

Q.II

Two random sample was drawn from two different population.

Sample 1 = 8, 10, 12, 11, 16, 15, 18, 7.

Sample 2 = 20, 15, 16, 9, 8, 10, 11, 12.

Test the hypothesis that there is no difference between the population mean at 5% level.

H<sub>0</sub> there is no difference in the population

t-test ( $x, y$ )

> t-test Two Sample Test

data :  $x$  by  $y$

$t = -0.36247$ , df = 13.837, p-value = 0.7225.  
alternative hypothesis : true difference in mean is not equal to 3.692719.

Sample estimates

mean of  $x$  mean of  $y$

12.125

12.845

p-value < 0.01 is accepted in H<sub>0</sub> on 1% level of signifi-

cance.

Q.III Following are the weights of 10 people

Before = (100, 125, 95, 96, 98, 102, 115, 104, 109, 110)

After = (95, 80, 95, 98, 90, 100, 110, 85, 100, 101)

H<sub>0</sub>. The Diet Program is not effective

>  $x = [100, 125, 95, 96, 98, 102, 115, 104, 109, 110]$

>  $y = [95, 80, 95, 98, 90, 100, 110, 85, 100, 101]$

> t-test ( $x, y$ , paired = T, alternative = "less")

Paired t-test

data :  $x$  and  $y$

$t = 2.3215$ , df = 9, p-value = 0.9473

Alternative hypothesis: True difference in means is less than 0, 95% confidence interval.

Test the hypothesis that there is no difference between the

population mean at 5% level.

-Test 12.99635

Sample estimate -

Mean of the differences is

of Marks before and after a training program is given below:

Before = 20, 25, 32, 28, 24, 36, 35, 25

After = 30, 35, 32, 37, 34, 40, 40, 23

Test the hypothesis that training program is effective or not.

$H_0$  : The training program is not effective.

> $x = c(20, 25, 32, 28, 24, 36, 35, 25)$

> $y = c(30, 35, 32, 37, 34, 40, 40, 23)$

> $t.test(x, y, paired = T, alternative = "greater")$

Paired t-test

Data :  $x$  and  $y$

$t = -3.3959, \text{ df} = 7, p\text{-value} = 0.9942$ .

Alternative hypothesis : True ratio of means is greater than 25  
to 1 at 95 percent confidence interval.

6.1933662 3.0360393

Sample estimates :  
Ratio of variances 0.796567

$H_0$  : The A.R of Sample 100 observations is 52 i.e.  $S_D \leq 7$  test the hypothesis that the population mean 55 or not at 5% of level of significance.

$n = 100$  6.1933662 3.0360393

$m_x = 52$  6.1933662 3.0360393

$m_{S_D} = 55$  6.1933662 3.0360393

$s_d = 7$  6.1933662 3.0360393

> $z_{cal} = (m_x - m_0) / (S_D / \sqrt{n})$

> $p\text{-value} = 2 * (1 - pnorm(z_{cal}))$

[1] 1.82153e-05

5) Two random sample were drawn from the normal population.

The values are :

A = 66, 67, 75, 76, 82, 84, 88, 90, 92

B = 64, 66, 74, 76, 82, 85, 87, 92, 93, 95, 97

Test whether the population have same variance at 5% level of significance.

$\mu_0$  = variance of the population are equal.

> $x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$

> $y = c(64, 66, 74, 76, 82, 85, 87, 92, 93, 95, 97)$

> $var.test(x, y)$ .

F test to compare two variances.

Data :  $x$  and  $y$

F = 0.70686, num df = 8, denom df = 10, p-value = 0.6399

Alternative hypothesis : True ratio of variances is not equal to 1 at 95 percent confidence interval.

6.1933662 3.0360393

## PRACTICAL - 9

## Chi-Square &amp; ANOVA

Use the following data to test whether the condition of the name depends upon the child condition or not.

Condition of name

		clean	dirty
lead	clean	70	50
child	fairly	80	20
	dirty		
	dirty	35	45

$\Rightarrow H_0$ : condition of the name and child are independent

$> x = c(70, 80, 35, 50, 20, 45)$

$> m = 3$

$> n = 2$

$> y = \text{matrix}(x, nrow = n, ncol = m)$

	[,1]	[,2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

$> pvalue = \text{chisq.test}(y)$

$> pvalue$ .

Pearson's Chi-squared test  
data = y

$\chi^2 = 25.646$ , df = 2, pvalue = 2.698e-06  
pvalue is less than 0.05 we reject H<sub>0</sub> at 5% LOS.

Table below shows the relation between the performances of mathematics and computer of 6 students.

Maths

	Mg	Mg	Lg
Hg	56	71	12
Mg	47	163	38
Lg	14	42	85

Q: performance between maths and computer are independent

x: c(56, 47, 14, 71, 163, 42, 12, 38, 85)

n: 2 (apple score, banana score) and p-value

n: 3 (apple, banana) were counted

y: matrix (2, nrow = m, ncol = n).

	[1,1]	[1,2]	[1,3]
[1,1]	56	71	12
[2,1]	47	163	38
[3,1]	14	42	85

Pvalue: chisq.test(y)

Pvalue

data y

x - squared = 145.75 , df = 4 , p.value < 2.2e-16 .

## Varieties      Observations

A                    50, 52

B                    53, 55, 53

C                    60, 58, 57, 56

D                    52, 54, 54, 55

Mean A, B, C, D

>  $x_1 = c(50, 52)$

>  $x_2 = c(53, 55, 53)$

>  $x_3 = c(60, 58, 57, 56)$

>  $x_4 = c(52, 54, 54, 55)$

> d = stack (list (b1=x1, b2=x2, b3=x3, b4=x4))

> oneway, test (values ~ ind, data=d, var.equal=TRUE)

anova = aov (values ~ ind, data=d)

F = 11.955, num df = 3, denom df = 9, p-value = 0.00016

summary (anova).

Acc | Pe,

## PRACTICAL -10

### Non-Parametric Test

Following are the amount of sulphur oxide.

Data :-

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 13, 6, 24, 14, 15  
23, 24, 26.

Apply sign test to test the hypothesis that population median is 21.5 against the alternative it is less than 21.5.

$H_0$  : population median = 21.5

$H_1$  : It is less than 21.5.

```
> x = c(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 13, 6, 24, 14  
15, 23, 24, 26)
```

> x

> m = 21.5

> sp = length(x[x > m])

> sn = length(x[x < m])

> n = sp + sn

> n

[1] 20

> pr = pbinom(sp, n, 0.5)

> pr

[1] 0.411

Note : If the alternative is greater than median,

$$pr = pbinom(sn, n, 0.5)$$

Date: 14/9/2017

2] For the observations

 $x = [12, 19, 31, 28, 43, 40, 55, 49, 70, 63]$ 

Apply sign test to test population median is 25 against the alternative is more than 25.

 $x = c(12, 19, 31, 28, 43, 40, 55, 49, 70, 63)$ 
 $m = 25$ 
 $s_p = \text{length}(x[x > m])$ 
 $s_n = \text{length}(x[x < m])$ 
 $n = s_p + s_n$ 
 $p_v = \text{pbinom}(s_n, n, 0.5)$ 
 $p_v$ 

(i) 0.054

3] 60, 65, 63, 89, 61, 71, 58, 51, 48, 66

Test the hypothesis using wilcoxon sign test.

For testing the hypothesis that the median is 60 against the alternative it is greater than 60.

$H_0$ : Median is 60.

$H_1$ : Median is greater than 60.

 $x = c(60, 65, 63, 89, 61, 71, 58, 51, 48, 66)$ 
 $s_p = \text{length}(x[x > m])$ 
 $s_n = \text{length}(x[x < m])$ 
 $n = s_p + s_n$ 
 $p_v = \text{pbinom}(s_n, n, 0.5)$ 

(i) 0.054

> wilcox.test(x, alter = "greater", mu = 60)  
 $v = 29$ , p-value = 0.2386.

alternative hypothesis: true location is greater than 60.

If the alternative is less,

wilcox.test(x, alter = "less", mu = -)

If the alternative is not equal to

wilcon-test(x, alter = "2.sided", mu = )

Using wilcoxon test, test the hypothesis where the median is 12 against the alternative is less than 12.

Data:

12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20)

> x = c(12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20)

> m = 12

> Sp = length(x[x >= m])

> Sn = length(x[x < m])

> n = Sn + Sp

> Pv = pbisoml(Sn, n, 0.5)

> Pv

[1]

> wilcon-test(x, alter = "less", mu = 12)

$v = 25$ , p-value = 0.775

Alternative hypothesis: true location is greater than 12.

DA  
11/3