

CM 3320 - Logic Programming
Assignment 2 (July 2018)

1. (a) Consider the following clauses in a Prolog program.

```
son_of (saman, ravi, manori).      % Saman is a son of Ravi and Manori.
son_of (kasun, ravi, manori).
son_of (amara, saman, amali).
son_of (sumith, kasun, sumana).
son_of (palitha, kasun, sumana).
son_of (sugath, shanaka, shalini).
son_of (jeewaka, shanaka, shalini).
son_of (prabath, lal, neela).
son_of (sahan, amara, nalini).
son_of (jeevan, kamal, ruwanthi).
son_of (mahesh, sumith, geetha).
son_of (sajith, sumith, geetha).
son_of (gihan, palitha, champa).
son_of (panduka, nihal, chandani).
daughter_of(shalini, ravi, manori). % Shalini is a daughter of Ravi and Manori.
daughter_of(neela, saman, amali).
daughter_of(praba, amara, nalini).
daughter_of(ruwani, kasun, sumana).
daughter_of(chandani, shanaka, shalini).
daughter_of(dilani, nihal, chandani).
daughter_of(nilushi, jeewaka, priyani).
```

Define the following relations:

(i)	father_of (X,Y).	% X is the father of Y
(ii)	mother_of (X,Y).	% X is the mother of Y
(iii)	parent_of (X,Y).	% X is a parent of Y
(iv)	brother_of (X,Y).	% X is a brother of Y
(v)	sister_of (X,Y).	% X is a sister of Y
(vi)	grandparent_of(X,Y).	% X is a grandparent of Y
(vii)	grandgrandfather_of(X,Y).	% X is a grand grandfather of Y
(viii)	husband_of(X,Y).	% X is the husband of Y
(ix)	married_to(X,Y).	% X is married to Y
(x)	cousin_of (X,Y).	% X is a cousin of Y
(xi)	uncle_of (X,Y).	% X is an uncle of Y
(xii)	father_in_law(X,Y).	% X is the farther-in-law of Y
(xiii)	brother_in_law(X,Y).	% X is the brother-in-law of Y
(xiv)	son_in_law (X,Y).	% X is the son-in-law of Y

- (b) Using the knowledge base in part 1(a), formulate Prolog queries for the following requests and questions.
- (i) Find all the brothers and sisters of Ruwani.
 - (ii) Who is the grand mother of Suranga.
 - (iii) Find all descendants of Kasun.
 - (iv) List all the fathers who appear in the database.
 - (v) Find all the cousins of Kasun.
 - (vi) By using the husband_of relation find the husband of Priyani and the wife of Sumith.
 - (vii) Who is the father-in-law of Champa?

2. (a) Define the relation,
 $\text{conc}(L1, L2, L)$,
 where L is the concatenation of the two lists $L1$ and $L2$.
 Using the conc relation, define the following relations.
- (i) $\text{sublist}(S, L)$ is true iff the list S occurs within the list L as its sub list.
 - (ii) $\text{shift}(L1, L2)$ is true iff $L2$ is $L1$, shift rotationally by an element to the left.
 For example,
 $|\text{?_shift}([1, 2, 3, 4, 5], L)$.
 gives the result
 $L = [2, 3, 4, 5, 1]$.
 - (iii) $\text{last}(\text{Item}, \text{List})$ is true iff Item is the last element of a list List .
- (b) Define two predicates,
 (i) $\text{evenlength}(\text{List})$
 (ii) $\text{oddlength}(\text{List})$,
 so that they are true if their arguments in a list of even or odd length respectively.
 For example, list $[e, v, e, n]$ is even length and $[o, d, d]$ is odd length.
3. (a) Define the relation,
 $\text{translateList}(\text{List1}, \text{List2})$
 to translate a list of numbers between 0 and 9 to a list of the corresponding words.
 For example:
 $|\text{?_translateList}([3, 4, 2, 4], \text{List2})$.
 Gives the result,
 $\text{List2} = [\text{three}, \text{four}, \text{two}, \text{four}]$.
- (Hint: Use the following as an auxiliary relations: $\text{means}(0, \text{zero})$, $\text{means}(1, \text{one})$, $\text{means}(2, \text{two})$, ..., $\text{means}(9, \text{nine})$)
- (b) Write predicates for the following:
- (i) $\text{cutlast}(L1, L2)$ which is true if $L2$ is $L1$ with the last element removed.
 - (1) Using the relation conc .
 - (2) Without using the relation conc .
 - (ii) $\text{trim}(L1, N, L2)$ which is true if $L2$ contains the first N elements of $L1$.
 - (1) Using the relation conc .
 - (2) Without using the relation conc .
4. (a) (i) Define the relation
 $\text{reverse}(\text{List}, \text{ReversedList})$
 that reverses the given list.
- (ii) A list is palindrome if it reads the same in the forward and in the backward direction. For example $[m, a, d, a, m]$.
 Define the relation, $\text{palindrome}(\text{List})$, with and without using reverse .
- (b) Will the following matching operations succeed or fail? If succeed what are the resulting instantiations of variables?
- (i) $\text{point}(A, B) = \text{point}(1, 2)$.

- (ii) `point(A,B)=point(X,Y,Z).`
 - (iii) `point(2,2)=4.`
 - (iv) `+(2,D)=+(E,2).`
 - (v) `triangle(point(-1,0),P2,P3)= triangle(P1,point(1,0),point(0,y)).`
- (c) Consider the following program:

```
f(1,one).
f(s(1),two).
f(s(s(1)),three).
f(s(s(s(X))),N):-f(X,N).
```

How will prolog answer the following questions? Whenever several answers are possible, give at least two.

- (i) `! ?_f(s(1),A).`
- (ii) `! ?_f(s(s(1)),two).`
- (iii) `! ?_f(s(s(s(s(s(1))))),C).`
- (iv) `! ?_f(D,three).`

5. (a) The algorithm for Merge Sort is as follows, to sort a list L:

1. Divide L into two lists A and B, of approximately equal length.
2. Sort A and B giving SA and SB.
3. Merge SA and SB giving sorted SL

Using the above algorithm, define the predicate, `msort(S, SL)`, where SL is the sorted list of list L.

- (b) Draw the search tree for the query

```
! ?_msort([6,1,3],A).
```

6. Assuming the operator definitions:

```
:-op(400,xfx,likes).
:-op(300,yfx,and).
:-op(200,fy,a).
```

Then the following terms are syntactically legal objects.

Term 1=`dulan likes mathematics and physics.`

Term 2=`dasun and maya likes mathematics and physics.`

Term 3=`dulan and dasun and maya likes mathematics and physics.`

- (a) How are these terms understood by Prolog?
- (b) What are their principal functors? and what is their structure?
- (c) What will be the answer to the following queries?
 - (i) `! ?_dasun and maya likes What.`
 - (ii) `! ?_Who likes mathematics and physics.`

7. (a) The following Prolog program defines the relation , count(N,X,L) , Which is true if and only if N is the number of terms in the list L, which have value less than X.

```
count(0,X,[]).
count(N,X,[H|T]):-H<X,count(P,X,T), N is P+1.
count(N,X,[H|T]):-H>=X,count(N,X,T).
```

Draw the search tree for the query `!_count(N,9,[8,6,10,5,12,3])`.

- (b) Consider the following Prolog program which calculates the mean of a given list of integers.

```
sum([],0).
sum([H|T],Sum):-sum(T,TSum),Sum is TSum+H.

length([],0).
length([X|R],Length):-length(R,RLength),Length is RLength+1.

Mean(L,Mean):-sum(L,Sum),length(L,N),Mean is Sum/N.
```

Draw the search tree for the query
`!_mean([4,13,-18,9],Mean)`.

8. (a) Let a program be:

```
p(1).
p(2):-!.
p(3).
```

Write all prolog answers to the following questions.

- (i) `!_p(X)`.
- (ii) `!_p(X),p(Y)`.
- (iii) `!_p(X),!,p(Y)`.

- (b) The following relation classified the number into three classes: positive, zero and negative.

```
class(Number,positive):-Number>0.
class(0,zero).
class(Number,negative):-Number<0.
```

Define the procedure in a more efficient way using cuts.

- (c) Define procedure `split(Number,Positive,Negative)` which splits a list of numbers into two lists, positive ones(including zero) and negative ones.

For example,

```
!_split([3,-9,0,5,-2],[3,0,5],[-9,-2]).
Yes.
```

Propose two versions:

- (i) With a cut
- (ii) Without cut