

1. No. of parakeets $n(p) = 8$
No. of green parakeets $n(g) = 4$
No. of blue parakeets $n(b) = 4$

In all permutation and combination of all 8 parakeets, below are only 2 possibilities where no adjacent parakeets are of same color.

1) G B G B G B G B

2) B G B G B G B G

Hence Total permutations and combinations of ordering parakeets $n = \frac{n(p)!}{n(g)!n(b)!}$

$$\therefore n = \frac{8!}{4!4!} = 70$$

\therefore Probability of no two adjacent parakeets $p = \frac{2}{70} = \frac{1}{35}$

2. Probability of a ~~core~~ computer core being defective $p(d) = 0.3$

\therefore Probability of it being non-defective ~~$p(nd)$~~ =
 $p(nd) = 1 - p(d) = 1 - 0.3 = 0.7$

(a) A CPU has 8 cores which functions independent of each other.

\therefore Probability of all 8 core functioning
 $p = (0.7)^8 = 0.05764$

(b) \rightarrow Extreme model has 8 functioning cores

\therefore Probability of getting extreme model
 $p(e) = (0.7)^8 = 0.05764$

\therefore In ~~extreme~~ 1000 CPUs, no. of extreme model

$$n(e) = 1000 \times p(e) = 1000 \times 0.05764 \\ = 57.64 \approx \boxed{58}$$

\rightarrow Advance model has at least 8 functioning core

\therefore ~~$p(a)$~~ \therefore It has 1

\therefore It includes probabilities of having 5 cores, 6, 7 and 8 cores.

$$\therefore P(A) = {}^8C_8 (0.7)^8 (0.3)^0 + {}^8C_7 (0.7)^7 (0.3)^1 + {}^8C_6 (0.7)^6 (0.3)^2 + {}^8C_5 (0.7)^5 (0.3)^3 + {}^8C_4 (0.7)^4 (0.3)^4$$

$$P(A) = (1)(0.7)^8 + 8(0.7)^7(0.3) + 28(0.7)^6(0.3)^2 + 56(0.7)^5(0.3)^3 + 14(0.7)^4(0.3)^4$$

$$P(A) = 0.94203$$

\therefore In 1000 CPU cores, there can be $1000 \times 0.94203 = 942$ model which has at least 4 functioning core which includes exact 8 models having exact 8 functioning cores.

$$\therefore \text{No. of advance model} = 942 - 58 = \boxed{884}$$

\rightarrow Probability of having at least 1 core function = $1 - \text{probability of no core functioning}$

$$\therefore P = 1 - (0.3)^8 = 0.999934$$

\therefore In 1000 CPU cores there are $1000 \times 0.999934 = 999.934 \approx 1000$ CPU which has at least 1 core functioning which includes

advance and extreme models.

\therefore No. of great models

$$= 1000 - 884 - 58 = \boxed{58}$$

\rightarrow \therefore No. of Great models = 58

No. of Adv. models = 884

No. of Extreme models = 58

(C) Great model's cost = \$ 50

\therefore Revenue from great model = 50×58

Adv. model's cost = \$ 100

\therefore Revenue from adv. model = 100×884

Extreme model's cost = \$ 1000

\therefore Revenue from extreme model = 1000×58
 $= 58000$

\therefore T

\therefore Total Revenue = $2900 + 88400 + 58000$

$$= \boxed{\$ 149300}$$

3. Probability of judge voting accused given actually guilty
 $P(J = \text{"guilty"} \mid A = \text{"guilty"}) = 0.7$

If defendant is innocent, it drops to 0.2
 $P(J = \text{"guilty"} \mid A = \text{"innocent"}) = 0.2$

70% accused are guilty
 $P(A = \text{"guilty"}) = 0.7$

a) Judge 1 votes guilty.
 \therefore Probability of person being guilty given judge voted guilty

$$P(A = \text{"guilty"} \mid J = \text{"guilty"}) = \frac{P(J = \text{"guilty"} \mid A = \text{"guilty"}) P(A = \text{"guilty"})}{P(J = \text{"guilty"})}$$

$$= \frac{P(J = \text{"guilty"} \mid A = \text{"guilty"}) \times P(A = \text{"guilty"})}{P(J = \text{"guilty"})}$$

$$= \frac{0.7 \times 0.7}{0.49 + 0.14}$$

$$= \frac{0.49}{0.49 + 0.14} = \frac{0.49}{0.63} = \boxed{0.7778}$$

$$\frac{0.49}{(0.7)(0.7) + (0.3)(0.2)} = \frac{0.49}{0.55} = \boxed{0.89}$$

b) All three judges vote guilty.

∴ We need to find probability that accused is in fact guilty.

$$∴ P(A = \text{"G"} \mid J_1 = \text{"G"}, J_2 = \text{"G"}, J_3 = \text{"G"})$$

$$∴ P(A \mid J_1, J_2, J_3) = \frac{P(J_1, J_2, J_3 \mid A) P(A)}{P(J_1, J_2, J_3)}$$

$$P(J_1 = \text{"G"}, J_2 = \text{"G"}, J_3 = \text{"G"}) = P(\text{J}_1 = \text{"G"} \mid A) \times$$

$$= P(J_1, J_2, J_3 \mid A) P(A) + P(J_1 = \text{"G"} \mid A = \text{"I"}) \times$$

$$P(J_2 = \text{"G"} \mid A = \text{"I"}) \times P(J_3 = \text{"G"} \mid A = \text{"I"}) \times P(A = \text{"I"})$$

$$= (0.7)(0.7)(0.7)(0.7) + (0.3)(0.3)(0.3)(0.3)$$

$$= 0.2401 + 0.0027$$

$$= 0.2428$$

$$∴ P(A \mid J_1, J_2, J_3) = \frac{(0.7)(0.7)(0.7)(0.7)}{0.2428}$$

$$= \frac{0.2401}{0.2428}$$

$$= 0.99$$

$$\boxed{= 0.99}$$

c) J_1 & J_2 have voted "innocent"

Probability of judge 3 $P(J = "G")$

$$P(J_3 = G \mid J_1 = I, J_2 = I) = \frac{P(J_1 = I, J_2 = I, J_3 = G)}{P(J_1 = I, J_2 = I)}$$

$$P(J_1 = I, J_2 = I, J_3 = G) = P(J_1 = I \mid A = G) P(J_2 = I \mid A = G) P(J_3 = G \mid A = G) P(A = G) + P(J_1 = I \mid A = I) P(J_2 = I \mid A = I) P(J_3 = G \mid A = I) P(A = I)$$

$$= P(J_1 = I \mid A = G) P(J_2 = I \mid A = G) P(J_3 = G \mid A = G) P(A = G) + P(J_1 = I \mid A = I) P(J_2 = I \mid A = I) P(J_3 = G \mid A = I) P(A = I) \\ = (0.3)(0.3)(0.7)(0.7) + (0.8)(0.8)(0.2)(0.3) \\ = 0.0825$$

$$P(J_1 = I, J_2 = I) = P(J_1 = I \mid A = G) P(J_2 = I \mid A = G) P(A = G) + P(J_1 = I \mid A = I) P(J_2 = I \mid A = I) P(A = I) \\ = (0.3)(0.3)(0.7) + (0.8)(0.8)(0.3) \\ = 0.063 + 0.192 \\ = 0.255$$

$$\therefore P(J_3 = G \mid J_1 = I, J_2 = I) = \frac{P(J_1 = I, J_2 = I, J_3 = G)}{P(J_1 = I, J_2 = I)} = \frac{0.0825}{0.255} \\ = 0.3235$$