

(Assignment no 15)

Sol 1) The parametric tests are based on the assumption about the population parameters.

Non parametric test does not make any assumption about the population.

Parametric Test

Z test t test

Non Parametric test

Run test.

Sol 2) Some non parametric tests are..

① Run test

② Sign Test

③ Wilcoxon paired sample sign rank test.

Sol 3)

(A) 8 10 12 13 14 16 18 22
(B) 7 9 14 8 16 12 20

$$n_A = 8$$

$$n_B = 7$$

$$\begin{array}{cccccccccccccccc} 8 & 8 & 9 & 10 & 10 & 12 & 12 & 13 & 14 & 14 & 16 & 16 & 18 & 20 \\ \hline 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \end{array}$$

22
9

$$\text{Run} = 9$$

$$U = 9$$

$$E(U) = \left(\frac{2n_1 n_2}{n_1 + n_2} \right) + 1 = \frac{2 \times 8 \times 7}{7 + 8} + 1 = 8.467$$

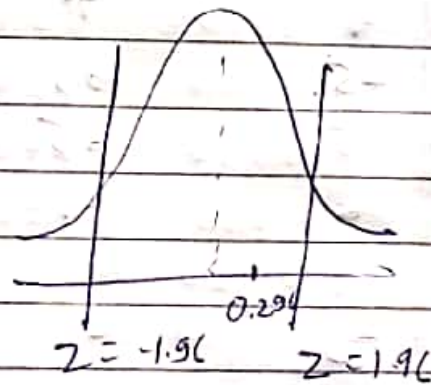
$$V(x) = \frac{2n_1 n_2 (2n_1 n_2 - n_1 - n_2)}{(n_1 + n_2)^2 (n_1 + n_2 - 1)}$$

$$= \frac{2 \times 8 \times 7 (2 \times 8 \times 7 - 8 - 7)}{(8+7)^2 (8+7-1)}$$

$$= \frac{112 \times (112 - 8 - 7)}{15^2 \times 14} = 3.45$$

$$Z = \frac{U - E(U)}{\sqrt{V(U)}} = \frac{9 - 8.45}{\sqrt{3.45}} = 0.296$$

We cannot reject null hypothesis mean they belong to same population density.



Q14

x_i	y_i	$H_0: f(x) = f(y)$	$H_A: f(x) \neq f(y)$
14	10		
17	15		
19	18		
21	18		
9	11		
11	18		
16	14		
20	29		
12	6		
16	21		
18	17		
20	15		

$$d_i = [+4, -2, +1, +3, -2, -7, +2, -9, +6, 5, +1, +5]$$

$$\text{Rank} = [1, 1, 2, 2, 3, 3, 4, 5, 5, 6, 7, 9]$$

$$z = [1.5, 1.5, 2, 4, 4, 6, 7, 8.5, 8.5, 10, 11, 12]$$

~~T~~

Rank value pair

~~(T)~~

difference

Rank

1

1.5

1

1.5

-2

4

+2

4

2

4

3

6

4

7

-5

8.5

5

8.5

6

10

-7

11

-9

12

$$(T^+) \rightarrow (42.5)$$

$$(T^-) \rightarrow (35.5)$$

$$\min(T^+, T^-) \rightarrow 35.5$$

$$E(T) = \frac{n(n+1)}{4} = \frac{12 \times 13}{4} = 39$$

$$V(T) = \frac{n(n+1)(2n+1)}{24}$$

$$= \frac{12 \times 13 \times 25}{24} = 162.5$$

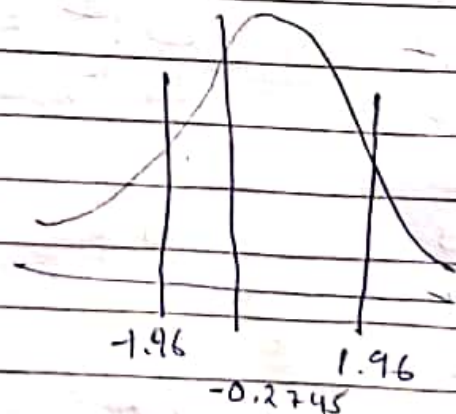
$$= 162.5$$

$$SD = 12.747$$

$$Z = \frac{35.5 - 39}{12.747}$$

$$= -0.2745$$

Now



We cannot reject null hypothesis

$$f(x) = f(y)$$