

1. What are the characteristics of a good estimator?
2. Mention the unbiased estimator of mean and variance.
3. What is the minimum variance unbiased estimator?
4. A random sample  $(X_1, X_2, X_3, X_4, X_5)$  of size 5 is drawn from a normal population with unknown mean  $\mu$ . Consider the following estimates of  $\mu$ .

a.  $t_1 = \frac{X_1 + X_2 + X_3 + X_4 + X_5}{5}$

b.  $t_2 = \frac{X_1 + X_2}{2} + X_3$

c.  $t_3 = \frac{2X_1 + X_2 + \lambda X_3}{3}$

Where  $\lambda$  is such that  $t_3$  is an unbiased estimator of  $\mu$ .

Find  $\lambda$ . Are  $t_1$  and  $t_2$  unbiased? State giving reasons, the estimator which is best among  $t_1$ ,  $t_2$  and  $t_3$ .