Translational Mechanical Systems Transfer Functions - Q.26

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Contents

Given Question

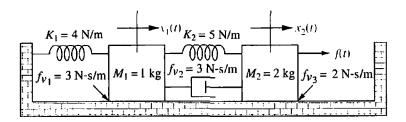
2 Solution

Given Question

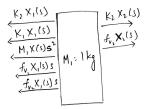
Problem 26

Q.26) For the system in the Figure below, find the transfer function

$$G(s) = X_1(s)/F(s) .$$



Free Body Diagrams



Forces acting on first block

$$\begin{array}{c|c}
f_{\lambda_{1}}X_{1}(3)s & F(3) \\
\hline
K_{\lambda_{1}}X_{1}(5) & K_{\lambda_{2}}X_{1}(5) \\
\hline
M_{\lambda_{1}}X_{1}(3)s^{2} & F_{\lambda_{2}}X_{1}(5) \\
\hline
M_{\lambda_{1}}X_{1}(3)s^{2} & F_{\lambda_{2}}X_{1}(5)
\end{array}$$

Forces acting on second block



Equations

From the Free Body Diagrams, we get the equations as below,

$$\implies 0 = (K_1 + K_2)X_1(s) + (f_{v_1} + f_{v_2})sX_1(s) + M_1s^2X_1(s) - K_2X_2(s) - f_{v_2}sX_2(s)$$

Equation of the second body,

$$\Longrightarrow F(s) =$$

$$K_2X_2(s) + (f_{v_2} + f_{v_3})sX_2(s) + M_2s^2X_2(s) - K_2X_1(s) - f_{v_2}sX_1(s)$$

Given Values

Substituting these values in the equations above,

$$K_1 = 4N/m$$

$$K_2 = 5N/m$$

$$M_1 = 1Kg$$

$$M_2 = 2Kg$$

$$f_{v_1} = 3Ns/m$$

$$f_{v_2} = 3Ns/m$$

$$f_{v_3} = 2Ns/m$$

Simplified Equations

$$\implies (s^2 + 6s + 9)X_1(s) - (3s + 5)X_2(s) = 0$$
$$\implies (2s^2 + 5s + 5)X_1(s) - (3s + 5)X_1(s) = F(s)$$

Solving for $X_1(s)$,

$$\implies X_1(s) = \frac{\begin{vmatrix} 0 & -(3s+5) \\ F(s) & (2s^2+5s+5) \end{vmatrix}}{\begin{vmatrix} (s^2+6s+9) & -(3s+5) \\ -(3s+5) & (2s^2+5s+5) \end{vmatrix}}$$

$$\implies$$
 $X_1(s) = \frac{(3s+5)F(s)}{2s^4+17s^3+44s^2+45s+20}$

Final Answer

... The Transfer Function is,

$$\implies$$
 G(s) = X₁(s)/F(s) = $\frac{(3s+5)}{2s^4+17s^3+44s^2+45s+20}$