Next....

- Implementation of parsers
- Two approaches
 - Top-down
 - Bottom-up
- First: Top-Down
 - Easier to understand and program manually
- Then: Bottom-Up
 - More powerful and used by most parser generators

Top down Parsing

• Construction of parse tree for the input, starting from root and creating the nodes of the parse tree in *preorder*.

 Equivalently, top-down parsing can be viewed as finding a leftmost derivation for an input string.

Example: Top down Parsing

Following grammar generates types of Pascals

Examples generated by this grammar (valid Pascal types):

- integer
- char
- . 1..10
- array[1..10] of integer
- array[char] of integer
- array[1..5] of array[1..10] of char

Example ... Parse Tree Construction Steps

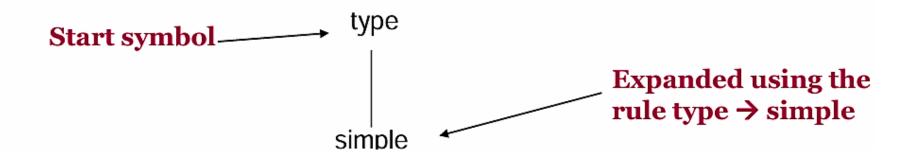
1. Start with the root node

The root is labeled with the start symbol of the grammar (something like <S> or <

2. Repeat two steps until the tree is complete

- Step 1: Expansion (Which production?) Decides how to expand a non-terminal.
 - o If the current node is a **non-terminal** (*like <expr> or <stmt>*), we must choose one of its grammar rules (productions).
 - \bullet Example: If $\langle \expr \rangle \rightarrow \langle \expr \rangle + \langle term \rangle$ | $\langle term \rangle$, we must decide which production rule applies.
 - After choosing, expand it by creating child nodes for each symbol in the production.
- Step 2: Next node (Which node?) Decides where to expand next in the tree.
 - After expanding, we look for the next non-terminal node in the tree that still needs to be expanded.
 - This continues until all non-terminals are replaced with terminal symbols (tokens from the input program).

Parse: array [num dotdot num] of integer



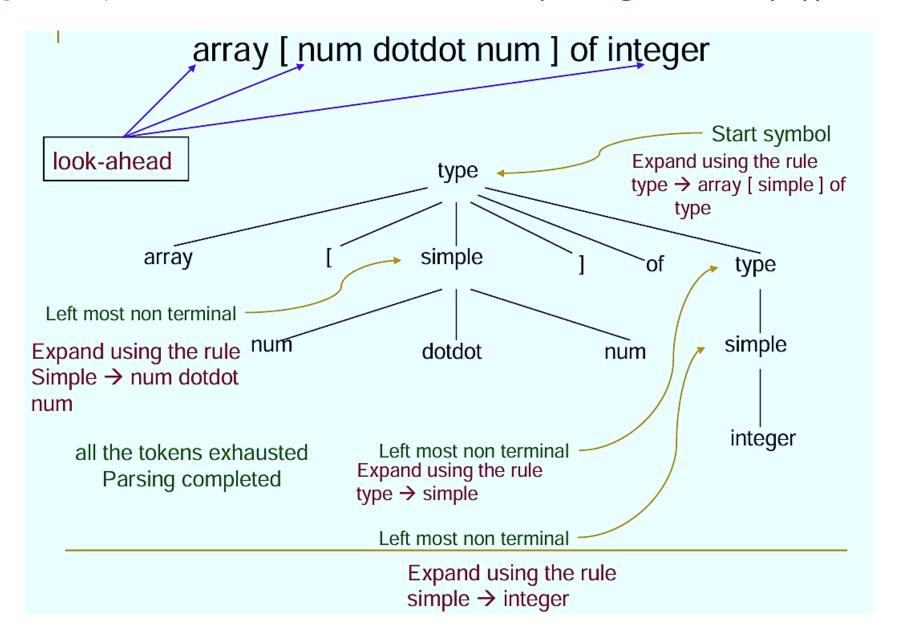
Problem with Expansion

- The non-terminal simple can never generate a string starting with "array".
- But our input starts with the token array.
- This means parsing fails at this stage, and the parser would need backtracking to try other rules.

Back-tracking is not desirable therefore, take help of a "look ahead" token here (array).

The current token is treated as look-ahead token.

Diagram represents leftmost derivation and parsing of an array type declaration

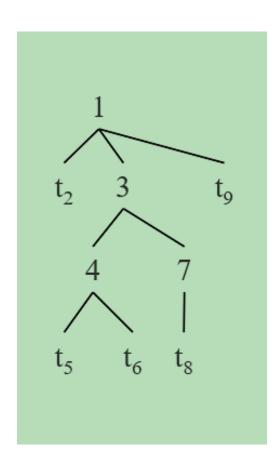


Introduction to Top-Down Parsing

• Terminals are seen in order of appearance in the token stream:

t2 t5 t6 t8 t9

- The parse tree is constructed
 - From the top
 - From left to right



Recursive Descent Parsing

Consider the grammar

$$E \rightarrow T + E \mid T$$

T \rightarrow int | int * T | (E)

The parser starts at the start symbol and calls functions that expand non-terminals to match input tokens.

- Token stream is: int5 * int2
- Start with top-level non-terminal E
- Try the rules for E in order

Recursive Descent Parsing. Example (Cont.)

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• Try E_0 \rightarrow T_1 + E_2
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Token stream: int5 * int2

- Then try a rule for $T_1 \rightarrow (E_3)$
 - But (does not match input token int X mismatch.
- Try $T_1 \rightarrow int$. Token matches.
 - But + after T_1 does not match input token * \times mismatch.
- Try $T_1 \rightarrow int * T_2$
 - This will match but + after T_1 will be unmatched \times mismatch.
- Has exhausted the choices for T_1
 - Backtrack to choice for E₀

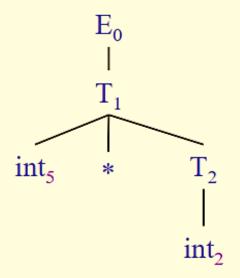
$$E \rightarrow T + E \mid T$$

 $T \rightarrow (E) \mid int \mid int * T$

Recursive Descent Parsing. Example (Cont.)

• Try $E_0 \rightarrow T_1$

- Token stream: int5 * int2
- Follow same steps as before for T_1
 - And succeed with $T_1 \rightarrow int_5 * T_2$ and $T_2 \rightarrow int_2$
 - With the following parse tree



$$\begin{array}{ccc} E \rightarrow T + E & \mid & T \\ T \rightarrow (E) & \mid int \mid int * T \end{array}$$

Recursive Descent Parsing → Notes

- Easy to implement by hand
- Somewhat inefficient (due to backtracking)
- But does not always work ...

This is **left-recursive** because the non-terminal **S** appears at the **leftmost position** on the right-hand side of its own production.

When Recursive Descent Does Not Work

S⇒Sa⇒Saa⇒Saaa⇒…

- Consider a production $S \to S$ a bool $S_1()$ { return S() && term(a); } bool S() { return $S_1()$; }
- S() will get into an infinite loop
- A <u>left-recursive grammar</u> has a non-terminal S $S \rightarrow^{+} S\alpha$ for some α
- Recursive descent does not work in such cases

Why Recursive Descent Fails

- Recursive descent works when the grammar is predictive (LL(1)):
 - No left recursion
 - No ambiguity
 - Parser can decide the production by looking at the next input token (1 lookahead)

Fixing the Grammar (Remove Left Recursion)

We transform the left-recursive rule:

$$S
ightarrow Sa \mid arepsilon$$

Eliminate left recursion by introducing a new non-terminal:

$$S \, o \, arepsilon \, S'$$

$$S' \ \rightarrow \ a \ S' \mid \varepsilon$$

Now the grammar is **right-recursive**, suitable for recursive descent parsing.

Elimination of Left Recursion

• Consider the left-recursive grammar $S \rightarrow S \alpha \mid \beta$

- 5 generates all strings starting with a β and followed by any number of α 's
- The grammar can be rewritten using rightrecursion

$$S \rightarrow \beta S'$$

 $S' \rightarrow \alpha S' \mid \epsilon$

Ex1:
$$P \rightarrow P + Q \mid Q$$

$$A \rightarrow A \quad \alpha \quad | \beta$$

$$A \rightarrow \alpha \quad | \beta$$

$$P o QP'$$
 $P' o +QP' \mid \varepsilon$

Ex2:
$$S \rightarrow SOS1S \mid OI$$

$$A \rightarrow \beta A'$$

$$A \rightarrow A \quad \alpha \quad \mid \beta$$

$$A \rightarrow \alpha A' \mid \epsilon$$

$$S \rightarrow O1S'$$

 $S' \rightarrow OS1SS' I \varepsilon$

Ex3:
$$A \rightarrow (B) \mid b$$

 $B \rightarrow B \times A \mid A$
 $A \rightarrow A \quad \alpha \quad \beta \quad \beta$
 $A \rightarrow A \quad \alpha \quad \beta \quad \beta$

$$A \rightarrow (B) \ I \ b$$
 $B \rightarrow AB'$
 $B' \rightarrow xAB' \ I \ \varepsilon$

Example

Consider grammar for arithmetic expressions

$$E \rightarrow E + T | T$$

 $T \rightarrow T * F | F$
 $F \rightarrow (E) | id$

- $E \rightarrow E + T$ is immediate left recursion.
- T → T * F is also immediate left recursion.
- F is fine (no left recursion).
- If we try recursive descent directly, it'll **loop forever** on E or T.

Step-by-step Transformation

$$A \to \beta A'$$

$$A' \to \alpha A' \mid \varepsilon$$

For E:
$$E \rightarrow E + T \mid T$$

For T:
$$T \rightarrow T * F \mid F$$

Here,
$$\alpha = + T$$
, $\beta = T$

Here, $\alpha = *F$, $\beta = F$

Rewrite:

$$E \rightarrow T E'$$

$$E' \rightarrow + T E' \mid \epsilon$$

Rewrite:

$$T \rightarrow F T'$$

$$T' \rightarrow * F T' \mid \epsilon$$

$$F \rightarrow (E) \mid id$$

No left recursion \rightarrow unchanged.

$$E \rightarrow E + T | T$$
 $T \rightarrow T * F | F$
 $F \rightarrow (E) | id$

$$E \rightarrow TE'$$

 $E' \rightarrow + TE' \mid E$
 $T \rightarrow FT'$
 $T' \rightarrow * FT' \mid E$
 $F \rightarrow (E) \mid id$

Given Grammer

After removal of left recursion, the grammar becomes