

Experiment: 4

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Aim: To find the closure, candidate keys, prime attributes and highest normal form using the given relation and functional dependencies.

Question 1

$R(ABCD), FDs = \{AB \rightarrow C, C \rightarrow D, D \rightarrow A\}$

Solution

Closure:

$AB^+ = \{A, B, C, D\}$

$BC^+ = \{B, C, A, D\}$

$BD^+ = \{B, D, A, C\}$

Candidate Key: AB, BD, BC

Prime Attributes: $\{A, B, C, D\}$

Non-Prime Attributes: $\{ \}$

Normal Form: It cannot be BCNF as C is a SK($C \rightarrow D$). All determinants have prime attributes, so the relation is in 3NF.

Question 2

$R(ABCDE), FDs = \{A \rightarrow D, B \rightarrow A, BC \rightarrow D, AC \rightarrow BE\}$

Solution

Closure:

$A^+ = \{A, D\}$

$B^+ = \{B, A, D\}$

$C^+ = \{C\}$

$BC^+ = \{B, C, A, D, E\}$

$AC^+ = \{A, B, C, D, E\}$

Candidate Key: AC, BC

Prime Attributes: $\{A, B, C\}$

Non-Prime Attributes: $\{D, E\}$

Normal Form: Partial dependency exists ($A \rightarrow D$). Hence relation is in 1NF.

Question 3

$R(ABCDE)$, FDs = $\{B \rightarrow A, A \rightarrow C, BC \rightarrow D, AC \rightarrow BE\}$

Solution

Closure:

$B^+ = \{A, B, C, D, E\}$

$A^+ = \{A, C, B, D, E\}$

Candidate Key: A, B

Prime Attributes: $\{A, B\}$

Non-Prime Attributes: $\{C, D, E\}$

Normal Form: All determinants are either CK or SK. So this relation is in BCNF.

Question 4

$R(ABCDEF)$, FDs = $\{A \rightarrow BCD, BC \rightarrow DE, B \rightarrow D, D \rightarrow A\}$

Solution

Closure:

$$A^+ = \{A, B, C, D, E\}$$

$$AF^+ = \{A, F, B, C, D, E\}$$

$$DF^+ = \{D, F, B, C, A, E\}$$

$$BF^+ = \{B, F, C, A, D, E\}$$

Candidate Key: AF, DF, BF

Prime Attributes: $\{A, D, B, F\}$

Non-Prime Attributes: $\{C, E\}$

Normal Form: Partial dependency exists ($A \rightarrow BCD$). Hence relation is in 1NF.

Question 5

FDs = $\{X \rightarrow Y, WZ \rightarrow X, WZ \rightarrow Y, Y \rightarrow W, Y \rightarrow X, Y \rightarrow Z\}$

Solution

Closure:

$$Y^+ = \{Y, X, W, Z\}$$

$$X^+ = \{X, Y, W, Z\}$$

$$WZ^+ = \{W, Z, X, Y\}$$

Candidate Key: Y, X, WZ

Prime Attribute: $\{X, Y, W, Z\}$

Non-Prime Attributes: $\{ \}$

Normal Form: All determinants are CK. Highest NF = BCNF.

Question 6

$R(ABCDEF), FDs = \{A \rightarrow BC, A \rightarrow D, D \rightarrow E, BC \rightarrow D\}$

Solution

Closure:

$A^+ = \{A, B, C, D, E\}$

$AF^+ = \{A, B, C, D, E, F\}$

Candidate Key: AF Prime

Attributes: $\{A, F\}$

Non-Prime Attributes: $\{B, C, D, E\}$

Normal Form: $A \rightarrow BC$ introduces partial dependency (A is part of key AF and BC is non-prime). Hence highest NF = 1NF.