

$$t = \left[\frac{-1}{\alpha} \ln(\beta - \alpha x) \right]_0^x$$

$$t = +\frac{1}{\alpha} \ln\left(\frac{\beta}{\beta - \alpha x}\right)$$

on simplifying

$$x = \frac{\beta}{\alpha} (1 - \exp(-\alpha t))$$

$$x = \left(1 + \frac{\tau_{rxn}}{\tau_n}\right) \left(1 - \exp\left(-t\left(\frac{1}{\tau_{rxn}} + \frac{1}{\tau_n}\right)\right)\right)$$

$$x = \frac{1 - \exp\left\{-t\left(\frac{1}{\tau_{rxn}} + \frac{1}{\tau_n}\right)\right\}}{\left(\tau_{rxn}\right)\left(\frac{1}{\tau_{rxn}} + \frac{1}{\tau_n}\right)}$$

like a 1st order differential eqn's solution

$$\tau = \left(\frac{1}{\frac{1}{\tau_{rxn}} + \frac{1}{\tau_n}}\right)$$

→ timescale or time constant

$\tau_n \uparrow \Rightarrow$ more time of residence {or time to react}
 $\tau_{rxn} \uparrow \Rightarrow$ conversion is lesser

τ_{rxn} is generally not controlled cause it is decided by the rxn

$\left\{ \tau_n \right\}$ can be controlled by controlling flow rate