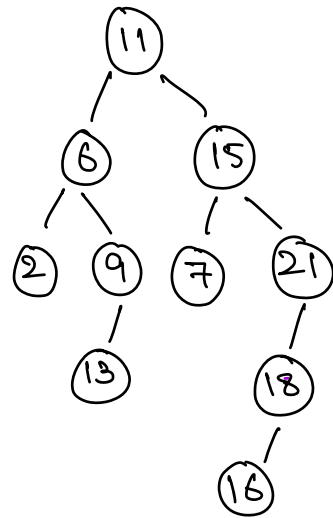


Q. Given a Binary Tree, Print the level order traversal.

11, 6, 15, 2, 9, 7, 21, 13, 18, 16



Queue < TreeNode > Q;

Q.

~~11, 6, 15, 2, 9, 7, 21, 13, 18, 16~~

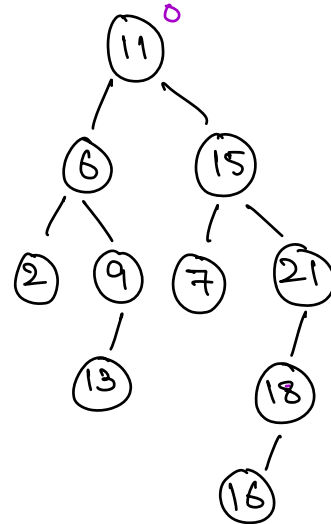
11, 6, 15, 2, 9, 7, 21, 13, 18, 16

*

List < List < int > >

[[11],
[6, 15],
[2, 9, 7, 21],
[13, 18],
[16]]

Approach 1:



Q

$\langle 11, 0 \rangle, \langle 6, 1 \rangle, \langle 15, 1 \rangle, \langle 2, 2 \rangle, \langle 9, 2 \rangle, \langle 7, 2 \rangle, \langle 21, 2 \rangle, \langle 13, 3 \rangle$

[11]

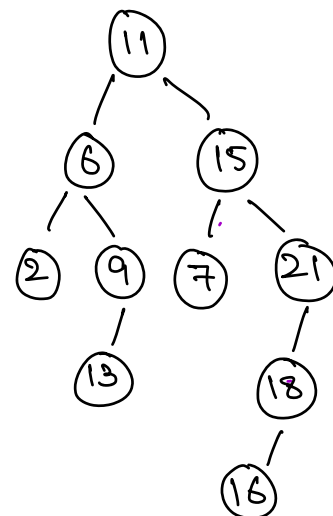
[6, 15]

[2, 9, 7, 21]

⋮

Approach 2 :-

⇒ Adding a marker / delimiter after every level.



Queue < TreeNode > Q

11, Null, 6, 15, Null, 2, 9, 7, 21, Null, 13, 18, Null, 16, Null

[11]

[6, 15]

[2, 9, 7, 21]

[13, 18]

[16]

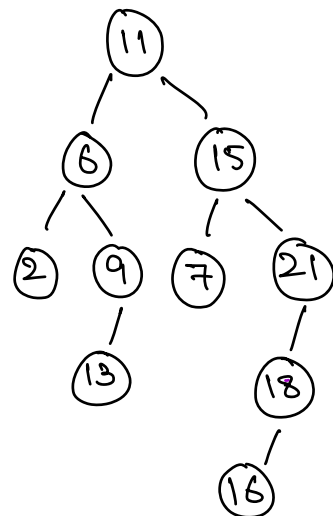
TC: $O(N)$

SC: $O(\text{width}) \Rightarrow O(N)$

↳ Max. no. of Nodes in any level (width of B.T)

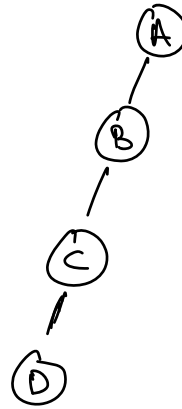
11, 6, 15, 2, 9, 7, 21, 13, 18, 16

size = 4



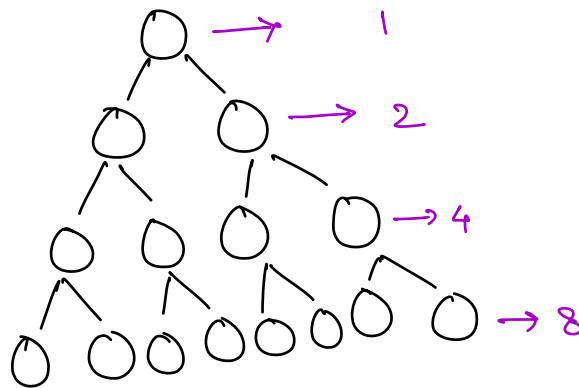
Srew Tree

A, B, C, D
Size = 4



Complete Binary Tree

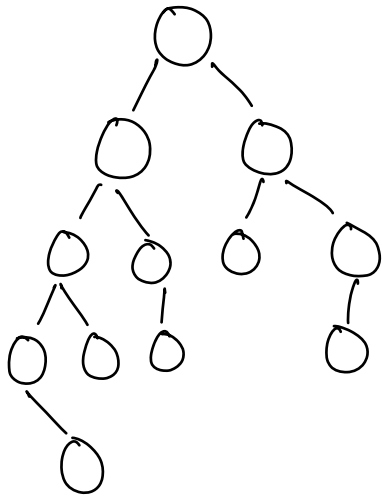
⇒ All the levels are completely filled.



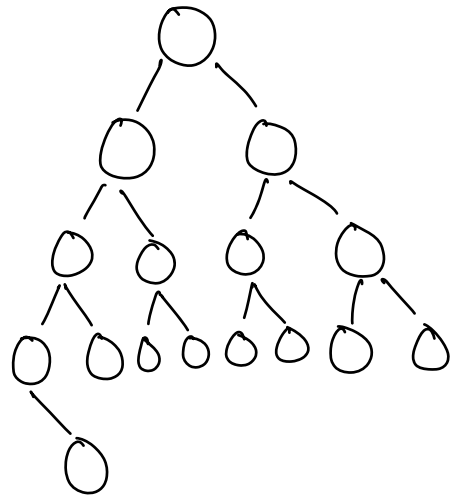
A binary tree where all the levels are completely filled

↳ except possibly the last level

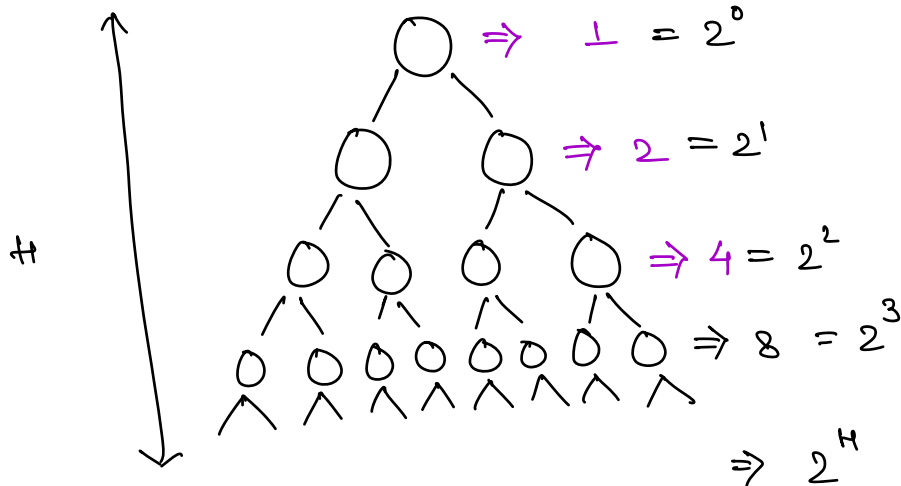
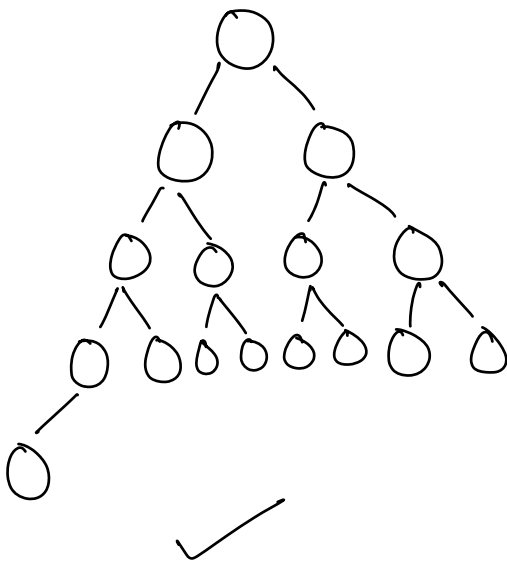
↳ Nodes in the last level are left aligned.



Not complete B.T



Not complete B.T



No. of nodes in the last level = 2^H

Total no. of nodes in the Tree \Rightarrow

$$2^0 + 2^1 + 2^2 + 2^3 + \dots + 2^H$$

\Rightarrow G.P

$$a = 1$$

$$r = 2$$

$$\# \text{ of terms} = H+1$$

$$\text{Sum} = \frac{1(2^{H+1} - 1)}{(2 - 1)} = 2^{H+1} - 1$$

$$\text{No of nodes} = 2^{H+1} - 1 = N.$$

$$2^{H+1} - 1 = N$$

$$2^{H+1} = N+1$$

$$H+1 = \log_2(N+1)$$

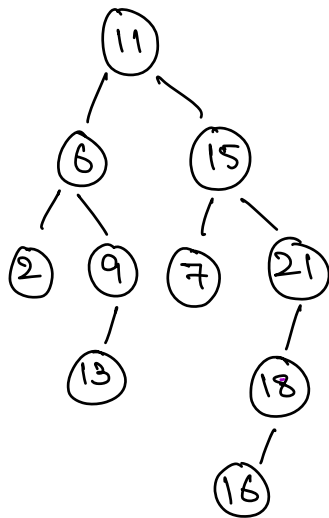
$$H = \log_2(N+1) - 1$$

$$H \approx O(\log N)$$

$$\begin{aligned}
 \text{No. of nodes in the last level} &= 2^H \\
 &= 2^{\log_2(N+1) - 1} \\
 &= \frac{2^{\log_2(N+1)}}{2} \\
 &= \frac{N+1}{2}
 \end{aligned}$$

Worst Case Space Complexity of level order $\Rightarrow O(N)$

Approach 3 :



<u>Q</u>	<u>No. of degenerate's</u>	<u>Size</u>
<u>11</u>	1	1
<u>6, 15</u>	2	2
<u>2, 9, 7, 21</u>	4	4
<u>13, 18</u>	2	2
<u>16</u>	1	1

No. of dequeues for every level \equiv size of the Queue

Code :-

```
list<list<int>> levelOrder (root) {  
    if (root == Null)  
        return null/empty list;  
    List<list<int>> ans;  
    Queue<TreeNode> Q;  
    Q.enqueue (root);  
    while (!Q.isEmpty()) {  
        int size = Q.size();  
        list<int> level;  
        for (i=0; i<size; i++) {  
            TreeNode temp = Q.poll();  
            level.add(temp.data);  
            if (temp.left != Null)  
                Q.enqueue (temp.left);  
            if (temp.right != Null)  
                Q.enqueue (temp.right);  
        }  
        ans.add (level);  
    }  
    return ans;  
}
```

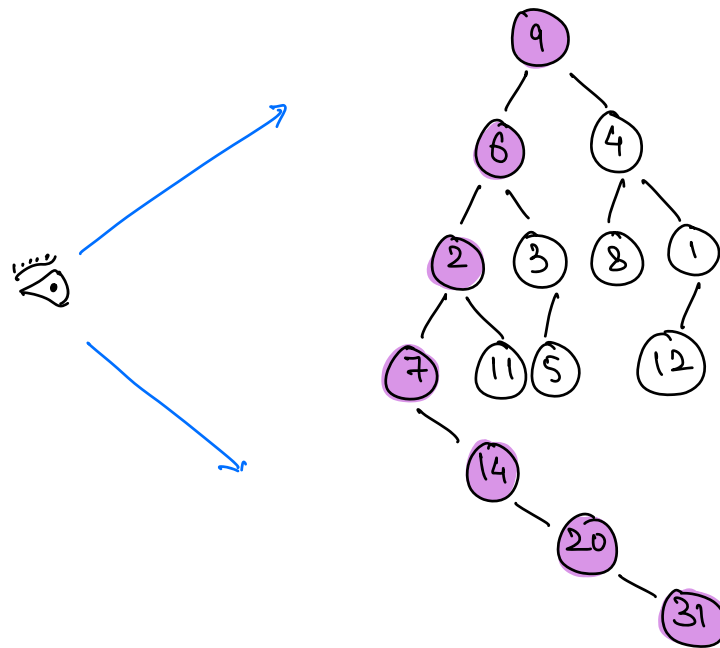
3

TC: $O(N)$

SC: $O(N)$ (Worst case)

Q.
Amazon
MS
Adobe

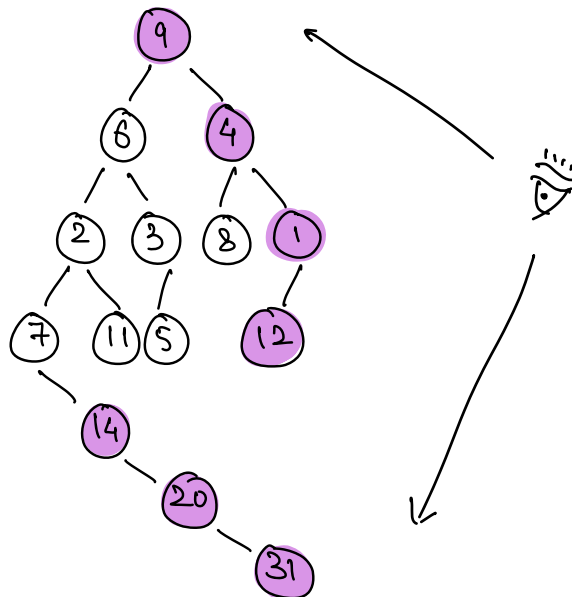
Given a Binary Tree, Print the left view of it.



Left View \Rightarrow 9, 6, 2, 7, 14, 20, 31

\rightarrow First node of every level in
Level Order traversal.

Q. Given a Binary Tree, Print the right view of it.



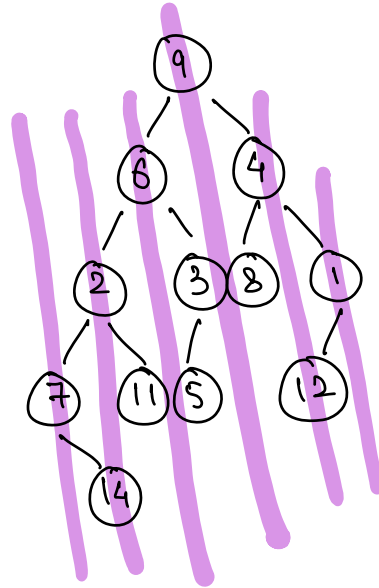
Right View \Rightarrow 9, 4, 1, 12, 14, 20, 31

\hookrightarrow Last node of every level in
Level Order traversal.

* print the node only for $i == \text{size}-1$
in prev. code.

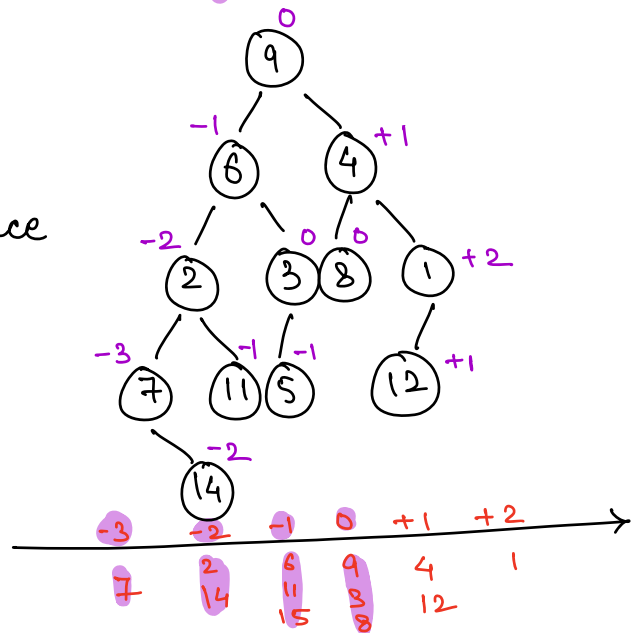
Q. Vertical Order Traversal.

[7],
[2, 14],
[6, 11, 5],
[9, 3, 8],
[4, 12],
[1]



Vertical Order traversal

\Rightarrow Nodes with same distance
from root node will
come under same
Vertical line.



$\text{HashMap} \langle \text{int}, \text{list} \langle \text{int} \rangle \rangle \text{ map}$
 $\downarrow \qquad \qquad \downarrow$
 dist Nodes which are
 dist apart from
 root node

```

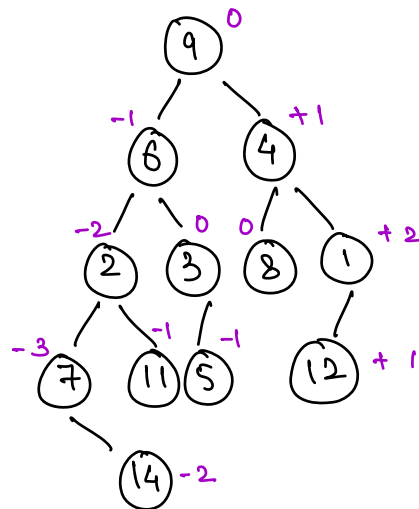
preOrder(root, 0dist) {
    if (root == Null)
        return ;
    if (!map.containsKey(dist)) {
        map.insert(dist, new ArrayList<int>());
    }
    map.get(dist).add(root.val);
    preOrder(root.left, dist-1);
    preOrder(root.right, dist+1);
}

```

HashMap

int : list of Node value

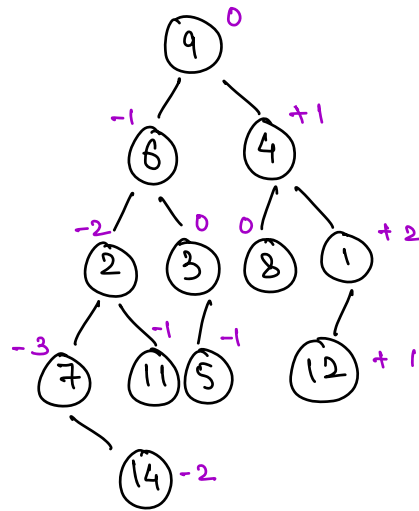
0 : 9
 -1 : 6, 20
 -2 : 2, 14
 -3 : 7



* Post Order
* In Order
* PreOrder } DFS X

Queue < Info > Q;

Class Info {
Tree Node node;
int dist;
}



~~{9, 0}~~, ~~{6, -1}~~, ~~{4, 1}~~, ~~{2, -2}~~, ~~{3, 0}~~, ~~{8, 0}~~, ~~{1, 2}~~, ~~{7, -3}~~

~~{11, -1}~~ ~~{5, -1}~~ ~~{12, 1}~~ ~~{14, -2}~~

HashMap :-

int : List of Node value

0 : [9, 3, 8]

-1 : [6, 11, 5]

1 : [4, 12]

-2 : [2, 14]

2 : [1,]

-3 : [7,]

⇒

[7]

[2, 14]

[6, 11, 5]

[9, 3, 8]

[4, 12]

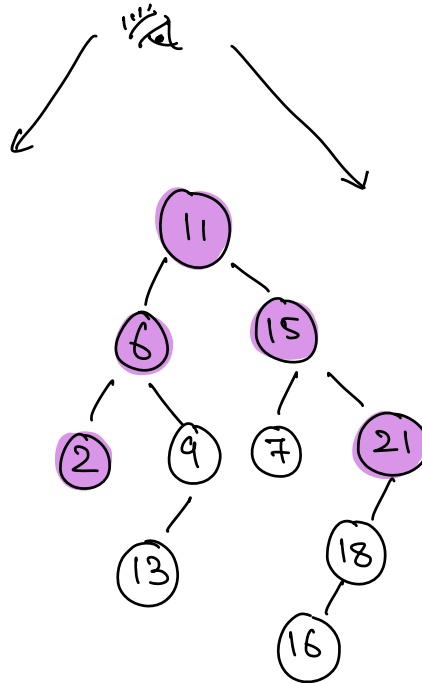
[1]

TC: O(N)

SC: O(N)

Q. Top View

⇒ first node in the
list against every
dist.



Q. Bottom View.

⇒ Last node in the
list against every
in map.

