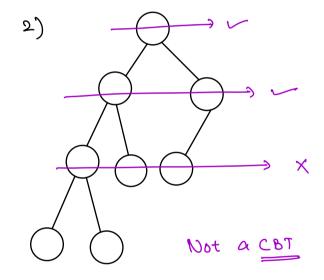
## Complete Binary Tree (CBT)

A binary trèe is said to be a CBT if it satisfies below properties.

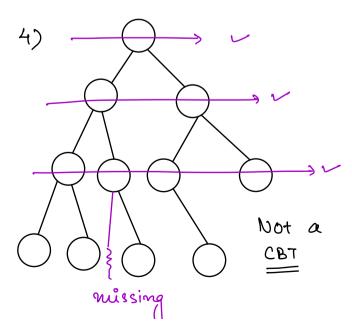
- i) All the nodes have to be filled revel by level from left to right.
- ii) All the levels should be completely filled encept the last revel.

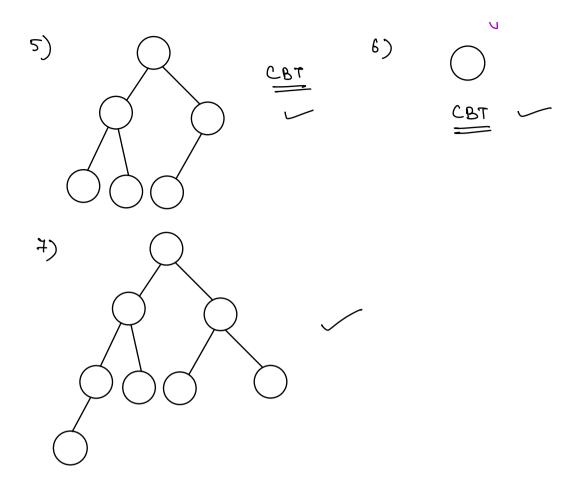
<u>|</u>-,-

Not a CBT

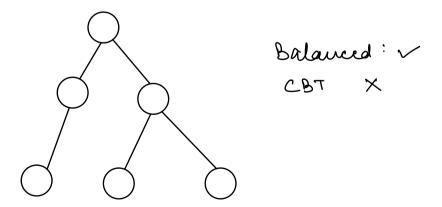


3)
Not a
CBT





Note: Au Balanced Binary Tree's are CBT? NO + nodes | h(LST) - h(RST) | <=1



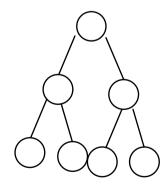
Note AU CBT's are Balanced Binary Tree's?
YES

Frence et max (1).

Buiz If there are N nodes in a CBT, theight?

Height (Balanced B.7) = Height (CBT) = log N

Height (CBT)	min Nodes	max Nodes
1	2 = 2 <sup>۱</sup>	$3 = 2^2 - 1$
2	4 = 22	$7 = 2^3 - 1$
3	8 = 23	15 = 24-1
4	16 = 2 <sup>4</sup>	31 = 2 <sup>S</sup> -1
` <u>`</u>		,
-14	24	24+1-1



$$2^{H} (Min Nodes)$$

$$2^{H+1} - 1 (Man Nodes)$$

$$2^{H} = N \Rightarrow H = log N$$

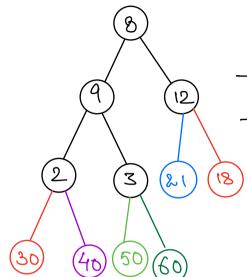
$$2^{H+1} - 1 = N \Rightarrow 2^{H+1} = N+1$$

$$4+1 = log(N+1)$$

$$4 = log(N+1) - 1 \approx log(N)$$

# Implementation of CBT:-





Pusent: 21, 18, 30, 40,50,60

8,97,12,25,21,18,30,40,50,60

Steps:-

7 Level Order traversal.

Whenever a new node is created, insert it in a queue 4 delete the front of the queue only if it's both left 4 right Children are fines.

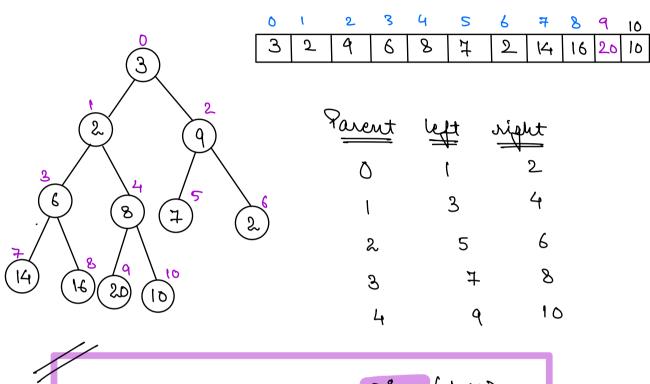
TC: O(N) for inserting N nodes. SC: D(N) L) Queue

Disadvantages:

- 8C: 0(N)
- 2) Iterating from child to parent is NOT allowed.

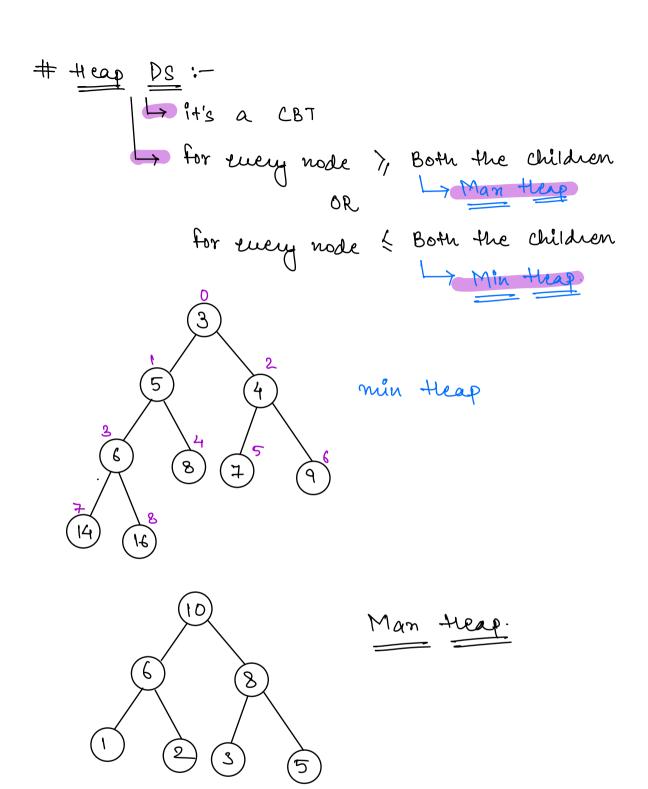


(; 5, 2, 9, 6, 8, 7, 2, 14, 16) Ust (int) | Vector (int)



inden i => Farent inden = [-1]

TC of inserting N elements: O(N) SC: O(1)



# Min Heap Insert: O(log N) get Min(): O(1) Search: O(N)

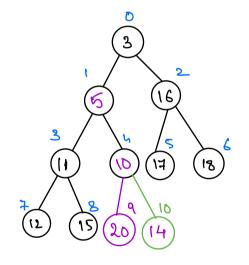
delete Min ():0(log N) delete Man ():0(log N)

Man Heap

Insert: O(logN)
getMan: O(1)

Search: O(N)

# Insert in Min heap.

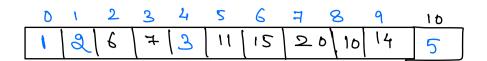


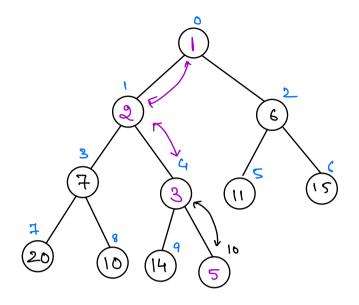
min trap Insert 20

inden Parent if (Alind) (
Alparent))

4 => Surap. 4

TC: 0( hag N)





Void insert (list (int) arr, int ele) {

arr. add (ele)

inden = arr. size() -1;

farent = (inden -1) | 2;

while (inden |= 0 4 arr [farent]) arr [inden]) {

Swap (arr [farent], arr [inden]);

inden = farent

farent = (inden -1) | 2;

3

3 \_\_\_ # get Min () / get Man () > O(1)
in Min

theap

theap

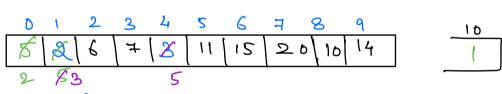
uturn list [0];

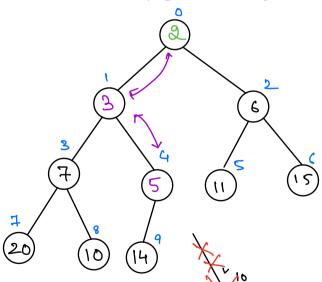
# search Operation:

Linear search on the list of elements.

TC: O(N) { Both min | man heap?

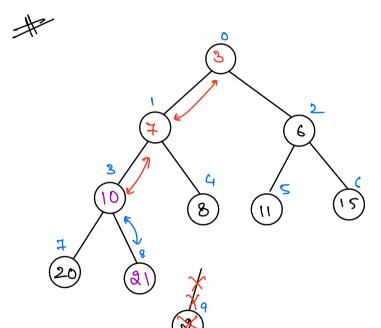
# Delite nun operation (MIN HEAP)





Steps: -

- (C1-01A, C01A) gaws (i
- ii) Pelete last element.
- III) Propogate down.



## Delete nin

- i) swap (A(O), A(A))
- 11) Delete Alaj

find 
$$A$$
  $x$   $min$ -ind

 $0$   $1$   $2$   $1$   $3wap$ 
 $1$   $3$   $4$   $3$   $3wap$ 
 $3$   $7$   $8$   $8$   $3wap$ 
 $8$   $?$   $?$ 
 $17$   $18$ 
 $x$   $x$   $\Rightarrow$   $Breek$ .

## TC: 0( Log N)

delete Min () } => O(log N)

delete Man ()

- i) Search: O(N)
- 11) Swap mith last inden: O(1)
- III) Delete the last inden: O(1)
- 111) Propogate Down: O(log N)

TC: 0(N)

Heap.	BBST
O(logN)	O(logN)
0(1)	0 (log N)
0 (log N)	0 (log 10)
0(10)	0 (log 1)
0(10)	0 (log N)
	0(logN) 0(1) 0(logN) 0(N)

#	T	below	3	aperations	are	Joeg ven	+ the	go with
	り	Iuser t					Heap !	D\$ .
	2)	get Mir	n ()	getMan				
	3)	delete	-Min	()   deleter	Man()			
#	In	built ==	libe a	ced				
				riority-qu				
	11)	Jawa	: 9	sionity Queu	e < -	>		
	(III)	Rython	÷	heapq				
		t t 1		;				
					→ G €	ogle com	_	
				<del>*</del>				