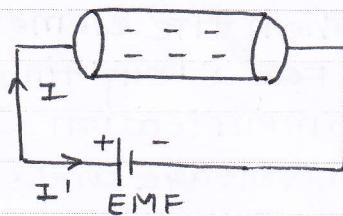


* power *



I' \rightarrow natural current
 I \rightarrow conventional current

- The flow of electron is called as current or the time rate of charge is also called as current

$$I = \frac{dQ}{dt} \text{ C/s or Amp} \quad Q_e = -1.602 \times 10^{-19} \text{ C}$$

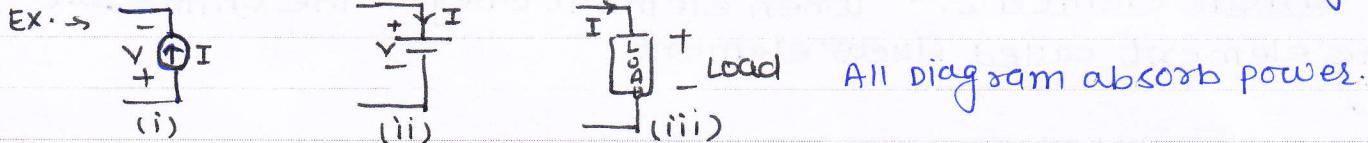
- To move e^- from one point to another point external force reqd is called EMF (V) $\therefore \frac{dw}{IL} = \text{ex. volt}$

$$V = \frac{dW}{dq} \quad \text{J/C or Volt}$$

- The time rate of energy called as power.

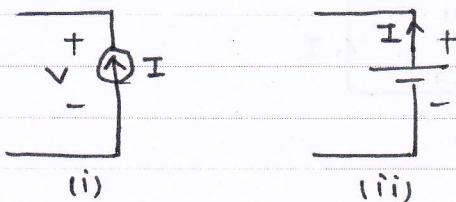
$$P = \frac{dW}{dt} \text{ J/sec or watt} = \frac{dW}{dQ} \cdot \frac{dQ}{dt} = V \cdot I$$

- When current enter positive terminal element absorbing power.



- When current leaving from positive terminal called element deliver power.

EX. →



- The capacity to do work called ENERGY

$$W = \int_0^t P \cdot dt \quad W \text{d}t \text{ - Sec or Joule.}$$

- ANY ckt Power Absorb = Power Delivers.

* Classification of Elements :→

* Active element :- When the element is capable of delivering energy independently for a long time (approx) ∞ or having property of internal amplification called Active element.

Example :- (i) Independent voltage and current source

(ii) Dependent Transistor or op-Amp source

→ During discharge capacitor can deliver energy at short time not a long time so it is not Active element.

* Passive element :→ When the element is not capable of delivering energy independently the element called passive element.

Example :- R, Bulb, Transformer, ($V_1 I_1 = V_2 I_2$)

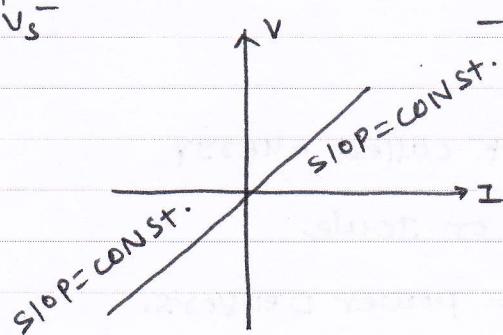
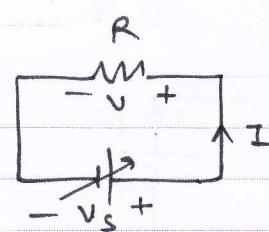
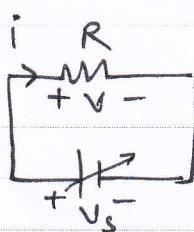
CMT * * If V/I ratio \oplus in both direction called Passive else Active * *

* Bidirectional element :→ When element have properties & characteristic are independent on the direction of current called Bi-directional (Bi-lateral) element.

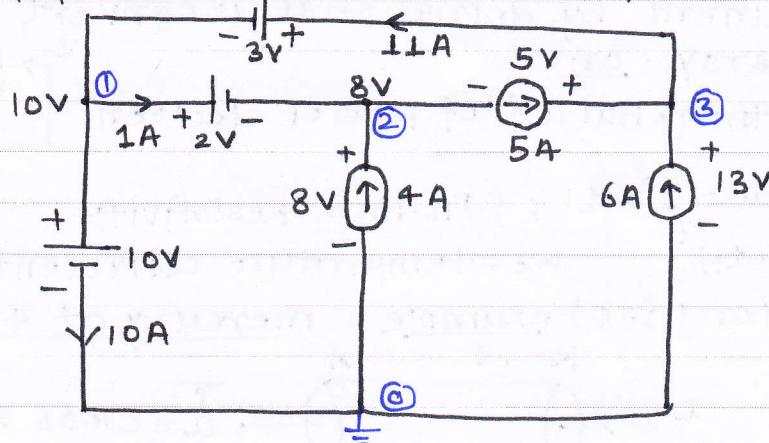
CMT * * When opposite coordinate figure same than Bidirectional else Uni-di.

* Linear element :→ When element obeys the Ohm's Law. the element called linear element

CMT * * Every linear element have Bidirectional property but Not vice-versa * *



Q.1. Find power of each element of Network shown



concept

$\frac{+}{-} I$ absorb

$\frac{-}{+} V$ Deliver

$$\text{Ans: } P_{10} = 10 \times 10 = 100 \text{ watt (absorb)}$$

$$P_{12} = 2 \times 1 = 2 \text{ watt (absorb)}$$

$$P_{23} = 5 \times 5 = 25 \text{ Watt (deliver)}$$

$$P_{13} = 11 \times 3 = 33 \text{ Watt (absorb)}$$

$$P_{20} = 8 \times 4 = 32 \text{ Watt (deliver)}$$

$$P_{30} = 13 \times 6 = 78 \text{ Watt (deliver)}$$

$$\text{Total power absorb } (100 + 2 + 33 = 135 \text{ Watt})$$

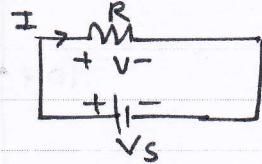
$$\text{Total power Deliver } (32 + 78 + 25 = 135 \text{ Watt})$$

Q.2. Identify given figure type of Element.

- (a) → Passive ($V/I \oplus 1 \& 3 \text{ quad.}$)
 → Unidirectional (not same fig 1 & 3 quad.)
 → Non linear (slope not const.).
- (b) → Passive ($V/I \oplus 1 \& 3 \text{ quad.}$)
 → Bidirectional (same fig 1 & 3 quad.)
 → Non linear (slope not const.).
- (c) → Active ($V/I \ominus 2 \& 4 \text{ quad.}$)
 → Bidirectional (same fig 2 & 4 quad.)
 → Linear (slope const.).
- (d) → Active ($V/I \oplus 1 \& 3 \text{ quad. } \& V/I \ominus 2 \& 4 \text{ quad.}$)
 → Non linear (slope not const.)
 → Unidirectional (not same fig in opposite quad.).

* Resistance * Resistor is a property of Resistor is always oppose a current by doing. so it is convert electrical energy to Heat energy. or

Resistance is nothing but a fⁿ of flow of electron



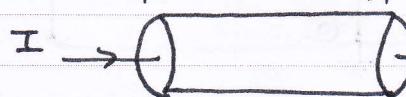
$$P = I^2 R ; R = \rho L / A ; W = I^2 R t ; \rho (\Omega \cdot m) = \text{Resistivity}$$

$$\rightarrow R_1 = R_0 [1 + \alpha_0 (t_2 - t_1)] \quad \alpha_0 = \text{temperature coefficient}$$

For superconductor ($\rho=0$) example:- mercury at 4.15 K temp.

$$\text{Length } l$$

* OHM'S LAW :-



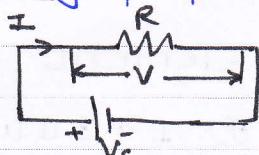
$a = \text{cross sectional Area.}$

Ohm's Law state that constant temp. and conductivity of material constant current density is directly proportional to electric field intensity. $J \propto E \Rightarrow J = \sigma E \Rightarrow I/a = \frac{1}{\rho} \cdot \frac{V}{l}$

$$\text{CMT} \Rightarrow \frac{V}{I} = \frac{\rho l}{a} = R ; J = \frac{I}{a} ; E = \frac{V}{l} ; \sigma = \frac{1}{\rho} \text{ mho/m or } (\Omega \cdot m)^{-1}$$

or

ohm's law state that potential difference across the element is directly proportional to current flowing to element.



$$V \propto I \Rightarrow V = IR \Rightarrow R = \frac{V}{I} = \text{const.}$$

$I \propto V_s (\text{EMF})$ or V (Voltage drop / P.D) $\propto I$ Both statement valid.

- (i) EMF independent on current and resistor magnitude
- (ii) potential difference depend on current & Resistor magnitude

* ELECTRICAL CIRCUIT

$$\rightarrow I = \frac{V}{R} = \frac{\text{EMF}}{R}$$

$$\rightarrow I = \frac{V}{R} = \frac{V/\rho l/a}{R} = \frac{\text{EMF}}{\rho l/a}$$

* MAGNETIC CIRCUIT *

$$\rightarrow \phi = \frac{\text{mmf}}{S \text{ (Reluctance)}}$$

$$\rightarrow \phi = \frac{NI}{l/a \mu_0 4 \pi r}$$

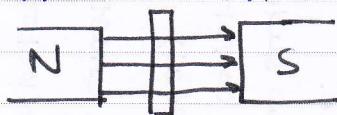
$$\rightarrow L = \frac{N^2 \mu_0 4 \pi r a}{l} = \frac{N^2}{l/a \mu_0 4 \pi r} = \frac{N^2}{s}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ H/m} ; \mu_r = 1 \text{ air}$$

\rightarrow permeability is the property of medium. l = length of core; a = area of cross sectional which magnetic field exists.

* Faraday Law: →

* First Law: → When conductor cuts a magnetic lines of force an emf induced in the conductor.



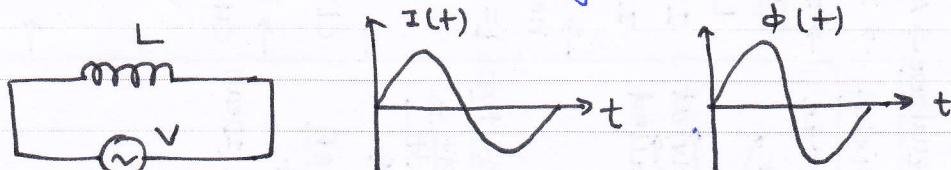
* Second Law: → EMF induced in the conductor is directly proportional to rate of change of flux.

$$e \propto \frac{d\phi}{dt} \Rightarrow e = BLV \sin \theta$$

CMT* $e = \boxed{\text{Dynamic Induced emf (Generator)}}$

B = Flux density, l = length of conductor, Velocity of conductor-V

θ = Angle b/w conductor & magnetic line.



$$e \propto \frac{d\phi}{dt}$$

CMT* $e = \boxed{-N \frac{d\phi}{dt}} = \text{Statically induced emf (Transformer).}$

→ Due to Lenz's Law

CMT

$$\text{Flux linkage } \Psi = N\phi = LI$$

$$V = \frac{d\Psi}{dt} = N \frac{d\phi}{dt}$$

$$V = L \frac{di}{dt}$$

Inductor (L).

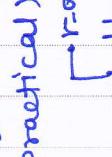
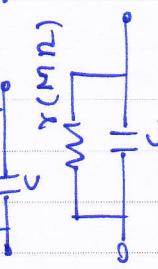
$$\begin{aligned} \rightarrow Q \propto V \Rightarrow Q = CV &\Rightarrow C = \frac{Q}{V} \left\{ \frac{\text{coulomb}}{\text{volt}} \text{ or Farad} \right\} \\ \rightarrow I = \frac{dQ}{dt} = C \frac{dV}{dt} \Rightarrow V = \frac{1}{C} \int_{-\infty}^t I \cdot dt \\ \rightarrow P_{\text{Inst.}} = V \cdot I = V \cdot \frac{CDV}{dt} \Rightarrow W = \int P_{\text{Inst.}} dt = \frac{1}{2} L I^2 \end{aligned}$$

Avg. Power dissipation in ideal capacitor equal zero
capacitor storage energy in form electric field.

When capacitance is independent on voltage magnitude called linear capacitor.
 $C = \frac{Q}{V} = \text{const.} \therefore V \propto I \text{ or } I \propto V$
when it depends on voltage magnitude called non linear capacitor: ex:- varactor diode

when it depends on voltage magnitude called non linear capacitor: ex:- varactor diode
 $C = Q/V = \text{variable.}$

steady state condition for DC source capacitor
As open circuit $\Rightarrow I = C \frac{dU}{dt} = 0$ (so $I = 0$)

capacitor does not allow sudden change of voltage because sudden change of voltage if required infinite current $I = C \frac{dU}{dt}$ at $t=0; I=\infty$. (ideal)
(Practical) - Finite time constant ($T=RC$)
 \rightarrow  Ideal capacitor
 \rightarrow  Practical capacitor.

Capacitor (C)

$$\begin{aligned} \rightarrow Q \propto V \Rightarrow Q = CV &\Rightarrow C = \frac{Q}{V} \left\{ \frac{\text{coulomb}}{\text{volt}} \text{ or Farad} \right\} \\ \rightarrow I = \frac{dQ}{dt} = C \frac{dV}{dt} \Rightarrow V = \frac{1}{C} \int_{-\infty}^t I \cdot dt \\ \rightarrow P_{\text{Inst.}} = V \cdot I = V \cdot \frac{CDV}{dt} \Rightarrow W = \int P_{\text{Inst.}} dt = \frac{1}{2} CV^2 \end{aligned}$$

Avg. Power dissipation in IDEAL inductor zero

Inductor store energy in form magnetic field (KE).
Inductance independent on current magnitude called linear inductor or Air core inductor

$$L = \frac{V}{dI/dt} = \text{const.} \quad \begin{array}{l} \uparrow \text{const.} \\ \downarrow \end{array} \quad \begin{array}{l} \uparrow \text{const.} \\ \downarrow \end{array}$$

$$I = \frac{V}{L} \propto t \quad \begin{array}{l} \uparrow \text{const.} \\ \downarrow \end{array} \quad \begin{array}{l} \uparrow \text{const.} \\ \downarrow \end{array}$$

$$I = \frac{N\phi}{L}; \quad \begin{array}{l} \uparrow \text{saturation} \\ \downarrow \end{array} \quad \begin{array}{l} \uparrow \text{saturation} \\ \downarrow \end{array}$$

Depend on current magnitude called non linear or iron core inductor.

$$I = \frac{N\phi}{L}; \quad \begin{array}{l} \uparrow \text{saturation} \\ \downarrow \end{array} \quad \begin{array}{l} \uparrow \text{saturation} \\ \downarrow \end{array}$$

under steady state for DC source AC short circuit. $V = L \frac{di}{dt} \Rightarrow V=0$.

Inductor does not allow sudden change of current bcs it required so voltage (practical).

$$V = L \frac{di}{dt}|_{dt \rightarrow 0} = \infty \text{ (ideal)}$$

Practical finite time const ($T = L/R$)

$$\rightarrow \begin{array}{c} \text{min} \\ \text{max} \end{array} \quad \begin{array}{c} L \\ M \end{array} \quad \text{(practical inductor).}$$

TOPIC

$$I = \frac{V}{L} \quad \begin{array}{l} \uparrow \text{const.} \\ \downarrow \end{array}$$

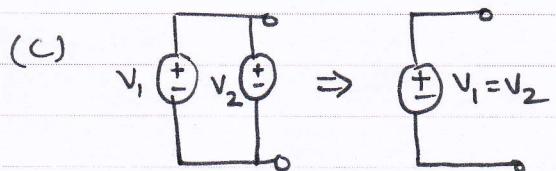
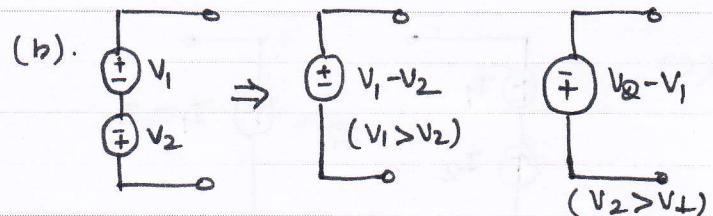
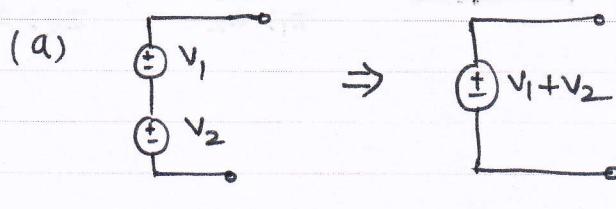
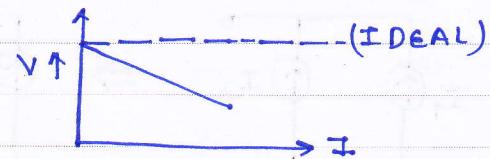
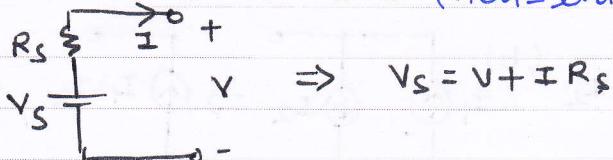
$$I = \frac{V}{L} \quad \begin{array}{l} \uparrow \text{const.} \\ \downarrow \end{array}$$

$$I = \frac{V}{L} \quad \begin{array}{l} \uparrow \text{const.} \\ \downarrow \end{array}$$

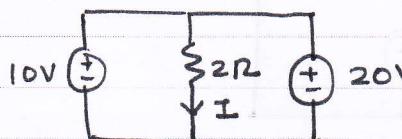
* Voltage Source: →

- Ideal voltage source delivers energy at specify voltage (V) which is independent on current delivers by source.
- Internal Resistance of ideal voltage source = zero. ($R_s=0$).
- practical voltage source delivers energy as specify voltage which depend on current delivers by source.
- Independent voltage source does not obey ohm's law.

V - I characteristic (non-linear & unidirectional).

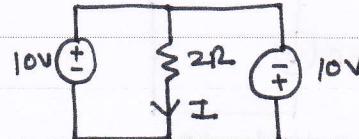


Q. Find current in 2Ω Resistor?



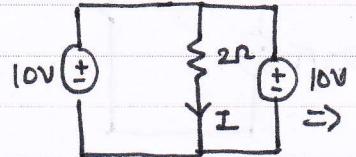
$$10 \neq 20$$

NOT satisfied KVL.



$$10 \neq -10$$

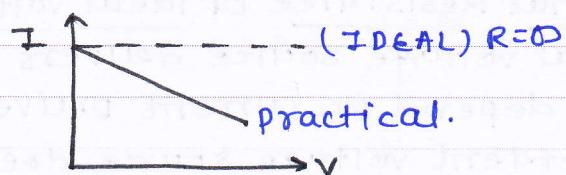
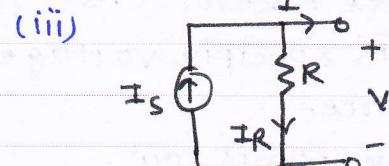
NOT satisfied KVL



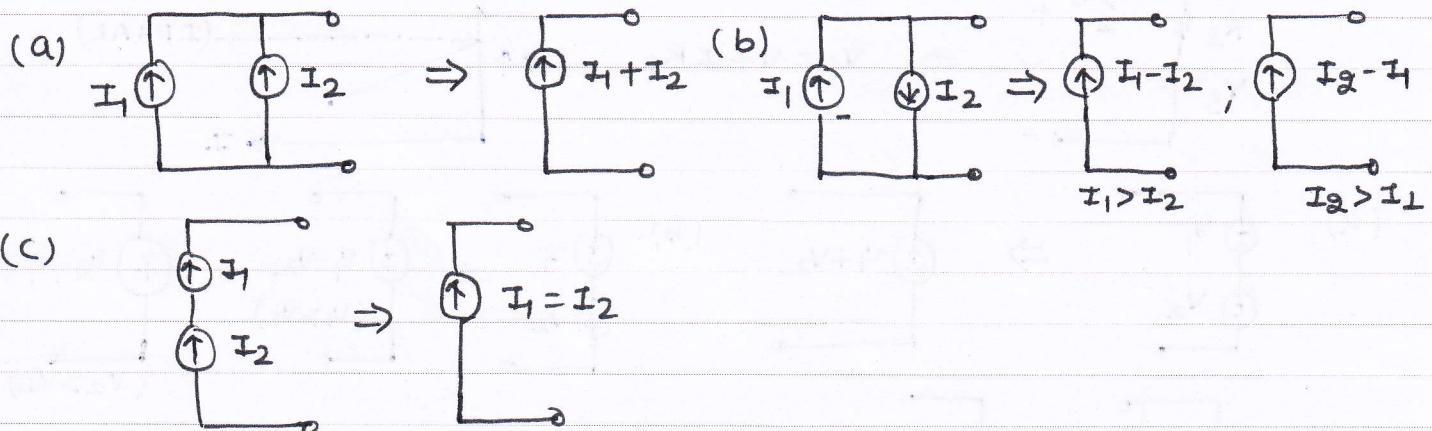
$$10 = 10 \text{ so } I = \frac{10}{2} = 5A$$

* CURRENT SOURCE *

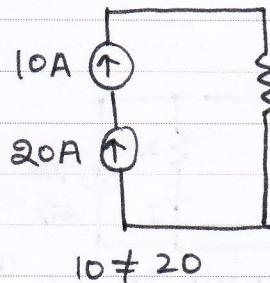
- (i) Ideal current source deliver energy at specified current
- (ii) which is independent on voltage across the source
- (iii) Internal Resistance of Ideal current source = infinite.



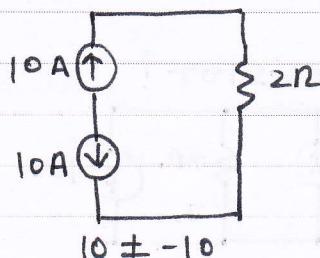
$$I_s = IR + I$$



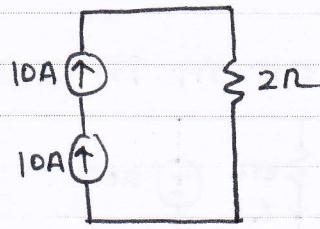
Q. Find current in $2R$ resistor?



NOT USE KCL



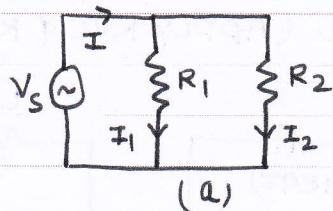
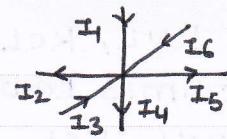
NOT USE KCL



USE KCL SO $I = 10A$ at $2R$.

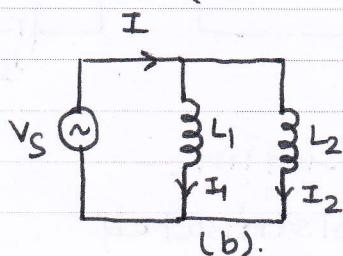
* KCL (Law of conservation of charge) →

- Algebraic sum of current = 0 at a point.
- When two point element connect common point called simple Node or more than two element called principal Node.
- $I_1 + I_3 + I_6 = I_2 + I_4 + I_5$
-



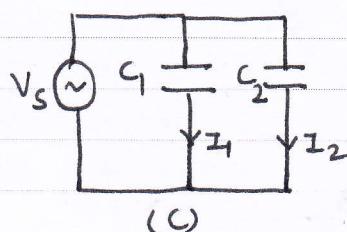
$$R_{eq} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

$$I_1 = \frac{I \cdot R_2}{R_1 + R_2}; \quad I_2 = \frac{I \cdot R_1}{R_1 + R_2}$$



$$L_{eq} = \frac{L_1 \cdot L_2}{L_1 + L_2}$$

$$I_1 = \frac{I \cdot L_2}{L_1 + L_2}; \quad I_2 = \frac{I \cdot L_1}{L_1 + L_2}$$

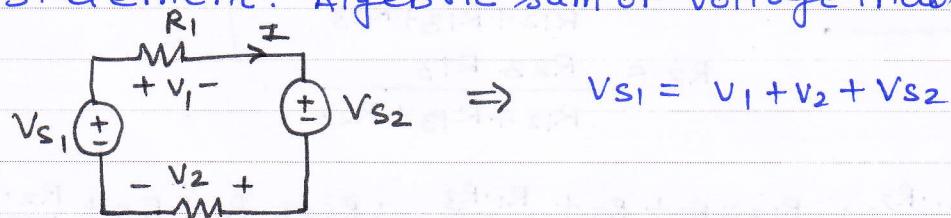


$$C_{eq} = C_1 + C_2$$

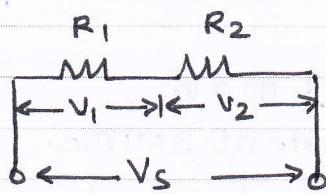
$$I_1 = \frac{I \cdot C_1}{C_1 + C_2}; \quad I_2 = \frac{I \cdot C_2}{C_1 + C_2}$$

* KVL (Law of conservation of energy) *

- Statement: Algebraic sum of voltage inclosed closed loop is zero.



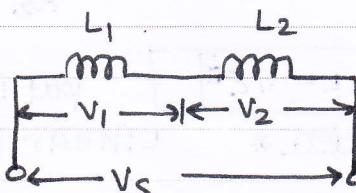
$$V_{S1} = V_1 + V_2 + V_{S2}$$



$$Req = R_1 + R_2$$

$$V_1 = \frac{V_s \cdot R_1}{R_1 + R_2}$$

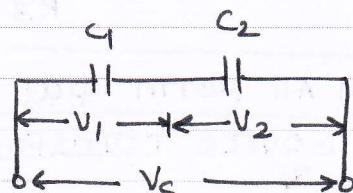
$$V_2 = \frac{V_s \cdot R_2}{R_1 + R_2}$$



$$Req = L_1 + L_2$$

$$V_1 = \frac{V_s \cdot L_1}{L_1 + L_2}$$

$$V_2 = \frac{V_s \cdot L_2}{L_1 + L_2}$$



$$Req = (C_1 || C_2) = \frac{C_1 \cdot C_2}{C_1 + C_2}$$

$$V_1 = \frac{V_s \cdot C_2}{C_1 + C_2}$$

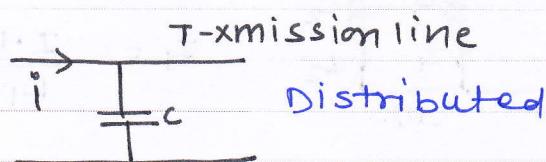
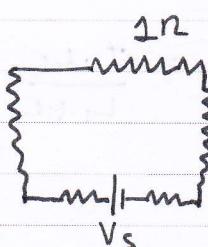
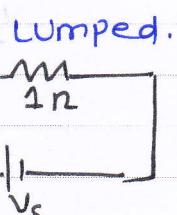
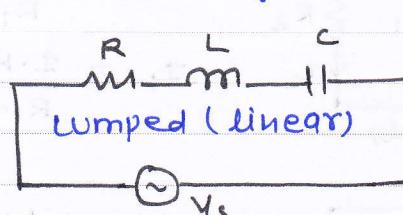
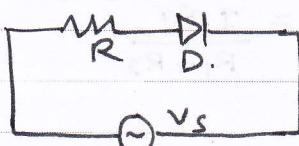
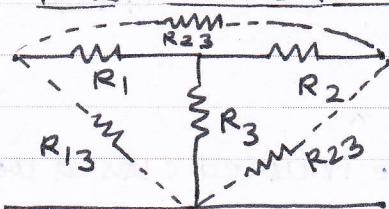
$$V_2 = \frac{V_s \cdot C_1}{C_1 + C_2}$$

- KVL, KCL Fails For distributed parameter
- Ohm's Law apply lumped or distributed parameter
- KVL, KCL Apply [Lumped + linear/Non linear + unidirectional + time variant or time invariant]

→

- * Field theory → APPLY Low & High Frequency (NOT APPLY KVL & KCL)
- * Network theory → Low Frequency (APPLY KVL & KCL).

Lumped (non-linear)

* Δ -Y CONVERSION * Δ to Y.

$$R_1 = \frac{R_{12} \cdot R_{13}}{R_{12} + R_{13} + R_{23}}$$

$$R_2 = \frac{R_{12} \cdot R_{23}}{R_{12} + R_{13} + R_{23}}$$

$$R_3 = \frac{R_{23} \cdot R_{13}}{R_{12} + R_{13} + R_{23}}$$

} - ①

Y to Δ

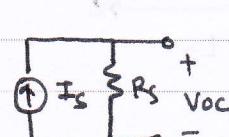
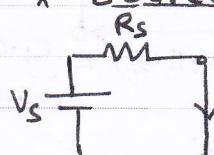
$$R_{12} = R_1 + R_2 + \frac{R_1 \cdot R_2}{R_3}; \quad R_{13} = R_1 + R_3 + \frac{R_1 \cdot R_3}{R_2}; \quad R_{23} = R_2 + R_3 + \frac{R_2 \cdot R_3}{R_1} \quad \text{--- ②}$$

In All Form put $[R=L=1/C^2]$

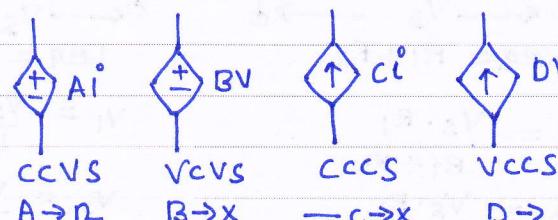
put in eqn ① & ②

* SOURCE TRANSFORMATION *

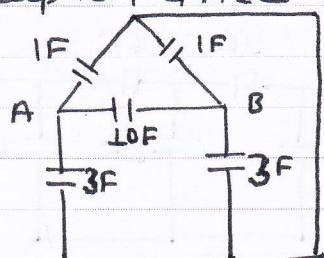
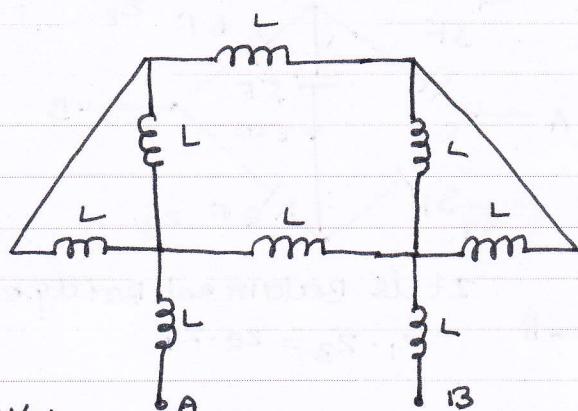
Linear Dependent Source.



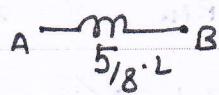
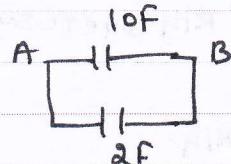
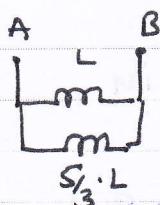
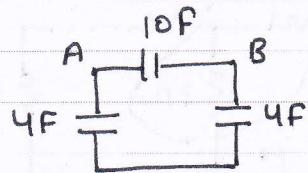
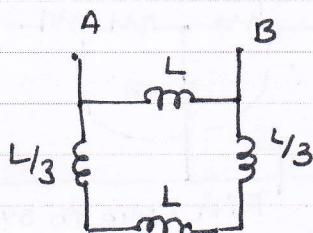
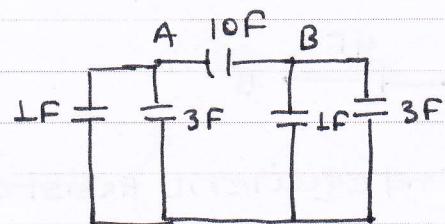
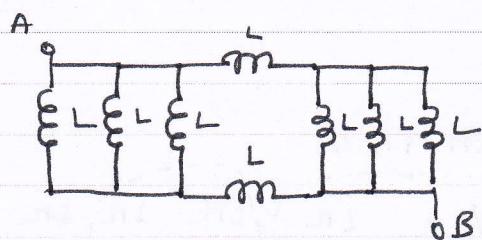
$$I_s = I_{sc} = V_s / R_s; \quad V_{oc} = V_s = I_{sc} \cdot R_s.$$



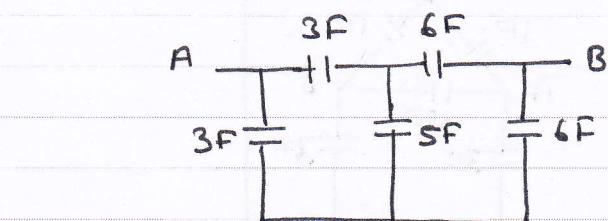
Q.3. Find equal inductance or capacitance between A & B is



ANS:-

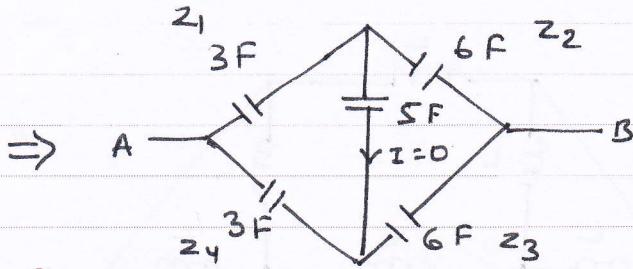


Q.4. Find equivalent capacitance b/w A & B.



$$z_1 = 3F \quad 6F = z_3$$

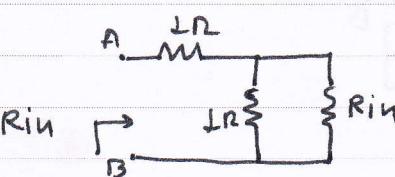
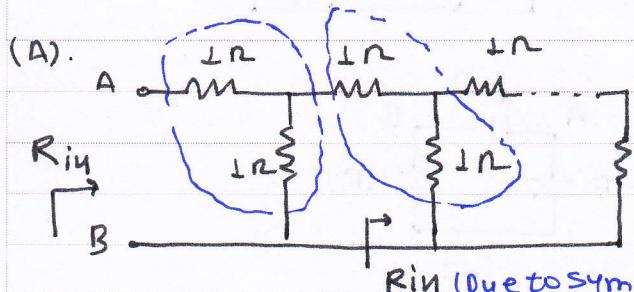
$$\Rightarrow A - \boxed{1 \parallel 1} - B \quad z_2 = 3F \quad 6F = z_4$$



It is Balanced Bridge so
 $z_1 \cdot z_3 = z_2 \cdot z_4$

$$\Rightarrow A - \boxed{4F} - B$$

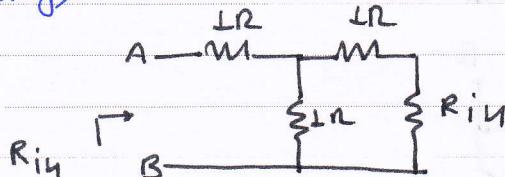
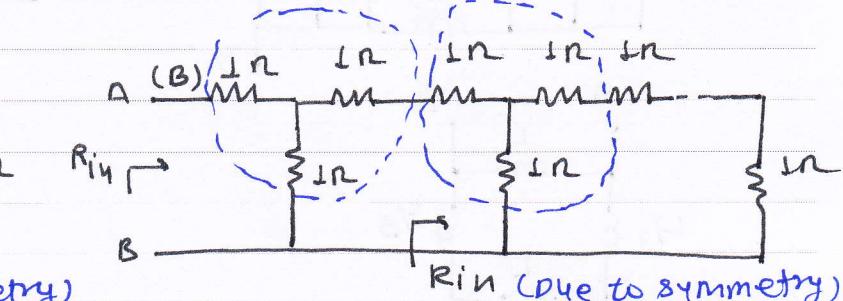
Q.5. Find equivalent resistance between A & B



$$R_{in} = 1 + \frac{1 \times R_{in}}{1 + R_{in}}$$

$$R_{in}^2 - R_{in} - 1 = 0$$

$$R_{in} = \frac{1 + \sqrt{5}}{2} R_{in}$$

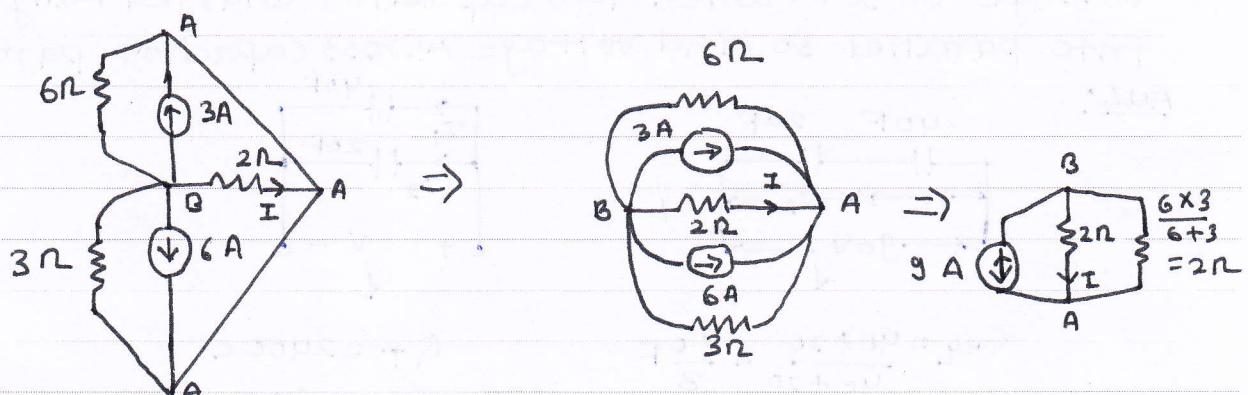


$$R_{in} = 1 + \frac{1 \times (1 + R_{in})}{1 + 1 + R_{in}} = \frac{3 + 2 R_{in}}{2 + R_{in}}$$

$$2 R_{in} + R_{in}^2 = 3 + 2 R_{in}$$

$$R_{in} = \sqrt{3} R$$

Q. 6 Find current in 2Ω resistor?

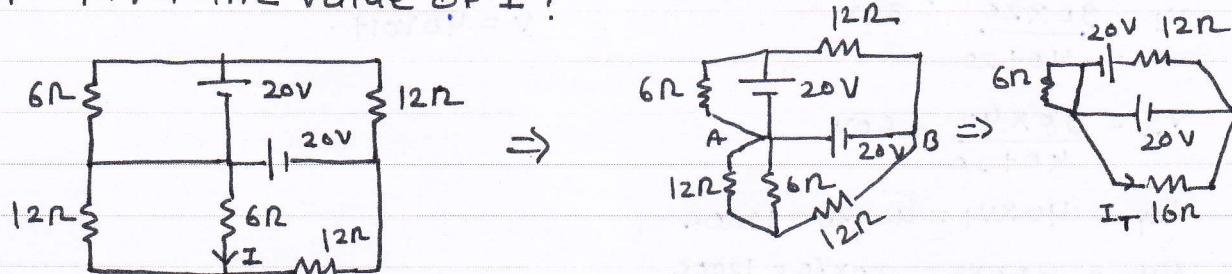


So current divider rule

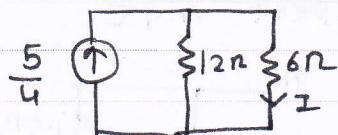
$$I = \frac{-9 \times 2}{4} = -4.5 \text{ Amp } (B \rightarrow A)$$

$$I = 4.5 \text{ Amp } (A \rightarrow B).$$

Q. 7. Find the value of I ?

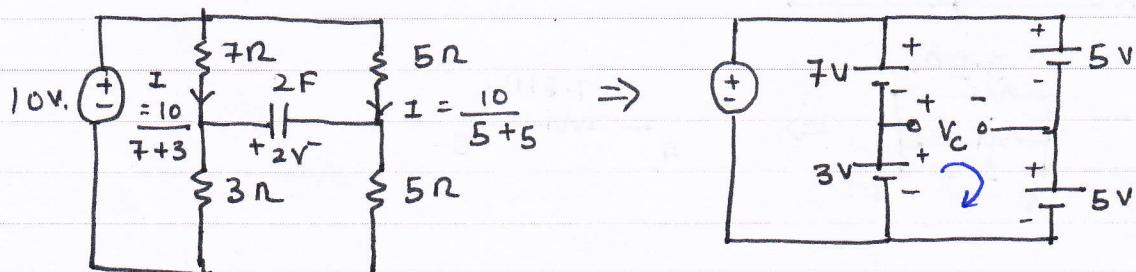


$$\text{Parallel voltage same } I_T = \frac{20}{16} = \frac{5}{4} \text{ Amp.}$$



$$I = \frac{\frac{5}{4} \times 12}{18} = \frac{15}{18} = \frac{5}{6} = 0.7 \text{ Amp.}$$

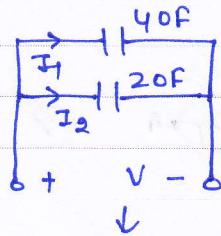
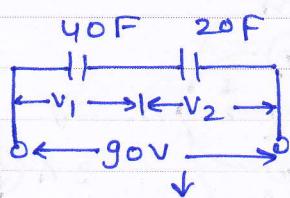
Q. 8. Find an energy of given capacitor?



$$-3 + V_C + 5 = 0 \Rightarrow V_C = -2V. ; \text{capacitor energy} = \frac{1}{2}CV^2 = \frac{1}{2} \times 2 \times 4 = 4 \text{ Watt}$$

Q.9. Two capacitor of 40F & 20F are connected in series to source voltage of 90V . When two capacitor charged fully & connected into parallel so find voltage across capacitor parallel connection?

Aus:-



$$C_{eq} = \frac{40+20}{40+20} = \frac{40}{3}\text{F}$$

$$Q = C_{eq} \cdot V = \frac{40}{3} \times 90$$

$$Q = 1200\text{C}$$

$$V_1 = \frac{90 \times 20}{40+20} = 30\text{V}$$

$$V_2 = \frac{90 \times 40}{40+20} = 60\text{V}$$

$$Q_{V_1} = 40 \times V_1 = 40 \times 30 = 1200\text{C}$$

$$Q_{V_2} = 20 \times V_2 = 20 \times 60 = 1200\text{C}$$

$$Q_T = Q_{V_1} + Q_{V_2} = 2400\text{C}$$

$$Q_T = 2400\text{C}$$

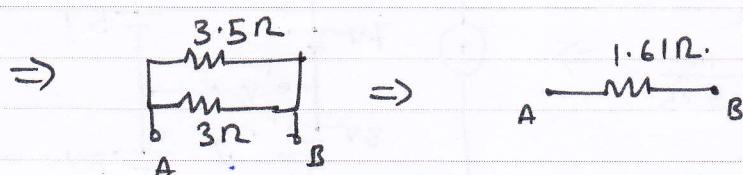
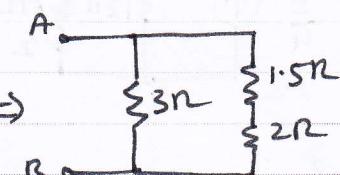
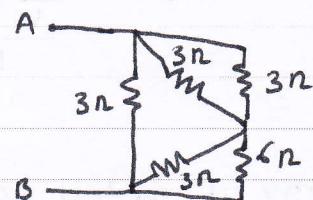
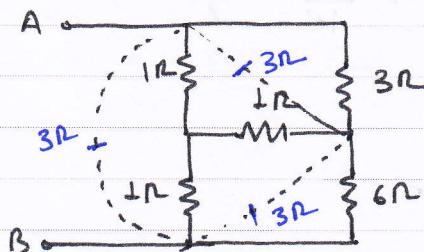
$$C_{eq} = 60\text{F}$$

$$Q_T = C_{eq} \cdot V$$

$$2400 = 60 \times V$$

$$V = 40\text{Volts.}$$

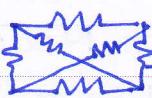
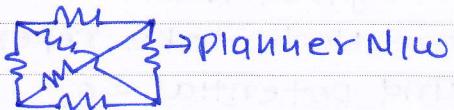
Q.10. Find equivalent Resistance with Respect A & B.



$$\Rightarrow 1.61\Omega$$

* Mesh Analysis :-

- mesh Analysis can be Applied only for planner Network
- A Network HAVE NO cross connection its diagonal element called planner Network



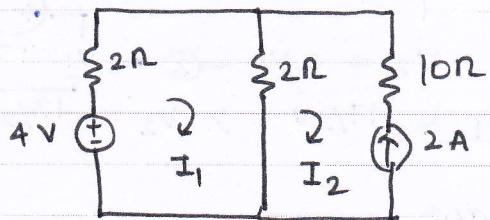
→ Nonplanner Network.

$$\rightarrow \text{NO OF KVL or mesh equation} = e = b - N + 1 = b - N + 1 = b - (N-1)$$

* Procedure *

- Identify total NO OF Mesh in the given Network by $e = b - (N-1)$
- assign current direction for each mesh (clockwise) $\rightarrow I$
- Devlop KVL eq^u for each mesh.
- By solving KVL eq^u find Loop current.

ex:-



$$(a) \text{ NO OF mesh eq}^u = b - (N-1) = 3 - (2-1) = 2$$

(b) take direction of current in loop clockwise

$$(c) \text{ APPLY KVL in 1st loop \& 2nd loop}$$

$$-4 + 2I_1 + 2(I_1 - I_2) = 0 \quad \textcircled{1}$$

$$10I_2 + 2(I_2 - I_1) = 0 \quad \textcircled{2}$$

$$I_2 = -2A \quad \textcircled{3}$$

do solution eq^u ①, ② & ③ $I_2 = -2A, I_1 = 0A$.

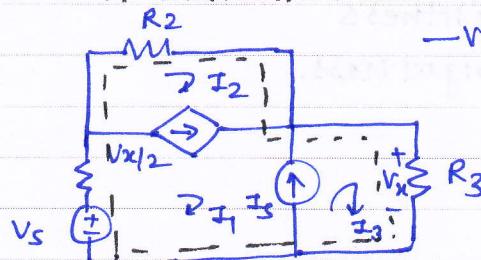
$$N = 2, b = 3$$

* Supermesh * When current source branch is common for two mesh. it is possible to find solution super mesh technique.

CMT * *
Mesh = KVL + Ohm's Law

Supermesh = KVL + KCL + Ohm's Law

Ex:- Devlop mathematical eq^u for Network shown



$$-V_s + R_1 I_1 + R_2 I_2 + R_3 I_3 = 0 \quad (\text{KVL})$$

$$I_1 - I_2 = \frac{V_x}{2} \quad (\text{KCL})$$

$$I_1 - I_3 = -I_s \quad (\text{KCL})$$

* Nodal Analysis *

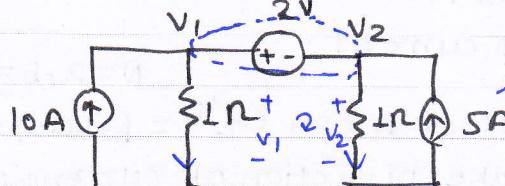
* It can applied linear or non linear or planer network

* Procedure:-

- Identify total NO OF Nodes in the given Network = $e = (N-1)$
- Assign voltage at each Node one Node take reference Node
CMT → Reference Node potential = Ground potential = 0
- Devlop KCL equation of each non-reference Node.
- Solving KCL equation Find Node voltages.

* Super Node * When ideal voltage source connected between two non-reference Node and find soln by Super Node method.

ex:-



$V_1 \& V_2$ common point due to Super Node

$$\text{so } \frac{V_1}{R_1} + \frac{V_2}{R_2} = 10 + 5 \quad \text{---(1)}$$

$$V_1 - V_2 = 2V \quad \text{---(2)}$$

$$V_1 = 17/2V ; V_2 = 13/2V.$$

Node = KCL + Σ Law
Super Node = KCL + KVL + Σ Law

* Bulb brightness *

Series connected Bulb

$$R_1, V_1, P_1 \quad R_2, V_2, P_2$$

$$I \rightarrow R_1 = \frac{V_1^2}{P_1}, \quad R_2 = \frac{V_2^2}{P_2}$$

$$P_1 = I^2 R_1, \quad P_2 = I^2 R_2$$

parallel connected bulb

$$R_1, I_1, P_1 \quad R_2, I_2, P_2$$

$$I \rightarrow R_1 = \frac{P_1}{I_1^2}, \quad R_2 = \frac{P_2}{I_2^2}$$

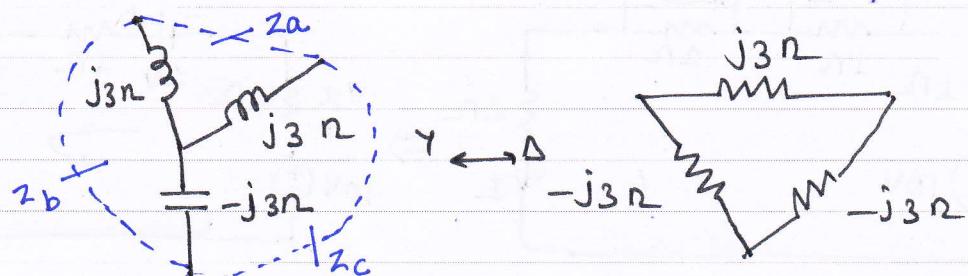
$$R_2, I_2, P_2$$

$$P_1 = \frac{V^2}{R_1}, \quad P_2 = \frac{V^2}{R_2}$$

When voltage Rating same:-

- series low rating bulb more Brightness
- parallel high rating bulb more Brightness.

Q.12. Identify element. Y-Δ conversion given connection.

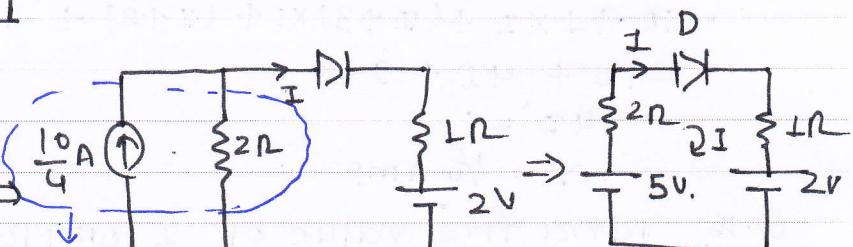
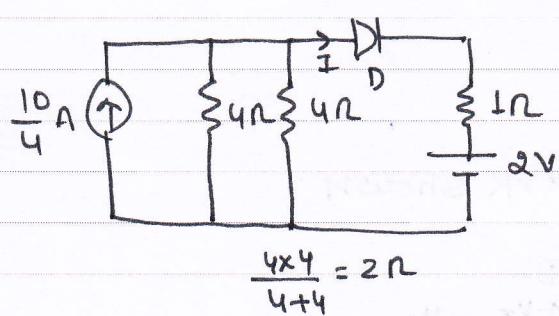
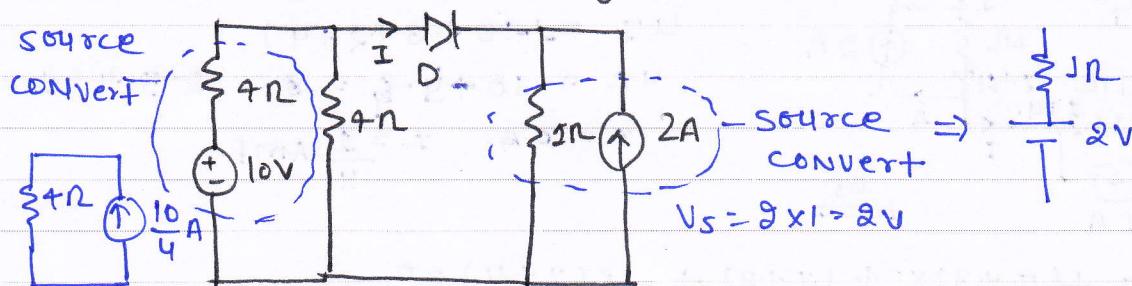


$$Z_a = j3 + j3 + \frac{j3 \times j3}{-j3} = j3n \quad (\text{Inductor})$$

$$Z_b = j3 - j3 + \frac{j3 \times -j3}{j3} = -j3n \quad (\text{capacitor})$$

$$Z_c = j3 - j3 + \frac{j3 \times -j3}{j3} = -j3n \quad (\text{capacitor})$$

Q.13. Find current through 2 diode is: $I = ?$

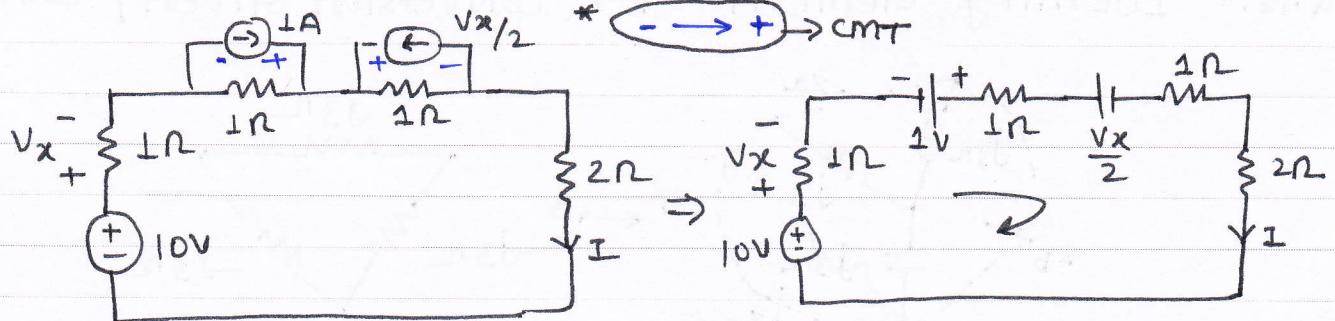


$$\frac{4 \times 4}{4+4} = 2\Omega$$

$$V = \frac{10}{4} \times 2 = 5 \text{ volt}$$

$$I = \frac{5-2}{3} = 1A.$$

Q.14. Find current of 2Ω Resistor on given N/W



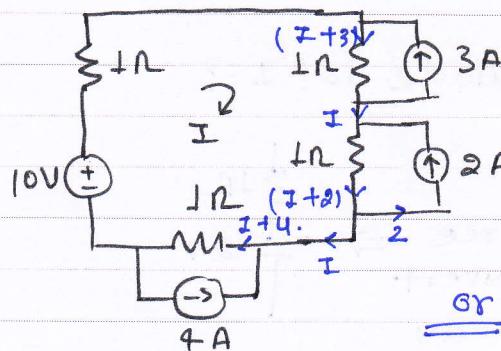
$$-10 + 5I - 1 + \frac{V_x}{2} = 0; \quad V_x = I$$

$$-10 + 5I - 1 + \frac{I}{2} = 0$$

$$\boxed{I = 2A}$$

* Good

Q.15 Find the value of I of the Network shown:



$$-10 + 1 \times I + I + 3 + I + 2 + 1 + 4 = 0$$

$$4I = 1$$

$$-10 + 4 \times I + (1 \times 3) + [1 \times (2)] + (1 \times 4) = 0$$

$$4I = -(-10 + 3 + 2 + 4)$$

$$4I = 10 + 5 - 6 = 9 \quad 10 - 5 - 4 = 1$$

$$I = \frac{9}{4} A. \quad I = \frac{1}{4} \text{ Amp.}$$

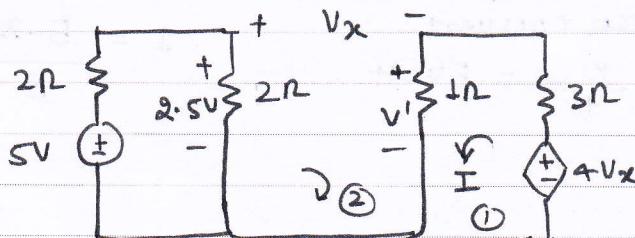
$$-10 + 1 \times I + (I + 3) \times 1 + (I + 2) + 1 \times (2 + 4) = 0$$

$$-10 + 4I + 9 = 0$$

$$4I = 1$$

$$I = \frac{1}{4} \text{ Amp}$$

Q.16. Find the value of I of Network shown



From ①

$$I = \frac{4V_x}{4} = V_x$$

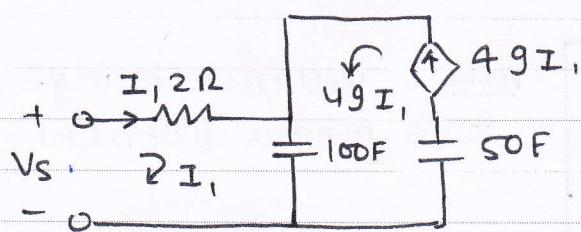
$$V' = 1 \times I = I$$

$$\text{From } ② \quad -2.5 + V_x + I = 0$$

$$2I = 2.5$$

$$I = 1.25 \text{ A.}$$

Q.17. Find equivalent capacitance w.r.t A & B



$$VS = 2I_1 + \frac{1}{100} \int 50I_1 dt$$

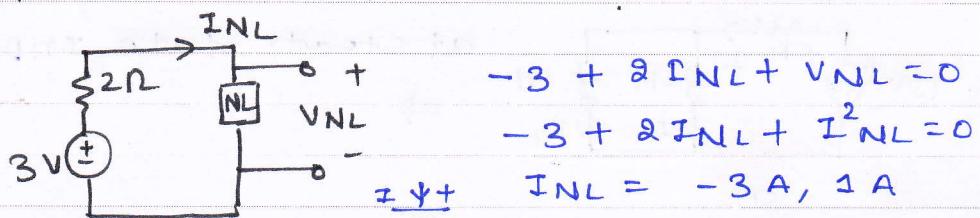
$$VS = 2I_1 + \frac{1}{2} \int I_1 dt \quad \text{--- (1)}$$

$$\text{General eqn } VS = R I_1 + \frac{1}{C_{eq}} \int I_1 dt \quad \text{--- (2) compare}$$

$$C_{eq} = 2F$$

Q.18. A practical DC source of 3V with internal resistance of 2Ω is connected to non linear resistor. The characteristic of Non linear Resistor given by $V_{NL} = I^2_{NL}$. Find power dissipation in non-linear Resistor?

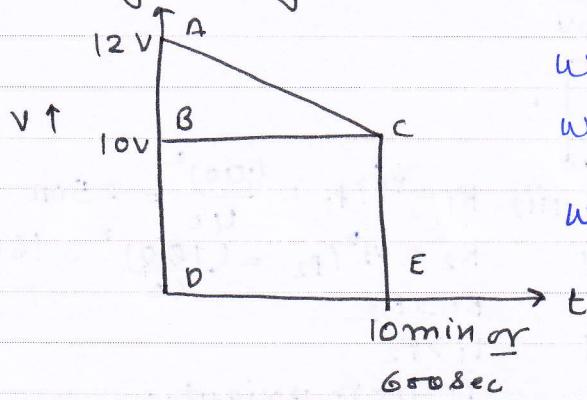
Ans:-



power dissipation (Power absorbed)

$$P_{NL} = V_{NL} \times I_{NL} = I_{NL}^3 = 1 \text{ watt}$$

Q.19 A fully charged mobile is good for 10min talk time during battery delivers a constant current of 2Amp. Find energy of the battery during talktime in given characteristic.

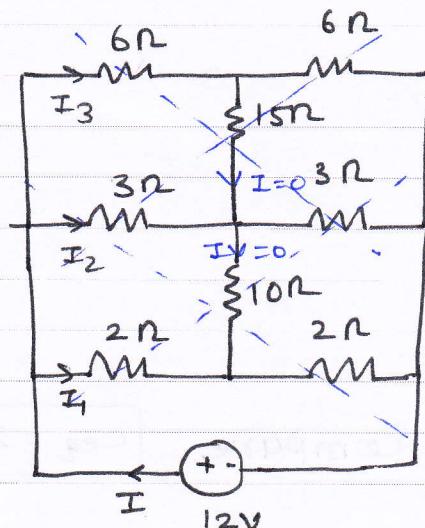


$$W = (\Delta ABC + \square BCDE) \times 2$$

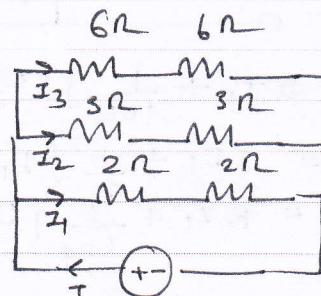
$$W = \left(\frac{1}{2} \times 600 \times 2 + 10 \times 600 \right) \times 2$$

$$W = 6600 \times 2 = 13.2 \text{ kJ}$$

Q.20. Find the value of I shown fig.

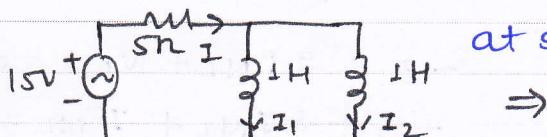


Ans:- Balance Bridge
I = 0 means open ckt

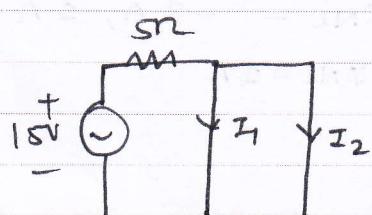


$$I = I_1 + I_2 + I_3 = \frac{12}{6+6} + \frac{12}{3+3} + \frac{12}{2+2} = 1+3+2 = 6 \text{ A.}$$

Q.21 Find steady state current I_1, I_2 in steady state condition.



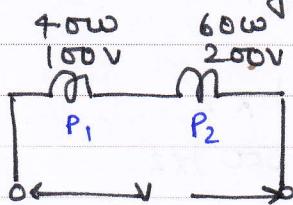
at steady state inductor behave & short ckt.



$$I_1 = I_2 \Rightarrow \frac{15}{3+2} = \frac{15}{5} = 3 \text{ A} = I_1 + I_2$$

$$I_1 = I_2 = 1.5 \text{ A.}$$

Q.22. Following connection which give more brightness.

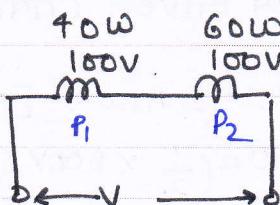


$$\text{Ans (i)} R_1 = \frac{P}{I^2} = \frac{V^2}{P}$$

$$R_1 = \frac{V_1^2}{P_1} = \frac{(100)^2}{40} = 250 \Omega$$

$$R_2 = \frac{V_2^2}{P_2} = \frac{(200)^2}{60} = 666.7 \Omega$$

$R_2 > R_1$; so $P_2 > P_1$ ∴ P_2 more bright



$$\text{(iii)} R_1 = \frac{V_1^2}{P_1} = \frac{(100)^2}{40} = 250 \Omega$$

$$R_2 = \frac{V_2^2}{P_2} = \frac{(100)^2}{60} = 166.67 \Omega$$

$R_1 > R_2$

$P_1 > P_2$

P_1 more bright.

* STEADY STATE AC CIRCUIT *

9784236981

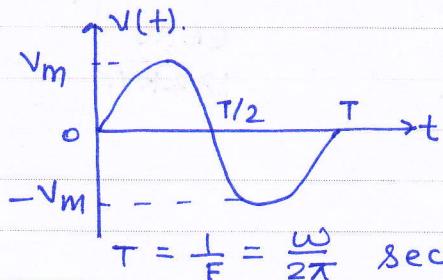
SUBJECT - NETWORK TOPIC STEADY STATE

A.C. circuit.

P. No: 23

Advantage of sine waves: → 1. It is easy to handle mathematical problem like differential or integral, rewrite in term of sine function by Fourier Analysis.

2. it is easy to generate in laboratory.

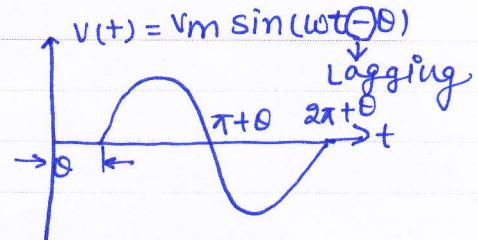
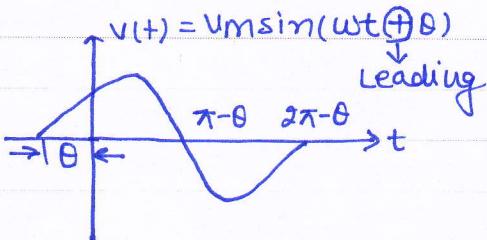
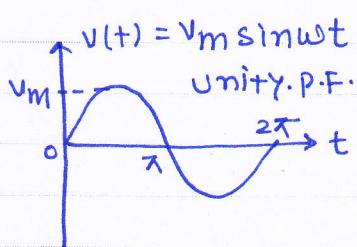


$$V(t) = V_m \sin \omega t$$

V_m = peak or maximum value.

ω = Angular frequency

$\omega T = 2\pi$ = Argument (rad).



RMS value (Root mean square) :→

1. RMS value is defined based on Heating effect of the waveform.
2. The voltage at which heat dissipation in AC ckt equal heat dissipation in DC ckt at equal resistance and time. ($W_{AC} = W_{DC} = I^2 R t$).

$$V_{RMS} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} V^2 d\omega t} = \sqrt{\frac{1}{T} \int_0^T V^2 dt}$$

Average value:

1. It is based on charge transfer in ckt
2. the voltage at which charge transfer in AC circuit equal to charge transfer in DC circuit at same resistance and time. ($Q_{AC} = Q_{DC} = It$)
3. Find Avg. Value of symmetric wave consider half cycle else used full cycle.
4. Average value of complete cycle of symmetric wave equal to zero.

→ To identify about shape of the waveform Form Factor and peak Factor concept are introduced.

$$\text{Form Factor} = \frac{V_{\text{Rms}}}{V_{\text{avg}}} = \frac{V_m/\sqrt{2}}{2V_m/\pi} = 1.11$$

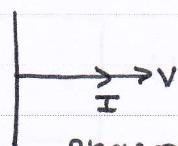
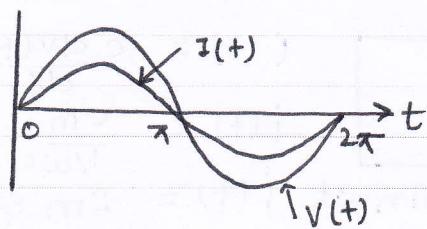
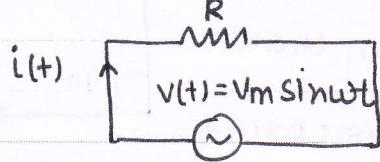
Power system

$$\left. \begin{array}{l} 11 \text{ KV} \\ 33 \text{ KV} \\ 66 \text{ KV} \\ 132 \text{ KV} \end{array} \right\} \text{F.F.}$$

$$\text{peak Factor} = \frac{V_m}{V_{\text{Rms}}} = \frac{V_m}{V_m/\sqrt{2}} = \sqrt{2}$$



* A.C. SOURCE ACROSS Resistor *



Phasor Diagram

$$P(t) = V(t) \cdot I(t) = V_m \sin \omega t \cdot I_m \sin \omega t = V_m I_m \sin^2 \omega t \quad \left\{ \sin^2 \omega t = \frac{1 - \cos 2\omega t}{2} \right.$$

$$P(t) = \frac{V_m I_m}{2} [1 - \cos 2\omega t]$$

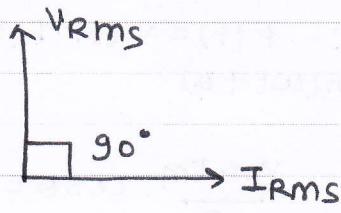
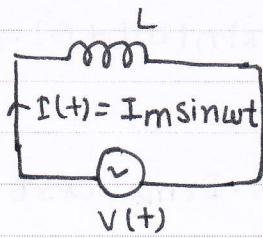
$$P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} P(t) \cdot dt = \frac{V_m I_m}{2}$$

$$P_{avg} = \frac{V_m I_m}{2} = \frac{V_m}{\sqrt{2}} \cdot \frac{I_m}{\sqrt{2}} = V_{rms} \cdot I_{rms}$$

$$F = 50 \text{ Hz (wave)}$$

$F_p = 2 \times 50 = 100 \text{ Hz}$
of power.

* A.C SOURCE ACROSS inductor (L) *



$$I(t) = I_m \sin \omega t \quad \text{---(1)}$$

$$V(t) = L \frac{di(t)}{dt}$$

$$V(t) = \omega L I_m \cos \omega t$$

$$V = V_m \sin(\omega t + 90^\circ) \quad \text{---(2)}$$

$$P(t) = V(t) \cdot D(t) = I_m \sin \omega t \cdot V_m \sin(\omega t + 90^\circ)$$

$$P(t) = \frac{V_m \cdot R_m}{2} \sin^2 \omega t$$

$$P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} P(t) \cdot dt \Rightarrow P_{avg} = 0$$

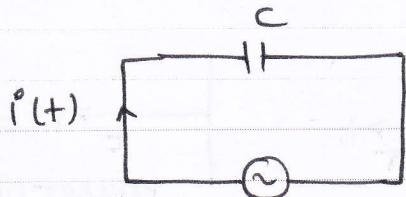
$$F = 50 \text{ Hz}$$

$$F_p = 100 \text{ Hz.}$$

→ Phasor Diagram take Rms value. In series circuit I is Reference and parallel circuit V take reference.

→ In (+) Half cycle inductor take Energy from source and (-) Half cycle taken source from inductor.

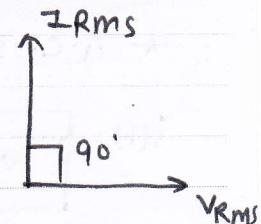
* A.C. Source Across capacitor (C):



$$i(t) = C \frac{dV(t)}{dt} = \omega C V_m \cos \omega t$$

$$i(t) = \frac{V_m}{\sqrt{2}\omega C} \cos \omega t = I_m \cos \omega t$$

$$V(t) = V_m \sin \omega t \quad i(t) = I_m \sin(\omega t + 90^\circ)$$



$$P(t) = V(t) \cdot I(t) = V_m \sin \omega t \cdot I_m \cos \omega t = \frac{V_m I_m}{2} \sin 2\omega t$$

* $P(t) = \frac{V_m I_m}{2} \sin 2\omega t$

* $F = 50 \text{ Hz}$
 $F_p = 100 \text{ Hz}$

* $P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} P(t) \cdot dt \omega t = 0$

* $P_{avg} = 0$

* POWER *

* → Instantaneous power: - $P(t) = V(t) \cdot I(t) = V_m \sin(\omega t + \theta) \cdot I_m \sin \omega t$

$$P(t) = V_m I_m \sin \omega t \cdot \sin(\omega t + \theta)$$

$$P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} P(t) \cdot dt \omega t = \frac{V_m \cdot I_m}{2} \cdot \cos \theta = V_{rms} \cdot I_{rms} \cdot \cos \theta$$

power factor = $\cos \theta = \frac{V_R}{V} = \frac{R}{Z} = \frac{P}{S} \Rightarrow \left\{ \begin{array}{l} \text{Voltage} \\ \text{Impedance} \\ \text{Power} \\ \text{Angle} \end{array} \right\}$

* → power Factor Angle indicated position of current phasor with respect to voltage phasor.

* → (watt) P = Active power / True power / Real power / Avg. power / effective power

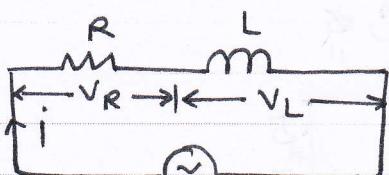
Q (VAR) = Volt Amperes Reactive / Inductive Reactive power.

S (VA) = Volt Amperes / Apparent power / complex. power.

$$P = I^2 R = VI \cos \theta; Q = I^2 X = VI \sin \theta, S = I^2 Z = VI^* = P + jQ$$

* → $P_L = VI \cos \theta$ For Unity p.f the losses are (VI) low.

* R-L series circuit:



BY KVL $\bar{V} = \bar{V}_R + j\bar{V}_L$

$$V = V_R \angle 0^\circ + V_L \angle +90^\circ$$

$$IR = I_R + jI_{XL}$$

$$Z = R + jX_L \quad \Omega$$

$$V = \sqrt{V_R^2 + V_L^2}$$

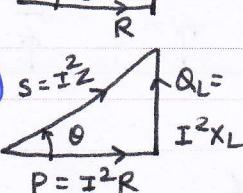
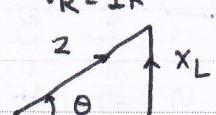
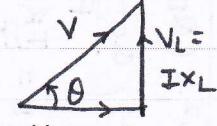
$$\theta = \tan^{-1} \left(\frac{V_L}{V_R} \right)$$

$$Z = \sqrt{R^2 + X_L^2}$$

$$\theta = \tan^{-1} \left(\frac{X_L}{R} \right)$$

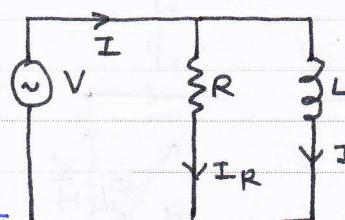
$$S = \sqrt{P^2 + Q^2}$$

$$\theta = \tan^{-1} \left(\frac{Q}{P} \right) \quad S = I^2 Z \quad Q_L = I^2 X_L$$



$$\cos \theta = \frac{V_R}{V} = \frac{R}{Z} = \frac{P}{S} \quad (\text{power factor (lead)})$$

* R-L parallel circuit:



BY KCL

$$I = I_R \angle 0^\circ + I_L \angle -90^\circ$$

$$V/Z = V/R - jV/X_L$$

$$VY = V_G - jV_B L$$

$$Y = G_1 - jB_1 L \quad \Omega^{-1} (\text{mho})$$

$$V = I_R \angle 0^\circ + I_L \angle -90^\circ$$

$$V_G = I_R$$

$$I_L = B_1 L \cdot V$$

$$I = \sqrt{I_R^2 + I_L^2}$$

$$\theta = \tan^{-1} \left(-\frac{I_L}{I_R} \right)$$

$$Y = \sqrt{G_1^2 + B_1 L^2}$$

$$\theta = \tan^{-1} \left(-\frac{B_1 L}{G_1} \right)$$

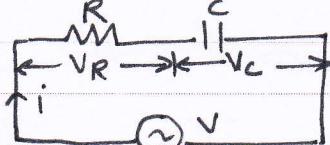
$$S = \sqrt{P^2 + Q^2}$$

$$\theta = \tan^{-1} \left(-\frac{Q}{P} \right)$$

$$P = V^2 G_1$$

$$Q = V^2 B_1 L$$

* RC - series circuit



$$V_R = IR \quad V = IZ$$

$$V = V_R \angle 0^\circ + V_C \angle -90^\circ$$

$$IZ = IR - jIX_C$$

$$Z = R - jX_C \quad (\Omega)$$

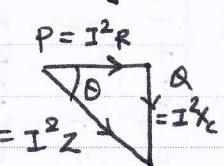
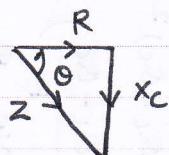
$$Z = \sqrt{R^2 + X_C^2}$$

$$\theta = \tan^{-1} \left(-\frac{X_C}{R} \right)$$

$$V = \sqrt{V_R^2 + V_C^2}$$

$$\theta = \tan^{-1} \left(-\frac{V_C}{V_R} \right)$$

$$\theta = \tan^{-1} \left(-\frac{Q}{P} \right); \cos \theta = \frac{V_R}{V} = \frac{R}{Z} = \frac{P}{S} \quad (\text{lead})$$



* RC - parallel circuit

$$I = \frac{V}{R} \quad I_C = \frac{V}{X_C}$$

$$I = I_R \angle 0^\circ + I_C \angle +90^\circ$$

$$V/Z = V/R + jV/X_C$$

$$VY = V_G + jV_B C$$

$$Y = G_1 + jB_1 C = \Omega^{-1} (\text{mho})$$

$$Y = \sqrt{G_1^2 + B_1 C^2}; \theta = \tan^{-1} \left(\frac{B_1 C}{G_1} \right)$$

$$T = \sqrt{I_R^2 + I_C^2}$$

$$\theta = \tan^{-1} \left(\frac{I_C}{I_R} \right)$$

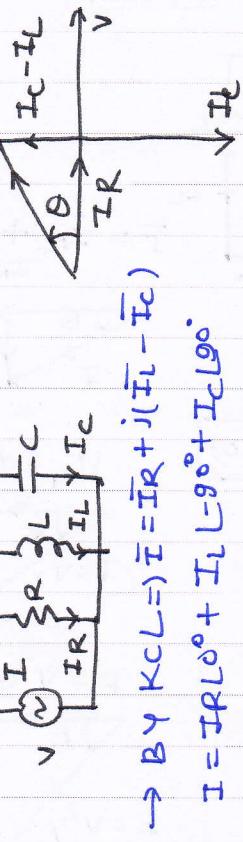
$$\theta = \tan^{-1} \left(\frac{Q}{P} \right)$$

$$\cos \theta = \frac{I_R}{I} = \frac{G_1}{Y} = \frac{P}{S} \quad (\text{lead})$$

$$Y = \frac{V^2}{Z} \quad B_1 C = Q$$

$$V^2 G_1 = P$$

* R-L-C parallel circuit $\uparrow I_C$



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$$x_1 = \alpha [L + j(B_c - E)]$$

$$Y = \frac{5j + j(B_C - B_L)}{k^2 + (B_C - B_L)^2}$$

$$\theta = \tan^{-1} \left(\frac{B_c - BL}{L_1} \right)$$

$$I = \int I^2 d\tau + (I_L - I_C)$$

$$\Rightarrow S = \frac{P^2 + (\Omega_F - \Omega_L)}{\pi R}$$

$$\theta = \tan^{-1} \left(\frac{p}{q - q_0} \right)$$

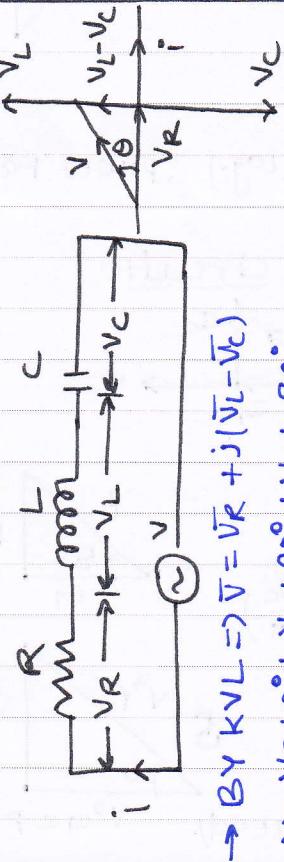
$$\rightarrow P.F = \cos \theta = \frac{I_R}{I} = \frac{5}{7} = \frac{P}{S}$$

(i) $I_{c1} > I_{c2}$ (Ledger)

$$(ii) \quad T_L > T_c \quad (\log.)$$

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* R-L-C series circuit



$$\rightarrow \text{By } kV_L \Rightarrow \bar{V} = V_R + j(V_L - V_C)$$

$$V \equiv \sqrt{R^2 - L^2} + \sqrt{R^2 + L^2}$$

$$L_2 = \pm [k + j(x_L - x_C)]$$

$$\theta = \tan^{-1} \left(\frac{x_L - x_C}{R} \right)$$

$$V = \sqrt{VR^2 + (V_L - V_C)^2}$$

$$\theta = \tan^{-1} \left(\frac{VR}{\sqrt{V^2 - VR^2}} \right)$$

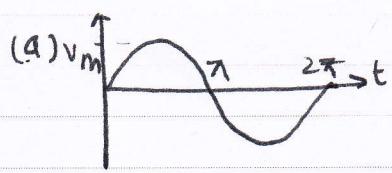
$$\theta = \tan^{-1} \left(\frac{q_1 - qc}{q_2 - qc} \right)$$

$$\Rightarrow P.F = \cos\theta = \frac{VR}{V} = \frac{R}{Z} = \frac{P}{S}$$

$$(ii) V_L > V_C > V_L \text{ (Load.)}$$

$$(iii) \quad V_L = V_C \quad (\text{unitary})$$

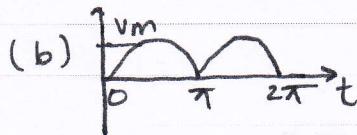
Q.1 Find the Average Value or Rms Value of Given Waveform.



$$\begin{aligned}V_{avg} &= \frac{1}{T} \int_0^{2\pi} V_m \sin \omega t \cdot d\omega t \\&= \frac{2V_m}{\pi}\end{aligned}$$

$$V_{RMS} = \frac{V_m}{\sqrt{2}}$$

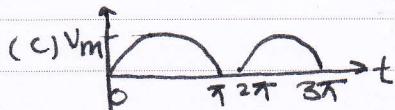
$$\begin{aligned}F.F &\neq P.F \\F.F &= 1.11 \\P.F &= 1.41\end{aligned}$$



$$V_{avg} = \frac{2V_m}{\pi}$$

$$V_{RMS} = \frac{V_m}{\sqrt{2}}$$

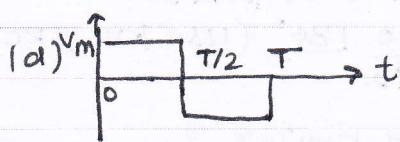
$$\begin{aligned}F.F &= 1.11 \\P.F &= 1.41\end{aligned}$$



$$V_{avg} = \frac{V_m}{\pi}$$

$$V_{RMS} = \frac{V_m}{\sqrt{2}}$$

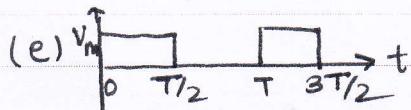
$$\begin{aligned}F.F &= 1.57 \\P.F &= 2\end{aligned}$$



$$V_{avg} = V_m$$

$$V_{RMS} = V_m$$

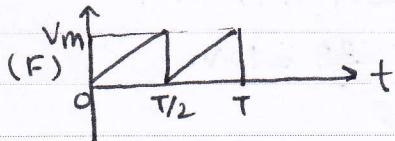
$$\begin{aligned}F.F &= 1 \\P.F &= 1\end{aligned}$$



$$V_{avg} = \frac{V_m}{2}$$

$$V_{RMS} = \frac{V_m}{\sqrt{2}}$$

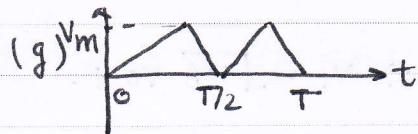
$$\begin{aligned}F.F &= \sqrt{2} \\P.F &= \sqrt{2}\end{aligned}$$



$$V_{avg} = \frac{V_m}{2}$$

$$V_{RMS} = \frac{V_m}{\sqrt{3}}$$

$$\begin{aligned}F.F &= \frac{2}{\sqrt{3}} \\P.F &= \sqrt{3}\end{aligned}$$



$$V_{avg} = \frac{V_m}{2}$$

$$V_{RMS} = \frac{V_m}{\sqrt{3}}$$

$$\begin{aligned}F.F &= \frac{2}{\sqrt{3}} \\P.F &= \sqrt{3}\end{aligned}$$

$$\text{FORM Factor} = \frac{V_{RMS}}{V_{avg}} ; \text{ Peak Factor} = \frac{V_m}{V_{RMS}}$$

Q.2. Find Rms value of following function

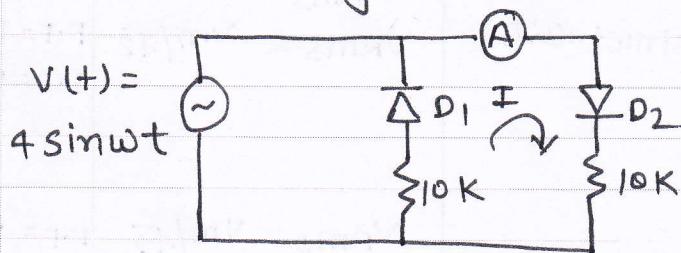
$$V(t) = 3 + \sin 3t + \cos t$$

$$\text{Ans. } V_{RMS} = \sqrt{(3)^2 + \left(\frac{1}{\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2} = \sqrt{10}$$

Q.3. Find power dissipation in the Resistor at $V_{RMS} = \frac{V_m}{\sqrt{2}}$

$$\begin{aligned}\text{Ans. } P_{av} &= \frac{V_{RMS}^2}{R} ; P_{Peak} = \frac{V_m^2}{R} \\P_{av} &= \frac{(V_m/\sqrt{2})^2}{R} = \frac{V_m^2}{2R}\end{aligned}$$

Q.4. When the N/W is having ideal diode, resistor avg. value of indicating ammeter. find Reading of Ammeter.



Aus: it work HALF wave Rectifier

$$I_{AV} = \frac{V_{AV}}{R} = \frac{V_m/\pi}{R} = \frac{4/\pi}{10K} = \frac{0.4}{\pi} \text{ mA.}$$

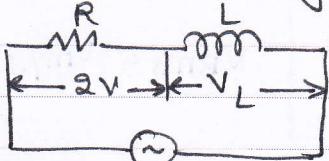
Q.5. $V(+) = 10 \sin(\omega t + 30^\circ)$ present in vector or phasor FORM?

Aus: Vector Form: $\rightarrow 10 \angle 30^\circ$; phasor Form $\rightarrow \frac{10}{\sqrt{2}} \angle 30^\circ$ (use KVL & KCL).

Q.6. $V = 10 \angle 30^\circ$; $i = 5 \angle 10^\circ$ Find complex power?

$$\text{Aus} : S = V I^* = 10 \angle 30^\circ * 5 \angle -10^\circ = 50 \angle 20^\circ$$

Q.7. Find voltage across inductor shown in ckt



$$V(P-P) = 20V. \quad V_m = \frac{20}{2} = 10V.$$

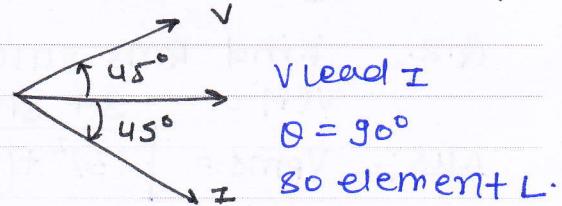
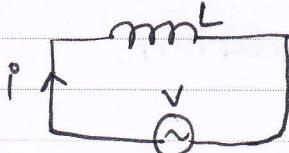
$$V = 10/\sqrt{2}$$

$$\text{Aus} : V = \sqrt{V_R^2 + V_L^2} \Rightarrow 10/\sqrt{2} = \sqrt{4 + V_L^2} \Rightarrow V_L = \sqrt{46} \text{ volt.}$$

Q.8. $V(+) = 9 \sin(t + 45^\circ)$; $I(+) = 3 \sin(t - 45^\circ)$

Find circuit element for given voltage and current equations:

Aus:



$$X_L = \frac{V}{I} = \frac{9/\sqrt{2}}{3/\sqrt{2}} = 3; \quad \omega = 1$$

$$X_L = \omega L = 3$$

$$L \times I = 3 \Rightarrow L = 3H.$$

Q.9. Find circuit element for given voltage and current eq^u

$$V(t) = 9 \sin(t + 30^\circ); I(t) = 3 \sin(2t + 60^\circ)$$

Aus: It is not possible to design the circuit element because frequency of voltage and current are unequal.

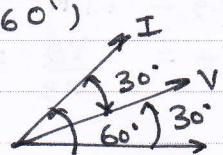
$$\omega_V = 1; \omega_I = 2; \omega_V \neq \omega_I$$

Q.10. Find Active and Reactive power by using voltage & current eq^u.

$$V(t) = 9 \sin(t + 30^\circ); I(t) = 3 \sin(t + 60^\circ)$$

Aus: Active power $P = V I \cos \theta$

$$P = \frac{9}{\sqrt{2}} \times \frac{3}{\sqrt{2}} \cos 30^\circ = \frac{27\sqrt{3}}{4} \text{ Watt}$$



Reactive power $Q = V I \sin \theta$

$$Q = \frac{9}{\sqrt{2}} \times \frac{3}{\sqrt{2}} \times \sin 30^\circ = \frac{27}{4} \text{ VAR (volt-Amp-Reactive).}$$

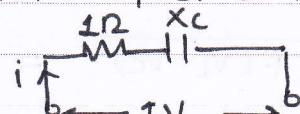
$$Z = \frac{V}{I} = \frac{9/\sqrt{2}}{3/\sqrt{2}} = 3 \Omega \quad \text{OR}$$

$$\cos \theta = R/Z = P/I = \cos 30^\circ \therefore R = 3\sqrt{3}/2 \Omega$$

$$Z^2 = X_C^2 + R^2 \Rightarrow 9 - 27/4 = X_C^2 \therefore X_C = 3/2 \Omega.$$

$$\text{power } P = I^2 R = \left(\frac{3}{\sqrt{2}}\right)^2 \times \frac{3\sqrt{3}}{2} = \frac{27\sqrt{3}}{4} \text{ Watt} \therefore Q = I^2 X_C = \left(\frac{3}{\sqrt{2}}\right)^2 \times \frac{3}{2} \\ Q = \frac{27}{4} \text{ VAR.}$$

Q.11. Find angle of current with respect source voltage when power dissipation 500 mW.



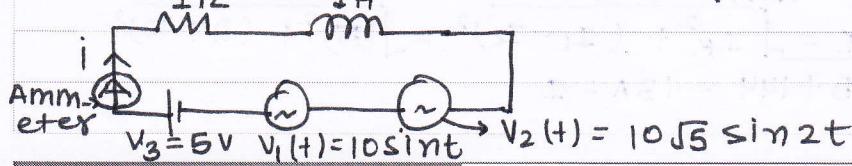
$$P = I^2 R = \frac{V^2}{Z^2} \times R$$

$$500 \times 10^{-3} = \frac{1}{\sqrt{1+X_C^2}} \times 1 \Rightarrow X_C = 1 \Omega$$

$$\text{so } Z = R - j X_C = 1 - j 1 \therefore \theta = \tan^{-1}(-X_C/R) = \tan^{-1}(-1) = -45^\circ$$

$$I = \frac{V}{Z} \angle -45^\circ = \frac{1}{\sqrt{2}} \angle 45^\circ$$

Q.12. Find Ammeter Reading in the circuit shown



AUS: only 1 voltage source active at a time.

For V_1 : $X_{L1} = \omega L \therefore V_1(+)=10 \sin t \therefore \omega=1 \text{ rad/s}$; $V_m=10 \text{ V} \therefore V=10/\sqrt{2}$

$$X_{L1} = 1 \times 1 = 1 \Omega$$

$$Z_1 = \sqrt{R^2 + X_{L1}^2} = \sqrt{1^2 + 1^2} = \sqrt{2}$$

$$I_1 = \frac{V_1}{Z_1} = \frac{10}{\sqrt{2} \times \sqrt{2}} = 5 \text{ A}$$

For V_2 $\therefore V_2(+)=10\sqrt{5} \sin 2t \therefore \omega=2 \text{ rad/s}$ $\therefore V=10\sqrt{5}/\sqrt{2}$

$$X_{L2} = \omega L = 2 \Omega$$

$$Z_2 = \sqrt{R^2 + X_{L2}^2} = \sqrt{1^2 + 2^2} = \sqrt{5}$$

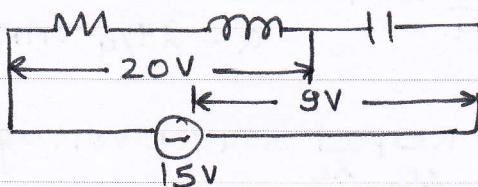
$$I_2 = \frac{V_2}{Z_2} = \frac{10\sqrt{5}}{\sqrt{2} \times \sqrt{5}} = \frac{10}{\sqrt{2}} \text{ A}$$

For $V_3=5 \text{ V}$, $\omega=0$; $X_L=0$ so $Z=R=1 \Omega$

$$I_3 = \frac{V_3}{R} = \frac{5}{1} = 5 \text{ A}$$

So Ammeter reading $I = \sqrt{I_1^2 + I_2^2 + I_3^2} = \sqrt{(5)^2 + (\frac{10}{\sqrt{2}})^2 + (5)^2} = 10 \text{ A}$

Q.13. Find voltage across capacitor shown in Fig.



$$\bar{V}_L - \bar{V}_C = 9 \text{ V}$$

$$\bar{V}_R + \bar{V}_L = 20 \text{ V}$$

$$\text{AUS: } V = \sqrt{V_R^2 + (V_L - V_C)^2} = 15 = \sqrt{V_R^2 + (9 \text{ V})^2}$$

$$V_R = 12 \text{ VOLT.}$$

$$\therefore 20 = \sqrt{V_R^2 + V_L^2} \therefore \Rightarrow 20 = \sqrt{(12)^2 + V_L^2} \therefore V_L = 16 \text{ VOLT.}$$

$$(i) V_L > V_C$$

$$V_L - V_C = 9$$

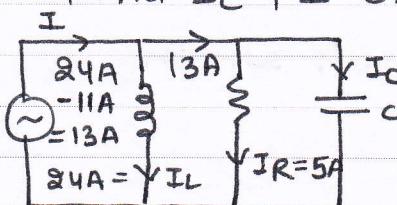
$$V_C = 16 - 9 = 7 \text{ VOLT.}$$

$$(ii) V_C > V_L$$

$$V_C - V_L = 9$$

$$V_C = 9 + 16 = 25 \text{ VOLT}$$

Q.14. Find I_C & I of the circuit shown:

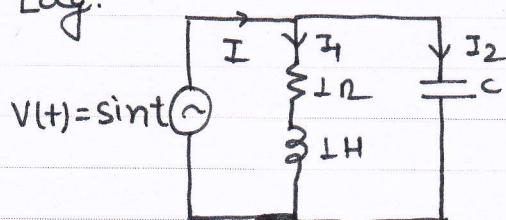


$$\text{AUS: } (13)^2 = \sqrt{I_R^2 + I_C^2} = \sqrt{25 + I_C^2}$$

$$I_C = 12 \text{ A}$$

$$\therefore I = \sqrt{I_R^2 + (I_L - I_C)^2} = \sqrt{(13)^2 + (24 - 12)^2} = \sqrt{25 + 144} = 13 \text{ A} = I$$

Q.15. Find capacitance of capacitor then power factor of circuit is 0.8 Lag.



$$\text{Ans} \Rightarrow \omega = 1, \cos \theta = 0.8; X_L = \omega L = 1 \times 1 = 1 \Omega \therefore X_C = \frac{1}{\omega C} = \frac{1}{C}$$

$$Y_{eq} = Y_1 + Y_2 = \frac{R}{R^2 + X_L^2} - j \frac{X_L}{R^2 + X_L^2} + \frac{j}{X_C}$$

$$Y_{eq} = \frac{1}{1+1} - j \frac{1}{1+1} + jC = \frac{1}{2} + j(C - \frac{1}{2})$$

$$\cos \theta = \frac{|Y|}{\sqrt{|Y|^2 + (B_C - B_L)^2}} = \frac{\frac{1}{2}}{\sqrt{(\frac{1}{2})^2 + (C - \frac{1}{2})^2}} = 0.8 = \frac{8}{10}$$

$$(\frac{1}{2})^2 + (C - \frac{1}{2})^2 = \frac{100}{64} \times \frac{1}{4} = \frac{100}{256}$$

$$(C - \frac{1}{2})^2 = \frac{100}{256} - \frac{1}{4} = \frac{9}{64}$$

$$C - \frac{1}{2} = \frac{3}{8}$$

$$C = \frac{3}{8} + \frac{1}{2} = \frac{7}{8} F.$$

IMP
CMT

A.C \rightarrow KVL, KCL \rightarrow Phasor sum
D.C \rightarrow KVL, KCL \rightarrow Airthmatic sum.

* THEOREM *

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SUBJECT -

TOPIC

P. No: 43.

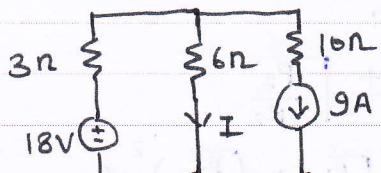
* Superposition theorem : → "In any linear bi-directional circuit Having more than 1 Independent source, the response In Any one of the Branch equal to algebraic sum of the Response caused by Individual sources while the rest of the source are replaced by its internal resistance".

NOTE

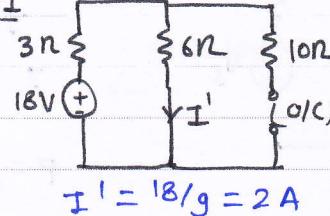
- While Applying superposition theorem depended source is Replaced by Neither open nor short circuit but Independed source voltage replaced by short circuit but current source replaced by open circuit.
- When Network is having linear bidirectional elements with respect to Homogeneity principle if Excitation is multiplied by constant K. the response of each element also multiplied by K.
- If the circuit have NO active independent source than voltage Across it terminal = 0 = Vth.

Point 1, 2 & 3 Are same for all theorem.

Q.1. Find the value of I by Superposition theorem: →

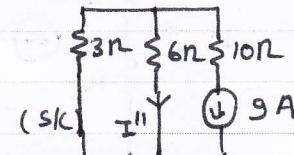


case-1



$$I' = 18/6 = 3 \text{ A}$$

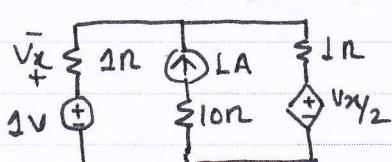
case-2



$$I'' = -9 \times 3/6 = -3 \text{ A}$$

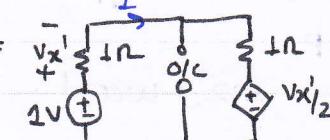
$$\text{So } I = I' + I'' = 3 - 3 = 0 \text{ A.}$$

Q.2 Find V_x by Superposition theorem:



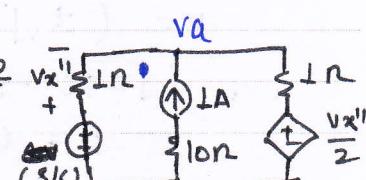
$$V_x = V_x'' + V_x' = \frac{2}{5} - \frac{2}{5} = 0.$$

case-1



$$V_x' = I' \cdot 1 = I'; -1 + 2I + V_{x/2} = 0 \\ 5/2 I = 1; I = \frac{2}{5} \text{ A} = V_x'$$

case-2



$$\frac{V_a}{1} + \frac{V_a - V_{x/2}}{1} = 1; V_a = -V_{x''} \\ \frac{V_a}{1} = -\frac{2}{5} \text{ V.}$$

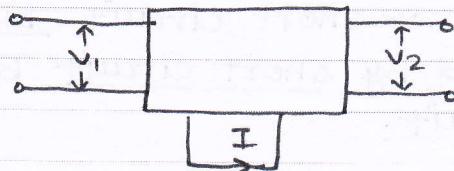
Q.3 In the circuit if source voltage increased by 10%. Find variation of power in resistor R.

Aus:- Case-1 No.1 : $V_s = V; R = R; P = V^2/R$

Case-2 No.2 $V_s = 1.1V; R = R; P = \frac{(1.1V)^2}{R} = 1.21P$

21% increased power.

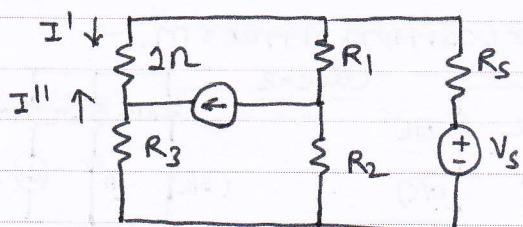
Q.4. Find I when $V_1 = 10V; V_2 = -15V$.



V_1	V_2	I
2V	0	+4A
0	3V	-2A

Aus:- It is superposition theorem because one source take at a time
 $V_1 = 2V$ than $I_1 = 4A$ so $V_1 = 10V$ so $I_1 = 4 \times 5 = 20A$
 $V_2 = 3V$ than $I_2 = -2A$ so $V_2 = -15V$ so $I_2 = -2 \times -5 = 10A$
total $I = I_1 + I_2 = 20 + 10 = 30A$.

Q.5. In the CKT shown power dissipation in the 1Ω resistor is 576 Watt when voltage source acting alone and $P.D$ in 1Ω resistor 1Watt when current source acting alone find total power dissipation in 2Ω resistor?



Aus:- $P = I^2 R; I = \pm \sqrt{P/R}$

$$I = I' + I''$$

$$I = \pm \sqrt{\frac{P_1}{R_1}} \pm \sqrt{\frac{P_2}{R_2}}$$

$$P = I^2 R = \left(\pm \sqrt{\frac{P_1}{R_1}} \pm \sqrt{\frac{P_2}{R_2}} \right)^2 \cdot R$$

When $R = R_1 = R_2 = 1\Omega$

$$P = (\pm \sqrt{P_1} \pm \sqrt{P_2})^2 \Rightarrow \sqrt{P^2} = \pm \sqrt{P_1} \pm \sqrt{P_2}$$

$$= (\sqrt{576} - \sqrt{1})^2 = P$$

$$P = (24-1)^2 = 529 \text{ Watt.}$$