

# Statistical Methods for Discrete Response, Time Series, and Panel Data (W271): Lab 3

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## Introduction

Load packages set some formatting preferences

```
pkg <- c('knitr', 'Hmisc', 'ggcorrplot', 'car',  
        'dplyr', 'ggplot2', 'jtools', 'readr')  
invisible(lapply(pkg, require, character.only = T))  
opts_chunk$set(tidy.opts=list(width.cutoff=60),tidy=TRUE)
```

**Question 1: E-Commerce Retail Sales as a Percent of Total Sales- Build a Seasonal ARIMA model and generate quarterly forecast for 2017**

Load data and quality-check the raw data

```
# Load csv file as df  
df_q1 <- read.csv("ECOMPCTNSA.csv", header = TRUE, sep = ",")  
str(df_q1)
```

```
## 'data.frame':    69 obs. of  2 variables:  
## $ DATE          : Factor w/ 69 levels "1999-10-01","2000-01-01",...: 1 2 3 4 5 6 7 8 9 10 ...  
## $ ECOMPCTNSA: num  0.7 0.8 0.8 0.9 1.1 1.1 1 1 1.3 1.3 ...
```

```
# View(df_q1) names(df_q1)  
head(df_q1)
```

```
##          DATE ECOMPCTNSA  
## 1 1999-10-01         0.7  
## 2 2000-01-01         0.8  
## 3 2000-04-01         0.8  
## 4 2000-07-01         0.9  
## 5 2000-10-01         1.1  
## 6 2001-01-01         1.1
```

```
describe(df_q1)
```

```
## df_q1  
##  
## 2 Variables      69 Observations  
## -----  
## DATE  
##      n missing distinct  
##      69      0       69  
##  
## lowest : 1999-10-01 2000-01-01 2000-04-01 2000-07-01 2000-10-01  
## highest: 2015-10-01 2016-01-01 2016-04-01 2016-07-01 2016-10-01  
## -----  
## ECOMPCTNSA  
##      n missing distinct      Info      Mean      Gmd      .05      .10  
##      69      0       50         1    3.835    2.524    0.94    1.10  
##      .25      .50      .75      .90      .95  
##      2.00     3.60     5.30     6.92     7.70  
##  
## lowest : 0.7 0.8 0.9 1.0 1.1, highest: 7.0 7.5 7.7 8.7 9.5  
## -----
```

```
# Create an R time-series object with our quarterly data
# starting with final quarter of 1999
q1_ts <- ts(df_q1$ECOMPCTNSA, frequency = 4, start = c(1999,
4))
str(q1_ts)
```

```
## Time-Series [1:69] from 2000 to 2017: 0.7 0.8 0.8 0.9 1.1 1.1 1 1 1.3 1.3 ...
```

```
head(q1_ts)
```

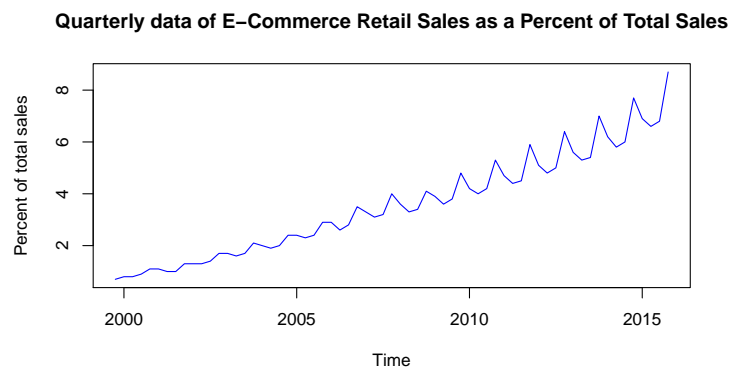
```
##      Qtr1 Qtr2 Qtr3 Qtr4
## 1999             0.7
## 2000  0.8  0.8  0.9  1.1
## 2001  1.1
```

We see that there are no missing values and that we are working with quarterly time series data. No anomalies are detected and there is not potential for top or bottom code. On gross visual inspection of the time series, we see that the starting values are all less than 1, with the later values all being greater than 7. This leads us to already suspect we are not dealing with a stationary series. We cannot make a confident comment on seasonality without further EDA for visualization.

## EDA

### Plot the data

```
# For modeling purposes we keep data between 1999 and 2015 as
# our training data; we hold-out 2016 as test data
q1_ts_train <- q1_ts[time(q1_ts) >= 1999 & time(q1_ts) < 2016]
q1_ts_train <- ts(q1_ts_train, frequency = 4, start = c(1999,
4))
q1_ts_test <- q1_ts[time(q1_ts) >= 2016]
q1_ts_test <- ts(q1_ts_test, frequency = 4, start = c(2016, 1))
# Plot the training data
plot.ts(q1_ts_train, main = "Quarterly data of E-Commerce Retail Sales as a Percent of Total Sales",
ylab = "Percent of total sales", col = "blue")
```

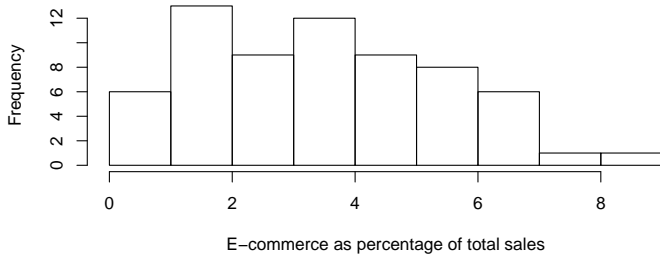


We are now able to clearly see that the e-commerce retail sales time series is not stationary in the mean and exhibits seasonality. We will attempt to stationarize our time series via differencing.

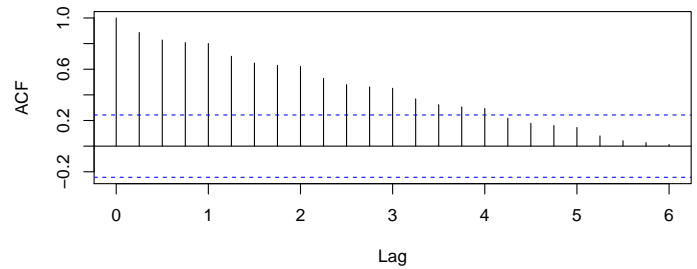
### Examine the ACF/PACF to determine if an AR(p) or MA(q) model is appropriate

```
# Plot frequency distribution, ACF, PACF
hist(q1_ts_train, main = "Frequency Distribution of E-commerce as Percentage of Total Sales",
xlab = "E-commerce as percentage of total sales")
acf(q1_ts_train, main = "Autocorrelation function", lag.max = 24)
pacf(q1_ts_train, main = "Partial Autocorrelation function",
lag.max = 24)
```

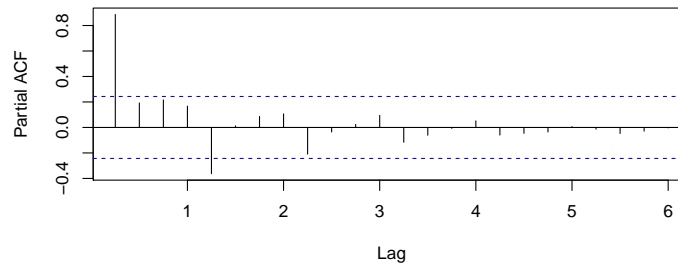
Frequency Distribution of E-commerce as Percentage of Total Sales



Autocorrelation function



Partial Autocorrelation function



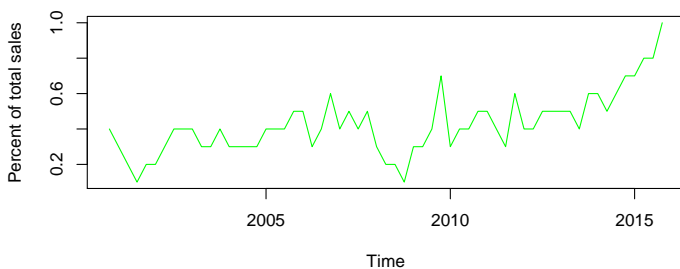
Although it has been dictated that we are to create a SARIMA model, we still need to check that this model is appropriate. We see that the autocorrelations are significant for a large number of lag (16 quarters). This slow decay in the autocorrelations is evidence of a trend in the data, thus telling us that the time series is not stationary. The gradual decay without any spikes at seasonal intervals tells us that we will need a non-seasonal AR term  $p$  but will not need a seasonal AR term  $P$ . We see that the partial autocorrelation plot has a significant spike at a lag of 1 quarter and at 4 quarters. We see that our PACF has a somewhat abrupt drop-off non-seasonally following lag-1 and but that there are spikes in the PACF at an annual lag (multiples of lag-4 given our quarterly data). This leads us to believe that our model will not require a non-seasonal MA term  $q$  but will require a seasonal MA term  $Q$ . The histogram of our data shows that the e-commerce as percentage of total sales is fairly normally distributed with positive skew; however, this tells us nothing about how the data are related in time.

### Difference the data to impose stationarity

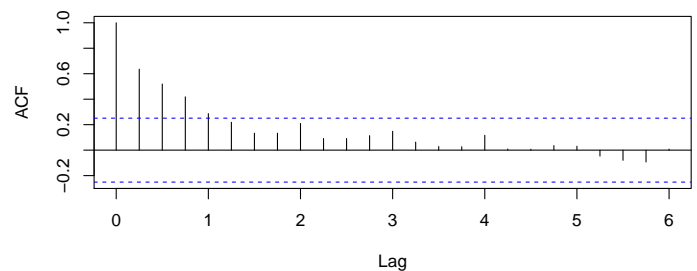
We have demonstrated evidence of both trend and seasonality in our time series. To impose stationarity, we will first apply a seasonal difference to the data and then re-evaluate the trend. If a trend remains, then we will take first differences.

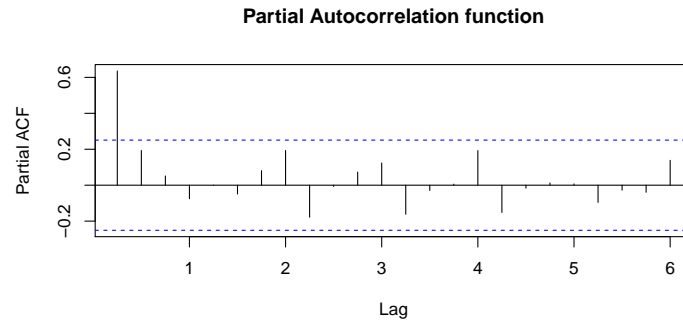
```
# Impose seasonal difference at one-year (4 quarters)
q1_ts_train_seasonal_diff = diff(q1_ts_train, 4)
plot.ts(q1_ts_train_seasonal_diff, main = "Quarterly E-Commerce Sales as % Total Sales- Seasonal Difference",
        ylab = "Percent of total sales", col = "green")
acf(q1_ts_train_seasonal_diff, main = "Autocorrelation function",
    lag.max = 24)
pacf(q1_ts_train_seasonal_diff, main = "Partial Autocorrelation function",
    lag.max = 24)
```

Quarterly E-Commerce Sales as % Total Sales- Seasonal Difference



Autocorrelation function

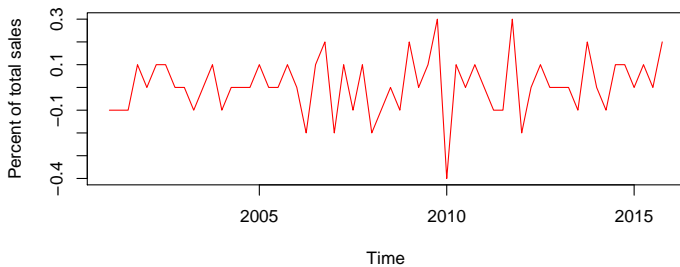




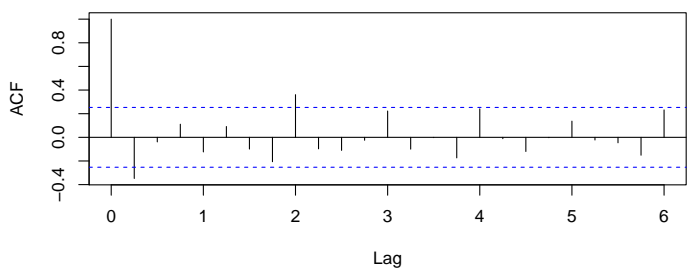
After creating a seasonal-differenced series, the series still appears to be non-stationary. For stationary time series, the ACF drops to zero relatively quickly, while for non-stationary data the ACF decreases slowly. We see improvement here as compared to our initial non-differenced model, but we have still not imposed stationarity. This provides evidence that we need to impose a first-difference.

```
# Impose additional first-difference
q1_ts_train_seasonal_and_first_diff = diff(q1_ts_train_seasonal_diff,
1)
plot.ts(q1_ts_train_seasonal_and_first_diff, main = "Quarterly E-Commerce Sales as % Total Sales- Seasonal & First Differenc",
ylab = "Percent of total sales", col = "red")
acf(q1_ts_train_seasonal_and_first_diff, main = "Autocorrelation function",
lag.max = 24)
pacf(q1_ts_train_seasonal_and_first_diff, main = "Partial Autocorrelation function",
lag.max = 24)
```

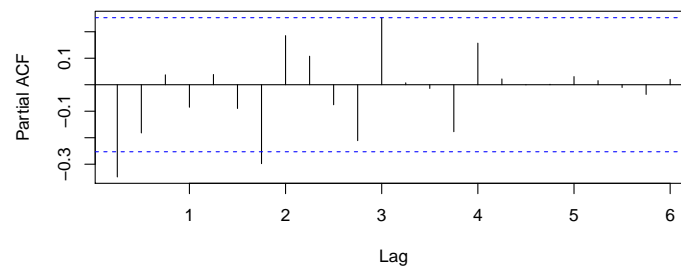
Quarterly E-Commerce Sales as % Total Sales- Seasonal & First Differenc



Autocorrelation function



Partial Autocorrelation function



After taking a first-difference we see that the seasonal-differenced and first-differenced series is stationary. Overall we do not see evidence that the volatility is increasing over time, so we do not take a difference in log to stabilize the series.

## Order Identification

The spike in the ACF at a lag of 1 quarter suggests a nonseasonal MA(1) ( $q=1$ ) component and the spikes at intervals of 4 quarters of lag suggest a seasonal MA(1) ( $Q=1$ ). Additionally, the spike at a lag of 1 quarter in the PACF and the spikes at intervals of 4 quarters of lag tells us that a nonseasonal AR(1) ( $p=1$ ) component and a seasonal AR(1) ( $P=1$ ) component are appropriate for our initial model. Therefore, our initial model will be of the form  $ARIMA(1, 1, 1)(1, 1, 1)_4$

## Model Creation: Build a Seasonal ARIMA model and generate quarterly forecast for 2017

We first start by building a model with our estimated components from our prior analysis. Next, we will see if an interactive method comparing difference combinations of component values as well as the `auto.arima` function all agree with our model having the lowest AIC/BIC.

```
q1_ts_train_seasonal_and_first_diff.fit <- Arima(q1_ts_train_seasonal_and_first_diff,
  order = c(1, 1, 1), seasonal = c(1, 1, 1))
summary(q1_ts_train_seasonal_and_first_diff.fit)

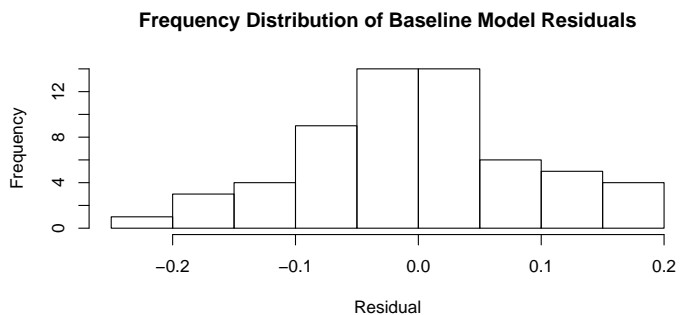
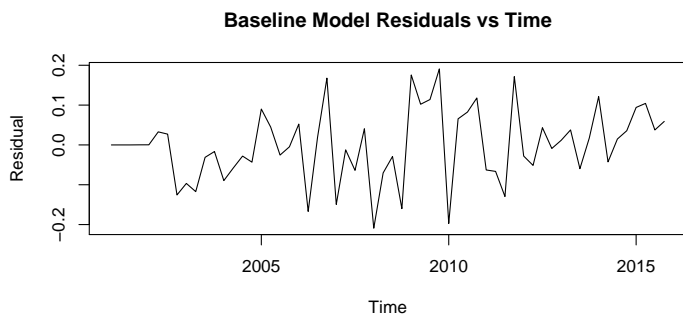
## Series: q1_ts_train_seasonal_and_first_diff
## ARIMA(1,1,1)(1,1,1)[4]
##
## Coefficients:
##          ar1      ma1      sar1      sma1
##       -0.36  -0.93  -0.45  -0.91
## s.e.    0.13   0.12   0.13   0.22
##
## sigma^2 estimated as 0.00965:  log likelihood=44
## AIC=-78   AICc=-76   BIC=-67
##
## Training set error measures:
##              ME  RMSE  MAE  MPE  MAPE  MASE   ACF1
## Training set -0.0012 0.091 0.07 NaN  Inf  0.46 -0.019

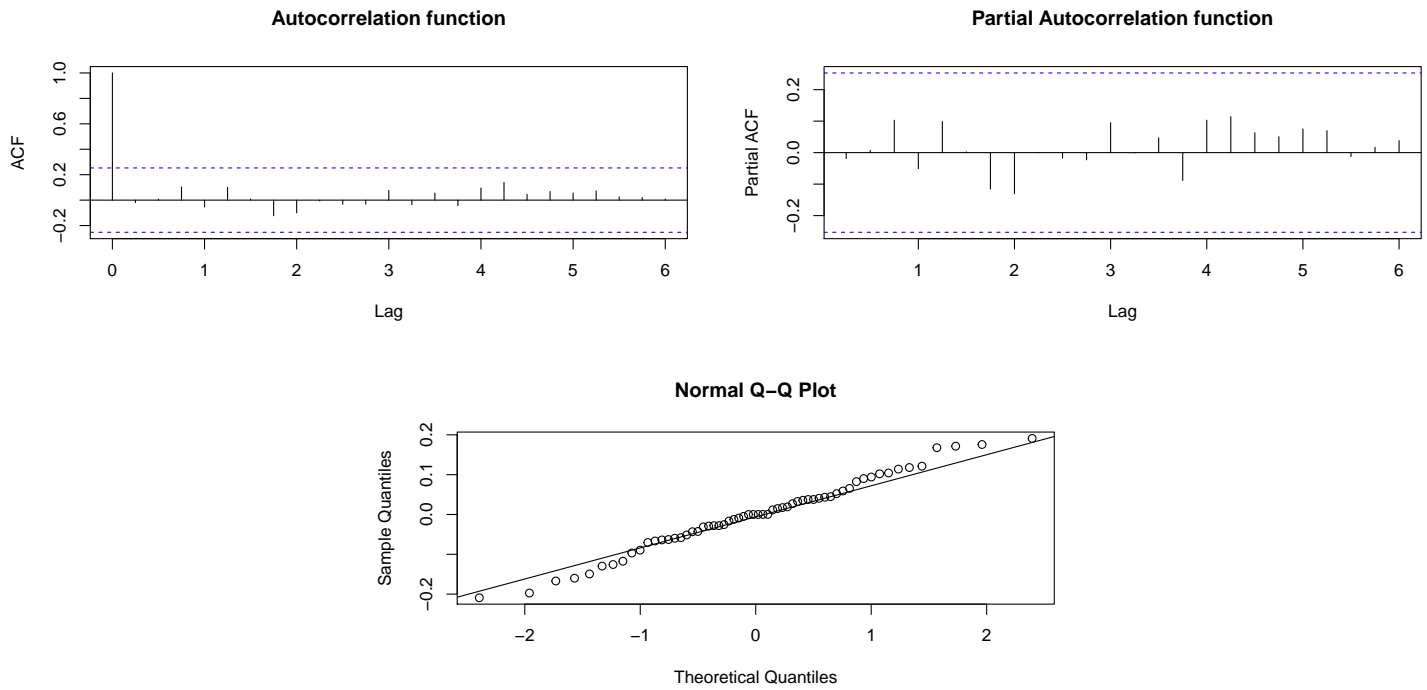
plot.ts(q1_ts_train_seasonal_and_first_diff.fit$resid, main = "Baseline Model Residuals vs Time",
  ylab = "Residual", col = "black")
hist(q1_ts_train_seasonal_and_first_diff.fit$resid, main = "Frequency Distribution of Baseline Model Residuals",
  xlab = "Residual")
acf(q1_ts_train_seasonal_and_first_diff.fit$resid, main = "Autocorrelation function",
  lag.max = 24)
pacf(q1_ts_train_seasonal_and_first_diff.fit$resid, main = "Partial Autocorrelation function",
  lag.max = 24)
shapiro.test(q1_ts_train_seasonal_and_first_diff.fit$resid)

##
## Shapiro-Wilk normality test
##
## data:  q1_ts_train_seasonal_and_first_diff.fit$resid
## W = 1, p-value = 0.8

qqnorm(q1_ts_train_seasonal_and_first_diff.fit$resid)
qqline(q1_ts_train_seasonal_and_first_diff.fit$resid)
Box.test(q1_ts_train_seasonal_and_first_diff.fit$resid, type = "Ljung-Box")

##
## Box-Ljung test
##
## data:  q1_ts_train_seasonal_and_first_diff.fit$resid
## X-squared = 0.02, df = 1, p-value = 0.9
```





Now we will look at other values for p,d,q,P,D,Q via an iterative method.

Lastly, we look at the `auto.arima` function to see if it agrees with our model thus far.

## Fit Evaluation

### Question 2: data\_2018Spring\_MTS.txt

#### Load data

```
# df_q2 <- read.csv('correlate-flight_prices.csv', header =
# TRUE, sep=',')
```

## EDA

### Order Identification

### Model Creation

### Fit Evaluation

## Conclusion