### **Important Reminders!**

- 1. Put your solution into a single Elm file (ending in .elm), and convert that file into a pdf file (e.g., via printing). Upload the pdf file to the Pensieve grading web site:
  - https://tutor.pensieve.co/student/classes/oregonstateuniversity\_cs381\_sp25/external-assignments
- 2. Only submit files that compile without errors! (Put all non-working parts in comments.)
- 3. You must do all homework assignments by yourself, without the help of others. Also, you must not use services such as Chegg or Course Hero. If you need help, simply ask on Canvas, and we will help!
- 4. You can work in teams of *up to four* students to create and submit homework assignments. You have to list the group members, sorted alphabetically by last name, at the beginning of the file as an Elm comment, like so:

```
{- GROUP:
    Helena Eagen
    Dylan George
    Mark Scout
-}
```

Each group submits *only one solution* by the *first member* of the group.

All group members will receive the same grade for the homework.

Download the file HW1\_Def.elm, and insert the following lines at the top of your file (which should have the name HW1\_Elm.elm).

```
module HW1_Elm exposing (..)
import HW1_Def exposing (..)
```

#### Exercise 1. Programming with Lists

Multisets, or bags, can be represented as list of pairs (x, n) where n indicates the number of occurrences of x in the multiset.

```
type alias Bag a = List (a, Int)
```

For the following exercises you can assume the following properties of the bag representation. *But note:* Your function definitions have to maintain these properties for any multiset they produce!

- (1) Each element *x* occurs in at most one pair in the list.
- (2) Each element that occurs in a pair has a positive counter.

As an example consider the multiset  $\{2, 3, 3, 5, 7, 7, 7, 8\}$ , which has the following representation (among others).

```
[(5,1),(7,3),(2,1),(3,2),(8,1)]
```

Note that the order of elements is not fixed. In particular, we cannot assume that the elements are sorted. Thus, the above list representation is just one example of several possible.

(a) Define the function insert that inserts an element into a multiset.

```
insert : a \rightarrow Bag a \rightarrow Bag a
```

(b) Define the function remove that removes a single element from a multiset. Note that removing 3 from  $\{2, 3, 3, 4\}$  yields  $\{2, 3, 4\}$  whereas removing 3 from  $\{2, 3, 4\}$  yields  $\{2, 4\}$ .

```
remove : a \rightarrow Bag \ a \rightarrow Bag \ a
```

(c) Define a function mkBag that takes a list of values and produces a multiset representation.

```
mkBag : List a \rightarrow Bag a

For example, with xs = [7,3,8,7,3,2,7,5] we get the following result.

> mkBag xs
[(5,1),(7,3),(2,1),(3,2),(8,1)]
```

Note: It's a good idea to use of the function insert defined earlier.

(d) Define a function is Subbag that determines whether its first argument bag is contained in the second.

```
isSubbag : Bag a \rightarrow Bag a \rightarrow Bool
```

*Note*: Bag b is contained in bag b' if every element that occurs n times in b occurs also at least n times in b'.

(e) Define a function size that computes the number of elements contained in a bag.

```
size : Bag a \rightarrow Int
```

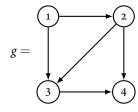
### Exercise 2. Graphs

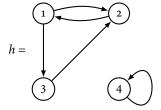
A simple way to represent a directed graph is through a list of edges. An edge is given by a pair of nodes. For simplicity, nodes are represented by integers.

```
type alias Node = Int
type alias Edge = (Node, Node)
type alias Graph = List Edge
```

(We ignore the fact that this representation cannot distinguish between isolated nodes with and without loops; see, for example, the loop/edge (4,4) in the graph h that represents an isolated node.)

Consider, for example, the following directed graphs.





These two graphs are represented as follows.

```
g : Graph
g = [(1,2),(1,3),(2,3),(2,4),(3,4)]
h : Graph
h = [(1,2),(1,3),(2,1),(3,2),(4,4)]
```

*Note*: In some of your function definitions you might want to use the function asSet (defined in the file HW1\_Def.elm) to remove duplicates from a list and sort it.

- (a) Define the function nodes: Graph  $\rightarrow$  List Node that computes the list of nodes contained in a given graph. For example, nodes g = [1,2,3,4].
- (b) Define the function suc: Node  $\rightarrow$  Graph  $\rightarrow$  List Node that computes the list of successors for a node in a given graph. For example, suc 2 g = [3,4], suc 4 g = [], and suc 4 h = [4].

(c) Define the function detach: Node  $\rightarrow$  Graph  $\rightarrow$  Graph that removes a node together with all of its incident edges from a graph. For example, detach 3 g = [(1,2),(2,4)] and detach 2 h = [(1,3),(4,4)].

Note: All functions can be succinctly implemented by using the higher-order list functions map and filter.

# Exercise 3. Programming with Data Types \_

The following definitions introduce a data type for representing a few basic shapes. A figure is a collection of shapes (represented as a list). The type BBox represents *bounding boxes* of objects by the points of the lower-left and upper-right hand corners of the smallest enclosing rectangle.

(a) Define the function width that computes the width of a shape.

```
width : Shape → Length
```

For example, the widths of the shapes in the figure f are as follows.

```
f = [Pt (4,4), Circle (5,5) 3, Rect (3,3) 7 2]
> map width f
[0,6,7]
```

(b) Define the function bbox that computes the bounding box of a shape.

```
bbox : Shape \rightarrow BBox
```

The bounding boxes of the shapes in the figure f are as follows.

```
> map bbox f [((4,4),(4,4)),((2,2),(8,8)),((3,3),(10,5))]
```

(c) Define the function minX that computes the minimum x coordinate of a shape.

```
minX : Shape \rightarrow Number
```

The minimum x coordinates of the shapes in the figure f are as follows.

```
> map minX f
[4,2,3]
```

(d) Define a function move that moves the position of a shape by a vector given by a point as its first argument.

```
move : Point \rightarrow Shape \rightarrow Shape
```

It is probably a good idea to define and use an auxiliary function addPoint : Point  $\rightarrow$  Point, which adds two points component-wise.

# A Note on Testing Your Function Definitions

To test your function definitions, you have to import the module HW1\_Elm.elm into the Elm REPL, like so.

```
> import HW1_Elm exposing (..)
```

At this point the definitions from HW1\_Def.elm have been imported only into your file HW1\_Elm.elm, but they are not imported into the REPL. Thus, to define test values such as f in the last exercise, you have to do one of two things.

(1) Define test values within HW1\_Elm.elm. For example, add the following definition at the bottom of your file.

```
f = [Pt (4,4), Circle (5,5) 3, Rect (3,3) 7 2]
```

These test values are then available in the REPL when you import HW1\_Elm.elm.

(2) Import HW1\_Def.elm into the REPL, that is, after importing HW1\_Elm.elm, write:

```
> import HW1_Def exposing (..)
```

Then all the definitions from HW1\_Def.elm are available directly in the REPL as well, and you can use constructors of the Shape type directly. For example:

```
width (Pt (4,4)) 0 : Length
```

You can then also define test values such as f directly in the REPL.

```
> f = [Pt (4,4), Circle (5,5) 3, Rect (3,3) 7 2]
[Pt (4,4),Circle (5,5) 3,Rect (3,3) 7 2]
    : List Shape
> map width f
[0,6,7] : List Length
```

However, these definitions are lost when you restart the REPL.