

Quiz 4

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Abstract—This document contains the solution of the question from NCERT 11th standard chapter 10 exercise 10.1 problem 6

1 EXERCISE 10.1

- 1) Without using the Pythagoras theorem, show that the points $(4, 4)$, $(3, 5)$ and $(-1, -1)$ are the vertices of a right angled triangle.

We need to show that points $(4,4)$, $(3,5)$ and $(-1,-1)$ are vertices of a right triangle.

Let,

$$(A) = \begin{bmatrix} 4 \\ 4 \end{bmatrix}, (B) = \begin{bmatrix} 3 \\ 5 \end{bmatrix}, \text{ and } (C) = \begin{bmatrix} -1 \\ -1 \end{bmatrix} \quad (1.0.1)$$

$$(B) - (A) = \begin{bmatrix} 3 \\ 5 \end{bmatrix} - \begin{bmatrix} 4 \\ 4 \end{bmatrix} = \begin{bmatrix} -1 \\ 1 \end{bmatrix} \quad (1.0.2)$$

$$(C) - (A) = \begin{bmatrix} -1 \\ -1 \end{bmatrix} - \begin{bmatrix} 4 \\ 4 \end{bmatrix} = \begin{bmatrix} -5 \\ -5 \end{bmatrix} \quad (1.0.3)$$

$$((B) - (A))^T ((A) - (C)) = \begin{bmatrix} -1 & 1 \end{bmatrix} * \begin{bmatrix} -5 \\ -5 \end{bmatrix} = 5 - 5 = 0 \quad (1.0.4)$$

$((A) - (B))^T ((A) - (C)) = 0 \Rightarrow$ angle between $(A) - (B)$ and $(B) - (C)$ is 90 degrees.

Hence, $\triangle ABC$ is a right angled triangle with right angle at vertex $A(4, 4)$.